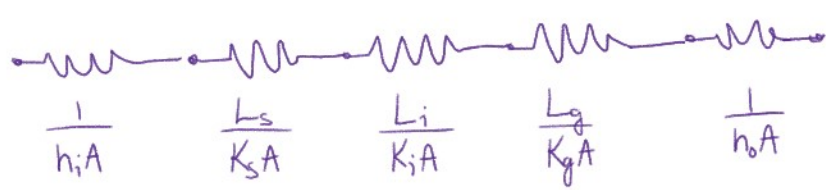
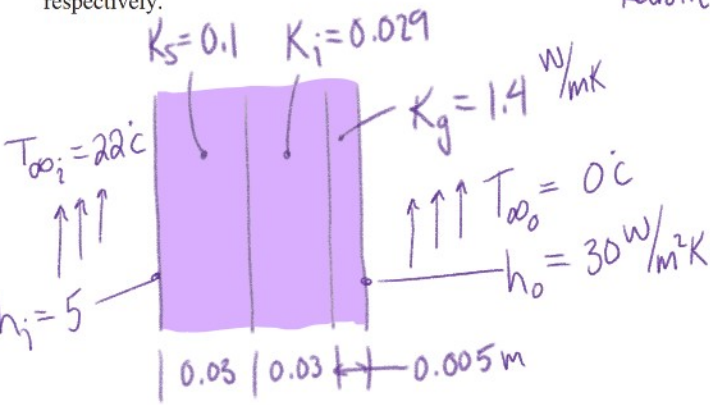


HW3.1

Tuesday, September 19, 2023 9:52 PM

Chapter3:
Problems: 4, 17, 34, 41 and 54

3.4 A dormitory at a large university, built 50 years ago, has exterior walls constructed of $L_s = 30\text{-mm}$ -thick sheathing with a thermal conductivity of $k_s = 0.1\text{ W/m}\cdot\text{K}$. To reduce heat losses in the winter, the university decides to encapsulate the entire dormitory by applying an $L_i = 30\text{-mm}$ -thick layer of extruded insulation characterized by $k_i = 0.029\text{ W/m}\cdot\text{K}$ to the exterior of the original sheathing. The extruded insulation is, in turn, covered with an $L_g = 5\text{-mm}$ -thick architectural glass with $k_g = 1.4\text{ W/m}\cdot\text{K}$. Determine the heat flux through the original and retrofitted walls when the interior and exterior air temperatures are $T_{\infty,i} = 22^\circ\text{C}$ and $T_{\infty,o} = 0^\circ\text{C}$, respectively. The inner and outer convection heat transfer coefficients are $h_i = 5\text{ W/m}^2\cdot\text{K}$ and $h_o = 30\text{ W/m}^2\cdot\text{K}$, respectively.



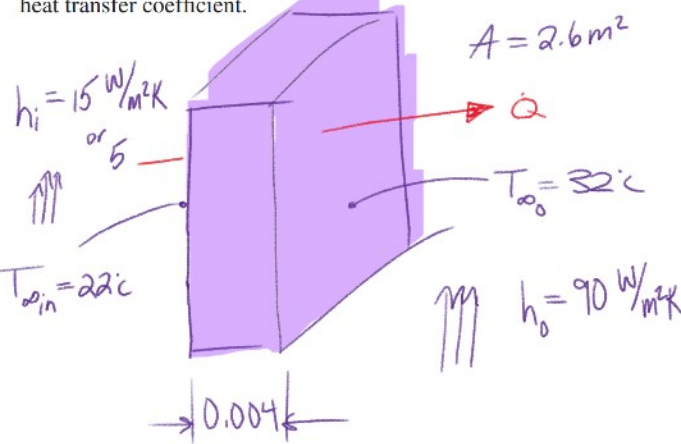
Retrofit

$$\frac{q''}{b/A} = \frac{\Delta T}{\sum R_{tot}} = \frac{q}{A} = \frac{T_{\infty,o} - T_{\infty,i}}{\frac{1}{A} \left(\frac{1}{h_i} + \frac{L_s}{k_s} + \frac{L_i}{k_i} + \frac{L_g}{k_g} + \frac{1}{h_o} \right)}$$
$$q'' = \frac{22 - 0}{\frac{1}{5} + \frac{0.03}{0.1} + \frac{0.03}{0.029} + \frac{0.005}{1.4} + \frac{1}{30}} = 14.0\text{ W/m}^2$$

Original

$$q'' = \frac{22 - 0}{\frac{1}{5} + \frac{0.03}{0.1} + \frac{1}{30}} = 41.25\text{ W/m}^2$$

3.17 The $t = 4\text{-mm}$ -thick glass windows of an automobile have a surface area of $A = 2.6\text{ m}^2$. The outside temperature is $T_{\infty,o} = 32^\circ\text{C}$ while the passenger compartment is maintained at $T_{\infty,i} = 22^\circ\text{C}$. The convection heat transfer coefficient on the exterior window surface is $h_o = 90\text{ W/m}^2\cdot\text{K}$. Determine the heat gain through the windows when the interior convection heat transfer coefficient is $h_i = 15\text{ W/m}^2\cdot\text{K}$. By controlling the airflow in the passenger compartment the interior heat transfer coefficient can be reduced to $h_i = 5\text{ W/m}^2\cdot\text{K}$ without sacrificing passenger comfort. Determine the heat gain through the window for the reduced inside heat transfer coefficient.

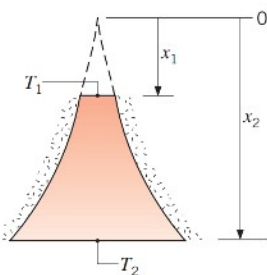


$$\dot{Q} = \frac{\Delta T}{R_{tot}}$$



$$\dot{Q} = \frac{T_{\infty,o} - T_{\infty,i}}{\frac{1}{A} \left(\frac{1}{h_i} + \frac{L}{k} + \frac{1}{h_o} \right)}$$
$$= \frac{(32) - (22)}{(2.6) \left(\frac{1}{15} + \frac{0.004}{1.4} + \frac{1}{90} \right)} = 47.7\text{ W/m}^2$$

3.34 A truncated solid cone is of circular cross section, and its diameter is related to the axial coordinate by an expression of the form $D = ax^{3/2}$, where $a = 2.0\text{ m}^{-1/2}$.



The sides are well insulated, while the top surface of the cone at x_1 is maintained at T_1 and the bottom surface at x_2 is maintained at T_2 .

- (a) Obtain an expression for the temperature distribution $T(x)$.
- (b) What is the rate of heat transfer across the cone if it is constructed of pure aluminum with $x_1 = 0.080\text{ m}$, $T_1 = 100^\circ\text{C}$, $x_2 = 0.240\text{ m}$, and $T_2 = 20^\circ\text{C}$?

$$D = 2x^{3/2}$$
$$A = \frac{\pi D^2}{4} = \pi x^3$$

a)

$$\dot{Q} = -KA \frac{dT}{dx} = -K \pi x^3 \frac{dT}{dx}$$
$$\frac{-\dot{Q}}{K \pi} \int_{x_1}^{x_2} x^3 dx = \int_{T_1}^{T_2} dT$$
$$\frac{\dot{Q}}{K \pi} \frac{x^4}{4} \Big|_{x_1}^{x_2} = T \Big|_{T_1}^{T_2}$$
$$\frac{\dot{Q}}{4 \pi K} \left(\frac{1}{x_2^4} - \frac{1}{x_1^4} \right) = (T - T_1)$$

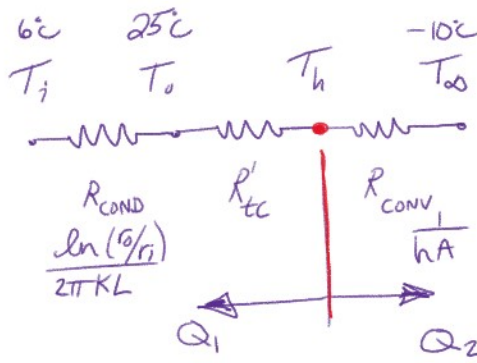
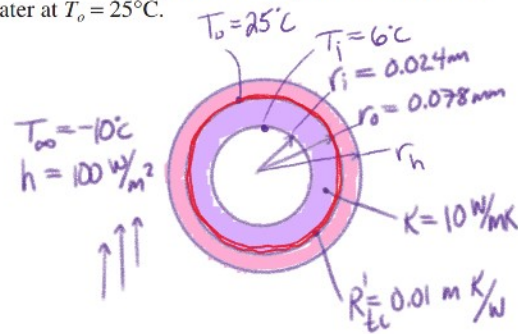
$$T(x) = \frac{\dot{Q}}{4 \pi K} \left(\frac{1}{x^4} - \frac{1}{x_1^4} \right) + T_1$$

b)

$$\dot{Q} = \frac{2 \pi K (T_2 - T_1)}{\frac{1}{x_2^4} - \frac{1}{x_1^4}}$$
$$= \frac{2 \pi (240) (20 - 100)}{\frac{1}{(0.24)^4} - \frac{1}{(0.08)^4}} = 868.6\text{ W}$$

At 20°C $\rightarrow 293\text{ K}$
 $\hookrightarrow K \approx 240\text{ W/mK}$

3.41 A thin electrical heater is wrapped around the outer surface of a long cylindrical tube whose inner surface is maintained at a temperature of 6°C. The tube wall has inner and outer radii of 24 and 78 mm, respectively, and a thermal conductivity of 10 W/m · K. The thermal contact resistance between the heater and the outer surface of the tube (per unit length of the tube) is $R'_{tc} = 0.01 \text{ m} \cdot \text{K/W}$. The outer surface of the heater is exposed to a fluid with $T_\infty = -10^\circ\text{C}$ and a convection coefficient of $h = 100 \text{ W/m}^2 \cdot \text{K}$. Determine the heater power per unit length of tube required to maintain the heater at $T_o = 25^\circ\text{C}$.



Why is no thickness given for heater?

$$\dot{Q} = \frac{2\pi KL(T_1 - T_2)}{\ln(r_2/r_1)}$$

$$\dot{Q} = \frac{\Delta T}{\sum R}$$

$$R = \frac{\ln(r_2/r_1)}{2\pi KL}$$

$$Q_{tot} = Q_1 + Q_2 = \frac{(T_o - T_i)}{R_{COND} + R'_{tc}} + \frac{(T_o - T_\infty)}{R_{CONV}}$$

$$Q_{tot} = \frac{(25) - (6)}{\frac{\ln(0.078/0.024)}{2\pi(10)L} + 0.01} + \frac{(25) - (-10)}{\frac{1}{(100)2\pi(r_o)L}}$$

THIS IS PER UNIT LENGTH
SO "L" IS TAKEN OUT OF
EQUATIONS

$$Q_{tot} =$$