**Homework #2**

Due date: 12/11/2022

Notes:

* If you used Python codes for your questions, compress them along with an answer sheet (a docx or pdf file).
* Name your winzip file as “**CS41507\_hw02\_yourname.zip**”
* Attached are “**myntl.py**”, “**lfsr.py**”, “**hw2\_helper.py**”, and “**client.py**” that you can use for the homework questions.
* Use “client.py” to communicate with the server. The main server is located at the campus therefore you need to **connect to the campus network using VPN** **(**ONLY IF YOU ARE OUTSIDE THE CAMPUS**).** Then, you can run your code as usual. See IT website for VPN connections.
* **The server’s IP address** is provided as “http://10.92.55.4:6000”. This IP is provided by default in **client.py.** Check the code.

1. (**18 pts**) Use the Python function ***getQ1***in “**client.py**” given in the assignment package to communicate with the server. The server will send you a number **n** and the number **t**, which is the order of a subgroup of . Please read the comments in the Python code.

Consider the group .

* 1. (**4 pts**) How many elements are there in the group? Send your answer to the server using function *checkQ1a.*
  2. (**8 pts**) Find a generator in . Send your answer to the server using function *checkQ1b.*
  3. (**8 pts**) Consider a subgroup of , whose order is **t**. Find a generator of this subgroup and send the generator to the server using function *checkQ1c.*

1. (**10 pts**) Use the Python code ***getQ2***in “**client.py**” given in the assignment package to communicate with the server. The server will send 2 numbers: **e**, and **c**.

Also, **p** and **q** are given below where n=p×q

p = 129711420978537746088867309342132426785901989689874594485896371555019986573705426172788805726178509467748040679168734095884433597017604012172054368990172572715857537355524013819947862920969421702067385445122242673064958991968666138544380365520456029952414962028711806175784928131826127885820644091951344318387

q = 174066672405085972657808881778978520582809763235147358374332409966322987290745416405220414323004782906757362579157117914494927198442645581197584273451379119673753279114693557694861941678350357667191083878100828920198503774539271289263633646647364198130180304138099281532660260760636194367337370132530987351081

Knowing that **d = e-1 mod φ(n)**. Compute **m = cd mod n**. Decode m into Unicode string and send the text you found to the server using the function ***checkQ2***.

1. (**18 pts**) Consider the following attack scenario. You obtained following ciphertexts that are encrypted using SALSA20 and want to obtain the plaintexts. Luckily, owner of the messages is lazy and uses same key and nonce for all the messages. You also know that the owner uses a 64-bit number the key.

**Key**: 14656892184006070584

**ciphertext 1:**

b"Vbq\x8a\xe3\xb7Rgl-\x14\x8bNS\xeb\x01\xbd\xdf\x1f\x14\x84{\xdanX,\xa5\x98RM\x98\r\xd7\x1e\x9dO\x14\xa7\x8cX\xcb\xad\xf2\xc9\x1f\xc1]\xef\x908I\xe0\xcf\x10%.ulh\xe7\xd6\x9d<\xb9a\xda\xb0\xa2d\xe9\x18\xef9\x99ttP\x9blw\x0e\xe7\xd6\xbb1\xf4?\x16kf\x87\x19\xbe\x94O\xe8\x1d\x08\xe4\xff)\x99']\xda\x191=|H"

**ciphertext 2:**

b'\eda\x01q+]\x8c\x06[\xa2/\xb8\xcaX\x1f\x8f:\xc97\x0f)\xa5\x84Y\t\xdc\x07\xd2L\xb3V\x14\xad\x8bU\x99\xa3\xf2\x9dK\xc8V\xab\xdd\nS\xe9\xcf\x05$r,\t<\x9e\xd0\x9b<\xbcx\x99\xaf\xed7\xf9\x13\xff9\x88r \\\x9b}>\x1d\xeb'

**ciphertext 3:** b'ea,\x14\x88NW\xbfh\xb9\xcdX\x0f\x83}\xc0cX5\xa5\x9e\x1e^\xd0\x03\xc5\x1e\xa3U@\xa1\x85H\xc0'

However, during the transmission of the ciphertexts, some bytes of 2 out of the 3 messages were corrupted. One or more bytes of the nonce parts are missing.

Attack the ciphertexts and find the messages. (See the Python code **salsa.py** in SUcourse+ to get your hands on this stream cipher).

(Hint: You can assume new Salsa instance is created for each encryption operation)

1. **(12 pts)** Solve the following equations of the form ax ≡ b mod n and find all solutions for x if a solution exists. Explain the steps and the results.
   1. n = 1593089977489628213419978935847037520292814625191902216371975

a = 1085484459548069946264190994325065981547479490357385174198606

b = 953189746439821656094084356255725844528749341834716784445794

* 1. n = 1604381279648013370121337611949677864830039917668320704906912

a = 363513302982222769246854729203529628172715297372073676369299

b = 1306899432917281278335140993361301678049317527759257978568241

* 1. n = 591375382219300240363628802132113226233154663323164696317092

a = 1143601365013264416361441429727110867366620091483828932889862

b = 368444135753187037947211618249879699701466381631559610698826

* 1. n = 72223241701063812950018534557861370515090379790101401906496

a = 798442746309714903219853299207137826650460450190001016593820

b = 263077027284763417836483401088884721142505761791336585685868

1. (**10 pts**) Consider the following binary connections polynomials for LFSR:

p1(x) = x6 + x5 + x4 + x+ 1

p2(x) = x6 + x2 + 1

p3(x) = x5 + x3 + 1

Do they generate maximum period sequences? (**Hint:** You can use the functions in lfsr.py)

1. (**12 pts**) Consider the following sequences that are generated using different random number generators. Which of sequences are predictable? (**Hint:** You can use the functions in lfsr.py)

x1 = [0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1, 0, 0, 0, 1, 1, 1, 0, 1, 1, 0, 0, 0, 0, 1, 1, 0, 0, 1, 0, 1, 0, 0, 0, 1, 0, 1, 1, 1, 0, 1, 0, 1, 0, 0, 0, 1, 0, 1, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0, 1, 1, 1, 0, 1, 1, 0, 1, 0, 1, 1, 0, 0]

x2 = [0, 1, 1, 0, 0, 0, 1, 0, 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 0, 0, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 0, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 1]

x3 = [1, 0, 0, 0, 0, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0, 1, 0, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 1, 1, 1, 0, 1, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 1, 1, 1, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1, 1, 1, 1, 0, 0, 0, 1, 1, 1, 0, 0, 1, 0, 0, 1, 0, 1, 0, 0, 1]

1. (**20 pts**) Consider the following ciphertext bit stream encrypted using a stream cipher. And you strongly suspect that an LFRS is used to generate the key stream:

ctext =

[1, 1, 0, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 1, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 0, 0, 1, 0, 1, 1, 1, 0, 0, 0, 0, 1, 1, 1, 1, 1, 0, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 0, 1, 0, 1, 1, 1, 1, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 0, 1, 1, 1, 0, 0, 0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1, 1, 0, 1, 1, 1, 1, 0, 0, 0, 1, 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1, 1, 0, 0, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 0, 1, 0, 0, 0, 1, 1, 1, 0, 1, 0, 1, 1, 1, 0, 0, 1, 0, 0, 1, 1, 0, 0, 1, 0, 0, 0, 0, 0, 1, 1, 0, 1, 0, 0, 0, 0, 1, 1, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0, 0, 1, 0, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 0, 1, 1, 1, 1, 0, 1, 0, 1, 0, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 0, 0, 1, 1, 1, 0, 0, 1, 1, 0, 0, 1, 1, 1, 0, 1, 0, 0, 0, 0, 1, 0, 1, 0, 1, 1, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 1, 0, 1, 1, 1, 1, 0, 1, 0, 1, 0, 0, 1, 1, 1, 1, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1, 1, 1, 0, 1, 1, 0, 0, 0, 0, 1, 1, 0, 0, 1, 0, 1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 0, 0, 1, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 1, 0, 1, 1, 0, 1, 1, 1, 0, 0, 0, 1, 0, 1, 0, 0, 1, 0, 1, 0, 0, 0, 1, 1, 0, 0, 1, 0, 0, 0, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 0, 1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 1, 1, 0, 1, 0, 1, 0, 0, 0, 0, 1, 0, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 1, 1, 0, 1, 0, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 1, 1, 0, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 0, 1, 1, 1, 0, 1, 0, 1, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0, 1, 1, 1, 0, 1, 0, 1, 1, 1, 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 0, 1, 0, 1, 1, 0, 0, 0, 0, 1, 1, 0, 0, 1, 1, 1, 1, 0, 1, 0, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 1, 0, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1, 0, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 1, 1, 0, 1, 0, 0, 1, 0, 0, 1, 1, 1, 1, 0, 1, 0, 0, 0, 1, 1, 1, 0, 1, 0, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 0, 1, 1, 1, 1, 1, 0, 0, 0, 1, 1, 0, 1, 1, 0, 0, 0, 1, 0, 1, 0, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0, 1, 0, 0, 1, 0, 1, 1, 1, 1, 1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 1, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1, 1, 1, 1]

Also, encrypted in the ciphertext you also know that there is a message to you from the instructor; and therefore, the message ends with the instructor’s name. Try to find the connection polynomial and plaintext. Is it possible to find them? Explain if it is not.

Note that the ASCII encoding (seven bits for each sASCII character) is used.

**(Hint:** You can use the ASCII2bin(msg) and bin2ASCII(msg) functions in (**hw2\_helper.py**) to make conversion between ASCII and binary)