

# Individual Fairness in Online Classification

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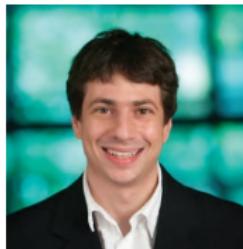
## **“Metric-Free Individual Fairness in Online Learning”**

Joint with Christopher Jung and Steven Wu. NeurIPS 2020 Oral.



## **“Individually Fair Learning with One-Sided Feedback”**

Joint with Aaron Roth. ICML 2023.



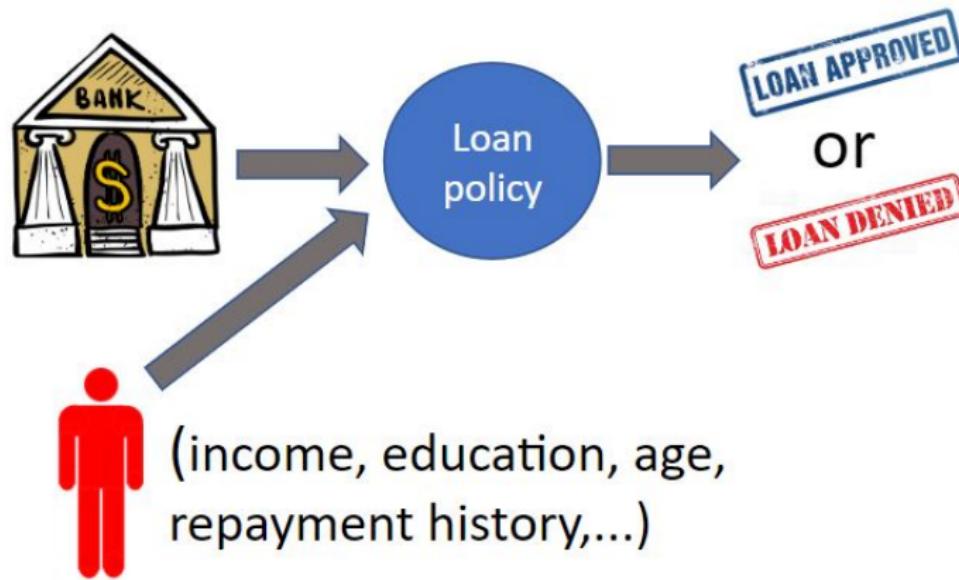
# High-Level Plan

- ① Re-examine commonly made assumptions regarding:
  - ▶ The level on which fairness is defined
  - ▶ The data generation process
  - ▶ The feedback model

# Running Example

## Example: **Loan Approvals**

For incoming loan applicants, predict whether each individual will **repay** or **default** on payments.



# Focus #1: Group Fairness Offers Weak Guarantees

The bulk of research in algorithmic fairness considers definitions that only bind on a **group level**.

## Statistical fairness

- Select a statistic (accuracy, FPR/FNR, PPV, . . . ).
- Define a set of groups in the population.
- (Approximately) equalize the statistic across groups.

## Focus #1: Group Fairness Offers Weak Guarantees

- Advantage: relatively easy to work with.
- Disadvantage: very weak guarantees **for individuals**.

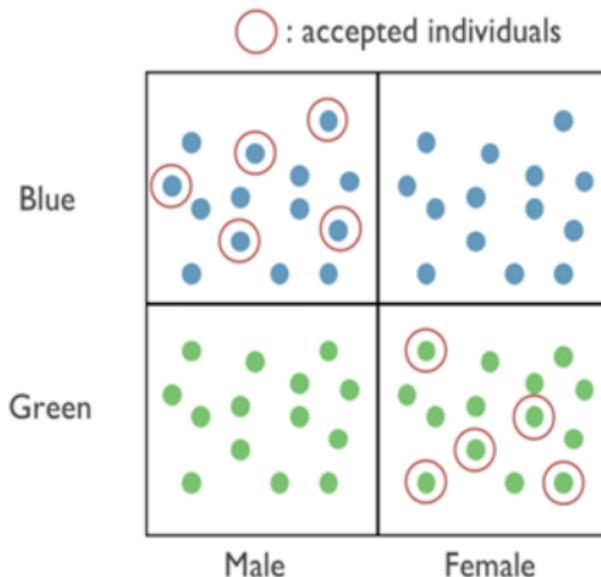


Figure: Fairness Gerrymandering: A Toy Example [Kearns et al., 2018]

## Focus #2: Standard Statistical Assumptions May Not Always Apply

The majority of the work in algorithmic fairness operates under **statistical data generation assumptions**.

However: in various setting where fairness is a major concern, arriving individuals may not necessarily follow i.i.d. assumptions, due to, e.g.:

- Strategic effects (feature modifications based on knowledge/in anticipation of a specific policy, choosing whether to apply based on the policy in effect).

# Learning in the Presence of Strategic Behavior

Individuals would like to receive

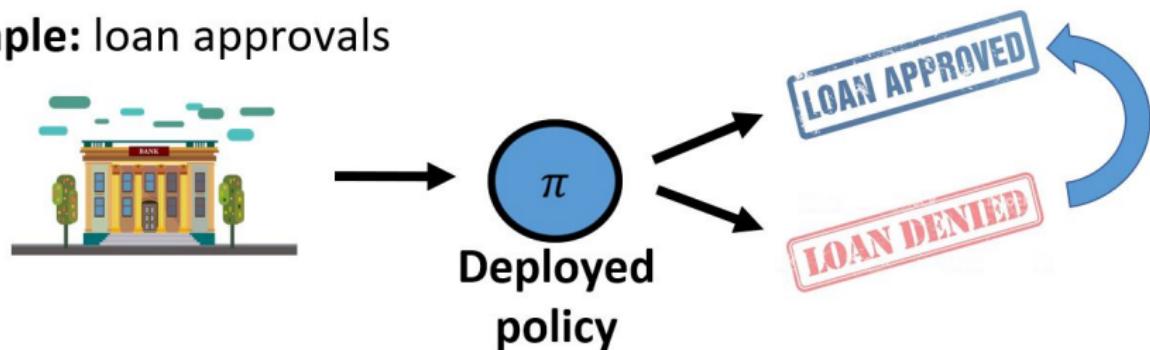
**more favorable** assessments

→ Act strategically

→ Strategic feature modifications



**Example:** loan approvals



# Strategic Feature Modifications

5 Ways to Improve Your Credit Score Fast

Watch later Share

# BOOST YOUR CREDIT SCORE FAST!

Excellent

Poor

Watch on YouTube

A YouTube thumbnail featuring a black background. On the left, there's a green circular icon with a white letter 'C'. To its right, the title "5 Ways to Improve Your Credit Score Fast" is displayed. In the top right corner are two buttons: "Watch later" with a clock icon and "Share" with a share icon. The central part of the thumbnail features the text "BOOST YOUR CREDIT SCORE FAST!" in large, bold, white letters. A red arrow points upwards through a small red YouTube play button icon. To the right of the text is a horizontal bar chart with five colored segments: green (labeled "Excellent"), teal, yellow, orange, and red (labeled "Poor"). At the bottom left, a black bar contains the text "Watch on YouTube".

# Strategic Feature Modifications



Obtain additional credit cards

Raise your credit limits

...

Reduce your debt

Increase your income

...





- SCHUFA is Germany's leading credit bureau.
- SCHUFA has 943 million records on 67.7 million natural persons, and 6 million companies. Schufa processes more than 165 million credit checks each year. Of those, 2.5 million are self-checks by citizens. Schufa employs 900 people (as of 2019). In 2016 Sales amounted to approx. 190 million Euros.



ein Projekt von



ALGORITHM  
WATCH

und



## OpenSCHUFA: The campaign is over, the problems remain – what we expect from SCHUFA and Minister Barley



[Results](#) · [Our demands](#) · [Press review](#) · [Deutsch](#)

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“We were able to motivate more than 4,000 people to provide us with their SCHUFA information – very sensitive information that people usually keep to themselves.”

# Beyond Standard Statistical Assumptions

Arriving individuals may not necessarily follow i.i.d. assumptions:

- Strategic effects (feature modifications based on knowledge/in anticipation of a specific policy, choosing whether to apply based on the policy in effect).
- distribution shifts over time (e.g. ability to repay a loan may be affected by changes to the economy or recent events).
- Adaptivity to previous decisions (e.g. if an individual receives a loan, that may affect the ability to repay future loans by this individual or his/her vicinity).

## Focus #3: Feedback May Not Be Fully Observable

The bulk of the literature on algorithmic fairness operates in either:

- Batch setting
- Online setting with full information
- Bandit setting

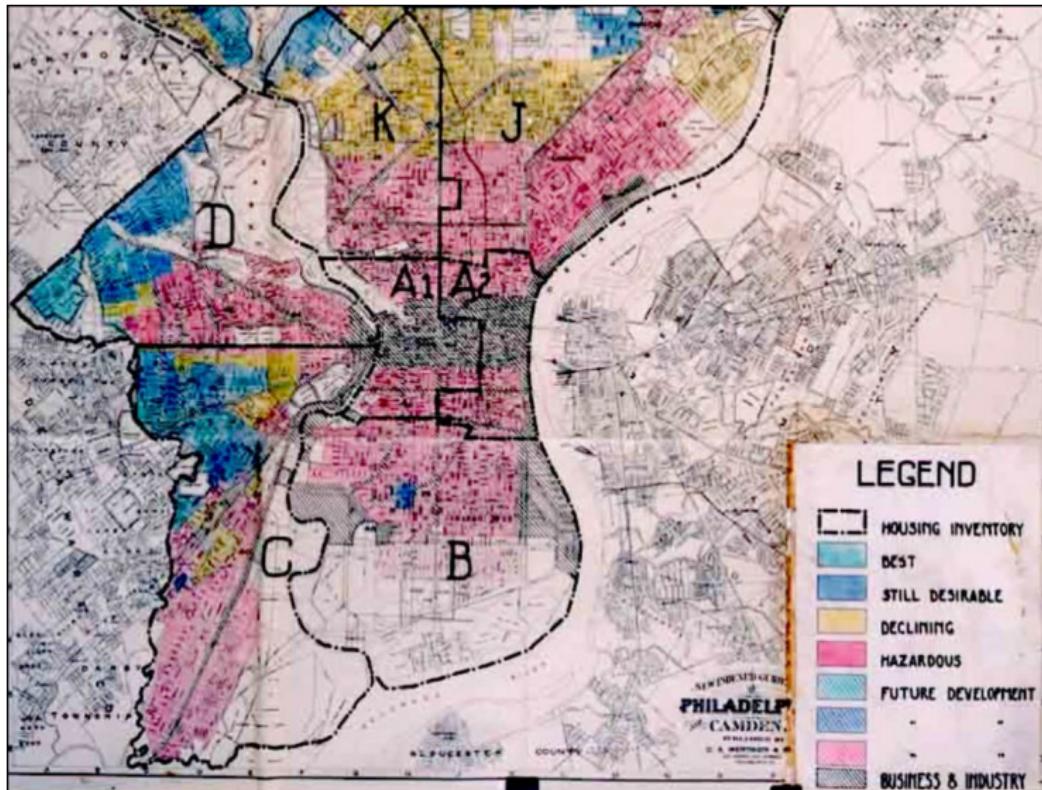
## Focus #3: Feedback May Not Be Fully Observable

However, in many domains where fairness is a major concern, feedback may arrive for **positively predicted** individuals only. Cannot observe counterfactuals.

- Loan approvals
- College admissions
- Hiring for jobs
- Online advertising
- ...

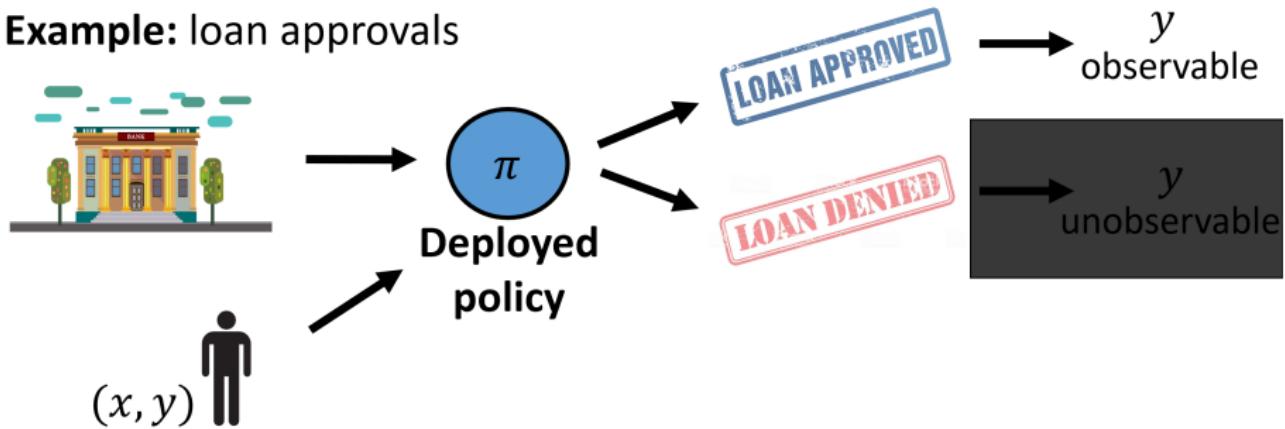
⇒ Batch setting - data could be “skewed” to only include individuals accepted by past policy. In particular, if not careful, could inherit biases of historical discriminatory policies.

# Redlining



# One-Sided Feedback

Example: loan approvals



This is **not** a bandit setting!

# High-Level Plan

- ➊ Re-examine the assumptions commonly made regarding:
  - ▶ The level on which fairness is defined
  - ▶ The data generation process
  - ▶ The feedback model
- ➋ Design efficient algorithms that:
  - ▶ Offer meaningful guarantees to individuals
  - ▶ Operate beyond standard statistical assumptions
  - ▶ Can handle limited feedback

# Outline

- Fairness Framework: Metric-Free Individual Fairness via Panels
- Individually Fair Online Batch Classification
- Reduction to Contextual Combinatorial Semi-Bandit
- Multi-Criteria No Regret Guarantees for Accuracy, Fairness
- Oracle-Efficient Algorithm

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# Individual Fairness

Dwork et al. 2011: “Fairness Through Awareness”

“Similar individuals should be treated similarly.”

$$\underbrace{|h(x) - h(x')|}_{\text{Diff. in predictions}} \leq \underbrace{d(x, x')}_{\text{Distance}}$$

$h : \mathcal{X} \rightarrow [0, 1]$  “soft” predictor.

**Assumption:** Access to similarity metric between individuals:

$$d : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}^+$$

# Challenges in Operationalizing Individual Fairness

**Problem:** Similarity metric is often **unavailable**.

- Unclear where such metric can be found.
- People have different opinions of who are similarly situated in the context of specific tasks.
- Even if an individual has a clear idea of which individuals are similarly situated, an exact mathematical formula for the metric might be **difficult to enunciate**.

# Difficulty of Enunciating a Metric

“What is the **exact** formula that measures similarity for loan applicants?”

“Hard to tell...”

# Difficulty of Answering Numerical Queries

“What is the distance between individuals #5 and #17?”

“Still Difficult for me to answer exactly.”

# Human Auditor for Fairness Violations

“Can you spot a pair of **similar** individuals who were treated **very differently**? ”

“Yes. Individuals #5 and #17.”



Auditor “**knows unfairness when he sees it.**”

**Auditor**

## Prior Work on Individual Fairness

- Dwork, Hardt, Pitassi, Reingold, Zemel, 2011: Conceptual introduction of individual fairness, relying on the availability of a similarity metric.
- Rothblum and Yona 2018: Assume metric is given, provide generalization results for accuracy and fairness in batch setting.
- Ilvento 2020: Learning the metric via distance and numerical comparison queries to human arbiters.
- Kim, Reingold, Rothblum, 2018: Group-based relaxation of individual fairness, relying on access to an auditor returning unbiased estimates of distances between pairs of individuals
- Gillen, Jung, Kearns, Roth, 2018: Auditor “knows unfairness when he sees it”. Assume specific parametric form of metric, auditor must report all violations on a given round.

# Model and Definitions

- $\mathcal{X}$  instance space.
- $\mathcal{Y} = \{0, 1\}$  label space.
- $\mathcal{H} : \mathcal{X} \rightarrow \mathcal{Y}$  hypothesis class.
- Assume  $\mathcal{H}$  contains a constant hypothesis – i.e.  $h$  such that  $h(x) = 0$  for all  $x \in \mathcal{X}$ .
- We allow for convex combinations of hypotheses for the purpose of randomizing the prediction and denote the simplex of hypotheses by  $\Delta\mathcal{H} : \mathcal{X} \rightarrow [0, 1]$ .
- For each prediction  $\hat{y} \in \mathcal{Y}$  and true label  $y \in \mathcal{Y}$ , there is an associated misclassification loss,  $\ell(\hat{y}, y) = \mathbb{1}(\hat{y} \neq y)$ .
- We overload notation and write, for  $\pi \in \Delta\mathcal{H}$ :

$$\ell(\pi(x), y) = (1 - \pi(x)) \cdot y + \pi(x) \cdot (1 - y) = \mathop{\mathbb{E}}_{h \sim \pi} [\ell(h(x), y)].$$

# Individual Fairness

- We assume that there is a distance function  $d : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}^+$  which captures the distance between individuals in  $\mathcal{X}$ .

## Definition ( $\alpha$ -fairness violation)

Let  $\alpha \geq 0$  and let  $d : \mathcal{X} \times \mathcal{X} \rightarrow [0, 1]$ . We say that a policy  $\pi \in \Delta \mathcal{H}$  has an  $\alpha$ -fairness violation (or simply “ $\alpha$ -violation”) on  $(x, x') \in \mathcal{X}^2$  with respect to  $d$  if

$$\pi(x) - \pi(x') > d(x, x') + \alpha.$$

where  $\pi(x) = \Pr_{h \sim \pi}[h(x) = 1]$ .

# Auditor

- An auditor reports **one**  $\alpha$ -violation if one or more exists.

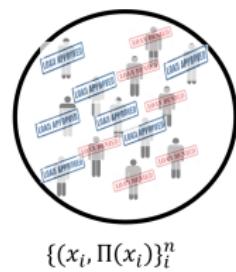
## Definition (Auditor)

Let  $\alpha \geq 0$ . We define a fairness auditor  $j^\alpha \in \mathcal{J}$  by,  $\forall \pi \in \Delta \mathcal{H}, \bar{x} \in \mathcal{X}^k$ ,

$$j^\alpha(\pi, \bar{x}) := \begin{cases} (\bar{x}^s, \bar{x}^l) \in V^j & \text{if } V^j := \{(\bar{x}^s, \bar{x}^l) : s \neq l \in [k], \\ & \pi(\bar{x}^s) - \pi(\bar{x}^l) > d^j(x, x') + \alpha\} \neq \emptyset, \\ (\nu, \nu) & \text{otherwise} \end{cases}$$

where  $\bar{x} = (\bar{x}^1, \dots, \bar{x}^k)$ ,  $d^j : \mathcal{X} \times \mathcal{X} \rightarrow [0, 1]$  is auditor  $j^\alpha$ 's (implicit) distance function, and  $\nu \in \mathcal{X}$  is some “default” context.

# Auditor



**Auditor $_{\alpha}$**

**(Features, Predictions)**

Individuals 5 and 17 are being treated unfairly

$$|\pi(x_5) - \pi(x_{17})| > d(x_5, x_{17}) + \alpha$$

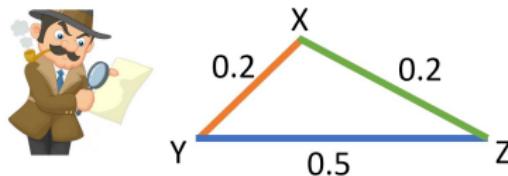
Or

I don't see any unfair treatments here.

**Fairness Feedback**

# Metric-Free Individual Fairness

**Q:** Auditors' preferences may be inconsistent. What if the specified feedback from the auditor does not obey metric form?



- In our formulation,  $d$  need not necessarily be a **metric**:
  - ▶  $d$  doesn't have to satisfy the triangle inequality.
  - ▶ The only two requirements on  $d$  is that it is always non-negative and symmetric.
- Furthermore, we place **no parametric assumptions** on  $d$ .

# How Should We Audit for Unfairness?

**So far:** single auditor, no metric assumption

**However:** unlikely that stakeholders would rely on a single auditor regarding fairness related judgements, especially in high-stakes domains:

- Human auditors may have implicit biases based on many factors: background, socio-economic level, education level, etc.
- A static auditing scheme may risk leaving too much power in the hands of the same (few) individuals over time.
- Practically speaking, may be infeasible for the same auditor to examine more than a certain amount of cases in a specific period of time.

# Our Approach: Dynamic Auditing by Panels

We propose an auditing scheme based on dynamically-selected panels of multiple auditors.



## Example:

- Ethicists familiar with the history of redlining
- Financial experts
- ...

# Handling Inconsistent Judgements

**Q:** In case judgments of different auditors are inconsistent with each other, how should we handle disagreements?

## Definition $((\alpha, \gamma)$ -fairness violation)

Let  $\alpha \geq 0$ ,  $0 \leq \gamma \leq 1$ ,  $m \in \mathbb{N} \setminus \{0\}$ . We say that a policy  $\pi \in \Delta \mathcal{H}$  has an  $(\alpha, \gamma)$ -fairness violation on  $(x, x') \in \mathcal{X}^2$  with respect to  $d^1, \dots, d^m : \mathcal{X}^2 \rightarrow [0, 1]$  if

$$\frac{1}{m} \sum_{i=1}^m \mathbb{1} [\pi(x) - \pi(x') - d^i(x, x') > \alpha] \geq \gamma.$$

# Auditing by Panels

## Definition (Panel)

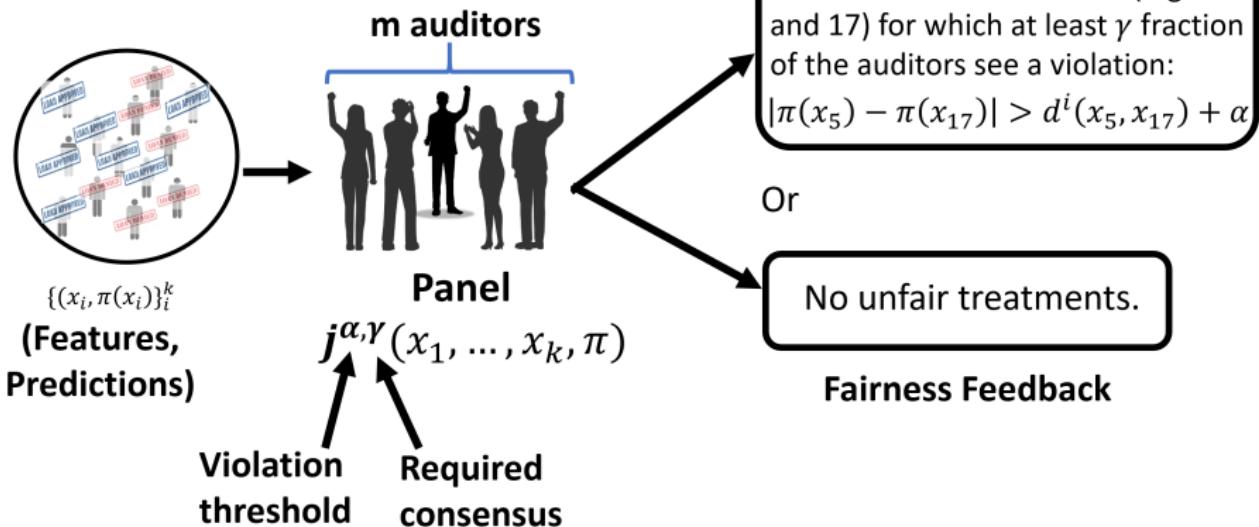
Let  $\alpha \geq 0$ ,  $0 \leq \gamma \leq 1$ ,  $m \in \mathbb{N} \setminus \{0\}$ . We define a fairness panel  $\bar{j}^{\alpha, \gamma}$  by,  
 $\forall \pi \in \Delta \mathcal{H}, \bar{x} \in \mathcal{X}^k$ ,

$$\bar{j}_{j_1, \dots, j_m}^{\alpha, \gamma}(\pi, \bar{x}) = \begin{cases} (\bar{x}^s, \bar{x}^l) \in V^{\bar{j}} & \text{if } V^{\bar{j}} := \{(\bar{x}^s, \bar{x}^l) : s \neq l \in [k] \wedge \exists i_1, \dots, i_{\lceil \gamma m \rceil} \in [m] \\ & \forall s \in [\lceil \gamma m \rceil], (\bar{x}^s, \bar{x}^{i_s}) \in V^{j^{i_s}}\} \neq \emptyset \\ (v, v) & \text{otherwise} \end{cases}$$

where  $\bar{x} := (\bar{x}^1, \dots, \bar{x}^k)$ ,  $d^j : \mathcal{X} \times \mathcal{X} \rightarrow [0, 1]$  is auditor  $j$ 's (implicit) distance function, and  $v \in \mathcal{X}$  is some “default” context.  $\bar{j}$ .

- Can vary  $\gamma$  and **algorithmically** explore the trade-off.

# Auditing by Panels



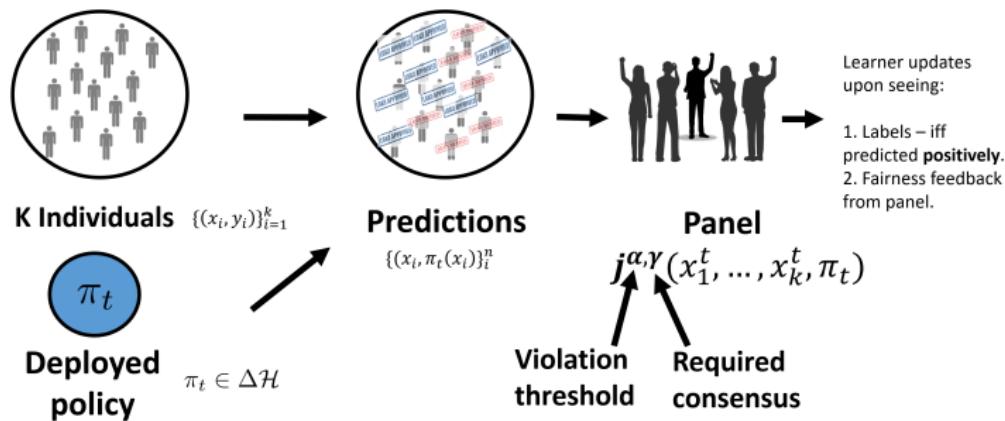
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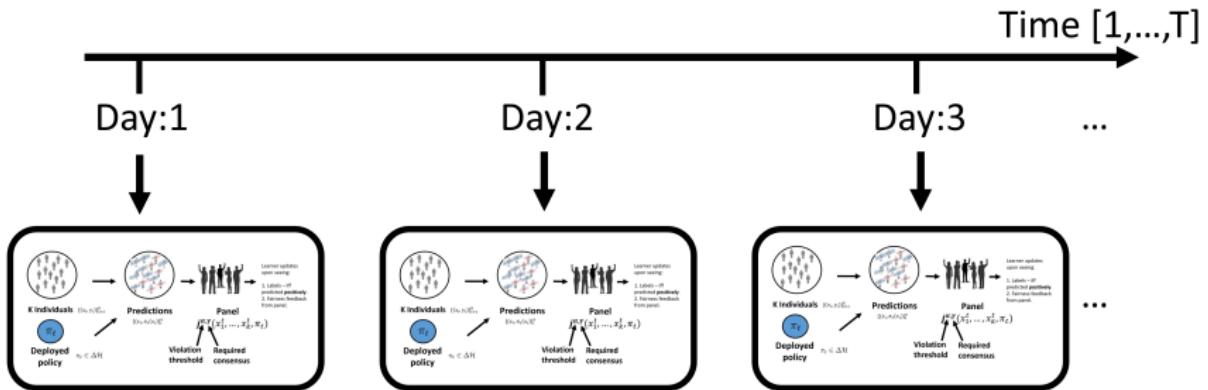
# Our Setting

- Online classification
- Arriving individuals:
  - ▶ Possibly adversarial
  - ▶ Possibly multiple arrivals each round
  - ▶ Label information for positive predictions only
- Auditing panels:
  - ▶ Dynamically selected

## Individually fair online batch classification: single round



# Our Setting



# Individually fair online batch classification with one-sided feedback

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**Algorithm 1:** Individually fair online batch classification with one-sided feedback

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**Input:** Number of rounds  $T$ , hypothesis class  $\mathcal{H}$ ;

Learner initializes  $\pi^1 \in \Delta\mathcal{H}$ ;

**for**  $t = 1, \dots, T$  **do**

    Environment selects individuals  $\bar{x}^t \in \mathcal{X}^k$ , and labels  $\bar{y}^t \in \mathcal{Y}^k$ , learner only observes  $\bar{x}^t$ ;

    Environment selects panel of auditors  $(j^{t,1}, \dots, j^{t,m}) \in \mathcal{J}^m$ ;

    Learner draws  $h^t \sim \pi^t$ , predicts  $\hat{y}^{t,i} = h^t(\bar{x}^{t,i})$  for each  $i \in [k]$ , observes  $\bar{y}^{t,i}$  iff  $\hat{y}^{t,i} = 1$ ;

    Panel reports its feedback  $\rho^t = \bar{j}_{j^t_1, \dots, j^t_m}^{t,\alpha,\gamma}(\pi^t, \bar{x}^t)$ ;

    Learner suffers misclassification loss  $Error(h^t, \bar{x}^t, \bar{y}^t)$  (not necessarily observed by learner);

    Learner suffers unfairness loss  $Unfair(\pi^t, \bar{x}^t, \bar{j}^t)$ ;

    Learner updates  $\pi^{t+1} \in \Delta\mathcal{H}$ ;

**end**

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# Online Fair Batch Classification

## Definition (Misclassification loss)

We define the misclassification loss as, for all  $\pi \in \Delta\mathcal{H}$ ,  $\bar{x} \in \mathcal{X}^k$ ,  $\bar{y} \in \{0, 1\}^k$  as:

$$Error(\pi, \bar{x}, \bar{y}) := \mathbb{E}_{h \sim \pi} [\ell^{0-1}(h, \bar{x}, \bar{y})].$$

Where for all  $h \in \mathcal{H}$ ,  $\ell^{0-1}(h, \bar{x}, \bar{y}) := \sum_{i=1}^k \ell^{0-1}(h, (\bar{x}^i, \bar{y}^i))$ , and  
 $\forall i \in [k] : \ell^{0-1}(h, (\bar{x}^i, \bar{y}^i)) = \mathbb{1}[h(\bar{x}^i) \neq \bar{y}^i]$ .

## Definition (Unfairness loss)

Let  $\alpha \geq 0$ ,  $0 \leq \gamma \leq 1$ . We define the unfairness loss as, for all  $\pi \in \Delta\mathcal{H}$ ,  $\bar{x} \in \mathcal{X}^k$ ,  
 $\bar{j} = \bar{j}^{\alpha, \gamma}_{j^1, \dots, j^m} : \mathcal{X}^k \rightarrow \mathcal{X}^2$ ,

$$Unfair^{\alpha, \gamma}(\pi, \bar{x}, \bar{j}) := \begin{cases} 1 & \bar{j}(\pi, \bar{x}) = (\bar{x}^s, \bar{x}^l) \wedge s \neq l \\ 0 & \text{otherwise} \end{cases},$$

where  $\bar{x} := (\bar{x}^1, \dots, \bar{x}^k)$ .

# Lagrangian Loss

## Definition (Lagrangian loss)

Let  $C > 0$ ,  $\rho = (\rho^1, \rho^2) \in \mathcal{X}^2$ . We define the  $(C, \rho)$ -Lagrangian loss as, for all  $\pi \in \Delta \mathcal{H}$ ,  $\bar{x} \in \mathcal{X}^k$ ,  $\bar{y} \in \{0, 1\}^k$ ,

$$L_{C,\rho}(\pi, \bar{x}, \bar{y}) := \text{Error}(\pi, \bar{x}, \bar{y}) + C \cdot [\pi(\rho^1) - \pi(\rho^2)].$$

Linear in  $\Delta \mathcal{H}$ .

# Regret

## Definition (Error regret)

We define the error regret of an algorithm  $\mathcal{A}$  against a comparator class  $U \subseteq \Delta\mathcal{H}$  to be

$$\text{Regret}^{\text{err}}(\mathcal{A}, T, U) = \sum_{t=1}^T \text{Error}(\pi^t, \bar{x}^t, \bar{y}^t) - \min_{\pi^* \in U} \sum_{t=1}^T \text{Error}(\pi^*, \bar{x}^t, \bar{y}^t).$$

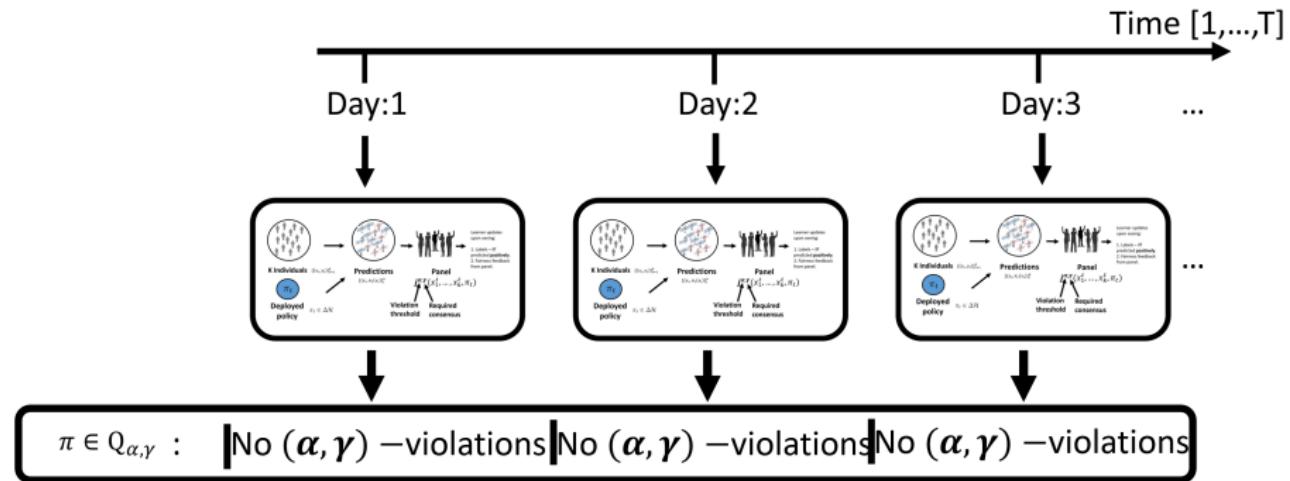
## Definition (Unfairness regret)

Let  $\alpha \geq 0$ ,  $0 \leq \gamma \leq 1$ . We define the unfairness regret of an algorithm  $\mathcal{A}$  against a comparator class  $U \subseteq \Delta\mathcal{H}$  to be

$$\text{Regret}^{\text{unfair}, \alpha, \gamma}(\mathcal{A}, T, U) = \sum_{t=1}^T \text{Unfair}^{\alpha, \gamma}(\pi^t, \bar{x}^t, \bar{j}^t) - \min_{\pi^* \in U} \sum_{t=1}^T \text{Unfair}^{\alpha, \gamma}(\pi^*, \bar{x}^t, \bar{j}^t).$$

# Measuring Performance

“Competing” against most accurate policy that does not violate individual fairness.



# Measuring Performance

We wish to compare performance with the highest-performing policy that is individually fair.

## Definition $((\alpha, \gamma)$ -fair policies)

Let  $\alpha \geq 0$ ,  $0 \leq \gamma \leq 1$ ,  $m \in \mathbb{N} \setminus \{0\}$ . We denote the set of all  $(\alpha, \gamma)$ -fair policies with respect to all of the rounds in the run of the algorithm as

$$Q_{\alpha, \gamma} := \left\{ \pi \in \Delta \mathcal{H} : \forall t \in [T], \bar{j}_{j^{t,1}, \dots, j^{t,m}}^{t, \alpha, \gamma}(\pi, \bar{x}^t) = (v, v) \right\}.$$

- Class is only defined **in hindsight** - realization is over both arriving individuals and panel members.

# Simultaneous No-Regret Guarantees

We want, **simultaneously**:

① **Accuracy:**

$$\text{Regret}^{\text{err}}(\mathcal{A}, T, Q_{\alpha, \gamma}) = o(T).$$

② **Fairness:**

$$\text{Regret}^{\text{unfair}, \alpha, \gamma}(\mathcal{A}, T, Q_{\alpha, \gamma}) = o(T).$$

We know:

Gillen, Jung, Kearns, Roth (2018) - If auditor's judgements are according to a metric, of **particular parametric form** (Mahalanobis), and reports **all violations** - this is possible (with fast, logarithmic rate for the fairness regret).

**Q:** Can we still achieve simultaneous sub-linear rates under:

- no parametric or metric assumptions?
- auditor not reporting **all** violations?

# Solution Strategy

- ① Construct a reduction from our setting to the contextual combinatorial semi-bandit problem.
- ② Show that, under certain conditions, the Lagrangian loss may be used to upper bound both error and unfairness losses.
- ③ Propose an oracle efficient algorithm by adapting Context-Semi-Bandit-FTPL (Syrgkanis et al. 2016), which would allow invoking our reduction.

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# Contextual Combinatorial Semi-Bandit

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**Algorithm 2:** Contextual Combinatorial Semi-Bandit

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**Parameters:** Class of predictors  $\mathcal{H}$ , number of rounds  $T$ ;

Learner deploys  $\pi^1 \in \Delta\mathcal{H}$ ;

**for**  $t = 1, \dots, T$  **do**

Environment selects loss vector  $\ell^t \in [0, 1]^k$  (without revealing it to learner);

Environment selects contexts  $\bar{x}^t \in \mathcal{X}^k$ , and reveals them to the learner;

Learner draws action  $a^t \in A^t \subseteq \{0, 1\}^k$  according to  $\pi^t$  (where

$A^t = \{a_h^t = (h(\bar{x}^{t,1}), \dots, h(\bar{x}^{t,k})) : \forall h \in \mathcal{H}\}$ );

Learner suffers linear loss  $\langle a^t, \ell^t \rangle$ ;

Learner observes  $\ell^{t,i}$  iff  $a^{t,1} = 1$ ;

Learner deploys  $\pi^{t+1}$ ;

**end**

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# Reduction

In describing the reduction, we use the following notations (For integers  $k \geq 2$ ,  $C \geq 1$ ):

- (i)  $\forall a \in \{\rho^{t,1}, \rho^{t,2}, 0, 1, 1/2\} : \bar{a} := \overbrace{(a, \dots, a)}^C \text{ times}, \bar{\bar{a}} := \overbrace{(a, \dots, a)}^{k+2C \text{ times}}$ .
- (ii)  $h(\bar{x}^t) := (h(\bar{x}^{t,1}), \dots, h(\bar{x}^{t,2k+4C}))$ .

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### Algorithm 3: Reduction to Contextual Combinatorial Semi-Bandit

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**Input:** Contexts  $\bar{x}^t \in \mathcal{X}^k$ , labels  $\bar{y}^t \in \{0, 1\}^k$ , hypothesis  $h^t$ , pair  $\rho^t \in \mathcal{X}^2$ , parameter  $C \in \mathbb{N}$ ;

Define:  $\bar{x}^t = (\bar{x}^t, \bar{\rho}^{t,1}, \bar{\rho}^{t,2}) \in \mathcal{X}^{k+2C}, \bar{\bar{y}}^t = (\bar{y}^t, \bar{0}, \bar{1}) \in \{0, 1\}^{k+2C}$ ;

Construct loss vector:  $\ell^t = (\bar{1} - \bar{\bar{y}}^t, 1/\bar{2}) \in [0, 1]^{2k+4C}$ ;

Construct action vector:  $a^t = (h^t(\bar{x}^t), \bar{1} - h^t(\bar{x}^t)) \in \{0, 1\}^{2k+4C}$ ;

**Output:**  $(\ell^t, a^t)$ ;

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# Reduction

In describing the reduction, we use the following notations (For integers  $k \geq 2$ ,  $C \geq 1$ ):

- (i)  $\forall a \in \{\rho^{t,1}, \rho^{t,2}, 0, 1, 1/2\} : \bar{a} := \overbrace{(a, \dots, a)}^C \text{ times}, \bar{\bar{a}} := \overbrace{(a, \dots, a)}^{k+2C \text{ times}}$ .
- (ii)  $h(\bar{\bar{x}}^t) := (h(\bar{x}^{t,1}), \dots, h(\bar{x}^{t,2k+4C}))$ .

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## Algorithm 4: Reduction to Contextual Combinatorial Semi-Bandit

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**Input:** Contexts  $\bar{x}^t \in \mathcal{X}^k$ , labels  $\bar{y}^t \in \{0, 1\}^k$ , hypothesis  $h^t$ , pair  $\rho^t \in \mathcal{X}^2$ , parameter  $C \in \mathbb{N}$ ;

Define:

$$\bar{\bar{x}}^t = (\bar{x}^t, \bar{\rho}^{t,1}, \bar{\rho}^{t,2}) \in \mathcal{X}^{k+2C}, \bar{\bar{y}}^t = (\bar{y}^t, \bar{0}, \bar{1}) \in \{0, 1\}^{k+2C};$$

Construct loss vector:  $\ell^t = (\bar{1} - \bar{\bar{y}}^t, 1/\bar{2}) \in [0, 1]^{2k+4C}$ ;

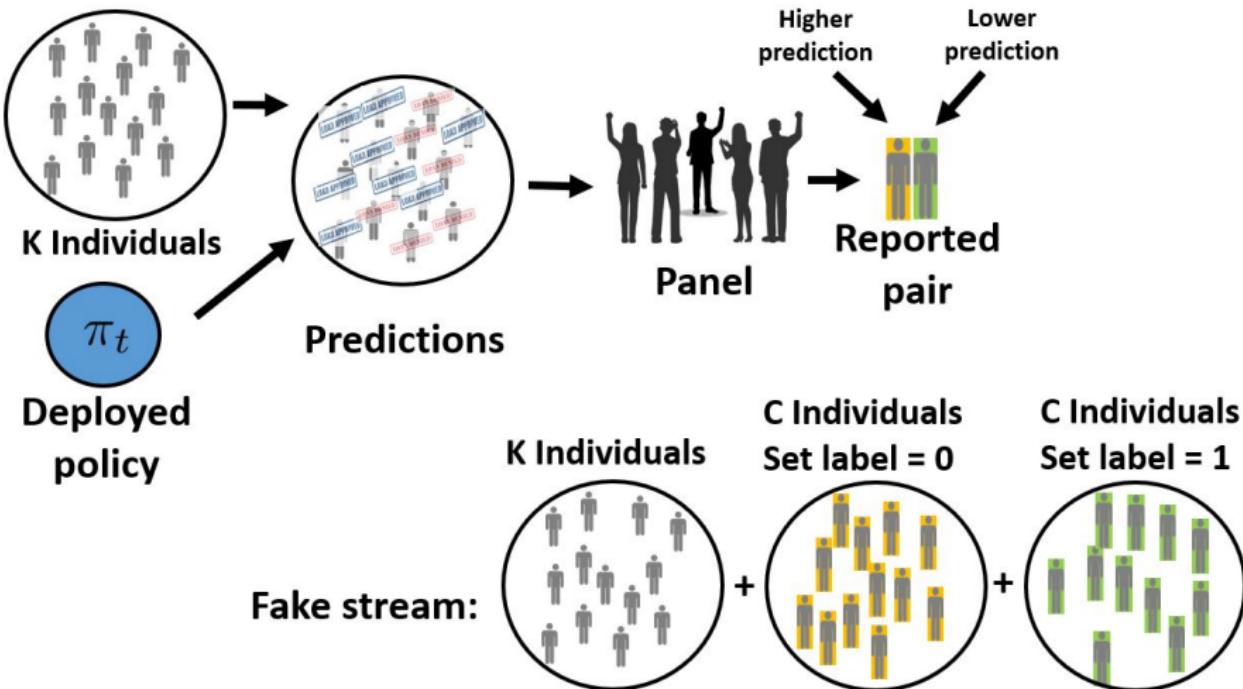
Construct action vector:  $a^t = (h^t(\bar{\bar{x}}^t), \bar{1} - h^t(\bar{\bar{x}}^t)) \in \{0, 1\}^{2k+4C}$ ;

**Output:**  $(\ell^t, a^t)$ ;

---

# Reduction

1. Encoding unfairness loss in terms of misclassification loss, by generating a “fake” stream of samples.



# Reduction

In describing the reduction, we use the following notations (For integers  $k \geq 2$ ,  $C \geq 1$ ):

- (i)  $\forall a \in \{\rho^{t,1}, \rho^{t,2}, 0, 1, 1/2\} : \bar{a} := \overbrace{(a, \dots, a)}^{C \text{ times}}, \bar{\bar{a}} := \overbrace{(a, \dots, a)}^{k+2C \text{ times}}$ .
- (ii)  $h(\bar{x}^t) := (h(\bar{x}^{t,1}), \dots, h(\bar{x}^{t,2k+4C}))$ .

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## Algorithm 5: Reduction to Contextual Combinatorial Semi-Bandit

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**Input:** Contexts  $\bar{x}^t \in \mathcal{X}^k$ , labels  $\bar{y}^t \in \{0, 1\}^k$ , hypothesis  $h^t$ , pair  $\rho^t \in \mathcal{X}^2$ , parameter  $C \in \mathbb{N}$ ;

Define:  $\bar{x}^t = (\bar{x}^t, \bar{\rho}^{t,1}, \bar{\rho}^{t,2}) \in \mathcal{X}^{k+2C}, \bar{y}^t = (\bar{y}^t, \bar{0}, \bar{1}) \in \{0, 1\}^{k+2C}$ ;

Construct loss vector:  $\ell^t = (\bar{1} - \bar{\bar{y}}^t, 1/2) \in [0, 1]^{2k+4C}$ ;

Construct action vector:  $a^t = (h^t(\bar{x}^t), \bar{1} - h^t(\bar{x}^t)) \in \{0, 1\}^{2k+4C}$ ;

**Output:**  $(\ell^t, a^t)$ ;

---

## 2. Handling one-sided feedback: misclassification loss manipulation:

$$\ell = \begin{array}{ll} & \begin{matrix} Good & Bad \end{matrix} \\ \begin{matrix} Accept \\ Reject \end{matrix} & \left( \begin{array}{cc} 0 & 1 \\ 1 & 0 \end{array} \right) \end{array} \rightarrow \tilde{\ell} = \begin{array}{ll} & \begin{matrix} Good & Bad \end{matrix} \\ \begin{matrix} Accept \\ Reject \end{matrix} & \left( \begin{array}{cc} 0 & 2 \\ 1 & 1 \end{array} \right) \end{array}$$

Manipulation is **regret-preserving**:

$$\forall h \in \mathcal{H} : \tilde{\ell}(h, (x, y)) = \ell(h, (x, y)) + \mathbb{1}[y = 0]$$

$$\implies \forall h, h' \in \mathcal{H} : \tilde{\ell}(h, (x, y)) - \tilde{\ell}(h', (x, y)) = \ell(h, (x, y)) - \ell(h', (x, y))$$

Allows for moving from one-sided to bandit setting.

# Upper Bounding Lagrangian Regret

For the following theorem, we will assume the existence of an algorithm  $\mathcal{A}$  for the contextual combinatorial semi-bandit setting (as summarized in Algorithm 2) whose expected regret (compared to only fixed hypotheses in  $\mathcal{H}$ ), against any adaptively and adversarially chosen sequence of loss functions  $\ell^t$  and contexts  $\bar{x}^t$ , is bounded by  $\text{Regret}(\mathcal{A}, T, \mathcal{H}) \leq R^{\mathcal{A}, T, \mathcal{H}}$ .

## Theorem (Upper Bounding Lagrangian Regret)

*In the setting of individually fair online learning with one-sided feedback (Algorithm 1), running  $\mathcal{A}$  while using the sequence  $(a^t, \ell^t)_{t=1}^T$  generated by the reduction in Algorithm 5 (when invoked every round on  $\bar{x}^t$ ,  $\bar{y}^t$ ,  $h^t$ ,  $\rho^t$ , and  $C$ ), yields the following guarantee, for any  $V \subseteq \Delta\mathcal{H}$ ,*

$$\sum_{t=1}^T L_{C, \rho^t}(\pi^t, \bar{x}^t, \bar{y}^t) - \min_{\pi^* \in V} \sum_{t=1}^T L_{C, \rho^t}(\pi^*, \bar{x}^t, \bar{y}^t) \leq (2k + 4C)R^{\mathcal{A}, T, \mathcal{H}}.$$

# Simultaneous No-Regret Guarantees

Reminder: we want, **simultaneously**:

- ➊ Accuracy:

$$\text{Regret}^{\text{err}}(\mathcal{A}, T, Q_{\alpha, \gamma}) = o(T).$$

- ➋ Fairness:

$$\text{Regret}^{\text{unfair}, \alpha, \gamma}(\mathcal{A}, T, Q_{\alpha, \gamma}) = o(T).$$

# Upper Bounding Misclassification, Unfairness

Theorem (Upper Bounding Misclassification, Unfairness Simultaneously)

For any  $\epsilon \in [0, \alpha]$ ,

$$\begin{aligned} & C\epsilon \sum_{t=1}^T \text{Unfair}^{\alpha, \gamma}(\pi^t, \bar{x}^t, \bar{j}^t) + \text{Regret}^{\text{err}}(\mathcal{A}, T, Q_{\alpha-\epsilon, \gamma}) \\ & \leq \sum_{t=1}^T L_{C, \rho^t}(\pi^t, \bar{x}^t, \bar{y}^t) - \min_{\pi^* \in Q_{\alpha-\epsilon, \gamma}} \sum_{t=1}^T L_{C, \rho^t}(\pi^*, \bar{x}^t, \bar{y}^t). \end{aligned}$$

And remember that the right hand side is upper bounded by  $(2k + 4C)R^{\mathcal{A}, T, \mathcal{H}}$ .

## Careful...

Theorem (Upper Bounding Misclassification, Unfairness Simultaneously)

For any  $\epsilon \in [0, \alpha]$ ,

$$\begin{aligned} & C\epsilon \sum_{t=1}^T \text{Unfair}^{\alpha, \gamma}(\pi^t, \bar{x}^t, \bar{j}^t) + \text{Regret}^{\text{err}}(\mathcal{A}, T, Q_{\alpha-\epsilon, \gamma}) \\ & \leq \sum_{t=1}^T L_{C, \rho^t}(\pi^t, \bar{x}^t, \bar{y}^t) - \min_{\pi^* \in Q_{\alpha-\epsilon, \gamma}} \sum_{t=1}^T L_{C, \rho^t}(\pi^*, \bar{x}^t, \bar{y}^t). \end{aligned}$$

$\text{Regret}^{\text{err}}(\mathcal{A}, T, Q_{\alpha-\epsilon, \gamma})$  can be **negative**!

⇒ Even if Lagrangian regret is sublinear, number of fairness violations can still be **linear**.

⇒ We will need to carefully interpolate between the two objectives.

# Outline

- Fairness Framework: Metric-Free Individual Fairness via Panels
- Individually Fair Online Batch Classification
- Reduction to Contextual Combinatorial Semi-Bandit
- Multi-Criteria No Regret Guarantees for Accuracy, Fairness
- Oracle-Efficient Algorithm

# So Far

- (Any) no regret algorithm for contextual combinatorial semi-bandit  
     $\implies$  simultaneous no regret for each of accuracy, fairness.
- Important: our reduction requires that the panel **sees the predictions** (not the realization!) of the deployed policy on incoming individuals:
  - ▶ Fine with exponential weights style algorithms.
  - ▶ FTPL style algorithms **do not** explicitly maintain the distribution deployed over base predictors every round.

## Multi-Criteria No-Regret Guarantees: Exp2 (“Expanded Exp”)

Exp2 (Bubeck et al. 2012) is an adaptation of the classical exponential weights algorithm for linear bandits.

- in order to cope with the semi-bandit nature of the online setting, leverages the linear structure of the loss functions in order to share information regarding the observed feedback between all experts (hypotheses in  $\mathcal{H}$ ).
- Such information sharing is then utilized in decreasing the variance in the formed loss estimators, resulting in a regret rate that depends only logarithmically (instead of linearly) on  $|\mathcal{H}|$ .

# Multi-Criteria No-Regret Guarantees: Exp2 (“Expanded Exp”)

## Theorem

In the setting of individually fair online learning with one-sided feedback (Algorithm 1), running Exp2 for contextual combinatorial semi-bandits (Algorithm 2) while using the sequence  $(a^t, \ell^t)_{t=1}^T$  generated by the reduction in Algorithm 5 (when invoked each round using  $\bar{x}^t$ ,  $\bar{y}^t$ ,  $h^t$ ,  $\rho^t$ , and  $C = T^{\frac{1}{5}}$ ), yields the following guarantees, for any  $\epsilon \in [0, \alpha]$ , simultaneously:

- ① **Accuracy:**  $\text{Regret}^{\text{err}}(\text{Exp2}, T, Q_{\alpha-\epsilon,\gamma}) \leq O\left(k^{\frac{3}{2}} T^{\frac{4}{5}} \log |\mathcal{H}|^{\frac{1}{2}}\right).$
- ② **Fairness:**  $\sum_{t=1}^T \text{Unfair}^{\alpha,\gamma}(\pi^t, \bar{x}^t, \bar{j}^t) \leq O\left(\frac{1}{\epsilon} k^{\frac{3}{2}} T^{\frac{4}{5}} \log |\mathcal{H}|^{\frac{1}{2}}\right).$

However, Exp2 has space and time requirements linear in  $T$ . Could be prohibitive for large classes.

# Multi-Criteria Guarantees: Context-Semi-Bandit-FTPL

Context-Semi-Bandit-FTPL (Syrgkanis et al. 2016) is an oracle-efficient algorithm for combinatorial bandits. It requires access to:

- (Offline) optimization oracle.
- Pre-computed (small) separator set.

However, in our specific setting, it cannot simply be applied off the shelf.

# Multi-Criteria Guarantees: Adapting Context-Semi-Bandit-FTPL

In order to not have runtime, memory complexity that scales with  $|\mathcal{H}|$ , Context-Semi-Bandit-FTPL **does not** explicitly maintain the deployed distribution over  $\mathcal{H}$ .

- Instead, it samples a single hypothesis according to this distribution every round, utilizing the linearity of the loss function.
- However, for individual fairness this is problematic, as it can lead to extreme overestimation of unfairness, if panel is queried using single hypotheses. This is since the unfairness loss is **sub-additive**.

## Lemma

There exist  $\alpha, \gamma, m, k > 0$ ,  $\mathcal{H} : \mathcal{X} \rightarrow \{0, 1\}$ ,  $\bar{x} \in \mathcal{X}^k$ ,  $\bar{j} : \mathcal{X}^k \rightarrow \mathcal{X}^2$ , and  $\pi \in \Delta \mathcal{H}$  for which, simultaneously,

- ①  $\mathbb{E}_{h \sim \pi} [unfair^{\alpha, \gamma}(h, \bar{x}, \bar{j})] = 1$ .
- ②  $unfair^{\alpha, \gamma}(\pi, \bar{x}, \bar{j}) = 0$ .

# Adapting Context-Semi-Bandit-FTPL

- **Potential solution:** Closed-form expression for the (implicit) weights the algorithm places on each  $h \in \mathcal{H}$ .
- However, the weights are generally not efficiently computable in closed form (see e.g. the discussion in Neu and Bartok 2013).
- **Our solution:** Instead, we will resample the deployed hypothesis every round.
- **Problem:** In order to use adversarial online learning algorithms, the realized randomness of the learner cannot be revealed to the adversary before it picks its loss vector.
- In general: adversary can tailor the losses to the realized randomness and force linear regret.

# Adapting Context-Semi-Bandit-FTPL

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**Algorithm 4:** Utilization of Context-Semi-Bandit-FTPL

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**Parameters:** Class of predictors  $\mathcal{H}$ , number of rounds  $T$ , separator set  $S$ , parameters  $\omega, L$ ;

Initialize Context-Semi-Bandit-FTPL-With-Resampling( $S, \omega, L$ );

Learner deploys  $\pi^1 \in \Delta\mathcal{H}$  according to

Context-Semi-Bandit-FTPL-With-Resampling;

**for**  $t = 1, \dots, T$  **do**

    Environment selects individuals  $\bar{x}^t \in \mathcal{X}^k$ , and labels  $\bar{y}^t \in \mathcal{Y}^k$ , learner only observes  $\bar{x}^t$ ;

    Environment selects panel of auditors  $(j^{t,1}, \dots, j^{t,m}) \in \mathcal{J}^m$ ;

$(\hat{\pi}^t, \hat{h}^t) = \text{Context-Semi-Bandit-FTPL-With-Resampling}(\bar{x}^t, \omega, L)$ ;

    Learner predicts  $\hat{y}^{t,i} = h^t(\bar{x}^{t,i})$  for each  $i \in [k]$ , observes  $\bar{y}^{t,i}$  iff  $\hat{y}^{t,i} = 1$ ;

    Panel reports its feedback  $\rho^t = \bar{j}_{j^1, \dots, j^m}^{t,\alpha, \gamma}(\hat{\pi}^t, \bar{x}^t)$ ;

$(\ell^t, a^t) = \text{Reduction}(\bar{x}^t, \bar{y}^t, \hat{h}^t, \rho^t, C)$ ;

    Update Context-Semi-Bandit-FTPL-With-Resampling with  $(\ell^t, a^t)$ ;

    Learner suffers misclassification loss  $\text{Error}(\hat{h}^t, \bar{x}^t, \bar{y}^t)$  (not necessarily observed by learner);

    Learner suffers unfairness loss  $\text{Unfair}(\hat{\pi}^t, \bar{x}^t, \bar{j}^t)$ ;

    Learner deploys  $\pi^{t+1} \in \Delta\mathcal{H}$  according to

        Context-Semi-Bandit-FTPL-With-Resampling;

**end**

---

# Adapting Context-Semi-Bandit-FTPL

- **Potential solution:** Closed-form expression for the (implicit) weights the algorithm places on each  $h \in \mathcal{H}$ .
- The weights are generally not efficiently computable in closed form (see e.g. the discussion in Neu and Bartok 2013).
- **Our solution:** Instead, we will resample the deployed hypothesis every round.
- **Problem:** In order to use adversarial online learning algorithms, the realized randomness of the learner cannot be revealed to the adversary before it picks its loss vector.
- In general: adversary can “tailor” its losses to the realized randomness and force linear regret.
- However, since our “adversary” is **restricted** to act according to the (fixed) implicit distance functions of the auditors in the panel, it cannot really adversarially adapt to the realized estimate: with high probability, the fairness loss for the realized (estimated) policy and the underlying distribution is close.

# Oracle-Efficient Algorithm: Context-Semi-Bandit-FTPL-With-Resampling

## Theorem

In the setting of individually fair online learning with one-sided feedback (Algorithm 1), running Context-Semi-Bandit-FTPL-With-Resampling for contextual combinatorial semi-bandit (Algorithm 5) as specified in Algorithm 4, with  $R = T$ , and using the sequence  $(\ell^t, a^t)_{t=1}^T$  generated by the reduction in Algorithm 5 (when invoked on each round using  $\bar{x}^t$ ,  $\bar{y}^t$ ,  $\hat{h}^t$ ,  $\hat{p}^t$ , and  $C = T^{\frac{4}{45}}$ ), yields, with probability  $1 - \delta$ , the following guarantees, for any  $\epsilon \in [0, \alpha]$ , simultaneously:

- ① **Accuracy:**  $\text{Regret}^{\text{err}}(\text{CSB-FTPL-WR}, T, Q_{\alpha-\epsilon, \gamma}) \leq \tilde{O}\left(k^{\frac{11}{4}} s^{\frac{3}{4}} T^{\frac{41}{45}} \log |\mathcal{H}|^{\frac{1}{2}}\right)$ .
- ② **Fairness:**  $\sum_{t=1}^T \text{Unfair}^{\alpha, \gamma}(\hat{\pi}^t, \bar{x}^t, \bar{j}^t) \leq \tilde{O}\left(\frac{1}{\epsilon} k^{\frac{11}{4}} s^{\frac{3}{4}} T^{\frac{41}{45}} \log |\mathcal{H}|^{\frac{1}{2}}\right)$ .

# Overview of Results

Full Information	Inefficient	<b>Accuracy:</b> $\tilde{O}\left(kT^{\frac{3}{4}}\right)$ <b>Fairness:</b> $\tilde{O}\left(\frac{1}{\alpha}kT^{\frac{3}{4}}\right)$
	Efficient	<b>Accuracy:</b> $\tilde{O}\left(s^{\frac{3}{4}}k^{\frac{5}{4}}T^{\frac{7}{9}}\right)$ <b>Fairness:</b> $\tilde{O}\left(\frac{1}{\alpha}s^{\frac{3}{4}}k^{\frac{5}{4}}T^{\frac{7}{9}}\right)$
One-Sided	Inefficient	<b>Accuracy:</b> $\tilde{O}\left(k^{\frac{3}{2}}T^{\frac{4}{5}}\right)$ <b>Fairness:</b> $\tilde{O}\left(\frac{1}{\alpha}k^{\frac{3}{2}}T^{\frac{4}{5}}\right)$
	Efficient	<b>Accuracy:</b> $\tilde{O}\left(s^{\frac{3}{4}}k^{\frac{11}{4}}T^{\frac{41}{45}}\right)$ <b>Fairness:</b> $\tilde{O}\left(\frac{1}{\alpha}s^{\frac{3}{4}}k^{\frac{11}{4}}T^{\frac{41}{45}}\right)$

# Limitations

- Exp2 prohibitive for large hypothesis classes.
- Context-Semi-Bandit-FTPL-WR:
  - ▶ Small separator sets only known for specific classes (conjunctions, disjunctions, parities, decision lists, discretized linear classifiers).
  - ▶ Our implementation requires  $O(T^2)$  calls to the (offline) optimization oracle.

We “inherit” some of the limitations from the contextual bandit literature.

# Rich Subgroup Fairness

- Kearns et al. 2018, Hébert-Johnson et al. 2018. Many follow up works.
- A “middleground” between group and individual fairness - equalizing across a pre-defined set of (potentially) exponentially many, possibly overlapping, groups in the population.
- Allows for significantly stronger guarantees for individuals than simple group notions.

# Individual Fairness and Rich Subgroup Fairness

- Individual fairness sits on one extreme of subgroup fairness, treating each individual as a subgroup.
- However, individual fairness does not equalize some statistic over all individuals, but rather according to a very specific structure - given by an extra component, specifying who is similar.
- Individual fairness gives direct influence to people's preferences in forming the fairness definition.
- However, harder to elicit. Could trigger larger tension with accuracy if similarity preferences are not well-aligned with labels.

# Takeaways

- Meaningful fairness guarantees to individuals, while minimizing surrounding assumptions, regarding:
  - ▶ The availability or form of similarity metrics
  - ▶ Data generation process
  - ▶ The observable feedback for made decisions
- Fairness auditing framework which can handle multiple auditors with (possibly) conflicting opinions
  - ▶ Possible to **algorithmically** change the required consensus for a fairness violation and explore the frontier.
- Possible to achieve simultaneous no regret for accuracy and individual fairness, under
  - ▶ No parametric (or even metric) assumptions on similarity judgements
  - ▶ Adversarial arrivals
  - ▶ One-sided label feedback

# Future Directions

- Is it possible to achieve faster rates? The regret lower bound for combinatorial bandits is  $\Omega(k\sqrt{T \log |\mathcal{H}|})$ .
- Can we give an oracle efficient algorithm in the general case (without requiring small separators)?
- Relaxing some of the assumptions:
  - ▶ What if only contexts are adversarial, but labels are selected from a distribution given the context?
  - ▶ What if panels are selected stochastically?
  - ▶ Parametric assumptions?
- Faster algorithms?