Supplementary Material for "Capacity of Wireless Channels Under Transceiver Hardware Impairments and Adaptive Transmission Techniques"

Yazan H. Al-Badarneh, Member, IEEE, Osamah S. Badarneh, Mustafa K. Alshawaqfeh, Mazen O. Hasna, Senior Member, IEEE, Tamer M. Khattab, Senior Member, IEEE

Table I: Capacity of the THZ link under THI

Transmission Technique

Capacity Expression

OPRA

$$\begin{split} C_{\mathrm{OPRA}} &= -\frac{\Lambda \ln \left(\gamma_0 k^2\right) \gamma_0 \frac{v}{2}}{\ln (2) (1 - k^2 \gamma_0) \frac{v}{2}} H_{2,3}^{3,0} \left[\frac{\beta \gamma_0 \frac{\alpha}{2}}{(1 - k^2 \gamma_0) \frac{\alpha}{2}} \right| \frac{(1,1), (1 - \frac{v}{2}, \frac{\alpha}{2})}{(-\frac{v}{2}, \frac{\alpha}{2}), (0,1), (C,1)} \right] \\ &- \frac{\Lambda \alpha \gamma_0 \frac{v}{2} - 1}{2 \ln (2) k^2 (1 - k^2 \gamma_0) \frac{v}{2} - 1} H_{1,1:2,2;1,2}^{1,0:2,1;2,0} \left[\frac{\frac{\beta \gamma_0 \frac{\alpha}{2}}{(1 - k^2 \gamma_0) \frac{\alpha}{2}}}{(\frac{k^2 \gamma_0) \frac{\alpha}{2}}{(1 - k^2 \gamma_0) \frac{\alpha}{2}}} \right| \frac{(2 - \frac{v}{2}, \frac{\alpha}{2}) : (1, \frac{\alpha}{2}), (2, \frac{\alpha}{2}) : (1, 1)}{(1 - \frac{v}{2}, \frac{\alpha}{2}) : (1, \frac{\alpha}{2}), (1, \frac{\alpha}{2}) : (0, 1), (C, 1)} \right], \quad k \neq 0. \end{split}$$

The optimal cut-off SNR γ_0 must satisfy

$$\begin{split} &\frac{\Lambda\left(\frac{1}{\gamma_0}-k^2\right)\gamma_0^{\frac{v}{2}}}{(1-k^2\gamma_0)^{\frac{v}{2}}}H_{2,3}^{3,0}\left[\frac{\beta\gamma_0^{\frac{\alpha}{2}}}{(1-k^2\gamma_0)^{\frac{\alpha}{2}}}\bigg| \begin{array}{c} (1,1),(1-\frac{v}{2},\frac{\alpha}{2})\\ (-\frac{v}{2},\frac{\alpha}{2}),(0,1),(C,1) \end{array}\right]\\ &-\frac{\Lambda\gamma_0^{\frac{v}{2}-1}}{(1-k^2\gamma_0)^{\frac{v}{2}-1}}H_{2,3}^{3,0}\left[\frac{\beta\gamma_0^{\frac{\alpha}{2}}}{(1-k^2\gamma_0)^{\frac{\alpha}{2}}}\bigg| \begin{array}{c} (1,1),(2-\frac{v}{2},\frac{\alpha}{2})\\ (1-\frac{v}{2},\frac{\alpha}{2}),(0,1),(C,1) \end{array}\right]=1. \end{split}$$

TIFR

$$C_{\mathrm{TIRF}} = \frac{1}{\ln(2)} \frac{\ln\left(1 + \mathcal{I}^{-1}\right) \Lambda \gamma_0^{\frac{v}{2}}}{(1 - k^2 \gamma_0)^{\frac{v}{2}}} H_{2,3}^{3,0} \left[\frac{\beta \gamma_0^{\frac{\alpha}{2}}}{(1 - k^2 \gamma_0)^{\frac{\alpha}{2}}} \right| \begin{array}{c} (1,1), (1 - \frac{v}{2}, \frac{\alpha}{2}) \\ (-\frac{v}{2}, \frac{\alpha}{2}), (0,1), (C,1) \end{array} \right],$$

$$\begin{split} \mathcal{I} = & \frac{k^2 \Lambda \gamma_0^{\frac{v}{2}}}{(1 - k^2 \gamma_0)^{\frac{v}{2}}} H_{2,3}^{3,0} \left[\frac{\beta \gamma_0^{\frac{\alpha}{2}}}{(1 - k^2 \gamma_0)^{\frac{\alpha}{2}}} \right| \frac{(1,1), (1 - \frac{v}{2}, \frac{\alpha}{2})}{(-\frac{v}{2}, \frac{\alpha}{2}), (0,1), (C,1)} \right] \\ & + \frac{\Lambda \gamma_0^{\frac{v}{2} - 1}}{(1 - k^2 \gamma_0)^{\frac{v}{2} - 1}} H_{2,3}^{3,0} \left[\frac{\beta \gamma_0^{\frac{\alpha}{2}}}{(1 - k^2 \gamma_0)^{\frac{\alpha}{2}}} \right| \frac{(1,1), (2 - \frac{v}{2}, \frac{\alpha}{2})}{(1 - \frac{v}{2}, \frac{\alpha}{2}), (0,1), (C,1)} \right]. \end{split}$$

CIFR

$$C_{\text{CIFR}} = \frac{1}{\ln(2)} \ln\left(1 + \mathcal{V}^{-1}\right), \quad \mathcal{V} = k^2 + \frac{2\Lambda \beta^{\frac{-v+2}{\alpha}}}{v-2} \Gamma\left(C + \frac{v-2}{\alpha}\right).$$

$$C_{\text{ORA}} = C_{\text{ORA}}^{(1)} - C_{\text{ORA}}^{(0)}$$

ORA

$$C_{\text{ORA}}^{(j)} = \frac{\Lambda \, \omega_j^{-\frac{v}{2}}}{\ln(2)} H_{4,3}^{1,4} \left[\beta^{-1} \omega_j^{-\frac{\alpha}{2}} \right| \\ \phantom{C_{\text{ORA}}^{(j)}} \left(1 + \frac{v}{2}, \frac{\alpha}{2} \right), (1 + \frac{v}{2}, \frac{\alpha}{2}), (1,1), (1 - C, 1) \\ \phantom{C_{\text{ORA}}^{(j)}} \left(1 + \frac{v}{2}, \frac{\alpha}{2} \right), (0,1), (\frac{v}{2}, \frac{\alpha}{2}) \right], \ \omega_j = j + k^2 \ \text{for} \ j \in \{0,1\}.$$