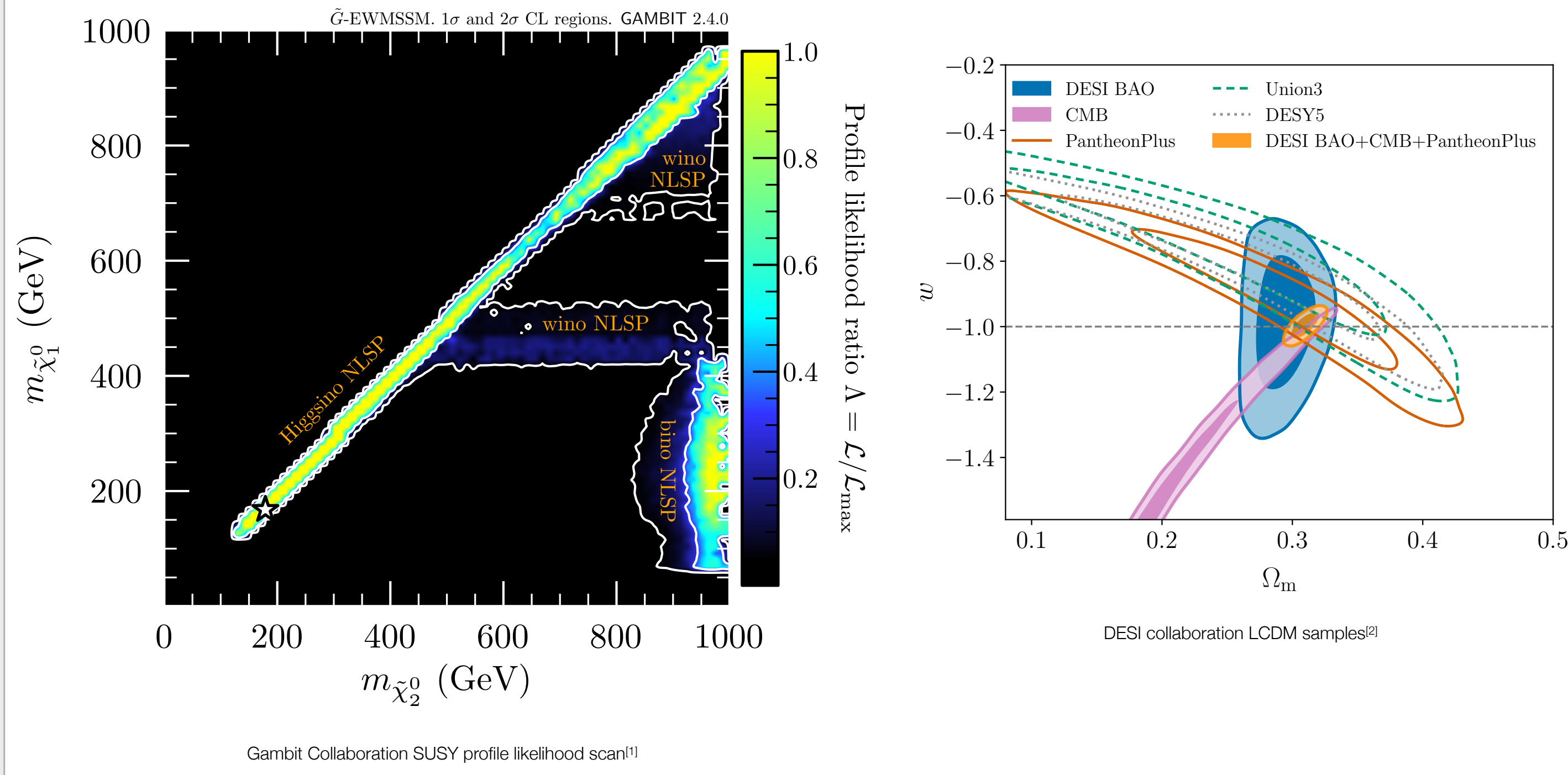


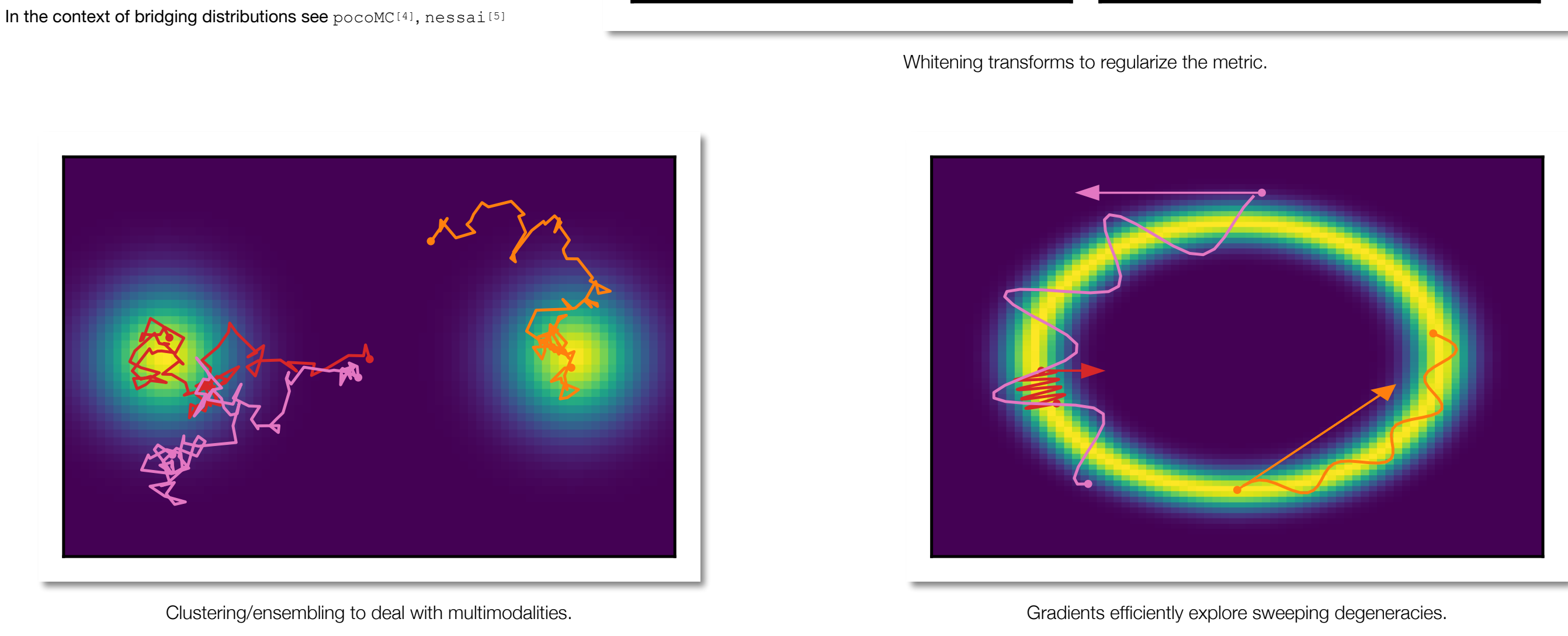
INFERENCE

Fundamental physics is full of hard inference problems. Our optimization or sampling algorithms have to be able to navigate complex geometry



GEOMETRY

Bad geometry^[3] in inference problems comes in many guises, and intuition gets progressively less clear in high dimension. Machine learnt neural mappings offer us a new tool to approach this.

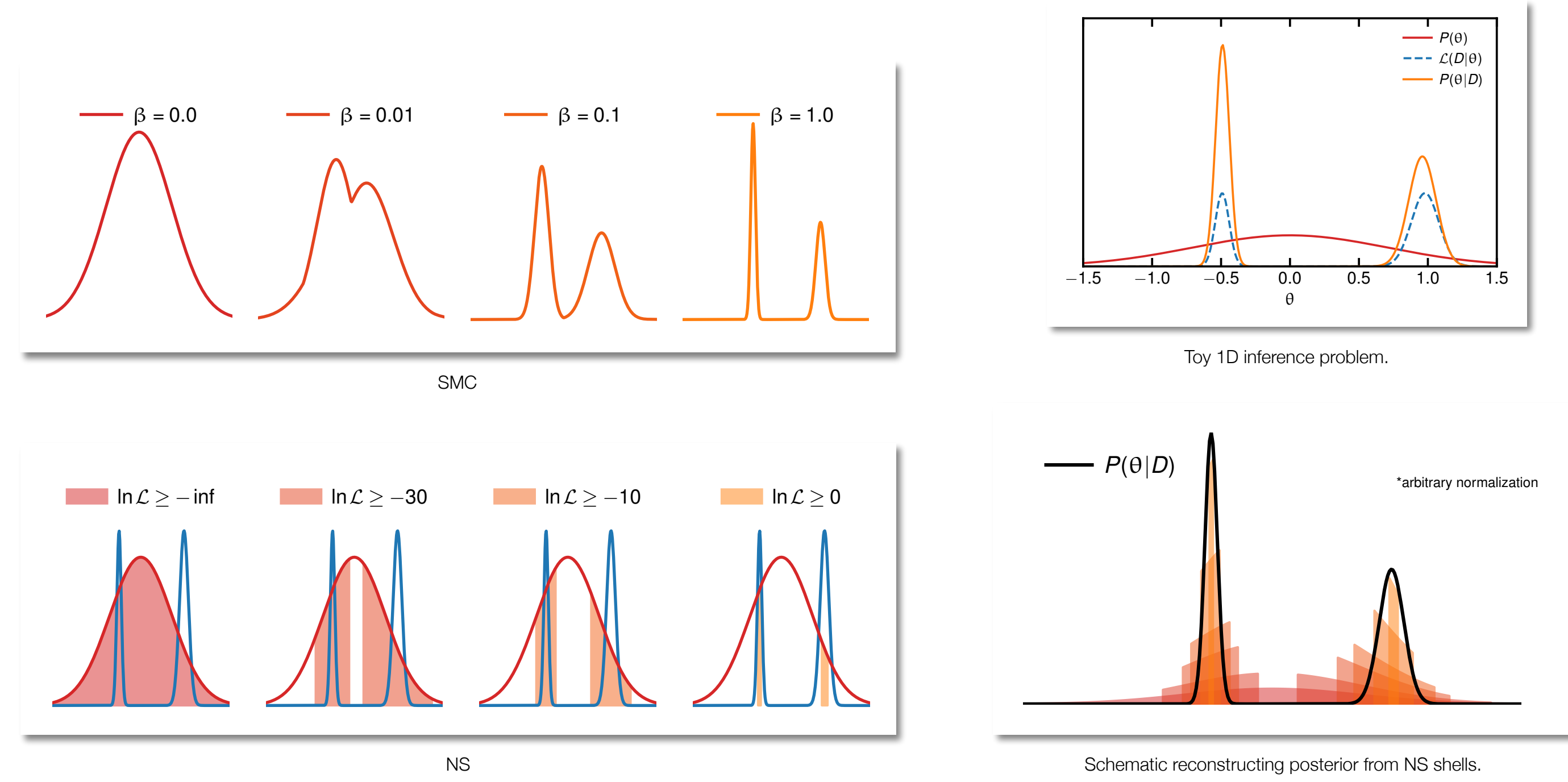


BRIDGING DISTRIBUTIONS

Population Monte Carlo methods — particle filters — form bridges from known (prior) to complex unknown (posterior) distributions. Sequential Monte Carlo (SMC) and Nested Sampling (NS) are two variants evolving populations of points^[6]. Both give us access to the normalizing constant Z .

$$P(\theta|D) = \frac{\mathcal{L}(D|\theta)P(\theta)}{Z}$$

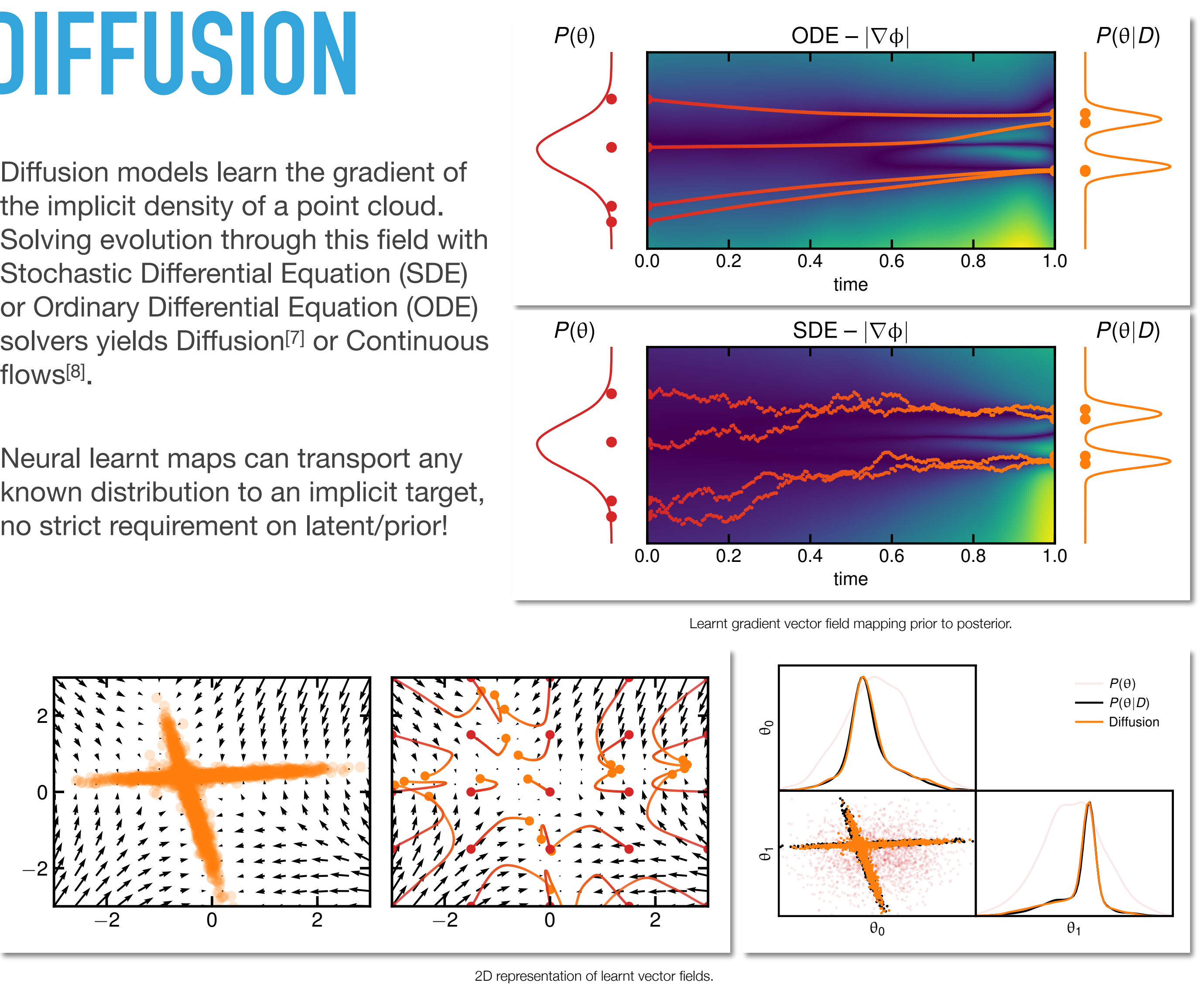
Bayes Rule



DIFFUSION

Diffusion models learn the gradient of the implicit density of a point cloud. Solving evolution through this field with Stochastic Differential Equation (SDE) or Ordinary Differential Equation (ODE) solvers yields Diffusion^[7] or Continuous flows^[8].

Neural learnt maps can transport any known distribution to an implicit target, no strict requirement on latent/prior!



DIFFUSION MEETS NESTED SAMPLING

NEUTRALISING BAD GEOMETRY IN BRIDGING INFERENCE PROBLEMS

DAVID YALLUP

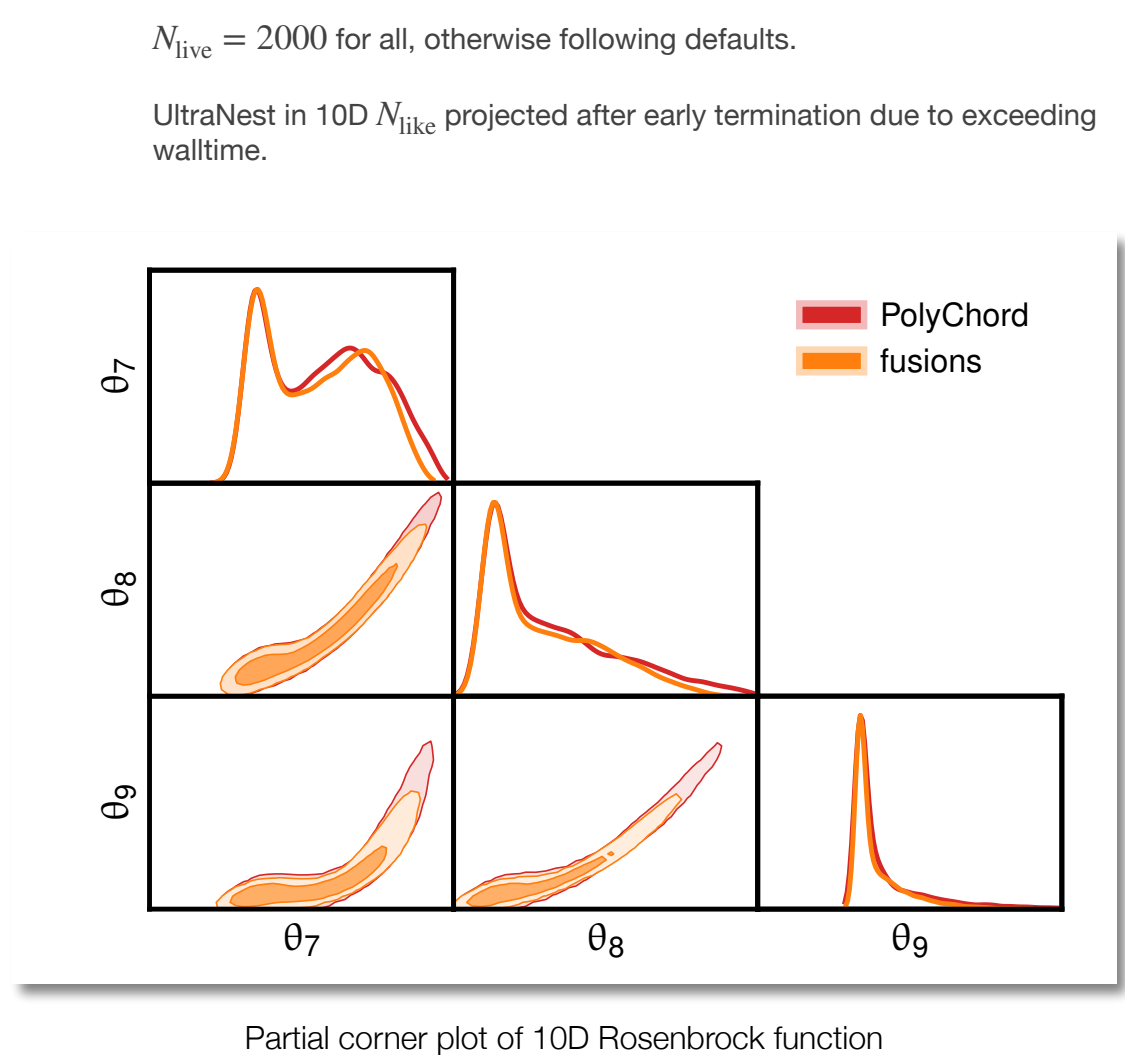
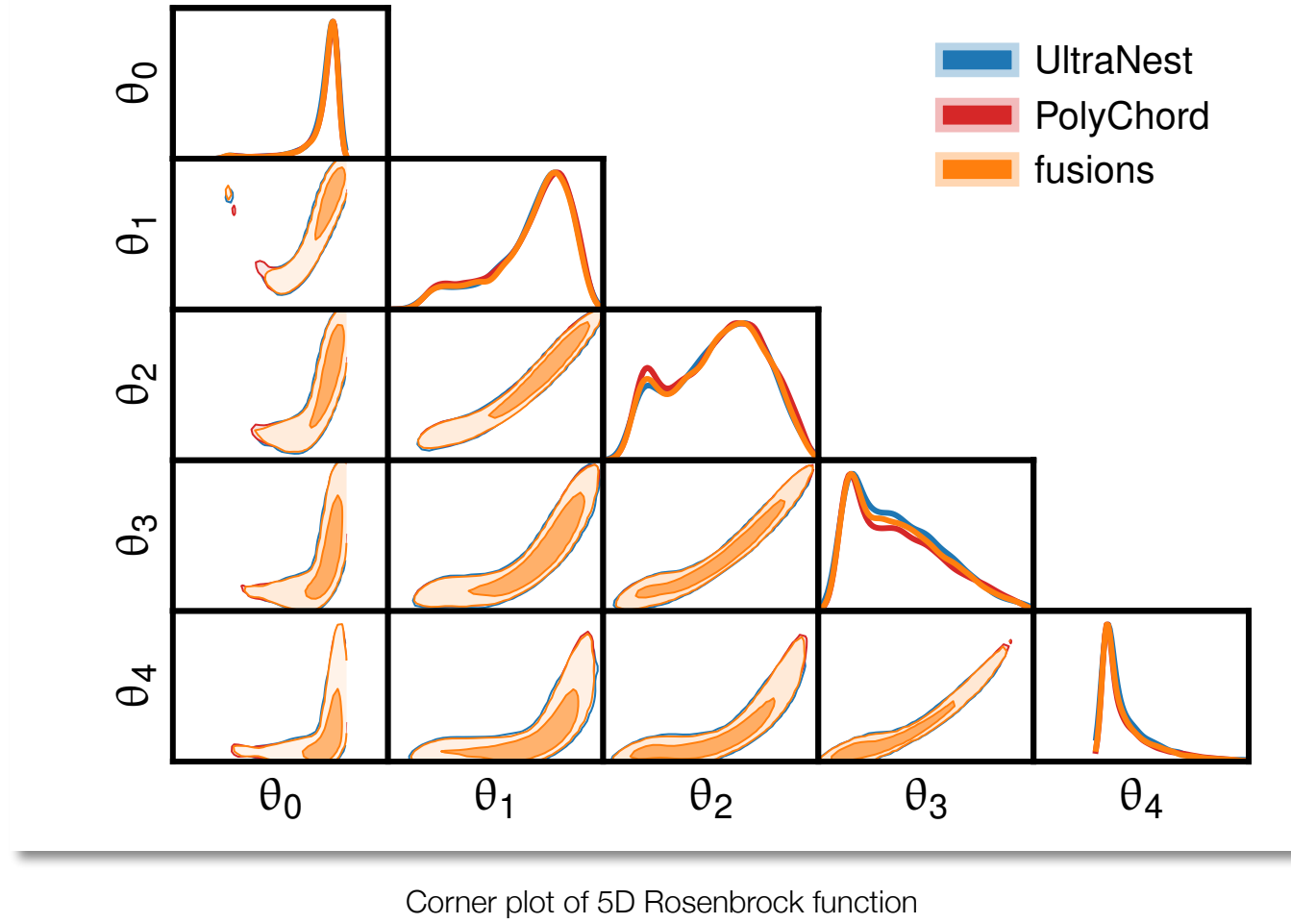
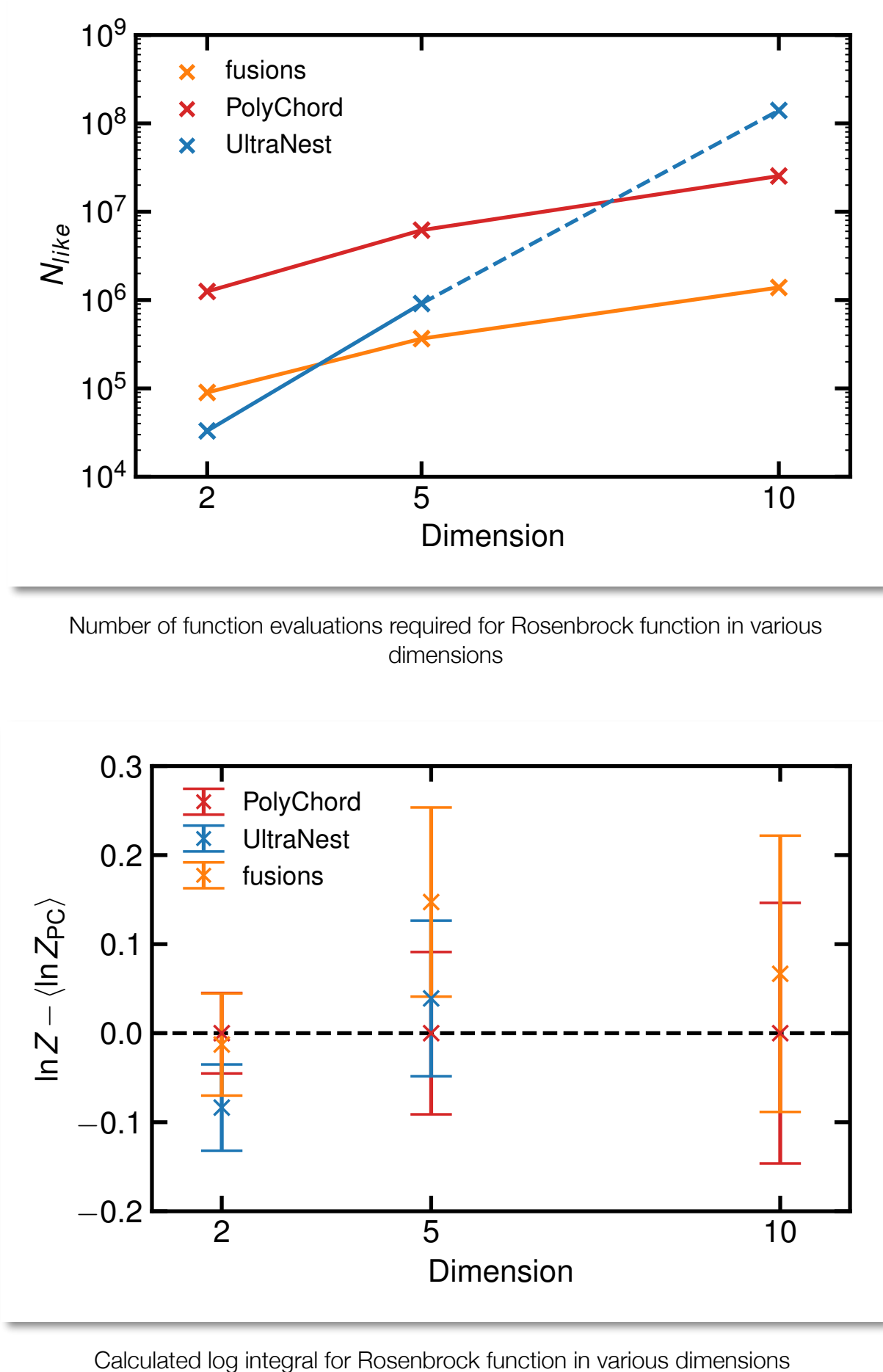
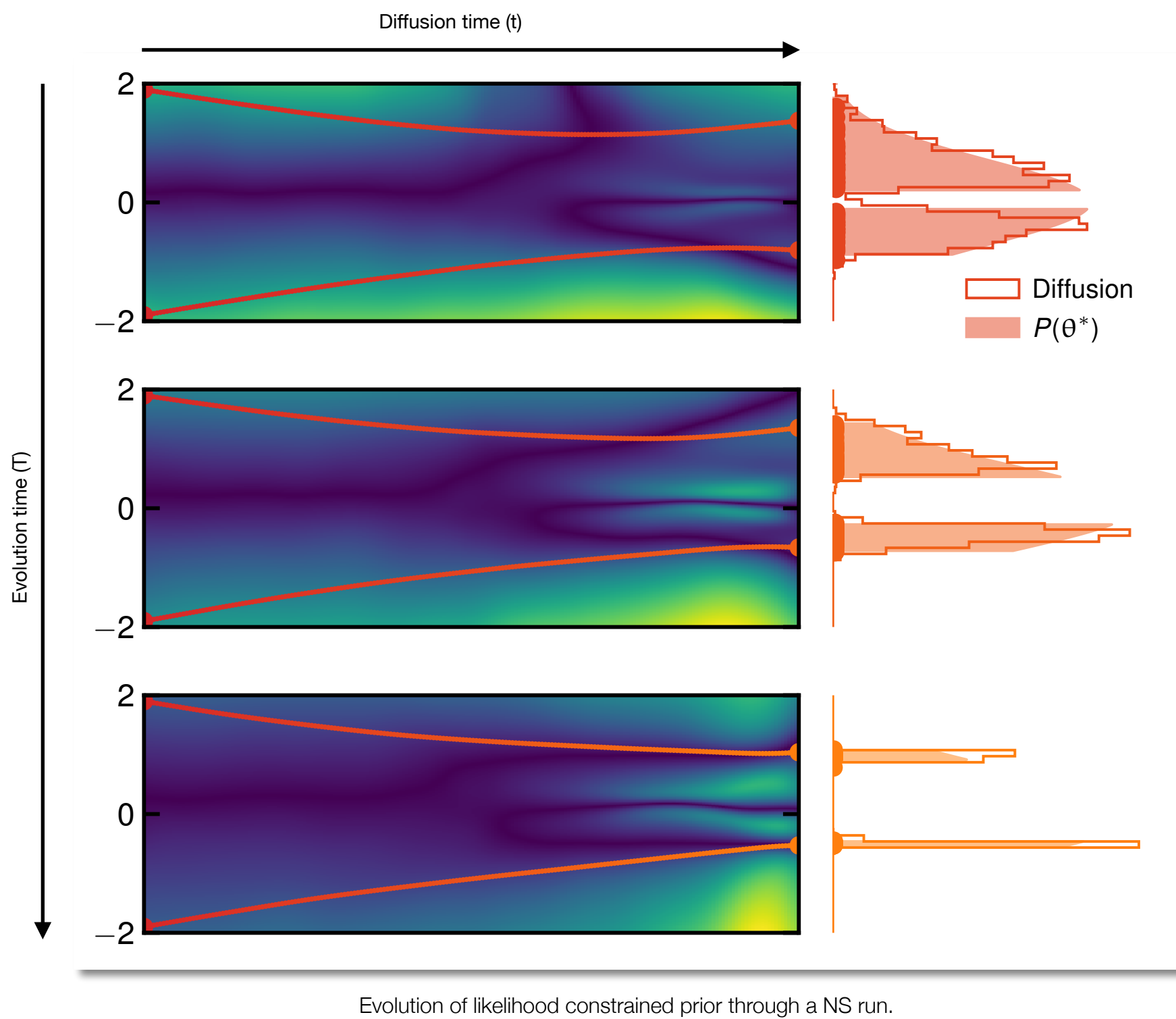
[yallup/fusions](https://github.com/yallup/fusions)

dy297@cam.ac.uk

[yallup@github.io](https://github.com/yallup)

RESULTS*

Diffusion models introduce time axis to the problem, bridging algorithms have another time axis we can efficiently evolve by fine tuning the score estimate.



Comparison to standard (non-neural) tools^[9,10] shows promising scaling, comparable to step samplers despite using rejection sampling, whilst maintaining accurate predictions on benchmark challenging problems.

Algorithm demonstrated uses *zero* classical methods, treating the geometry of the problem solely with neural networks and score based models.

* Work in progress, comparison to other neural methods^[4,5,11,12], plenty left on the table to tune in the algorithm.

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