Atomic swaps

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Parties U_0 and U_1 hold assets a on blockchain \mathbb{A} and assets b on chain \mathbb{B} respectively. We define with $\mathsf{swp}(a)$ and $\mathsf{swp}(b)$ the amount of the assets the parties agreed to swap before starting the protocol.

We define the following oracles to interact with the blockchains.

- PubTx $(\sigma_{tx}, tx, \mathbb{A})$ publish the transaction tx with signature σ_{tx} on chain \mathbb{A}
- InitTx $(pk_{tx}, pk_{rx}, amnt, \mathbb{A})$ create an unsigned transaction paying amnt from pk_{tx} to pk_{rx} on chain \mathbb{A}
- Watch $\mathsf{Tx}(tx,\mathbb{A})$ wait for the transaction tx to be confirmed on chain \mathbb{A}
- $\mathsf{GetBal}(pk, \mathbb{A})$ get the balance of assets held by pk
- $\mathsf{GetSig}(pk, \mathbb{A})$ get the signature σ_{tx} of the latest transaction in pk's record on chain \mathbb{A}

 U_1 starts counting the timeout from the moment they send the VTD commitment to U_0 , and respectively U_0 starts counting down from the moment they receive it.

If the timeout expires before the protocol is completed:

- U_1 will transfer the coins from pk(1) to another wallet on \mathbb{B} . From this moment on, if U_0 tries to $\mathsf{PubTx}(\sigma_{\mathsf{swp}(10)}, tx_{\mathsf{swp}}, \mathbb{A})$, the transaction will get rejected.
- U_0 will wait until Π_{VTD} .ForceOp(C) is completed to get the other secret key share $sk_1(01)$ of pk(10) to retrieve sk(10) and transfer back assets a to pk(0).

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U_0(pk(0), sk(0))
                                                                                                                                                       U_1(pk(1), sk(1))
                                                                                               \Gamma_{\mathsf{KeyGen}}(\mathbb{G},G,q)
                                                                                          \leftarrow (sk_0(01), pk(01))
                                                                                         (sk_1(01), pk(01)) \longrightarrow
                                                                                                                                                       (C,\pi) \leftarrow \Pi_{\mathsf{VTD}}.\mathsf{Commit}(sk_1,T)
                                                                                                         (C,\pi)
starts \mathsf{Timeout}(T-\Delta)
                                                                                                                                                       starts \mathsf{Timeout}(T - \Delta)
if \Pi_{\text{VTD}}.\text{Verify}(pk,C,\pi) \neq 1
         abort
tx_{\mathsf{frz}} \leftarrow \mathsf{InitTx}(pk(0), pk(01), \mathsf{swp}(\mathsf{a}), \mathbb{A})
\sigma_{\mathsf{frz}} \leftarrow \Pi_{\mathsf{DS}}.\mathsf{Sign}(sk(0), tx_{\mathsf{frz}})
\mathsf{PubTx}(\sigma_{\mathsf{frz}}, tx_{\mathsf{frz}}, \mathbb{A})
starts \Pi_{VTD}. Force Op(C)
                                                                                                                                                       do bal \leftarrow \mathsf{GetBal}(pk(01), \mathbb{A})
                                                                                                                                                       \mathsf{while}\:\mathsf{bal} \neq \mathsf{swp}(\mathsf{a})
                                                                                                         pk(1)
(pk(10), sk(10)) \leftarrow \Pi_{DS}.\mathsf{KeyGen}(1^{\lambda})
tx_{\mathsf{swp}} \leftarrow \mathsf{InitTx}(pk(1), pk(10), \mathsf{swp}(\mathsf{b}), \mathbb{A})
                                                                                                            \Gamma_{\mathsf{Swap}}
                                                                                          U_0 \longrightarrow (sk_0(01), tx_{\text{swp}})
                                                                                        (sk_1(01), sk(1)) \longleftarrow U_1
                                                                                  lk := \sigma_{swp}(10) \oplus sk_0(01) \xrightarrow{\longrightarrow}
                                                                                                 \leftarrow \sigma_{swp}(10)
\mathsf{PubTx}(\sigma_{\mathsf{swp}(\mathsf{10})}, tx_{\mathsf{frz}}, \mathbb{A})
                                                                                                                                                       do \sigma_{swp}(10) \leftarrow \mathsf{GetSig}(pk(1), \mathbb{B})
                                                                                                                                                                sk(01) \leftarrow (lk \oplus \sigma_{swp}(10)) \oplus sk_1
                                                                                                                                                                 \sigma_m \leftarrow \Pi_{\mathsf{DS}}.\mathsf{Sign}(sk(01),1)
                                                                                                                                                       while \Pi_{\mathsf{DS}}.\mathsf{Verify}(m,pk,\sigma_m) \neq 1
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Figure 1: Protocol execution for a successful swap

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\begin{split} & \frac{U_0(pk(0)\,,sk(0))}{sk(01) := sk_0(01) \oplus sk_1(01)} \\ & \frac{\sigma_{swp}(10) \leftarrow \Pi_{\text{DS}}.\mathsf{Sign}(sk(1),tx_{\text{swp}})}{lk := \sigma_{swp}(10) \oplus sk_0(01)} \end{split}
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Figure 2: Protocol definition of 2PC Γ_{Swap}