Time Series Analysis

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About

Disclaimer

The material here is not comprehensive and does not constitute a stand alone course in Time Series Analysis. This is only the support material for the actual presential course I give.

When and Where?

Day of the week, from 00:00 to 24:00 Computer classroom #16

Syllabus

Course description

Data analysis of time series, with practical examples from environmental sciences.

Course aims

This course aims at giving the students a broad overview of the main steps involved in the analysis of time series: data management, data wrangling, visualization, analysis, and forecast. The course will provide a hands-on approach, where students will actively engage with real-life datasets from the field of environmental science.

Learning outcomes

On successful completion of this module, students should be able to:

- Explore a time-series dataset, while formulating interesting questions.
- Choose the appropriate tools to attack the problem and answer the questions.
- Communicate their findings and the methods they used to achieve them, using graphs, statistics, text, and a well-documented code.

Course content

- Data wrangling: organization, cleaning, merging, filling gaps, excluding outliers, smoothing, resampling.
- Visualization: best practices for graph making using leading python libraries.
- Analysis: stationarity, seasonality, (auto)correlations, lags, derivatives, spectral analysis.
- Forecast: ARIMA
- Data management: how to plan ahead and best organize large quantities of data. If there is enough time, we will build a simple time-series database.

Books and other sources

Course evaluation

There will be 2 projects during the semester (each worth 25% of the final grade), and one final project (50%).

Weekly program

Week 1

- Lecture: Course overview, setting of expectations. Introduction, basic concepts, continuous vs discrete time series, sampling, aliasing
- Exercise: Loading csv file into python, basic time series manipulation with pandas and plotting

Week 2

- Lecture: Filling gaps, removing outliers
- Exercise: Practice the same topics learned during the lecture. Data: air temperature and relative humidity

Week 3

- Lecture: Interpolation, resampling, binning statistics
- Exercise: Practice the same topics learned during the lecture. Data: air temperature and relative humidity, precipitation

Week 4

- Lecture: Time series plotting: best practices. Dos and don'ts and maybes
- Exercise: Practice with Seaborn, Plotly, Pandas, Matplotlib

Project 1

Basic data wrangling, using real data (temperature, relative humidity, precipitation) downloaded from USGS. 25% of the final grade

Week 5

- Lecture: Smoothing, running averages, convolution
- Exercise: Practice the same topics learned during the lecture. Data: sap flow, evapotranspiration

Week 6

- Lecture: Strong and weak stationarity, stochastic processes, auto-correlation
- Exercise: Practice the same topics learned during the lecture. Data: temperature and wind speed

Week 7

- Lecture: Correlation between signals. Pearson correlation, time-lagged cross-correlations, dynamic time warping
- Exercise: Practice the same topics learned during the lecture. Data: temperature, solar radiation, relative humidity, soil moisture, evapotranspiration

Week 8

Same as lecture 7 above

Week 9

- Lecture: Download data from repositories, using API, merging, documentation
- Exercise: Download data from USGS, NOAA, Fluxnet, Israel Meteorological Service

Project 2

Students will study a Fluxnet site of their choosing. How do gas fluxes (CO2, H2O) depend on environmental conditions? 25% of the final grade

Week 10

- Lecture: Fourier decomposition, filtering, Nyquist-Shannon sampling theorem
- Exercise: Practice the same topics learned during the lecture. Data: dendrometer data

Week 11

- Lecture: Seasonality, seasonal decomposition (trend, seasonal, residue), Hilbert transform
- Exercise: Practice the same topics learned during the lecture. Data: monthly atmospheric CO2 concentration, hourly air temperature

Week 12

- Lecture: Derivatives, differencing
- Exercise: Practice the same topics learned during the lecture. Data: dendrometer data

Week 13

- Lecture: Forecasting. ARIMA
- Exercise: Practice the same topics learned during the lecture. Data: vegetation variables (sap flow, ET, DBH, etc)

Final Project

In consultation with the lecturer, students will ask a specific scientific question about a site of their choosing (from NOAA, USGS, Fluxnet), and answer it using the tools learned during the semester. The report will be written in Jupyter Notebook, combining in one document all the calculations, documentation, figures, analysis, and discussion. 50% of the final grade.

Part I Introduction

1 First Steps — basic time series analysis

Import packages. If you don't have a certain package, e.g. 'newpackage', just type pip install newpackage

```
import urllib
import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
import os.path
import matplotlib.dates as mdates
import datetime as dt
import matplotlib as mpl
from pandas.tseries.frequencies import to_offset
from scipy.signal import savgol_filter
```

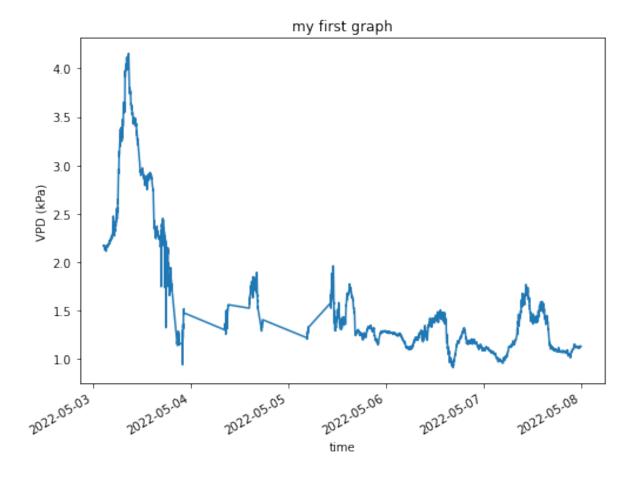
This is how you download data from Thingspeak

```
filename1 = "test_elad.csv"
# if file is not there, go fetch it from thingspeak
if not os.path.isfile(filename1):
    # define what to download
    channels = "1690490"
    fields = "1,2,3,4,6,7"
    minutes = "30"
    # https://www.mathworks.com/help/thingspeak/readdata.html
    # format YYYY-MM-DD%20HH:NN:SS
    start = "2022-05-01%2000:00:00"
    end = "2022-05-08\%2000:00:00"
    # download using Thingspeak's API
    # url = f"https://api.thingspeak.com/channels/{channels}/fields/{fields}.csv?minutes={
    url = f"https://api.thingspeak.com/channels/{channels}/fields/{fields}.csv?start={star
    data = urllib.request.urlopen(url)
    d = data.read()
```

```
# save data to csv
file = open(filename1, "w")
file.write(d.decode('UTF-8'))
file.close()
```

You can load the data using Pandas. Here we create a "dataframe", which is a fancy name for a table.

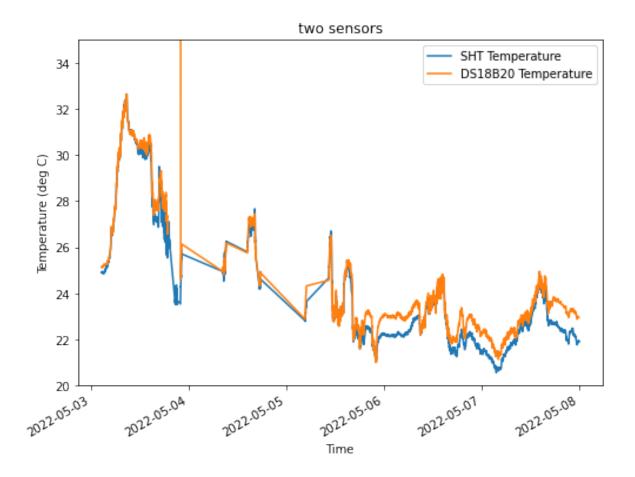
1.0.1 First graph



1.0.2 Two columns in the same graph

```
plt.gcf().autofmt_xdate()
ax.legend(loc="upper right")
```

<matplotlib.legend.Legend at 0x7fe6c9730610>



1.0.3 Calculate stuff

You can calculate new things and save them as new columns of your dataframe.

```
def calculate_es(T):
    es = np.exp((16.78 * T - 116.9) / (T + 237.3))
    return es

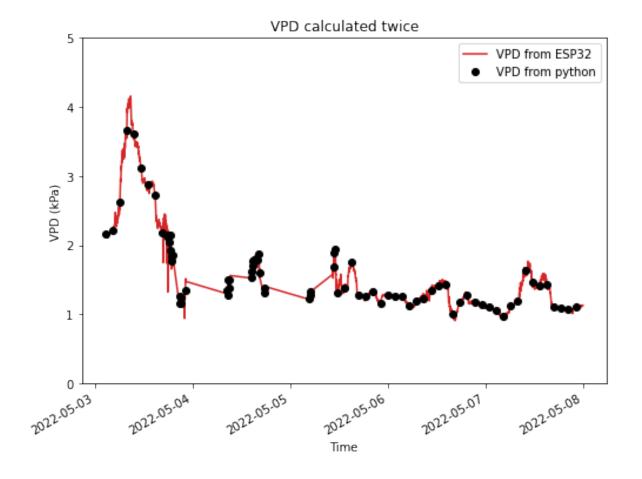
def calculate_ed(es, rh):
```

```
return es * rh / 100.0

es = calculate_es(df['T1'])
ed = calculate_ed(es, df['RH'])
df['VPD2'] = es - ed
```

See if what you calculated makes sense.

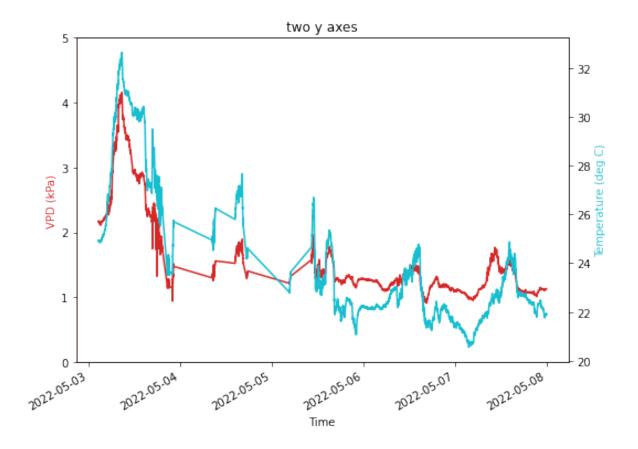
<matplotlib.legend.Legend at 0x7fe6989ca700>



1.0.4 Two y axes

```
ax.spines['left'].set_color('red')
ax2.set_ylabel('Temperature (deg C)', color='tab:cyan')
```

Text(0, 0.5, 'Temperature (deg C)')



1.1 NaN, Missing data, Outliers

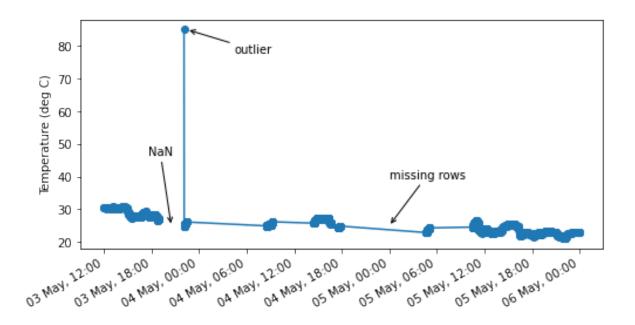
```
# %matplotlib widget

start = "2022-05-03 12:00:00"
end = "2022-05-06 00:00:00"

fig, ax = plt.subplots(1, figsize=(8,4))
```

```
# plot using pandas' plot method
df.loc[start:end, 'T2'].plot(ax=ax,
                             linestyle='-',
                             marker='o',
                             color="tab:blue",
                             label="data")
# annotate examples here:
# https://jakevdp.github.io/PythonDataScienceHandbook/04.09-text-and-annotation.html
ax.annotate("NaN",
                                                # text to write, if nothing, then ""
                                                # (x,y coordinates for the tip of the arrow
            xy=('2022-05-03\ 20:30:00',\ 25),
            xycoords='data',
                                                # xy as 'data' coordinates
                                               # xy coordinates for the text
            xytext = (-20, 60),
            textcoords='offset points',
                                              # xytext relative to xy
            arrowprops=dict(arrowstyle="->") # pretty arrow
ax.annotate("outlier",
            xy=('2022-05-03 22:30:00', 85),
            xycoords='data',
            xytext=(40, -20),
            textcoords='offset points',
            arrowprops=dict(arrowstyle="->")
ax.annotate("missing rows",
            xy=('2022-05-05\ 00:00:00',\ 25),
            xycoords='data',
            xytext=(0, 40),
            textcoords='offset points',
            arrowprops=dict(arrowstyle="->")
           )
ax.xaxis.set_major_formatter(mdates.DateFormatter('%d %b, %H:00'))
plt.gcf().autofmt_xdate()
ax.set(xlabel="",
       ylabel="Temperature (deg C)")
```

[Text(0.5, 0, ''), Text(0, 0.5, 'Temperature (deg C)')]



The arrows (annotate) work because the plot was df['column'].plot()

If you use the usual

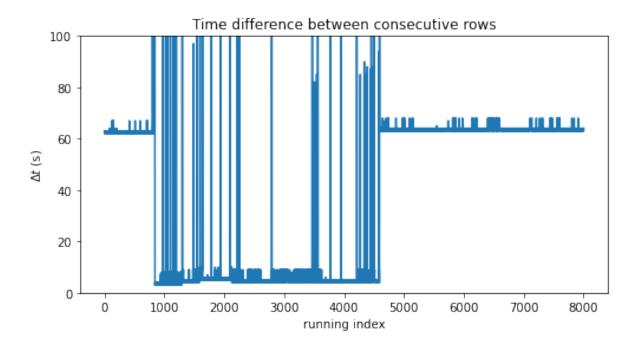
ax.plot(df['column'])

then you matplotlib will not understand timestamps as x-positions. In this case follow the instructions below.

```
arrowprops=dict(arrowstyle="->")
t_outlier = '2022-05-03 22:30:00'
x_outlier = mdates.date2num(dt.datetime.strptime(t_outlier, "%Y-%m-%d %H:%M:%S"))
ax.annotate("outlier",
            xy=(x_outlier, 85),
            xycoords='data',
            xytext=(40, -20),
            textcoords='offset points',
            arrowprops=dict(arrowstyle="->")
           )
t missing = '2022-05-05 00:00:00'
x_missing = mdates.date2num(dt.datetime.strptime(t_missing, "%Y-%m-%d %H:%M:%S"))
ax.annotate("missing rows",
            xy=(x_missing, 25),
            xycoords='data',
            xytext=(0, 40),
            textcoords='offset points',
            arrowprops=dict(arrowstyle="->")
# code for hours, days, etc
# https://docs.python.org/3/library/datetime.html#strftime-and-strptime-format-codes
ax.xaxis.set_major_formatter(mdates.DateFormatter('%d %b, %H:00'))
plt.gcf().autofmt_xdate()
ax.set(xlabel="",
       ylabel="Temperature (deg C)")
```

[Text(0.5, 0, ''), Text(0, 0.5, 'Temperature (deg C)')]

```
03 May, 03 May, 04 May, 04 May, 04 May, 02 May
```



1.2 Resample

1.2.1 Downsampling

```
# %matplotlib widget

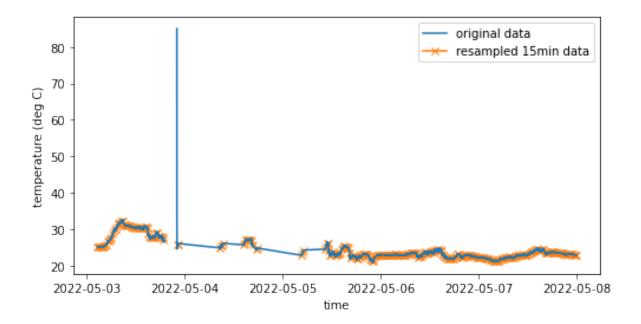
fig, ax = plt.subplots(1, figsize=(8,4))

# Downsample to spaced out data points. Change the number below, see what happens.
window_size = '15min'

df_resampled = (df['T2'].resample(window_size)  # resample doesn't do anything yet, just doesn't doesn'
```

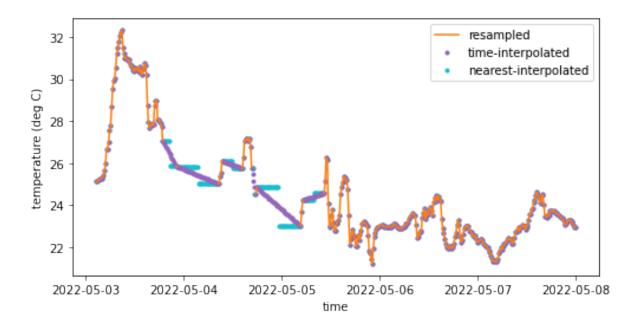
```
ax.set(xlabel="time",
     ylabel="temperature (deg C)")
```

[Text(0.5, 0, 'time'), Text(0, 0.5, 'temperature (deg C)')]



1.2.2 Filling missing data

[Text(0.5, 0, 'time'), Text(0, 0.5, 'temperature (deg C)')]



1.3 Smoothing noisy data

Let's first download data from a different project.

```
filename2 = "test_peleg.csv"
# if file is not there, go fetch it from thingspeak
if not os.path.isfile(filename2):
    # define what to download
    channels = "1708067"
    fields = "1,2,3,4,5"
    minutes = "30"

# https://www.mathworks.com/help/thingspeak/readdata.html
# format YYYY-MM-DD%20HH:NN:SS
```

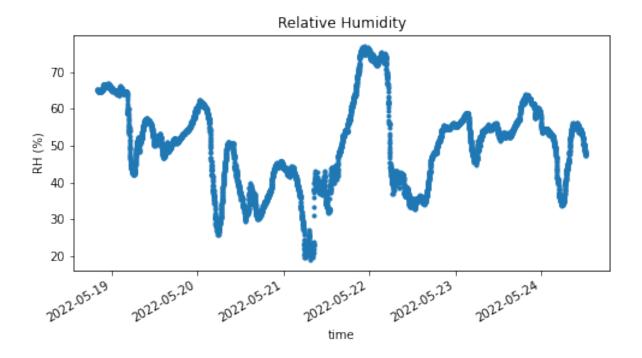
```
start = "2022-05-15%2000:00:00"
    end = "2022-05-25\%2000:00:00"
    # download using Thingspeak's API
    # url = f"https://api.thingspeak.com/channels/{channels}/fields/{fields}.csv?minutes={
    url = f"https://api.thingspeak.com/channels/{channels}/fields/{fields}.csv?start={star
    data = urllib.request.urlopen(url)
    d = data.read()
    # save data to csv
    file = open(filename2, "w")
    file.write(d.decode('UTF-8'))
    file.close()
# load data
df = pd.read_csv(filename2)
# rename columns
df = df.rename(columns={"created_at": "timestamp",
                        "field1": "T",
                        "field2": "Tw",
                        "field3": "RH",
                        "field4": "VPD",
                        "field5": "dist",
# set timestamp as index
df['timestamp'] = pd.to_datetime(df['timestamp'])
df = df.set_index('timestamp')
```

df

	entry_id	${ m T}$	Tw	RH	VPD	dist
timestamp						
2022-05-18 20:09:31+00:00	24716	23.85	23.3125	65.32	1.02532	7.208
2022-05-18 20:10:32+00:00	24717	23.88	23.2500	65.32	1.02717	7.208
2022-05-18 20:11:33+00:00	24718	23.90	23.2500	65.23	1.03107	7.276
2022-05-18 20:12:33+00:00	24719	23.90	23.2500	65.19	1.03226	7.208
2022-05-18 20:13:34+00:00	24720	23.89	23.2500	65.15	1.03282	7.633
						•••
2022-05-24 12:18:35+00:00	32711	27.47	26.1250	47.49	1.92397	8.925
2022-05-24 12:19:36+00:00	32712	27.47	26.1250	47.62	1.91921	8.925

	entry_id	Т	Tw	RH	VPD	dist
timestamp		1	111	1011	VID	dist
2022-05-24 12:20:39+00:00	32713	27.47	26.1250	47.96	1.90675	8.925
2022-05-24 12:21:40+00:00	32714	27.47	26.1875	47.75	1.91444	8.925
2022-05-24 12:22:41+00:00	32715	27.49	26.1875	47.94	1.90971	8.925

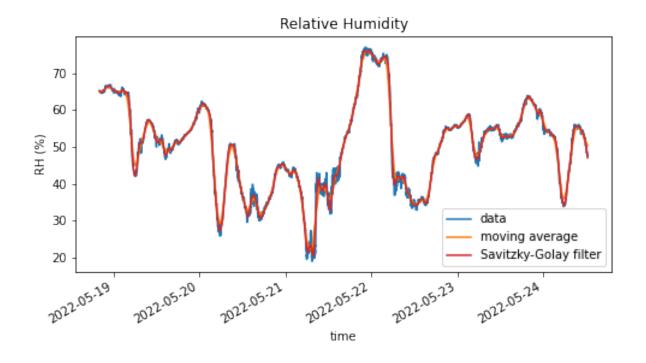
1.4 Smoothing noisy data



1.4.1 Moving average and SavGol

```
# %matplotlib widget
fig, ax = plt.subplots(1, figsize=(8,4))
# apply a rolling average of size "window_size",
# it can be either by number of points, or by window time
# window_size = 30  # number of measurements
window_size = '120min' # minutes
RH_smooth = df['RH'].rolling(window_size, center=True).mean().to_frame()
RH_smooth.rename(columns={'RH': 'rolling_avg'}, inplace=True)
RH_smooth['SG'] = savgol_filter(df['RH'], window_length=121, polyorder=2)
ax.plot(df['RH'], color="tab:blue", label="data")
ax.plot(RH smooth['rolling avg'], color="tab:orange", label="moving average")
ax.plot(RH_smooth['SG'], color="tab:red", label="Savitzky-Golay filter")
# add labels and title
ax.set(xlabel = "time",
       ylabel = "RH (%)",
       title = "Relative Humidity")
# makes slanted dates
plt.gcf().autofmt_xdate()
ax.legend()
```

<matplotlib.legend.Legend at 0x7fe6a0525730>

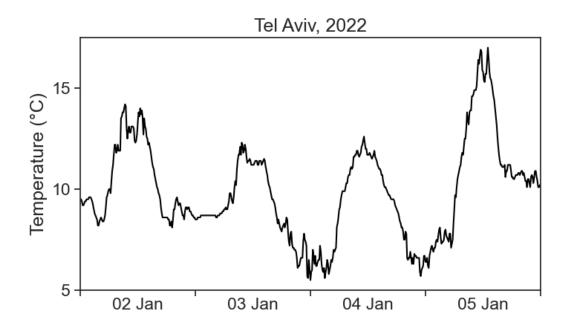


Part II Smoothing

2 Convolution

Running windows of different shapes (kernels)

This is the temperature for Tel Aviv, between 2 and 5 of January 2022. Data is in intervals of 10 minutes, and was downloaded from the Israel Meteorological Service.



We see that the temperature curve has a rough profile. Can we find ways of getting smoother curves?

Convolution is a fancy word for averaging a time series using a running window. We will use the terms **convolution**, **running average**, **and rolling average** interchangeably. See the animation below. We take all temperature values inside a window of width 500 minutes (51 points), and average them with equal weights. The weights profile is called **kernel**.

The pink curve is much smoother than the original! However, the running average cannot describe sharp temperature changes. If we decrease the window width to 200 minutes (21 points), we get the following result.

There is a tradeoff between the smoothness of a curve, and its ability to describe sharp temporal changes.

2.1 Kernels

We can modify our running average, so that values closer to the center of the window have higher weights, and those further away count less. This is achieved by changing the weight profile, or the shape of the kernel. We see below the result of a running average using a triangular window of base 500 minutes (51 points).

Things can get as fancy as we want. Instead of a triangular kernel, which has sharp edges, we can choose a smoother gaussian kernel, see the difference below. We used a gaussian kernel with 60-minute standard deviation (the window in the animation is 4 standard deviations wide).

2.2 Math

The definition of a convolution between signal f(t) and kernel k(t) is

$$(f*k)(t) = \int f(\tau)k(t-\tau)d\tau.$$

The expression f*k denotes the convolution of these two functions. The argument of k is $t-\tau$, meaning that the kernel runs from left to right (as t does), and at every point the two signals (f and k) are multiplied together. It is the product of the signal with the weight function k that gives us an average. Because of $-\tau$, the kernel is flipped backwards, but this has no effect to symmetric kernels, like to ones in the examples above. Finally, the actual running average is not the convolution, but

$$\frac{(f*k)(t)}{\int k(t)dt}.$$

Whenever the integral of the kernel is 1, then the convolution will be identical with the running average.

2.3 Numerics

Running averages are very common tools in time-series analysis. The pandas package makes life quite simple. For example, in order to calculate the running average of temperature using a rectangular kernel, one writes

```
df['temperature'].rolling(window='20', center=True).mean()
```

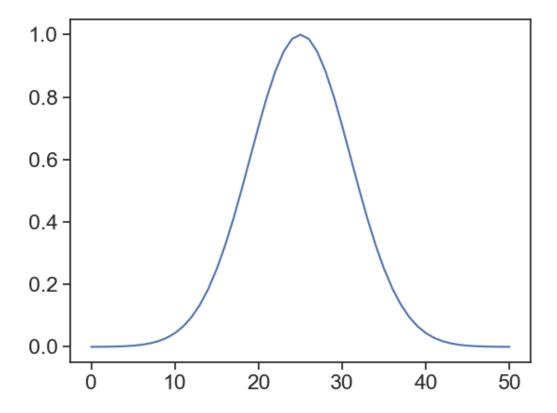
- window=20 means that the width of the window is 20 points. Pandas lets us define a window width in time units, for example, window='120min'.
- center=True is needed in order to assign the result of averaging to the center of the window. Make it False and see what happens.
- mean() is the actual calculation, the average of temperature over the window. The rolling part does not compute anything, it just creates a moving window, and we are free to calculate whatever we want. Try to calculate the standard deviation or the maximum, for example.

It is implicit in the command above a "rectangular" kernel. What if we want other shapes?

2.3.1 Gaussian

where * window_width is an integer, number of points in your window * std_gaussian is the standard deviation of your gaussian, measured in sample points, not time!

For instance, if we have measurements every 10 minutes, and our window width is 500 minutes, then window_width = 500/10 + 1 (first and last included). If we want a standard deviation of 60 minutes, then std_gaussian = 6. The gaussian kernel will look like this:



You can take a look at various options for kernel shapes here, provided by the scipy package. The graph above was achieved by running:

```
g = scipy.signal.gaussian(window_width, std)
plt.plot(g)
```

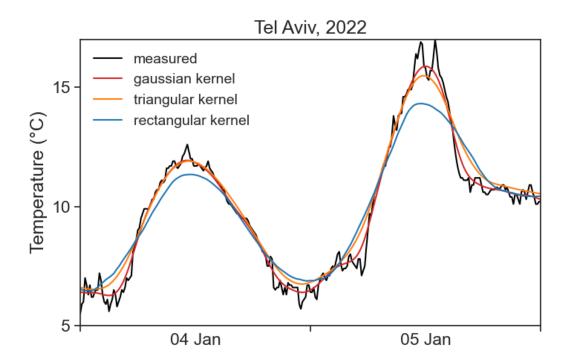
2.3.2 Triangular

Same idea as gaussian, but simpler, because we don't need to think about standard deviation.

2.4 Which window shape and width to choose?

)

Sorry, there is not definite answer here... It really depends on your data and what you need to do with it. See below a comparison of all examples in the videos above.



Part III Time Lags

3 Dynamic Time Warp

Part IV Seasonality

4 Seasonal Decomposition

```
import numpy as np
import matplotlib.pyplot as plt
import pandas as pd
from pandas.plotting import register_matplotlib_converters
register_matplotlib_converters() # datetime converter for a matplotlib
import seaborn as sns
sns.set(style="ticks", font_scale=1.5)
from statsmodels.tsa.seasonal import seasonal_decompose
import matplotlib.dates as mdates
from matplotlib.dates import DateFormatter
```

5 Trends in Atmospheric Carbon Dioxide

Mauna Loa CO2 concentration. data from NOAA

```
url = "https://gml.noaa.gov/webdata/ccgg/trends/co2/co2_weekly_mlo.csv"
df = pd.read_csv(url, header=47, na_values=[-999.99])

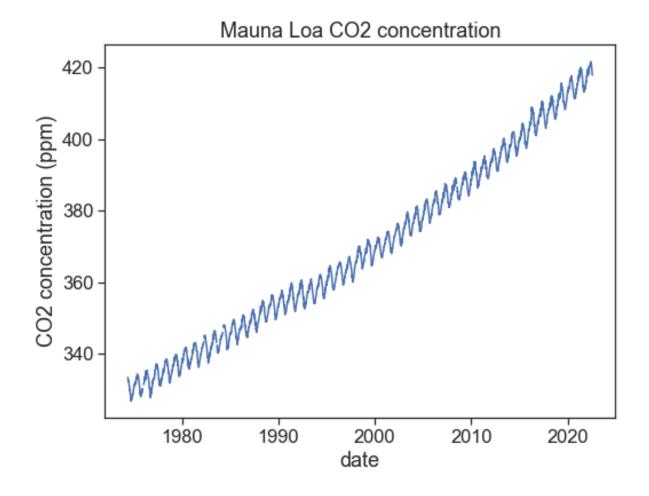
# you can first download, and then read the csv
# filename = "co2_weekly_mlo.csv"
# df = pd.read_csv(filename, header=47, na_values=[-999.99])

df
```

	year	month	day	decimal	average	ndays	1 year ago	10 years ago	increase since 1800
0	1974	5	19	1974.3795	333.37	5	NaN	NaN	50.40
1	1974	5	26	1974.3986	332.95	6	NaN	NaN	50.06
2	1974	6	2	1974.4178	332.35	5	NaN	NaN	49.60
3	1974	6	9	1974.4370	332.20	7	NaN	NaN	49.65
4	1974	6	16	1974.4562	332.37	7	NaN	NaN	50.06
2510	2022	6	26	2022.4836	420.31	7	418.14	395.36	138.71
2511	2022	7	3	2022.5027	419.73	6	417.49	395.15	138.64
2512	2022	7	10	2022.5219	419.08	6	417.25	394.59	138.52
2513	2022	7	17	2022.5411	418.43	6	417.14	394.64	138.41
2514	2022	7	24	2022.5603	417.84	6	415.68	394.11	138.36

```
df['date'] = pd.to_datetime(df[['year', 'month', 'day']])
df = df.set_index('date')
df
```

	year	month	day	decimal	average	ndays	1 year ago	10 years ago	increase since 180
date									
1974-05-19	1974	5	19	1974.3795	333.37	5	NaN	NaN	50.40
1974-05-26	1974	5	26	1974.3986	332.95	6	NaN	NaN	50.06
1974-06-02	1974	6	2	1974.4178	332.35	5	NaN	NaN	49.60
1974-06-09	1974	6	9	1974.4370	332.20	7	NaN	NaN	49.65
1974-06-16	1974	6	16	1974.4562	332.37	7	NaN	NaN	50.06
•••							•••	•••	•••
2022-06-26	2022	6	26	2022.4836	420.31	7	418.14	395.36	138.71
2022-07-03	2022	7	3	2022.5027	419.73	6	417.49	395.15	138.64
2022-07-10	2022	7	10	2022.5219	419.08	6	417.25	394.59	138.52
2022-07-17	2022	7	17	2022.5411	418.43	6	417.14	394.64	138.41
2022-07-24	2022	7	24	2022.5603	417.84	6	415.68	394.11	138.36



fill missing data. interpolate method: 'time' interpolation methods visualized

	year	month	day	decimal	average	ndays	1 year ago	10 years ago	increase since 180
date									
1974-05-19	1974	5	19	1974.3795	333.37	5	NaN	NaN	50.40
1974-05-26	1974	5	26	1974.3986	332.95	6	NaN	NaN	50.06
1974-06-02	1974	6	2	1974.4178	332.35	5	NaN	NaN	49.60
1974-06-09	1974	6	9	1974.4370	332.20	7	NaN	NaN	49.65

	year	month	day	decimal	average	ndays	1 year ago	10 years ago	increase since 180
date									
1974-06-16	1974	6	16	1974.4562	332.37	7	NaN	NaN	50.06
2022-06-26	2022	6	26	2022.4836	420.31	7	418.14	395.36	138.71
2022-07-03	2022	7	3	2022.5027	419.73	6	417.49	395.15	138.64
2022-07-10	2022	7	10	2022.5219	419.08	6	417.25	394.59	138.52
2022-07-17	2022	7	17	2022.5411	418.43	6	417.14	394.64	138.41
2022-07-24	2022	7	24	2022.5603	417.84	6	415.68	394.11	138.36

5.1 decompose data

seasonal_decompose returns an object with four components:

• observed: Y(t)• trend: T(t)• seasonal: S(t)• resid: e(t)

Additive model:

$$Y(t) = T(t) + S(t) + e(t)$$

Multiplicative model:

$$Y(t) = T(t) \times S(t) \times e(t)$$

5.1.0.1 Interlude

learn how to use zip in a loop

```
letters = ['a', 'b', 'c', 'd', 'e']
numbers = [1, 2, 3, 4, 5]
# zip let's us iterate over to lists at the same time
for l, n in zip(letters, numbers):
    print(f"{1} = {n}")
```

a = 1

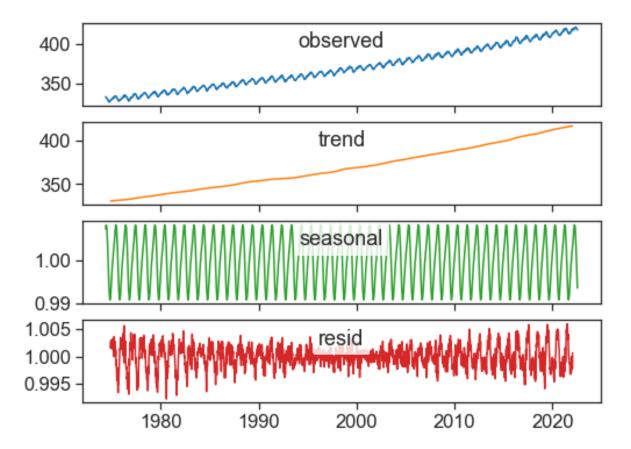
b = 2

c = 3

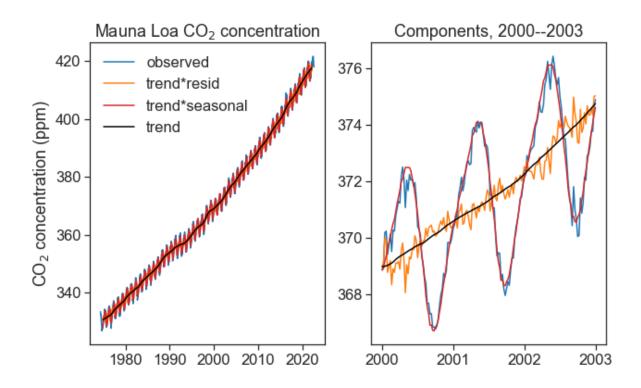
d = 4

e = 5

Plot each component separately.



```
# %matplotlib widget
decomposed = decomposed_m
fig, ax = plt.subplots(1, 2, figsize=(10,6))
ax[0].plot(df['co2'], color="tab:blue", label="observed")
ax[0].plot(decomposed.trend * decomposed.resid, color="tab:orange", label="trend*resid")
ax[0].plot(decomposed.trend * decomposed.seasonal, color="tab:red", label="trend*seasonal"
ax[0].plot(decomposed.trend, color="black", label="trend")
ax[0].set(ylabel="CO$_2$ concentration (ppm)",
          title="Mauna Loa CO$_2$ concentration")
ax[0].legend(frameon=False)
start = "2000-01-01"
end = "2003-01-01"
zoom = slice(start, end)
ax[1].plot(df.loc[zoom, 'co2'], color="tab:blue", label="observed")
ax[1].plot((decomposed.trend * decomposed.resid)[zoom], color="tab:orange", label="trend*r
ax[1].plot((decomposed.trend * decomposed.seasonal)[zoom], color="tab:red", label="trend*s
ax[1].plot(decomposed.trend[zoom], color="black", label="trend")
date_form = DateFormatter("%Y")
ax[1].xaxis.set_major_formatter(date_form)
ax[1].xaxis.set_major_locator(mdates.YearLocator(1))
ax[1].set_title("Components, 2000--2003");
```



References