

COMP206: Mathematical Modeling and Algorithmic Thinking

Answer to Question 1

Part a

```
A = rand(100,1)*100;  
A = sort(A);  
  
exponential = exp(A);  
plot(A,exponential);
```

Part b

```
A = rand(100,1)*100;  
A = sort(A);  
  
logarithmic = log(A);  
plot(A,logarithmic);
```

Part c

```
A = rand(100,1)*100;  
A = sort(A);  
  
sinus = sin(A);  
plot(A,sinus);
```

Part d

```
A = rand(100,1)*100;  
A = sort(A);  
  
cosinus = cos(A);  
plot(A,cosinus);
```

Answer to Question 2

```
%% Question 2  
  
H = readmatrix('input.txt');  
A = spconvert(H);  
D = sum(A,2);  
DHalf = diag(sqrt(D));  
  
identity = eye(10708);  
  
P = identity - (DHalf*A*DHalf);
```

```

%% part a
tic;
[eigenVectors, eigenValues] = eigs(P,2);
toc;

P = full(P);

%% part b

prp = size(P,1);
empty = 1:1:prp;

scatter(empty, eigenVectors(:,1), 'magenta');
hold on;
scatter(empty, eigenVectors(:,2), 'cyan');

%% part c

partc = eig(P + (0.6)*identity);

%% part d

tic
[eigenVectorsPowered, eigenValuesPowered] = eig(P^20);
toc

Elapsed time is 8.030583 seconds for part a. Elapsed time is 465.660931 seconds for part d. Q3)

```

Answer to Question 3

```

%% part a

H = readmatrix ("input.txt");
A = spconvert(H);
D = sum(A,2);
Dhalf = diag(sparse(1./sqrt(D)));

identity = eye(10708);

Q3PProof = identity - (0.85 * (Dhalf * (A * Dhalf)));

b = zeros(10708,1);

for i = 1:10
    b(i,1) = 1/10;
end

inverseQ3PProof = inv(Q3PProof);

tic;
q3PartAX = Q3PProof\b;
toc;

%% part b

```

```

tic;
q3PartAXEfficient = zeros(10708,1);
for i = 1:10708
    q3PartAXEfficient(i,1) = inverseQ3PProof(i,:) * b(:,1);
end
toc;

```

Elapsed time is 7.282455 seconds for part a. Elapsed time is 1.641797 seconds for part b.

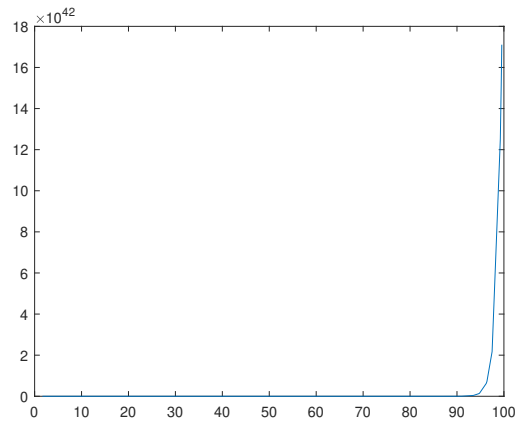


Figure 1: q_1 exp

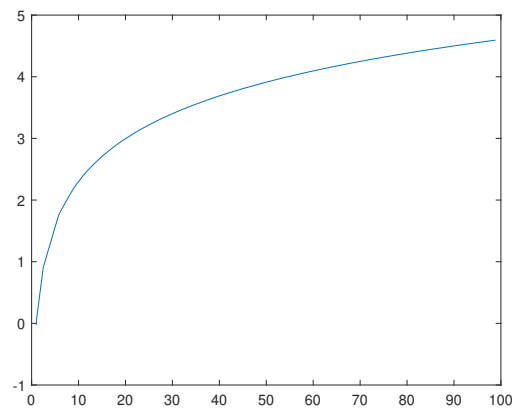


Figure 2: q_1 log

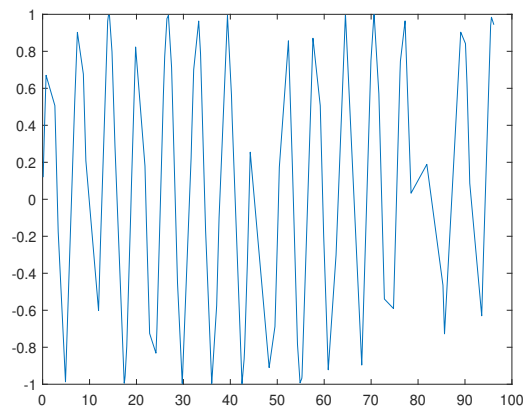


Figure 3: Q1 sinus

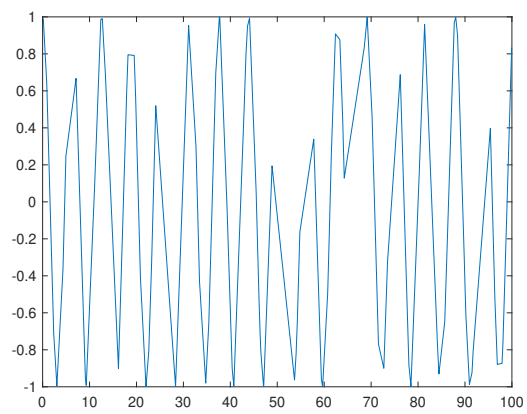


Figure 4: Q1 cosinus

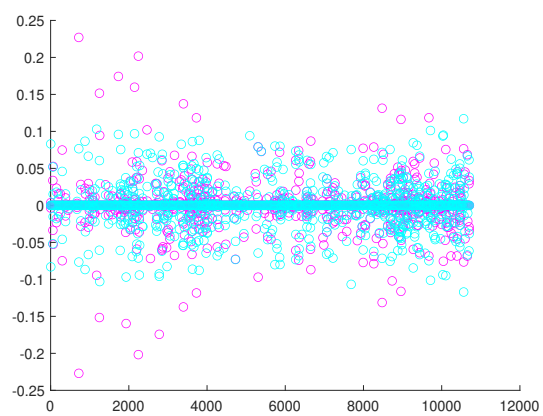


Figure 5: Q2 part b scatter