

Not All Pairs are Equal: Hierarchical Learning for Average-Precision-Oriented Video Retrieval

Yang Liu¹, Qianqian Xu^{2,*}, Peisong Wen^{1,2}, Siran Dai⁴, Qingming Huang^{1,2,3,*}

1 School of Computer Science and Technology, University of Chinese Academy of Sciences 3 BDKM, University of Chinese Academy of Sciences

2 Institute of Computing Technology, Chinese Academy of Sciences 4 Institute of Information Engineering, Chinese Academy of Sciences

This paper was presented with the **Honourable Mention Award** at the ACM MultiMedia 2024 Conference.



Alignment of the Objective with the Metric

Evaluation Metric: Average Precision (AP)

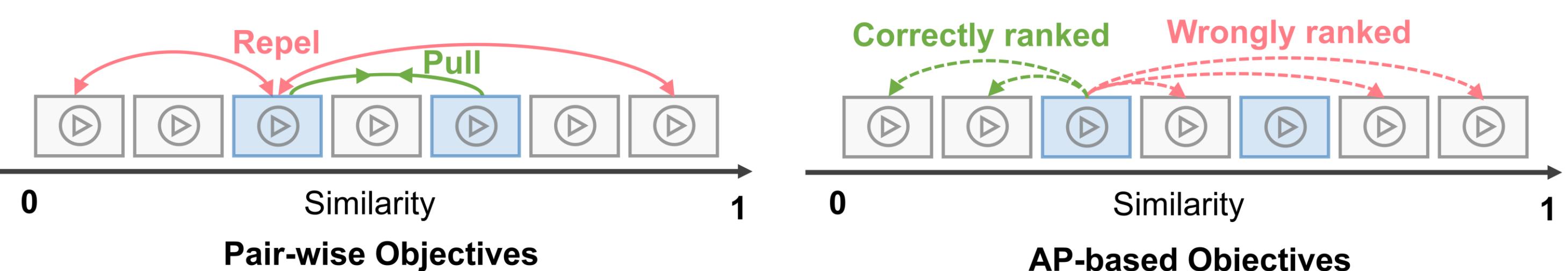
- Evaluates the overall rankings of relevant videos $AP = \frac{1}{n} \sum_{i=1}^n \frac{i}{r_i}$
- Assigns larger weights on higher-ranked instances

Previous Training Objectives: Pair-wise Objectives

- Pull the positive instances closer and repel the negative ones
- Treat all mis-ranked pairs equally
- Mismatch with the evaluation metric

New Training Objectives: AP-based Objectives

- Rectify the wrongly ranked positive-negative pairs in the list
- Fill the gap between training objectives and evaluation metrics



Two Challenges for Video-Oriented AP Optimization

- Current AP losses are suboptimal for **video-level** retrieval
- Noisy **frame-level** matching leads to a biased AP estimation

Gradient-Enhanced AP Optimization

Optimization Problem:

- Maximizing the AP score

$$\max_f AP(f) = \frac{1}{N} \sum_{k=1}^N AP_k(f)$$

$$AP_k(f) = \frac{1}{|S^{k+}|} \sum_{s_{ki} \in S^{k+}} \frac{\mathcal{R}(s_{ki}, S^{k+})}{\mathcal{R}(s_{ki}, S^{k+} \cup S^{k-})}$$

$$= \frac{1}{|S^{k+}|} \sum_{s_{ki} \in S^{k+}} \frac{1 + \sum_{s_{kj} \in S^{k+}} \mathcal{H}(d_{ji}^k)}{1 + \sum_{s_{kj} \in S^{k+} \cup S^{-}} \mathcal{H}(d_{ji}^k)}$$

Objective Reformulation:

- Minimizing the AP risk

$$\min_f AP_k^{\downarrow}(f) = \frac{1}{N} \sum_{k=1}^N AP_k^{\downarrow}(f)$$

$$\mathcal{R}(s, S) = 1 + \sum_{s' \in S} \mathcal{H}(s' - s)$$

$$d_{ji}^k = s_{kj} - s_{ki} \quad h(x) = \frac{x}{1+x}$$

$$AP_k^{\downarrow}(f) = 1 - \frac{1}{|S^{k+}|} \sum_{s_{ki} \in S^{k+}} \frac{1 + \sum_{s_{kj} \in S^{k+}} \mathcal{H}(d_{ji}^k)}{1 + \sum_{s_{kj} \in S^{k+} \cup S^{-}} \mathcal{H}(d_{ji}^k)}$$

$$= \frac{1}{|S^{k+}|} \sum_{s_{ki} \in S^{k+}} \frac{\sum_{s_{kj} \in S^{-}} \mathcal{H}(d_{ji}^k)}{1 + \sum_{s_{kj} \in S^{k+} \cup S^{-}} \mathcal{H}(d_{ji}^k)}$$

$$= \frac{1}{|S^{k+}|} \sum_{s_{ki} \in S^{k+}} h \left(\frac{\sum_{s_{kj} \in S^{-}} \mathcal{H}(d_{ji}^k)}{1 + \sum_{s_{kj} \in S^{k+}} \mathcal{H}(d_{ji}^k)} \right)$$

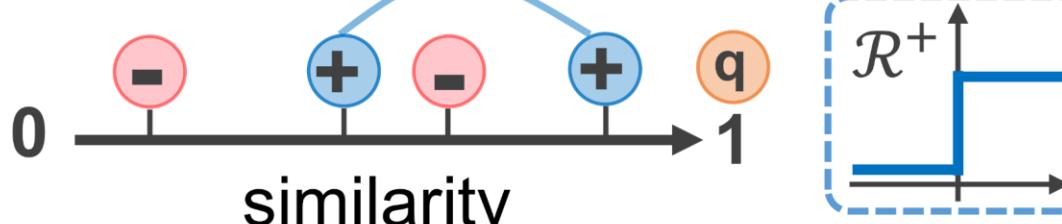
Rethinking the Components of AP Risk: QuadLinear-AP

$$AP_k^{\downarrow}(f) = \frac{1}{|S^{k+}|} \sum_{s_{ki} \in S^{k+}} h \left(\frac{\sum_{s_{kj} \in S^{-}} \mathcal{H}(d_{ji}^k)}{1 + \sum_{s_{kj} \in S^{k+}} \mathcal{H}(d_{ji}^k)} \right) \rightarrow \widehat{AP}_k^{\downarrow}(f) = \frac{1}{|S^{k+}|} \sum_{s_{ki} \in S^{k+}} h \left(\frac{\sum_{s_{kj} \in S^{-}} \mathcal{R}^-(d_{ji}; \delta)}{1 + \rho \sum_{s_{kj} \in S^{k+}} \mathcal{R}^+(d_{ji})} \right)$$

Positive-positive Pairs

- Serve as weights
- No need for optimization

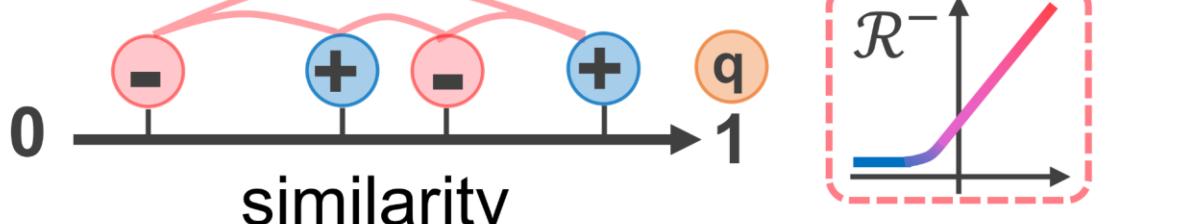
$$\mathcal{R}^+(x) = \mathcal{H}(x) = \begin{cases} 1, & \text{if } x > 0 \\ 0, & \text{if } x \leq 0 \end{cases}$$



Positive-negative Pairs

- Rankings should be corrected
- Need proper gradients for optimization

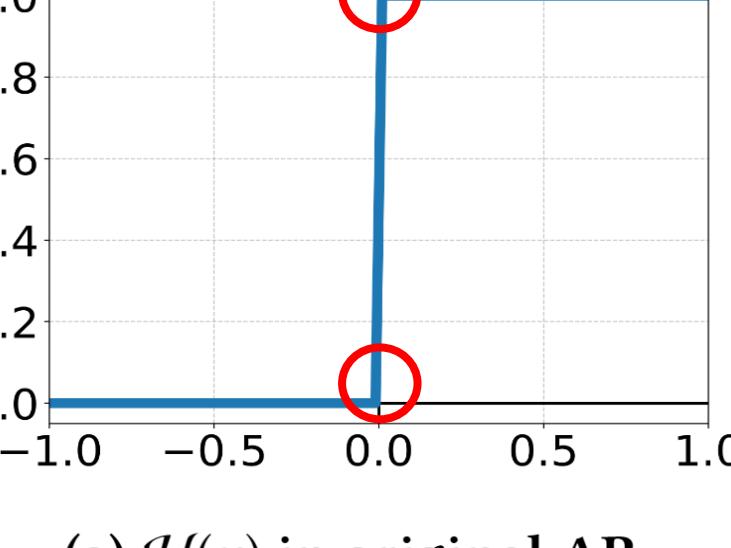
$$\mathcal{R}^-(x; \delta) = \begin{cases} \mathcal{H}(-x) \cdot \frac{1}{\delta^2} x^2 + \frac{2}{\delta} x + 1, & \text{if } x \geq -\delta \\ 0, & \text{if } x < -\delta \end{cases}$$



Original AP

$$\frac{\sum_{s_{kj} \in S^{-}} \mathcal{H}(d_{ji}^k)}{1 + \sum_{s_{kj} \in S^{k+}} \mathcal{H}(d_{ji}^k)}$$

Non-differentiability

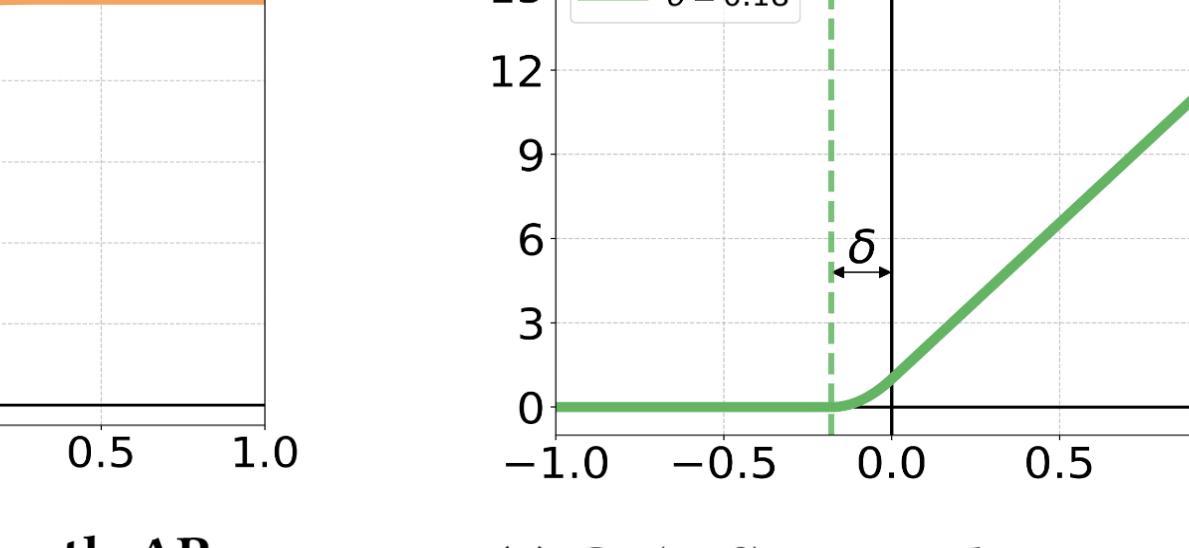


(a) $\mathcal{H}(x)$ in original AP.

Smooth-AP

$$\frac{\sum_{s_{kj} \in S^{-}} \mathcal{G}(d_{ji}^k; \tau)}{1 + \sum_{s_{kj} \in S^{k+}} \mathcal{G}(d_{ji}^k; \tau)}$$

Gradient Vanishing

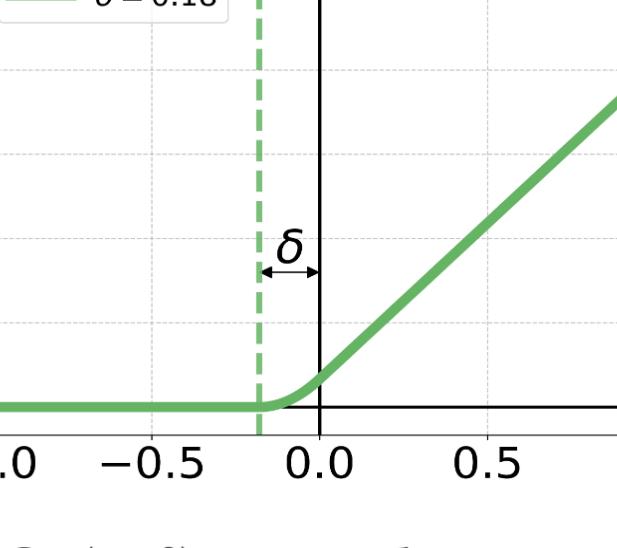


(c) $\mathcal{G}(x; \tau)$ in Smooth-AP.

QuadLinear-AP (Ours)

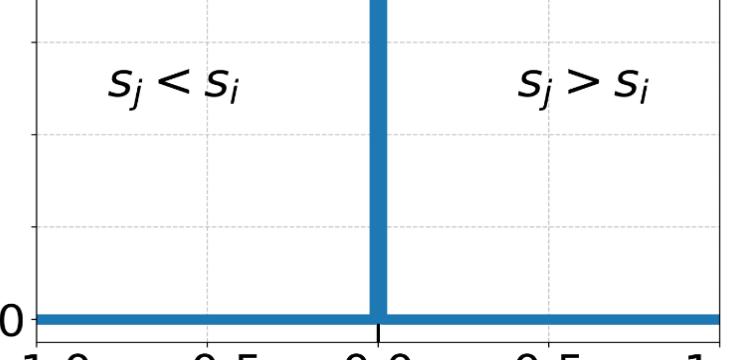
$$\frac{\sum_{s_{kj} \in S^{-}} \mathcal{R}^-(d_{ji}^k; \delta)}{1 + \rho \sum_{s_{kj} \in S^{k+}} \mathcal{R}^+(d_{ji}^k)}$$

Favorable properties



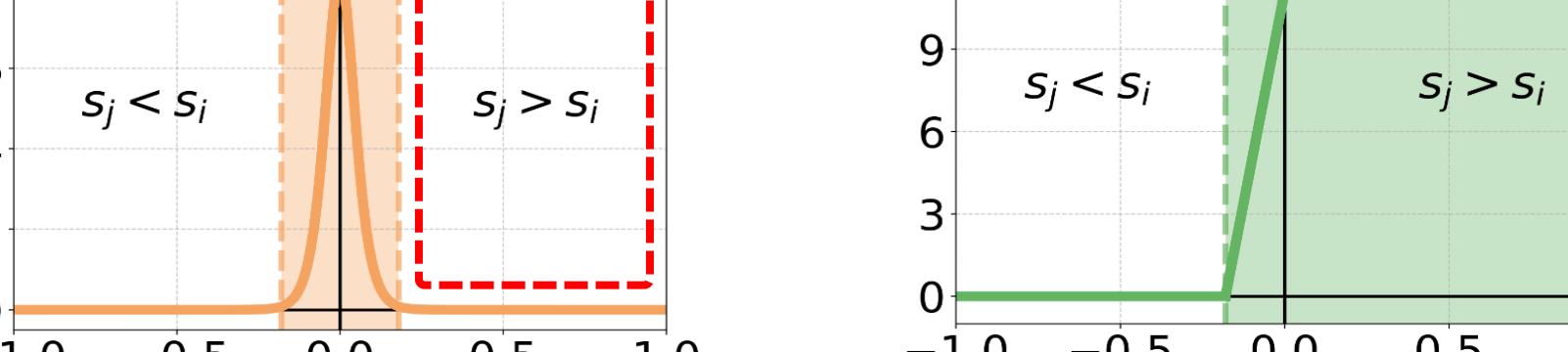
(e) $\mathcal{R}^-(x; \delta)$ in QuadLinear-AP.

Derivative of $\mathcal{H}(x)$



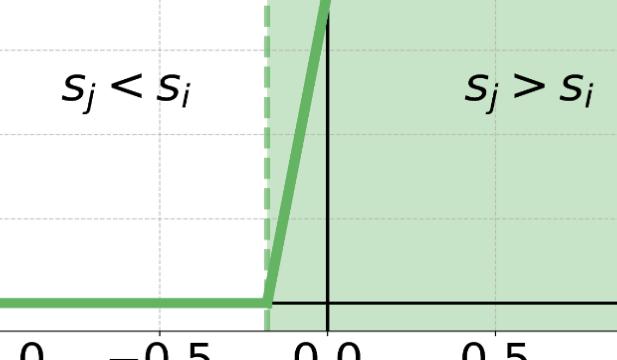
(b) Derivative of $\mathcal{H}(x)$.

Derivative of $\mathcal{G}(x; \tau)$



(d) Derivative of $\mathcal{G}(x; \tau)$.

Derivative of $\mathcal{R}^-(x; \delta)$



(f) Derivative of $\mathcal{R}^-(x; \delta)$.

Favorable Properties of QuadLinear-AP

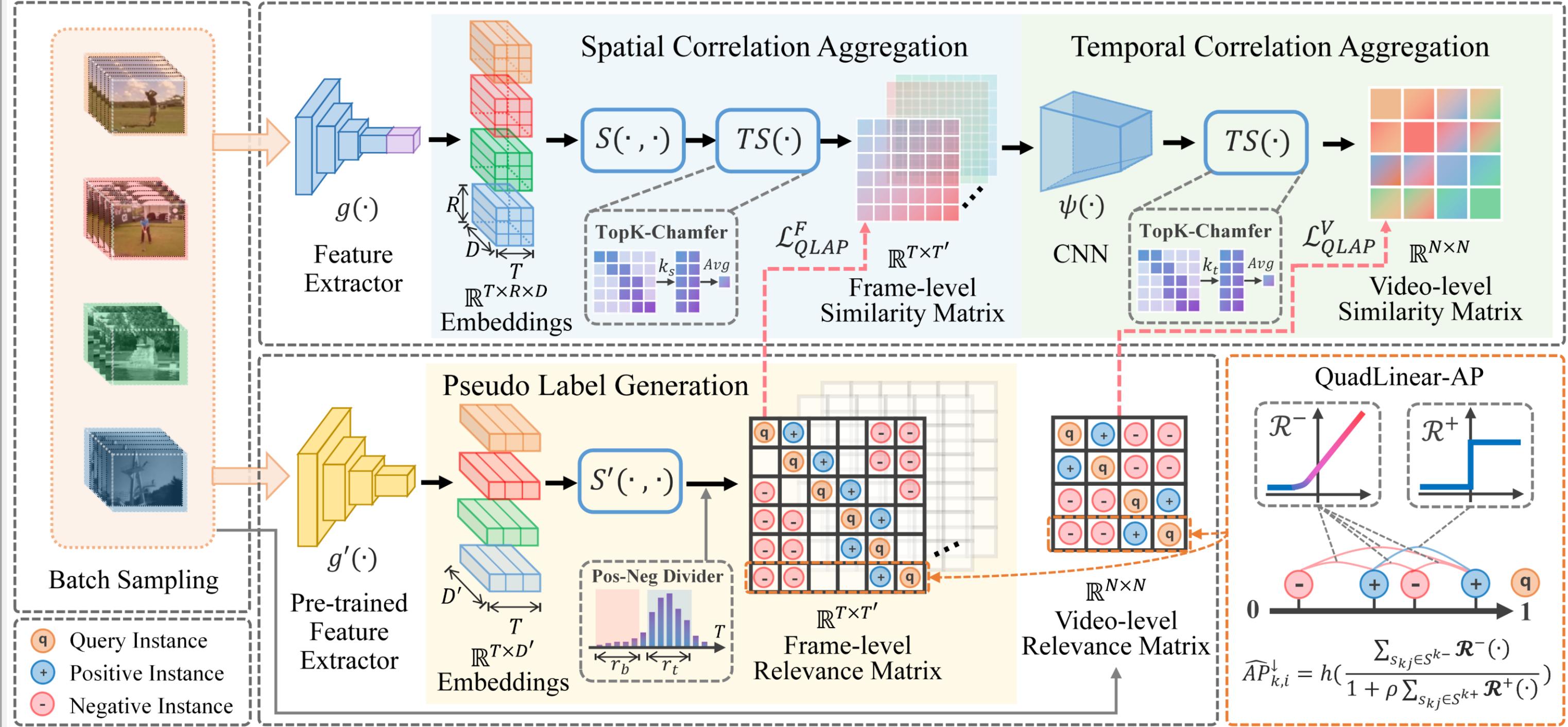
- Differentiable AP optimization
- Suitable gradients for low AP area
- Continuous, Smooth, and Convex
- Monotonically increasing (non-strictly)
- Upper bound of Heaviside function

$$\mathcal{L}_{QLAP} = \frac{1}{N} \sum_{k=1}^N \widehat{AP}_k^{\downarrow}(f)$$

Hierarchical Learning Framework

Overall Framework: HAP-VR

Hierarchical learning for Average-Precision-oriented Video Retrieval



Video-Oriented AP Optimization Algorithm

- Step1: Bottom-up video similarity measure

- Step2: Pseudo-label generation

- Step3: Hierarchical AP optimization

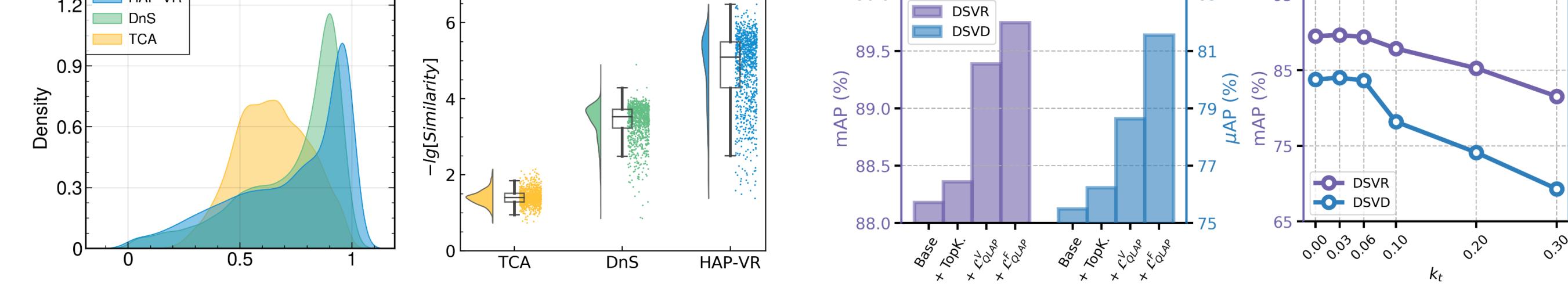
$$\mathcal{L} = \underbrace{\lambda_f \mathcal{L}_{QLAP}^F}_{\text{frame-level}} + \underbrace{\lambda_v \mathcal{L}_{QLAP}^V}_{\text{video-level}} + \mathcal{L}_{base}$$

Evaluation Results

Overall Performance of Our Proposed HAP-VR

HAP-VR improves mAP and μ AP effectively on multiple tasks

Method	Label	Trainset	Retrieval (mAP)			Detection (μ AP)						
			EVVE	SVD	FIVR-200K		EVVE	SVD	FIVR-200K			
			DSVR	CSVVR	ISVR		DSVD	CSVD	ISVD			
DML [†] [32]	✓	VCDB (C&D)	61.10	85.00	52.80	51.40	44.00	75.50	/	39.00	36.50	30.00
TMR [†] [46]	✓	internal	61.80	86.30	52.40	50.70	42.50	/	/	/	/	/
TCA [53]	✓	VCDB (C&D)	63.08	89.82	86.81	82.31	69.61	76.90	56.93	69.09	62.28	49.24
ViSiL [†] [30]	✓	VCDB (C&D)	65.80	88.10	89.90	85.40	72.30	79.10	/	75.80	69.00	53.00
DnS (S _a) [34]	✓	DnS-100K	65.33	90.20	92.09	87.54	74.08	74.56	72.24	79.66	69.51	54.20
DnS (S _b) [34]	✓	DnS-100K	64.41	89.12	90.89	86.28	72.87	75.80	66.53	78.05	68.52	53.48
LAMV [†] [2]	✗	YFCC100M	62.00	88.00	61.90	58.70	47.90	80.60	/	55.40	50.00	38.80
VR [†] [24]	✗	internal	/	/	90.00	85.80	70.90	/	/	/	/	/
ViSiL _f [†] [30]	✗	ImageNet	62.70	/	89.00	84.80	72.10	74.60	/	66.90	59.50	45.90
S ² VS [33]	✗	VCDB (D)	67.17	88.40	92.53	87.73	74.51	80.72	65.04	86.12	77.41	63.26
HAP-VR (Ours)	✗	VCDB (D)	69.15	89.00	92.83	88.21	74.72	82.88	67.87	88.41	79.85	64.79



Effectiveness of Our Proposed QuadLinear-AP

- QuadLinear-AP outperforms previous pair-wise/AP-based losses

Losses	Retrieval (mAP)			Detection (μ AP)		
DSVR	CSVVR	ISVR	DSVD	CSVD	ISVD	

</tbl