

Latent Gaussian Process Spatial Model

- Binomial model for public opinion with spatial demography.

$$y_{it} \sim \text{Binomial}(\theta_{it}, N_{it})$$

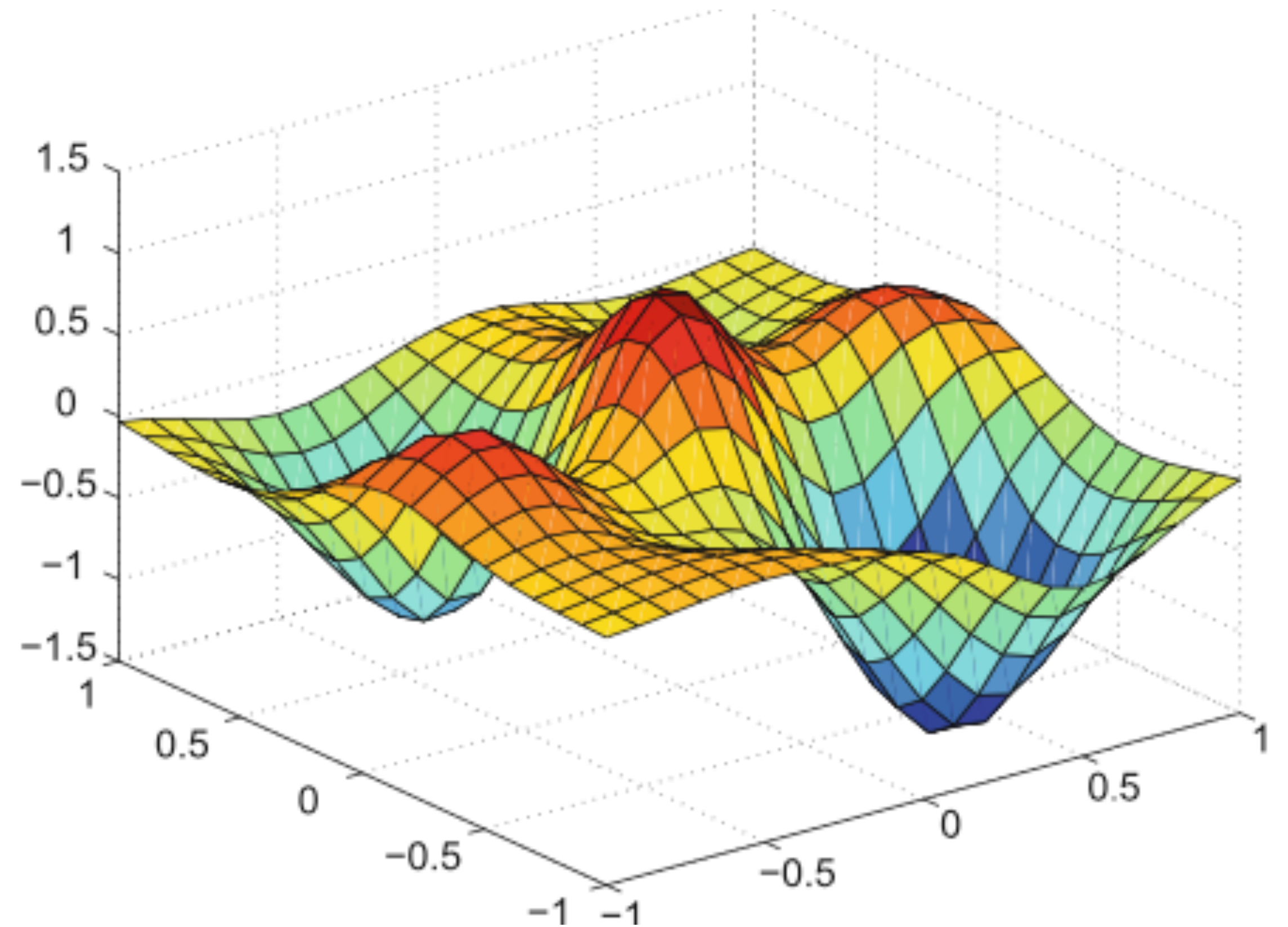
$$\theta_{it} = \Phi(f_{it}) = \int_{-\infty}^{f_{it}} \mathcal{N}(0,1)dz$$

$$f_{it} \sim \mathbb{GP}(\mu, K)$$

$$\mu(x) = [\text{lon}, \text{lat}, \text{race}, \text{gender}, \text{year}]^T \mathbf{w}$$

$$K(x, x') = \exp\left(-\sum_d ||x_d - x'_d||^2 / \ell_d^2\right)$$

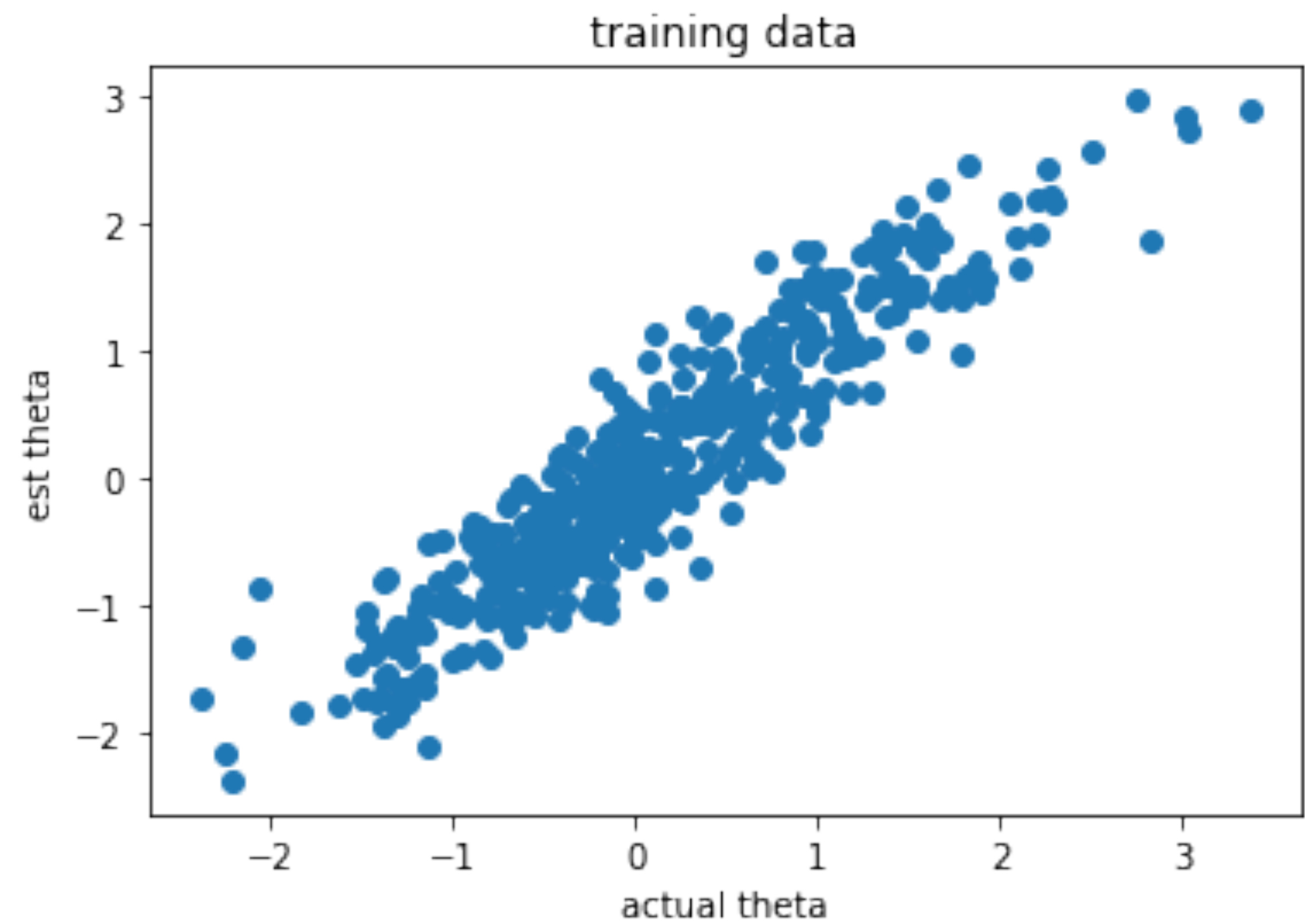
- Predict opinion for new county new demography.



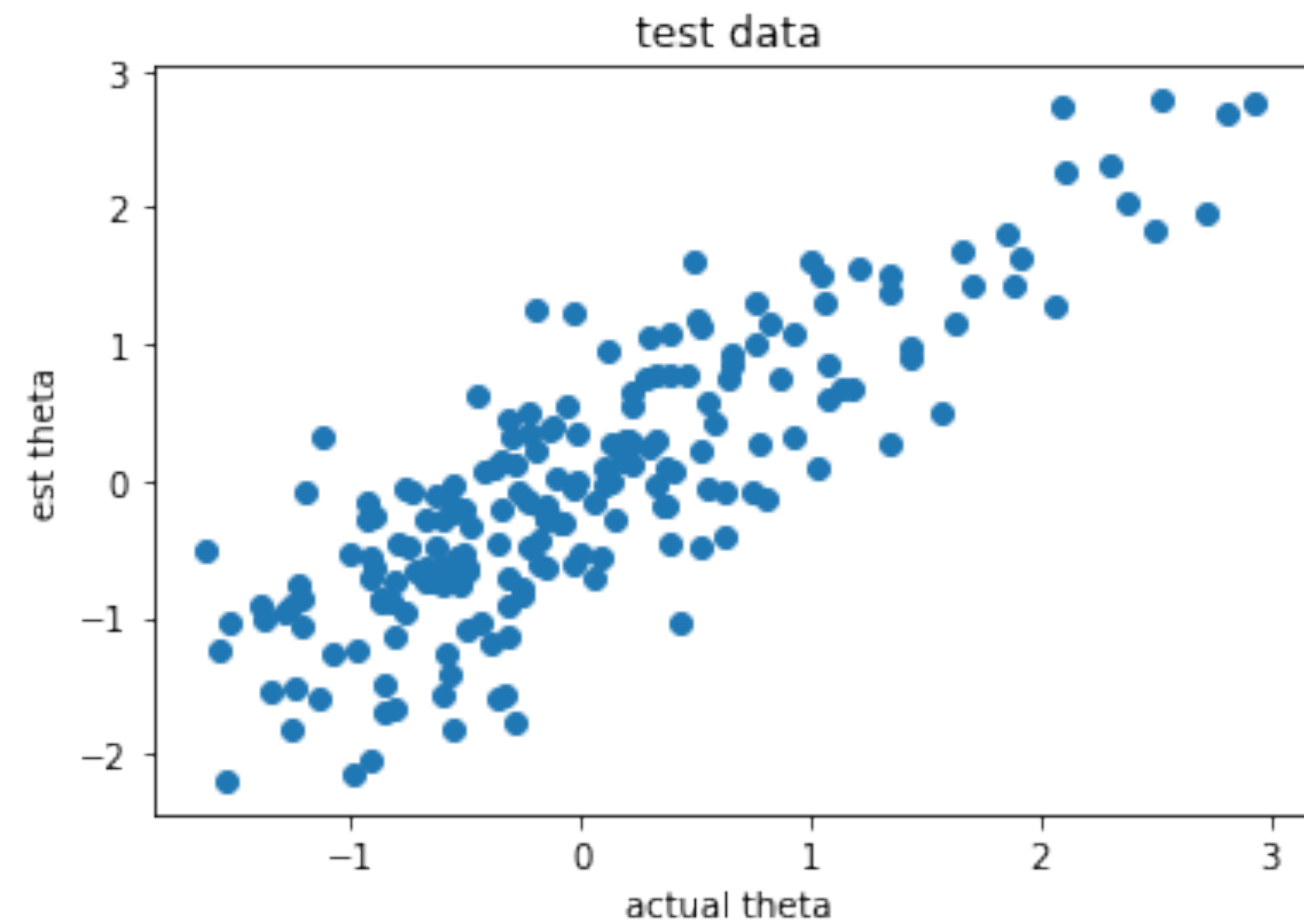
Gaussian process estimation of spatial surface.
Ramakrishnan et al. (2008). Gaussian Process Models in Spatial Data Mining.

Preliminary Results

| Length scale | latitude | longitude | genderMale | genderFe | genderNonb | raceWhite | raceBlack | raceHispanic | raceAsian | raceOther | year |
|--------------|----------|-----------|------------|----------|------------|-----------|-----------|--------------|-----------|-----------|------|
| Actual | 0.5 | 0.5 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 0.5 |
| Est | 0.48 | 0.31 | 2.08 | 1.40 | 1.51 | 1.61 | 1.63 | 1.90 | 0.99 | 1.36 | 0.56 |



Train correlation: 0.930



Test correlation: 0.837