Solve the following recurrence for $n, k \geq 0$:

$$Q_{n,0} = 1$$
 $Q_{0,k} = [k = 0];$
$$Q_{n,k} = Q_{n-1,k} + Q_{n-1,k-1} + \binom{n}{k}, \text{ for } n, k > 0.$$

AMS matrices.