

**PLEASE WRITE YOUR NAME AT THE BOTTOM OF THE BACK OF THIS SHEET, NOT ON THE FRONT.**

Be sure to explain your reasoning clearly. Correct answers without clear and correct justification will receive little credit.

1. Suppose that  $x_{n+1} = \sqrt{1 + x_n^2}$  for all  $n \in \mathbb{N}$ . Show that  $\langle x \rangle$  does not converge.

2. PODASIP: If  $a_n < b_n$  for all  $n \in \mathbb{N}$  and  $\sum b_n$  converges, then  $\sum a_n$  converges.

3. What number has  $.222\dots$  as its  $k$ -ary expansion?