



# **EB5103 Advanced Analytics**

# PCA / Cluster Analysis of **Credit Card Clients of a Taiwanese Bank**

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### 1. Introduction

The credit department of a Taiwanese bank is interested in predicting loan default based on known data like demographic factors, credit data, history of payment and bill statements of its customers. The bank would also like to identify different segments of its clientele based on data collected from April to September 2005. This report describes the use of Principal Component Analysis (PCA), K-means clustering and Logistic Regression to achieve these objectives.

# 2. Data Preparation and Exploration

### 2.1 Dataset information

The dataset used for this analysis contains information on default payments, demographic factors, credit data, history of payment, and bill statements of credit card clients from a Taiwanese Bank from April to September 2005. In total, there are 30,000 observations with 25 variables. The data dictionary is included in **Appendix A**.

# 2.2 Data Preparation

While no missing values in the dataset was detected, discrepancies were found. As they were assessed to negatively influence further analysis, actions were taken to resolve them and is summarised in Table 1 below.

Table 1: List of observations found during inspection

| Variable Name                  | Possible values  | Observation   | Actions Taken   |
|--------------------------------|--|---|---|
| default.payment.next.<br>month | 1=yes, 0=no  | 209 instances where Pay_0 = 1, Pay_2, 3, 4, 5, 6 = -2, BILL_AMT1,2,3,4,5,6 = 0, but default = 1  108 instances where Pay_0, 2, 3, 4, 5, 6 = - 2, BILL_AMT1,2,3,4,5,6 = 0, but default = 1 | These instances describe clients with no debit in the preceding 6 months but defaults on the 7 <sup>th</sup> month. This is illogical and are removed from the dataset after being assessed as data errors. |
| Education                      | 1=graduate<br>school,<br>2=university,<br>3=high school,<br>4=others,<br>5=unknown,<br>6=unknown | 15 instances of '0', 280 instances of '5' and 51 instances of '6'   | There is no appreciable difference between '0', '5' and '6'. Hence, these entries are subsumed under "4 = others"   |
| Marriage                       | 1=married,<br>2=single,<br>3=others  | There are 54 instances of '0'   | There is no appreciable difference between '0' and '3'. Hence, these entries are subsumed under "3=others"  |





### 2.3 Multi-collinearity

Multi-collinearity of the variables was tested first as it adversely impacts logistic regression. This was done via visual inspection of the scatterplots for all continuous variables, modelled pairwise in JMP. There were several groups of variables which demonstrates multi-collinearity, one of which is shown in Figure 1 below, involving the amount billed to the client over various months. As such, PCA was assessed to be a suitable dimension reduction technique as it also removes multi-collinearity, which facilitates subsequent logistic regression modelling.

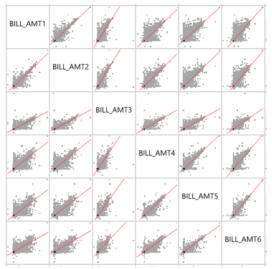


Figure 1: Selected Evidence of Multi-collinearity in the Dataset

# 3. Principal Component Analysis

# 3.1 Selection of Variables for Reduction

PCA is typically performed on continuous variables although ordinal variables with sufficient distinction (e.g. Likert Scale with sufficient intervals) may be considered. As such, the following variables were chosen:

| LIMIT_BAL | PAY_3 | BILL_AMT1 | BILL_AMT5 | PAY_AMT3 |
|-----------|-------|-----------|-----------|----------|
| AGE       | PAY_4 | BILL_AMT2 | BILL_AMT6 | PAY_AMT4 |
| PAY_0     | PAY_5 | BILL_AMT3 | PAY_AMT1  | PAY_AMT5 |
| PAY_2     | PAY_6 | BILL_AMT4 | PAY_AMT2  | PAY_AMT6 |

Table 2: List of Variables Chosen for PCA

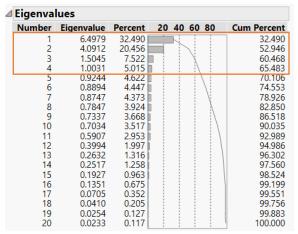
Due to insufficient resolution for the ordinal variable "EDUCATION", it was not considered in this PCA.





## **3.2** Selection of Principal Components

There were a few considerations when deciding the number of Principal Components to extract. The Eigenvalue Criterion, which suggests considering only components with values greater than 1, indicates that four components should be extracted. This is also supported by the Scree Test Criterion shown below, where the elbow is at the 4<sup>th</sup> component. Furthermore, the selected variables are able to explain about 65% of the variability which is consistent with heuristics on variance criterion where explained variability of 60% to 65% is considered acceptable. As such, the first four principal components were selected.



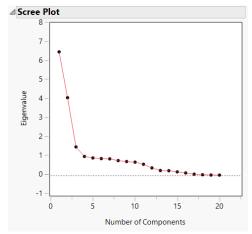


Figure 2: Eigenvalues and Cumulative Percentages

Figure 3: Scree Plot

# 3.3 Naming of Principal Components

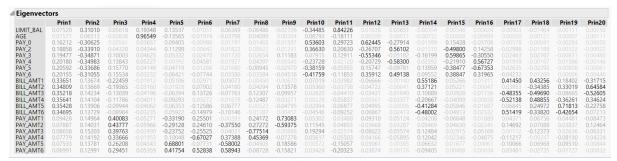


Figure 4: Eigenvector of each Principal Component

### 3.3.1 Prin1

Based on the Eigenvectors of the Principal Components shown in Figure 4, the linear combination of each principal component was derived. The first principal component was named as "Cumulative 6 months amount billed" because BILL\_AMT1 to BILL\_AMT6, which correspond to the billed amount for each of the last 6 months, has a higher loading as compared to other variables. The formula of Prin1 is given by:

```
\begin{split} Prin1 &= 0.07520 LIMIT_{BAL} + 0.01571 AGE + 0.16212 PAY_0 + 0.18858 PAY_2 + 0.19477 PAY_3 \\ &+ 0.2018 PAY_4 + 0.20592 PAY_5 + 0.20155 PAY_6 + 0.33651 BILL_{AMT1} \\ &+ 0.34809 BILL_{AMT2} + 0.35218 BILL_{AMT3} + 0.35641 BILL_{AMT4} \\ &+ 0.35428 BILL_{AMT5} + 0.34695 BILL_{AMT6} + 0.09426 PAY_{AMT1} + 0.07887 PAY_{AMT2} \\ &+ 0.08658 PAY_{AMT3} + 0.07779 PAY_{AMT4} + 0.07533 PAY_{AMT5} + 0.06991 PAY_{AMT6} \end{split}
```





#### 3.3.2 Prin2

For the second principal component, LIMIT\_BAL (credit limit), PAY\_0 and PAY\_2 to PAY\_6 (payment status) has a higher loading as compared to the other variables. Since these are factors which are taken into consideration during credit limit reviews, this principal component was named as "Credit worthiness score".

It should be noted that since PAY\_0 and PAY\_2 to PAY\_6 are ordinal in nature, and a positive value represents poor payment history, this means that negative values in these variables implies a better credit status of the customer.

The formula of Prin2 is given by:

```
\begin{split} Prin2 &= 0.31010 LIMIT_{BAL} + 0.06513 AGE - 0.30625 PAY_0 - 0.3391 PAY_2 - 0.34871 PAY_3 \\ &- 0.34983 PAY_4 - 0.33686 PAY_5 - 0.31055 PAY_6 + 0.13674 BILL_{AMT1} \\ &+ 0.13669 BILL_{AMT2} + 0.14234 BILL_{AMT3} + 0.14104 BILL_{AMT4} \\ &+ 0.13906 BILL_{AMT5} + 0.13729 BILL_{AMT6} + 0.14964 PAY_{AMT1} + 0.14031 PAY_{AMT2} \\ &+ 0.15203 PAY_{AMT3} + 0.14102 PAY_{AMT4} + 0.13781 PAY_{AMT5} + 0.12991 PAY_{AMT6} \end{split}
```

#### 3.3.3 Prin3

The third principal component was named as "Cumulative 6 months amount paid" because PAY\_AMT1 to PAY\_AMT6, which correspond to the payment amount over each of the last 6 months, has a higher loading as compared to other variables.

```
The formula of Prin3 is given by:
```

```
\begin{split} Prin3 &= 0.05618 LIMIT_{BAL} - 0.02836 AGE + 0.00561 PAY_0 + 0.04328 PAY_2 + 0.1003 PAY_3 \\ &+ 0.13843 PAY_4 + 0.15770 PAY_5 + 0.15534 PAY_6 - 0.22459 BILL_{AMT1} \\ &- 0.19365 BILL_{AMT2} - 0.13039 BILL_{AMT3} - 0.11786 BILL_{AMT4} \\ &- 0.09944 BILL_{AMT5} - 0.08984 BILL_{AMT6} + 0.40083 PAY_{AMT1} + 0.43777 PAY_{AMT2} \\ &+ 0.39763 PAY_{AMT3} + 0.33666 PAY_{AMT4} + 0.26208 PAY_{AMT5} + 0.29451 PAY_{AMT6} \end{split}
```

#### 3.3.4 Prin4

The fourth principal component was named as "Age" because it has a higher loading as compared to other variables.

The formula of Prin4 is given by:

```
\begin{split} Prin4 &= 0.19348 LIMIT_{BAL} + 0.96549 AGE + 0.03657 PAY_0 + 0.04344 PAY_2 + 0.04625 PAY_3 \\ &+ 0.05227 PAY_4 + 0.04149 PAY_5 + 0.03232 PAY_6 - 0.01912 BILL_{AMT1} \\ &- 0.03160 BILL_{AMT2} - 0.04196 BILL_{AMT3} - 0.04011 BILL_{AMT4} \\ &- 0.04062 BILL_{AMT5} - 0.03235 BILL_{AMT6} + 0.05271 PAY_{AMT1} + 0.05966 PAY_{AMT2} \\ &+ 0.02490 PAY_{AMT3} + 0.01953 PAY_{AMT4} + 0.04343 PAY_{AMT5} + 0.05359 PAY_{AMT6} \end{split}
```



# 4. Cluster Analysis

# 4.1 Clustering Method

Cluster analysis was performed on the 4 principal components from PCA to profile customers into different segments based on distinct attributes. Hierarchical clustering was ruled out as the algorithm was not optimised to handle large dataset with more than thousands of records. K-Means was chosen instead due to its efficiency to handle bigger datasets, which allows quick comparison and optimisation on the number of clusters.

#### 4.2 Number of Clusters

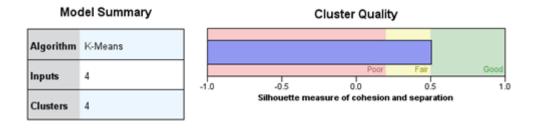


Figure 5: Cluster Quality for k=4 clusters

Upon running the stream in SPSS, it was found that 4 was the ideal number of clusters as it had the best silhouette measure of 0.5. A high silhouette measure tells us that the clusters are well spaced apart, with the elements within each cluster relatively close to each other with respect to the elements from other clusters. This can be summed up in the equation  $(\mathbf{D}_{ave} - \mathbf{d}_{ave}) / \text{Max}(\mathbf{D}_{ave}, \mathbf{d}_{ave})$ .

#### 4.3 Characteristics of Clusters

From Figure 6, Cluster 1 (53.6% of the sample) has a lower than average amount billed in the last 6 months (Prin1), lower than average credit worthiness score (Prin2), average amount paid in the last 6 months (Prin3) and a younger than average age group (Prin4). These characteristics matches typical young working adults who just entered the workforce. The lower credit scores are likely due to a lower disposable income and little personal assets. In addition, it is likely that they spend less on big ticket items with their credit cards at this stage of their lives, which translates to lower amounts billed and paid to the bank. This group of customers should be slowly grown as their net value will likely increase with time.





#### Clusters



| Cluster     | cluster-1        | cluster-4        | cluster-3    | cluster-2 |
|-------------|------------------|------------------|--------------|-----------|
| Label       |                  |                  |              |           |
| Description |                  |                  |              |           |
| Size        | 53.6%<br>(15901) | 34.0%<br>(10106) | 12.4% (3671) | 0.0%      |
| Inputs      | Prin1            | Prin1            | Prin1        | Prin1     |
|             | -0.80            | -0.53            | 4.92         | 20.01     |
|             | Prin2            | Prin2            | Prin2        | Prin2     |
|             | -0.26            | -0.11            | 1.40         | 22.29     |
|             | Prin3            | Prin3            | Prin3        | Prin3     |
|             | 0.03             | 0.09             | -0.42        | 38.37     |
|             | Prin4            | Prin4            | Prin4        | Prin4     |
|             | -0.65            | 1.11             | -0.22        | -4.00     |

Figure 6: Centroid of Clusters

Cluster 2 (with only 5 elements) appears to be an extreme outlier group consisting of <u>ultra-rich</u> <u>youngsters</u> with much higher than average credit worthiness scores and lower average age. They are also very financial active with high bill amount and payment amount and should be maintained to ensure they continue their business with the bank.

Cluster 3 (12.4% of the sample) are <u>high earners and spenders</u> who are relatively young, have above average credit worthiness scores with high bill amounts, and lowest repayment to the bank. This group of customers appears to have the highest risk of defaulting as the incurred expense and repayment does not commensurate each other. Care should be placed on this group of customers to ensure their net debit does not spiral out of control.

Cluster 4 (34% of the sample) can be generalised as <u>older working adults</u> when comparing their credit worthiness scores, age, average bill and paid amounts against Cluster 1. This is a group of stable clients where their incurred expenses and payment exceeds those of Cluster 1 but remains relatively consistent. This group of customers should be grown as they may have other assets which can be capitalised on.

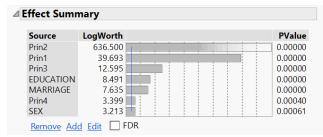




# 5. Logistic Regression

## 5.1 Model Building

The categorical variables not used in PCA such as EDUCATION, MARIAGE and SEX, along with the 4 principal components were used to develop the logistic regression model. The P Values (Figure 7) of the model suggest that all the variables used are significant (i.e. P<0.05). The Chi Square results (Figure 8) from the parameter estimates further provides resolution on the significance level for each variable.



ChiSquare Prob>ChiSq Term **Estimate** Std Error 1.45610173 0.0516108 795.98 Intercept -0.0961593 0.0070291 187 15 0.44594522 Prin2 0.0100053 1986.6 Prin3 0.16685973 0.0242289 Prin4 -0.061333 0.0172881 12.59 0.0004\* SEX[1] -0.0533027 0.0155347 11.77 0.0006 EDUCATION[2-1] EDUCATION[3-2] 0.0703309 0.04031018 0.035618 3.90 0.88 0.0428494 0.3468 EDUCATION[4-3] 0.91534329 23.84 MARRIAGE[1] -0.1321767 0.0468178 7.97 2.32 MARRIAGE[2] 0.07339257 0.0481782 0.1277

△ Parameter Estimates

Figure 7: Effect Summary

Figure 8 : Parameter Estimates

### 5.2 Goodness of Fit

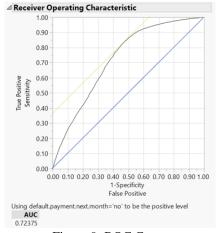


Figure 9: ROC Curve

From Figure 9, it was observed that the Receiver Operating Characteristic (ROC) curve has a positive predicted response as it is above the 45° diagonal line. The Area Under the Curve (AUC) is ~0.72 which suggest the model is a relatively good fit for the data set.





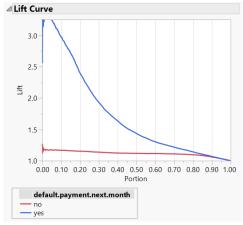


Figure 10: Lift Curve

In addition, the lift curve gives a lift of 3.0 for the first 10% of the data set. This means the model demonstrate 3 times more responses than if the data were selected at random. This will be useful to compare model accuracy modeled from the same dataset in future studies.

### 5.3 Model Accuracy

| Confusion Matrix |                            |              |      |
|------------------|----------------------------|--------------|------|
|                  | Training                   |              |      |
|                  | Actual                     | Predi<br>Cou |      |
|                  | default.payment.next.month | no           | yes  |
|                  | no                         | 22785        | 579  |
|                  | yes                        | 5097         | 1222 |

| Figure 11 : Confusion | Matrix |
|-----------------------|--------|
|-----------------------|--------|

| Accuracy                                 | 80.88% |
|--|--------|
| True Positive Rate/Sensitivity or Recall | 19.34% |
| False Positive Rate/ Type I error        | 2.48%  |
| True Negative rate / Specificity         | 97.52% |
| False Negative rate/ Type II error       | 80.66% |

Figure 12: Model attributes

From Figure 11 and 12, it is noted that while model accuracy and specificity is relatively high at 80.88% and 97.52% respectively, sensitivity is very low at 19.34%. This means that while the model is capable of predicting non-defaulter, it is unable to do the same for defaulters. The low sensitivity also corresponds to a high type II error, which means that the model is unable to differentiate defaulters from non-defaulters. Hence, more data (with more variables) would likely be needed to improve model sensitivity.

### **5.4** Model Equation

From the model building process, the equation of the logistic regression model developed is shown in Figure 13.





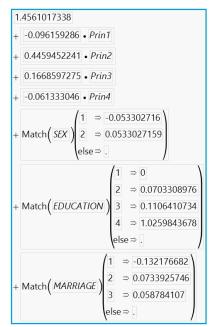


Figure 13: Equation of Logistic Regression Model

## 6. Conclusion

In meeting the Bank's requirement to accurately predict the default rate of existing clients, a logistic regression model was proposed. PCA was first performed to simplify modelling and remove multicollinearity in the dataset. Thereafter, K-means clustering was used, and 4 customer segments were identified for targeted marketing activities for the bank. With the logistic regression model, it was found that while it is capable of predicting non-defaulters, it is poor at detecting actual defaulters (or differentiate them from non-defaulters).

To improve the regression model, it is recommended that data with variables beyond this study be considered and incorporated into the modelling of an updated regression model. Furthermore, once a model with acceptable sensitivity is obtained, regression models can also be built for each customer segment identified from clusters analysis earlier for even better prediction capability.





# **Data Dictionary**

| Variable Name              | Explanation   |
|----------------------------|---|
| ID                         | ID of each Client   |
| LIMIT_BAL                  | Amount of given credit in NT dollars (includes individual and family/supplementary credit   |
| SEX                        | Gender (1=male, 2=female)   |
| EDUCATION                  | (1=graduate school, 2=university, 3=high school, 4=others, 5=unknown, 6=unknown)  |
| MARRIAGE                   | Marital status (1=married, 2=single, 3=divorced, 0=others)  |
| AGE                        | Age in years  |
| PAY_0                      | Repayment status as on September 2005 (-2= No Consumption, -1=pay duly, 0=uses revolving credit 1=payment delay for one month, 2=payment delay for two months, 8=payment delay for eight months, 9=payment delay for nine months and above) |
| PAY_2                      | Repayment status in August 2005 (scale same as above)   |
| PAY_3                      | Repayment status in July 2005 (scale same as above)   |
| PAY_4                      | Repayment status in June 2005 (scale same as above)   |
| PAY_5                      | Repayment status in May 2005 (scale same as above)  |
| PAY_6                      | Repayment status in April 2005 (scale same as above)  |
| BILL_AMT1                  | Amount of bill statement in September 2005 (NT dollar)  |
| BILL_AMT2                  | Amount of bill statement in August 2005 (NT dollar)   |
| BILL_AMT3                  | Amount of bill statement in July 2005 (NT dollar)   |
| BILL_AMT4                  | Amount of bill statement in June 2005 (NT dollar)   |
| BILL_AMT5                  | Amount of bill statement in May 2005 (NT dollar)  |
| BILL_AMT6                  | Amount of bill statement in April 2005 (NT dollar)  |
| PAY_AMT1                   | Amount of previous payment in September 2005 (NT dollar)  |
| PAY_AMT2                   | Amount of previous payment in August 2005 (NT dollar)   |
| PAY_AMT3                   | Amount of previous payment in July 2005 (NT dollar)   |
| PAY_AMT4                   | Amount of previous payment in June 2005 (NT dollar)   |
| PAY_AMT5                   | Amount of previous payment in May 2005 (NT dollar)  |
| PAY_AMT6                   | Amount of previous payment in April 2005 (NT dollar)  |
| default.payment.next.month | Default payment (1=yes, 0=no)   |



