

## CS 351 – DAA Lab Problems

### Lab Cycle - I

#### Divide and Conquer

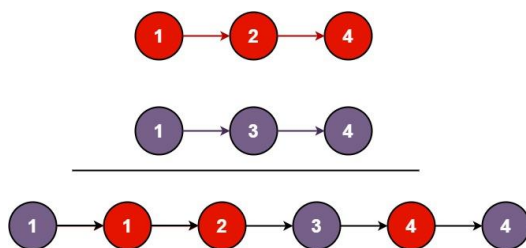
##### 1. Merge Two Sorted Lists

You are given the heads of two sorted linked lists `list1` and `list2`.

Merge the two lists in a one **sorted** list. The list should be made by splicing together the nodes of the first two lists.

Return *the head of the merged linked list*.

##### Example 1:



**Input:** `list1 = [1,2,4]`, `list2 = [1,3,4]`

**Output:** `[1,1,2,3,4,4]`

##### Example 2:

**Input:** `list1 = []`, `list2 = []`

**Output:** `[]`

##### Example 3:

**Input:** `list1 = []`, `list2 = [0]`

**Output:** `[0]`

##### Constraints:

- The number of nodes in both lists is in the range `[0, 50]`.
- `-100 <= Node.val <= 100`
- Both `list1` and `list2` are sorted in **non-decreasing** order.

Link: <https://leetcode.com/problems/merge-two-sorted-lists/>

## 2. Merge Sorted Array

You are given two integer arrays `nums1` and `nums2`, sorted in **non-decreasing order**, and two integers `m` and `n`, representing the number of elements in `nums1` and `nums2` respectively.

**Merge** `nums1` and `nums2` into a single array sorted in **non-decreasing order**.

The final sorted array should not be returned by the function, but instead be *stored inside the array* `nums1`. To accommodate this, `nums1` has a length of `m + n`, where the first `m` elements denote the elements that should be merged, and the last `n` elements are set to 0 and should be ignored. `nums2` has a length of `n`.

### Example 1:

**Input:** `nums1 = [1,2,3,0,0,0]`, `m = 3`, `nums2 = [2,5,6]`, `n = 3`

**Output:** `[1,2,2,3,5,6]`

**Explanation:** The arrays we are merging are `[1,2,3]` and `[2,5,6]`.

The result of the merge is `[1,2,2,3,5,6]` with the underlined elements coming from `nums1`.

### Example 2:

**Input:** `nums1 = [1]`, `m = 1`, `nums2 = []`, `n = 0`

**Output:** `[1]`

**Explanation:** The arrays we are merging are `[1]` and `[]`.

The result of the merge is `[1]`.

### Example 3:

**Input:** `nums1 = [0]`, `m = 0`, `nums2 = [1]`, `n = 1`

**Output:** `[1]`

**Explanation:** The arrays we are merging are `[]` and `[1]`.

The result of the merge is `[1]`.

Note that because `m = 0`, there are no elements in `nums1`. The 0 is only there to ensure the merge result can fit in `nums1`.

### Constraints:

- `nums1.length == m + n`
- `nums2.length == n`
- `0 <= m, n <= 200`
- `1 <= m + n <= 200`
- `-109 <= nums1[i], nums2[j] <= 109`

Link: <https://leetcode.com/problems/merge-sorted-array/>

### 3. Merge k Sorted Lists

You are given an array of  $k$  linked-lists `lists`, each linked-list is sorted in ascending order.

*Merge all the linked-lists into one sorted linked-list and return it.*

#### Example 1:

**Input:** `lists = [[1,4,5],[1,3,4],[2,6]]`

**Output:** `[1,1,2,3,4,4,5,6]`

**Explanation:** The linked-lists are:

```
[  
  1->4->5,  
  1->3->4,  
  2->6  
]
```

merging them into one sorted list:

1->1->2->3->4->4->5->6

#### Example 2:

**Input:** `lists = []`

**Output:** `[]`

#### Example 3:

**Input:** `lists = [[]]`

**Output:** `[]`

#### Constraints:

- $k == \text{lists.length}$
- $0 \leq k \leq 10^4$
- $0 \leq \text{lists}[i].\text{length} \leq 500$
- $-10^4 \leq \text{lists}[i][j] \leq 10^4$
- `lists[i]` is sorted in **ascending order**.
- The sum of `lists[i].length` will not exceed  $10^4$ .

Link: <https://leetcode.com/problems/merge-k-sorted-lists/>

#### 4. Sort an Array

Given an array of integers `nums`, sort the array in ascending order and return it.

You must solve the problem **without using any built-in** functions in  $O(n \log(n))$  time complexity and with the smallest space complexity possible.

##### Example 1:

**Input:** `nums = [5,2,3,1]`

**Output:** `[1,2,3,5]`

**Explanation:** After sorting the array, the positions of some numbers are not changed (for example, 2 and 3), while the positions of other numbers are changed (for example, 1 and 5).

##### Example 2:

**Input:** `nums = [5,1,1,2,0,0]`

**Output:** `[0,0,1,1,2,5]`

**Explanation:** Note that the values of `nums` are not necessarily unique.

##### Constraints:

- $1 \leq \text{nums.length} \leq 5 * 10^4$
- $-5 * 10^4 \leq \text{nums}[i] \leq 5 * 10^4$

Link: <https://leetcode.com/problems/sort-an-array/>

## Lab Cycle - II

### Greedy Programming

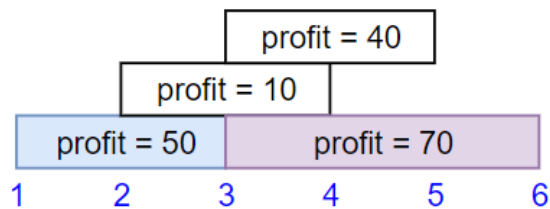
#### 1. Maximum Profit in Job Scheduling

We have  $n$  jobs, where every job is scheduled to be done from  $startTime[i]$  to  $endTime[i]$ , obtaining a profit of  $profit[i]$ .

You're given the  $startTime$ ,  $endTime$  and  $profit$  arrays, return the maximum profit you can take such that there are no two jobs in the subset with overlapping time range.

If you choose a job that ends at time  $X$  you will be able to start another job that starts at time  $X$ .

##### Example 1:

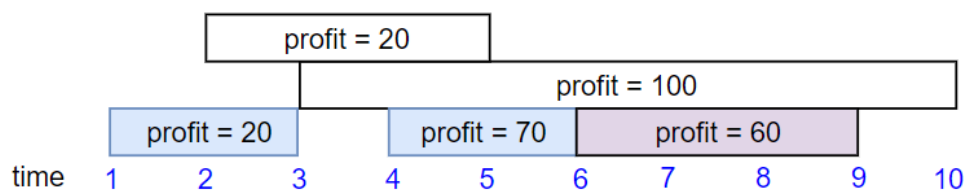


**Input:**  $startTime = [1, 2, 3, 3]$ ,  $endTime = [3, 4, 5, 6]$ ,  $profit = [50, 10, 40, 70]$

**Output:** 120

**Explanation:** The subset chosen is the first and fourth job. Time range  $[1-3] + [3-6]$ , we get profit of  $120 = 50 + 70$ .

##### Example 2:

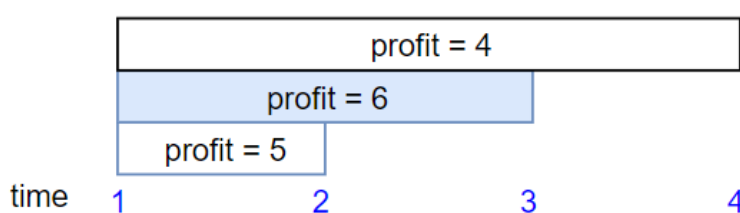


**Input:**  $startTime = [1, 2, 3, 4, 6]$ ,  $endTime = [3, 5, 10, 6, 9]$ ,  $profit = [20, 20, 100, 70, 60]$

**Output:** 150

**Explanation:** The subset chosen is the first, fourth and fifth job. Profit obtained  $150 = 20 + 70 + 60$ .

##### Example 3:



**Input:** startTime = [1,1,1], endTime = [2,3,4], profit = [5,6,4]

**Output:** 6

**Constraints:**

- $1 \leq \text{startTime.length} == \text{endTime.length} == \text{profit.length} \leq 5 * 10^4$
- $1 \leq \text{startTime}[i] < \text{endTime}[i] \leq 10^9$
- $1 \leq \text{profit}[i] \leq 10^4$

Link: <https://leetcode.com/problems/maximum-profit-in-job-scheduling/>

## 2. Coin Change

You are given an integer array coin representing coins of different denominations and an integer **amount** representing a total amount of money.

Return *the fewest number of coins that you need to make up that amount*. If that amount of money cannot be made up by any combination of the coins, return -1.

You may assume that you have an infinite number of each kind of coin.

**Example 1:**

**Input:** coins = [1,2,5], amount = 11

**Output:** 3

**Explanation:**  $11 = 5 + 5 + 1$

**Example 2:**

**Input:** coins = [2], amount = 3

**Output:** -1

**Example 3:**

**Input:** coins = [1], amount = 0

**Output:** 0

**Constraints:**

- $1 \leq \text{coins.length} \leq 12$
- $1 \leq \text{coins}[i] \leq 2^{31} - 1$
- $0 \leq \text{amount} \leq 10^4$

Link: <https://leetcode.com/problems/coin-change/>

### 3. Maximum Units on a Truck

You are assigned to put some amount of boxes onto **one truck**. You are given a 2D array `boxTypes`, where `boxTypes[i] = [numberOfBoxesi, numberOfUnitsPerBoxi]`:

- `numberOfBoxesi` is the number of boxes of type `i`.
- `numberOfUnitsPerBoxi` is the number of units in each box of the type `i`.

You are also given an integer `truckSize`, which is the **maximum** number of **boxes** that can be put on the truck. You can choose any boxes to put on the truck as long as the number of boxes does not exceed `truckSize`.

Return *the **maximum** total number of **units** that can be put on the truck*.

#### Example 1:

**Input:** `boxTypes = [[1,3],[2,2],[3,1]]`, `truckSize = 4`

**Output:** 8

**Explanation:** There are:

- 1 box of the first type that contains 3 units.
- 2 boxes of the second type that contain 2 units each.
- 3 boxes of the third type that contain 1 unit each.

You can take all the boxes of the first and second types, and one box of the third type.

The total number of units will be  $= (1 * 3) + (2 * 2) + (1 * 1) = 8$ .

#### Example 2:

**Input:** `boxTypes = [[5,10],[2,5],[4,7],[3,9]]`, `truckSize = 10`

**Output:** 91

**Constraints:**

- $1 \leq \text{boxTypes.length} \leq 1000$
- $1 \leq \text{numberOfBoxes}_i, \text{numberOfUnitsPerBox}_i \leq 1000$
- $1 \leq \text{truckSize} \leq 10^6$

Link: <https://leetcode.com/problems/maximum-units-on-a-truck/>

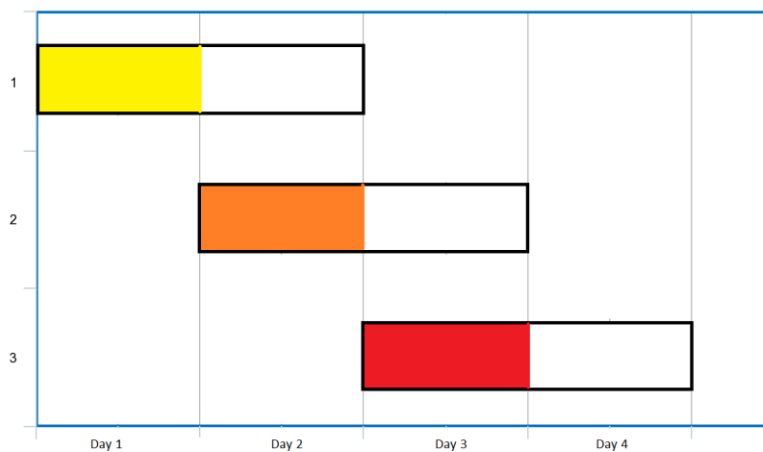
#### 4. Maximum Number of Events That Can Be Attended

You are given an array of `events` where `events[i] = [startDayi, endDayi]`. Every event `i` starts at `startDayi` and ends at `endDayi`.

You can attend an event `i` at any day `d` where `startDayi ≤ d ≤ endDayi`. You can only attend one event at any time `d`.

Return *the maximum number of events you can attend*.

##### Example 1:



**Input:** `events = [[1,2],[2,3],[3,4]]`

**Output:** 3

**Explanation:** You can attend all the three events.

One way to attend them all is as shown.

Attend the first event on day 1.

Attend the second event on day 2.

Attend the third event on day 3.

##### Example 2:

**Input:** `events = [[1,2],[2,3],[3,4],[1,2]]`

**Output:** 4

**Constraints:**

- `1 ≤ events.length ≤ 105`
- `events[i].length == 2`
- `1 ≤ startDayi ≤ endDayi ≤ 105`

Link: <https://leetcode.com/problems/maximum-number-of-events-that-can-be-attended/>



## Lab Cycle - III

### Dynamic Programming & Graphs

#### 1. Reverse Words in a String

Given an input string `s`, reverse the order of the **words**.

A **word** is defined as a sequence of non-space characters. The **words** in `s` will be separated by at least one space.

Return *a string of the words in reverse order concatenated by a single space*.

**Note** that `s` may contain leading or trailing spaces or multiple spaces between two words. The returned string should only have a single space separating the words. Do not include any extra spaces.

##### Example 1:

**Input:** `s = "the sky is blue"`

**Output:** `"blue is sky the"`

##### Example 2:

**Input:** `s = " hello world "`

**Output:** `"world hello"`

**Explanation:** Your reversed string should not contain leading or trailing spaces.

##### Example 3:

**Input:** `s = "a good example"`

**Output:** `"example good a"`

**Explanation:** You need to reduce multiple spaces between two words to a single space in the reversed string.

##### Constraints:

- $1 \leq s.length \leq 10^4$
- `s` contains English letters (upper-case and lower-case), digits, and spaces ' '.
- There is **at least one** word in `s`.

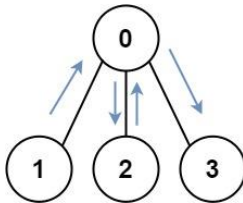
Link: <https://leetcode.com/problems/reverse-words-in-a-string/>

## 2. Shortest Path Visiting All Nodes

You have an undirected, connected graph of  $n$  nodes labeled from  $0$  to  $n - 1$ . You are given an array `graph` where `graph[i]` is a list of all the nodes connected with node  $i$  by an edge.

Return *the length of the shortest path that visits every node*. You may start and stop at any node, you may revisit nodes multiple times, and you may reuse edges.

### Example 1:

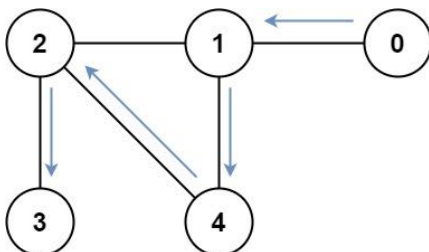


**Input:** `graph = [[1,2,3],[0],[0],[0]]`

**Output:** 4

**Explanation:** One possible path is `[1,0,2,0,3]`

### Example 2:



**Input:** `graph = [[1],[0,2,4],[1,3,4],[2],[1,2]]`

**Output:** 4

**Explanation:** One possible path is `[0,1,4,2,3]`

### Constraints:

- $n == \text{graph.length}$
- $1 \leq n \leq 12$
- $0 \leq \text{graph}[i].\text{length} < n$
- `graph[i]` does not contain  $i$ .
- If `graph[a]` contains  $b$ , then `graph[b]` contains  $a$ .
- The input graph is always connected.

Link: <https://leetcode.com/problems/shortest-path-visiting-all-nodes/>

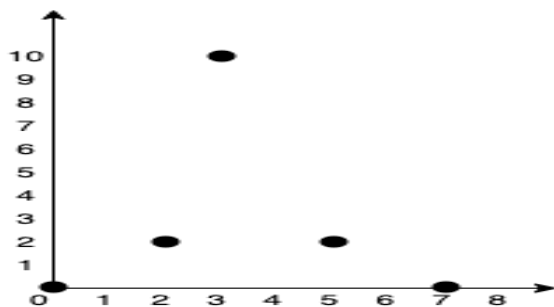
### 3. Min Cost to Connect All Points

You are given an array `points` representing integer coordinates of some points on a 2D-plane, where `points[i] = [xi, yi]`.

The cost of connecting two points `[xi, yi]` and `[xj, yj]` is the **manhattan distance** between them:  $|x_i - x_j| + |y_i - y_j|$ , where  $|val|$  denotes the absolute value of `val`.

Return *the minimum cost to make all points connected*. All points are connected if there is **exactly one** simple path between any two points.

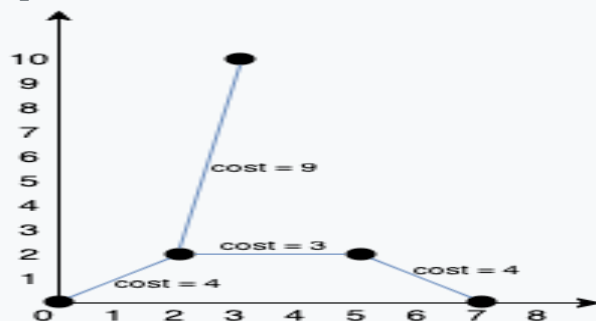
#### Example 1:



**Input:** `points = [[0,0],[2,2],[3,10],[5,2],[7,0]]`

**Output:** 20

#### Explanation:



We can connect the points as shown above to get the minimum cost of 20. Notice that there is a unique path between every pair of points.

#### Example 2:

**Input:** `points = [[3,12],[-2,5],[-4,1]]`

**Output:** 18

#### Constraints:

- $1 \leq \text{points.length} \leq 1000$
- $-10^6 \leq x_i, y_i \leq 10^6$
- All pairs  $(x_i, y_i)$  are distinct.

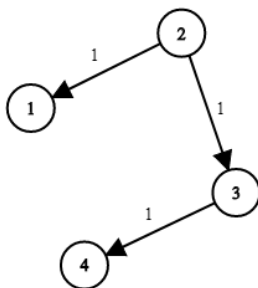
Link: <https://leetcode.com/problems/min-cost-to-connect-all-points/>

#### 4. Network Delay Time

You are given a network of  $n$  nodes, labeled from 1 to  $n$ . You are also given `times`, a list of travel times as directed edges `times[i] = (ui, vi, wi)`, where  $u_i$  is the source node,  $v_i$  is the target node, and  $w_i$  is the time it takes for a signal to travel from source to target.

We will send a signal from a given node  $k$ . Return *the **minimum** time it takes for all the  $n$  nodes to receive the signal*. If it is impossible for all the  $n$  nodes to receive the signal, return `-1`.

##### Example 1:



**Input:** `times = [[2,1,1],[2,3,1],[3,4,1]]`,  $n = 4$ ,  $k = 2$

**Output:** 2

##### Example 2:

**Input:** `times = [[1,2,1]]`,  $n = 2$ ,  $k = 1$

**Output:** 1

##### Example 3:

**Input:** `times = [[1,2,1]]`,  $n = 2$ ,  $k = 2$

**Output:** -1

##### Constraints:

- $1 \leq k \leq n \leq 100$
- $1 \leq \text{times.length} \leq 6000$
- `times[i].length == 3`
- $1 \leq u_i, v_i \leq n$
- $u_i \neq v_i$
- $0 \leq w_i \leq 100$
- All the pairs  $(u_i, v_i)$  are **unique**. (i.e., no multiple edges.)

Link: <https://leetcode.com/problems/network-delay-time/>

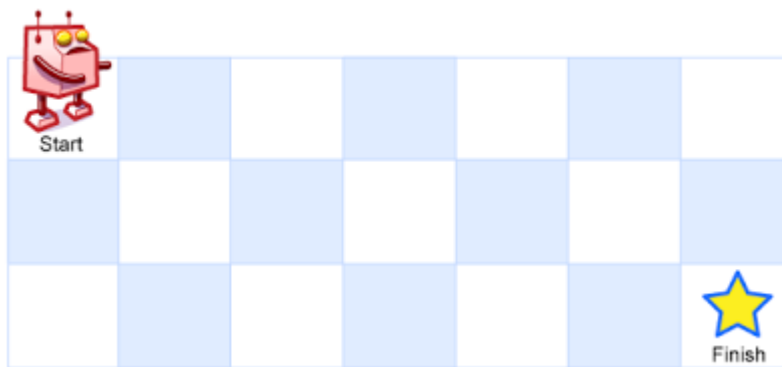
## 5. Unique Paths

There is a robot on an  $m \times n$  grid. The robot is initially located at the **top-left corner** (i.e., `grid[0][0]`). The robot tries to move to the **bottom-right corner** (i.e., `grid[m - 1][n - 1]`). The robot can only move either down or right at any point in time.

Given the two integers  $m$  and  $n$ , return *the number of possible unique paths that the robot can take to reach the bottom-right corner*.

The test cases are generated so that the answer will be less than or equal to  $2 * 10^9$ .

### Example 1:



**Input:**  $m = 3, n = 7$

**Output:** 28

### Example 2:

**Input:**  $m = 3, n = 2$

**Output:** 3

**Explanation:** From the top-left corner, there are a total of 3 ways to reach the bottom-right corner:

1. Right -> Down -> Down
2. Down -> Down -> Right
3. Down -> Right -> Down

### Constraints:

- $1 \leq m, n \leq 100$

Link: <https://leetcode.com/problems/unique-paths/>

## Lab Cycle - IV

### Backtracking & String Matching

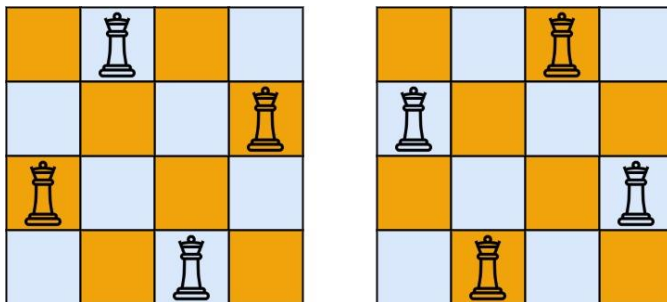
#### 1. N-Queens

The **n-queens** puzzle is the problem of placing **n** queens on an **n x n** chessboard such that no two queens attack each other.

Given an integer **n**, return *all distinct solutions to the n-queens puzzle*. You may return the answer in **any order**.

Each solution contains a distinct board configuration of the n-queens' placement, where 'Q' and '.' both indicate a queen and an empty space, respectively.

#### Example 1:



**Input:** n = 4

**Output:** [[".Q.", "...Q", "Q...", "..Q."], ["..Q.", "Q...", "...Q", ".Q.."]]

**Explanation:** There exist two distinct solutions to the 4-queens puzzle as shown above

#### Example 2:

**Input:** n = 1

**Output:** [["Q"]]

**Constraints:**

- $1 \leq n \leq 9$

Link: <https://leetcode.com/problems/n-queens/>

## 2. Longest Substring Without Repeating Characters

Given a string `s`, find the length of the **longest substring** without repeating characters.

### Example 1:

**Input:** `s = "abcabcbb"`

**Output:** 3

**Explanation:** The answer is "abc", with the length of 3.

### Example 2:

**Input:** `s = "bbbbbb"`

**Output:** 1

**Explanation:** The answer is "b", with the length of 1.

### Example 3:

**Input:** `s = "pwwkew"`

**Output:** 3

**Explanation:** The answer is "wke", with the length of 3.

Notice that the answer must be a substring, "pwke" is a subsequence and not a substring.

### Constraints:

- $0 \leq s.length \leq 5 * 10^4$
- `s` consists of English letters, digits, symbols and spaces.

Link: <https://leetcode.com/problems/longest-substring-without-repeating-characters/>

## 3. Longest Common Prefix

Write a function to find the longest common prefix string amongst an array of strings.

If there is no common prefix, return an empty string `""`.

### Example 1:

**Input:** `strs = ["flower", "flow", "flight"]`

**Output:** "fl"

### Example 2:

**Input:** `strs = ["dog", "racecar", "car"]`

**Output:** ""

**Explanation:** There is no common prefix among the input strings.

**Constraints:**

- $1 \leq \text{strs.length} \leq 200$
- $0 \leq \text{strs}[i].\text{length} \leq 200$
- `strs[i]` consists of only lowercase English letters.

Link: <https://leetcode.com/problems/longest-common-prefix/>