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```
clear all; clc;

% system of linear equations

%  $4x - y + z = 7$ 
%  $4x - 8y + z = -21$ 
%  $-2x + y + 5z = 15$ 
%  $AX = B$ 

% A matrix should be strictly diagonally dominant

A = [4 -1 1
      4 -8 1
      -2 1 5];

B = [7;-21;15];
N = length(B);

maxI = 100;
delta = 1e-6;

P0 = [1;2;2];
P = P0;
X = zeros(N,maxI);
for k=1:maxI % until it converges
    for j = 1:N % number of variables
        if j == 1
            X(j,k) = (B(j) - A(j,j+1:N)*P([j+1:N]))/A(j,j);
        elseif j == N
            X(j,k) = (B(j) - A(j,1:j-1)*X(1:j-1,k))/A(j,j);
        else
            X(j,k) = (B(j) - A(j,1:j-1)*X(1:j-1,k) - A(j,j+1:N)*P(j+1:N))/
A(j,j);
        end
    end
    err = norm(X(:,k)-P);
    relerr = err/(norm(X(:,k) + delta));
    P = X(:,k);
    if (err < delta) && (relerr < delta)
        break
    end
end

k = (0:1:k)';
x_k = [P0(1) X(1,1:k(end))]'';
y_k = [P0(2) X(2,1:k(end))]'';
z_k = [P0(3) X(3,1:k(end))]'';

Data = [k,x_k,y_k,z_k]
```

Data =

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|        |        |        |        |
|--------|--------|--------|--------|
| 0      | 1.0000 | 2.0000 | 2.0000 |
| 1.0000 | 1.7500 | 3.7500 | 2.9500 |
| 2.0000 | 1.9500 | 3.9688 | 2.9863 |
| 3.0000 | 1.9956 | 3.9961 | 2.9990 |
| 4.0000 | 1.9993 | 3.9995 | 2.9998 |
| 5.0000 | 1.9999 | 3.9999 | 3.0000 |
| 6.0000 | 2.0000 | 4.0000 | 3.0000 |
| 7.0000 | 2.0000 | 4.0000 | 3.0000 |
| 8.0000 | 2.0000 | 4.0000 | 3.0000 |
| 9.0000 | 2.0000 | 4.0000 | 3.0000 |

*Published with MATLAB® R2021b*