

# Recitation 7

---

## Checkpoint 0

---

$$\begin{aligned} O(1) = O(4) \subset O(\log(\log(n))) \subset O(\log(n)) \subset O(\log^2(n)) \subset O(n) = O(4n + 3) \\ \subset O(n \log(n)) \subset O(n^2) = O(n^2 + 20000n + 3) \subset O(2^n) \subset O(n!) \end{aligned}$$

## Checkpoint 1

---

记  $f(n) = n^3 + 300n^2$ ,  $g(n) = n^3$ , 则  $\lim_{n \rightarrow \infty} \frac{f(n)}{g(n)} = 1$ , 可令  $c = 2$ ,  $n_0 = 301$ , 使得  $f(n) \leq c * g(n)$  成立

## Checkpoint 2

---

$\exists c, n_0, s.t. \forall n > n_0, f(n) \leq c * g(n)$ , 又因为  $k > 0$ , 则  $k * f(n) \leq k * c * g(n)$ , 令  $c' = k * c > 0$ ,  $n'_0 = n_0$ , 可使定义成立