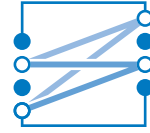




TECHNISCHE UNIVERSITÄT MÜNCHEN  
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Master's Thesis

# Polar FEC chain development in Software for 5G

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Ich versichere hiermit wahrheitsgemäß, die Arbeit bis auf die dem Aufgabensteller bereits bekannte Hilfe selbständig angefertigt, alle benutzten Hilfsmittel vollständig und genau angegeben und alles kenntlich gemacht zu haben, was aus Arbeiten anderer unverändert oder mit Abänderung entnommen wurde.

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Ort, Datum (Yadhunandana Rajathadripura Kumaraiah)



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# Abstract

The abstract comes here.



# 1 Introduction and Motivation

In 1948, scientists at the Bell Laboratories achieved two landmark research results: Claude E. Shannon published his paper *A mathematical theory of communication* [Sha48], and John Bardeen, Walter Brattain and William Shockley announced the invention of the *transistor effect*.

[Ari09]

A binomial distribution is shown in Figure 1.1.

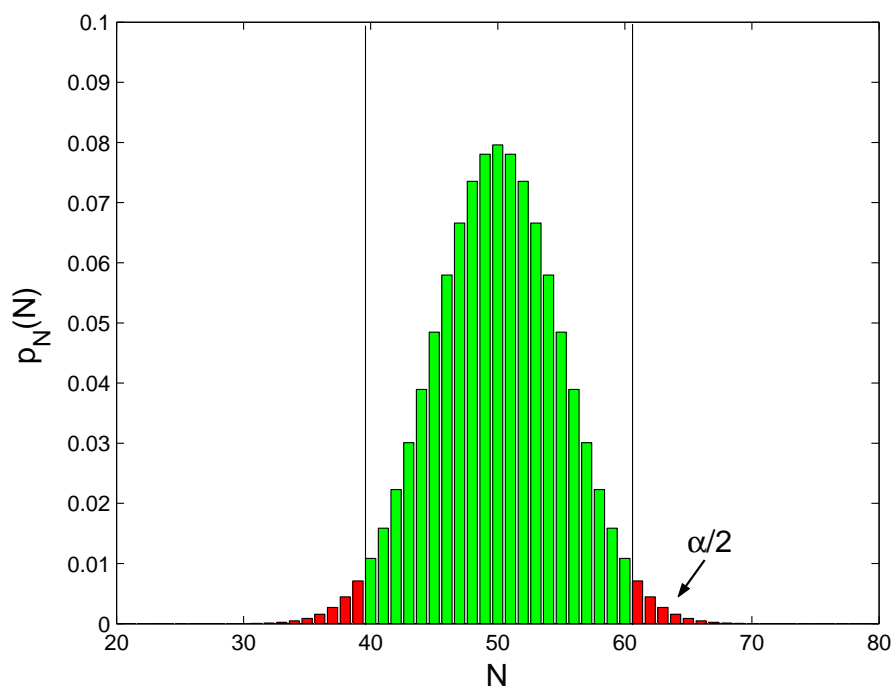


Figure 1.1: PDF  $p_N(N)$  of the number  $N$  of times that the head side is up.

For further information, the reader is referred to [CT91, Cla01, Sac92, ?, BGT93, Che03, Onk02, Hag01, Wei].

Traditionally FEC chains are developed in hardware i.e FPGAs or ASICs to achieve low latency and high throughput. Development in FPGA/hardware requires more time and

costly. With recent advances in General Purpose Processors it is possible to achieve required latency and throughput with software implementations without custom hardware. Software implementations are flexible and easy to maintain compared hardware implementations.

However algorithms need to be adopted/optimized to efficiently implement in software. Recent advances in the modern processors such as SIMD units can be utilized to achieve low latency and high throughput.

## 2 Polar Codes Background

Polar codes were invented by erdal arikan in his seminal work [Ari09]. These are first theoretically capacity achieving codes. However their performance is not comparable with the LDPC or Turbo codes at short block lengths.





### 3 Encoding FEC Chain

Work I have done Until now.

Optimizations to the original implementations until now. Generic optimizations - Using optimization primitives such as likely and unlikely. - Aligning memory to 32 bytes so copying of data can be vectorized. Polar transform optimization - Replace binary additions with xor. instead of addition and then modulus two. - division and multiplications by left and right shift operations. - Avoided copy operations in polarTransform operations. Optimization in getting reliability indices. - Avoided remove and erase operations which have huge overhead. Wrote a efficient mechanism(reduced the latency by 176 us). - Instead removing and erasing I mark the element as removed. - Since the reliability indexes won't change. I built a look up table in place of searching all (1024)indices reduced the latency by 40us - Avoided copying operations of interleaved indexes. - Unrolled the loop to reduce the jumps. Rate matching optimizations. - optimization in subblock interleaving, Rewrote the logic to avoid E number of division and modulus operations. - Unrolled the for loops in subblock interleaving method. - Implemented optimal version of bit selection, Avoided E number of modulus operations which are very costly. - Again optimization primitives for helping the branch predictor.

Fast version of Encoding API's. In the original implementation of the polar encoding each of the bit is treated as 32 bit integer. This is highly inefficient when the goal is to process multiple bits at time. With each bit considered as 32 bit integer SIMD instructions won't provide any performance improvement. Reason is SIMD instruction can process multiple bits at time. avx2 instructions 256bits at a time. if we have 32 bits to represent a single bit. we can process only 8 bits at time. Which doesn't significantly improve the performance. To avoid this disadvantage and make use of SIMD capability. each 64 bit integer is considered as 64 bits of data. so one avx2 instruction can process 256 data bits in a single instruction. - Built a look up table to avoid last eight stages of polar encoding instead of traversing till end of tree. - Implemented SIMD instruction based encoding. Encoding happens within 0.6 us for  $N = 512$ . - Implemented optimal version of CRC calculation which can calculate CRC for PDCCH chain within 0.8 us. Original implementation was taking 7 us. - Implemented a bit interleaver which can deal with this format of data.

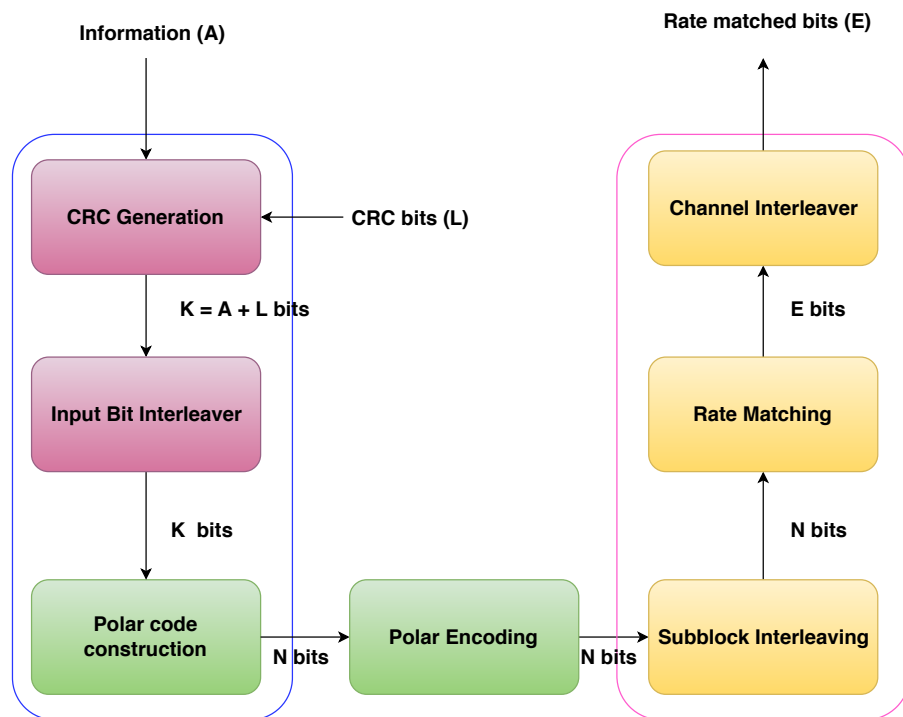


Figure 3.1: Polar Encoding FEC chain for PDCCH/PBCH

## 4 Decoding FEC Chain

Decoding is of serial nature, has lot of latency.

### 4.1 Decoding algorithms



## 5 Conclusion



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