

UNIT - I

27/6/18

Compressive Strength of Concrete :

It is defined as characteristic Compressive strength of 150mm Cubes of the age of 28 days $\rightarrow M_{20}$ grade

M \rightarrow Mix proportion

20 \rightarrow characteristic Compressive strength of Concrete in MPa

1. Ordinary Concrete - M₁₀ to M₂₀

2. Standard Concrete - M₂₅ to M₅₅

3. High strength Concrete - M₆₀ to M₈₀

Mix proportions:

M₅ - 1 : 5 : 10

M_{7.5} - 1 : 4 : 8

M₁₀ - 1 : 3 : 6

M₁₅ - 1 : 2 : 4

M₂₀ - 1 : 1½ : 3

Steel reinforcement: Steel bars are essentially used in tension zone of flexural members to resist the tensile stresses.

Why steel is used as reinforcement?

- Its tensile strength is very high.
- It can develop good bond with Concrete.
- The thermal Coefficient value is more.
- It is easily available.

Reinforcement Serves the following functions:

1. To resist the bending tension.
2. To increase the load carrying capacity.
3. To resist the diagonal tension due to shear.
4. To reduce the shrinkage of Concrete.
5. To resist wide cracks & spiral cracks.

Types of reinforcement:

1. Mild steel & medium tensile steel.
2. High yield strength deformed steel bars [HYS]
3. Steel wire fabric.
4. Structural steel.

Mild steel bars: These are plain bars of grade Fe 250 whereas,

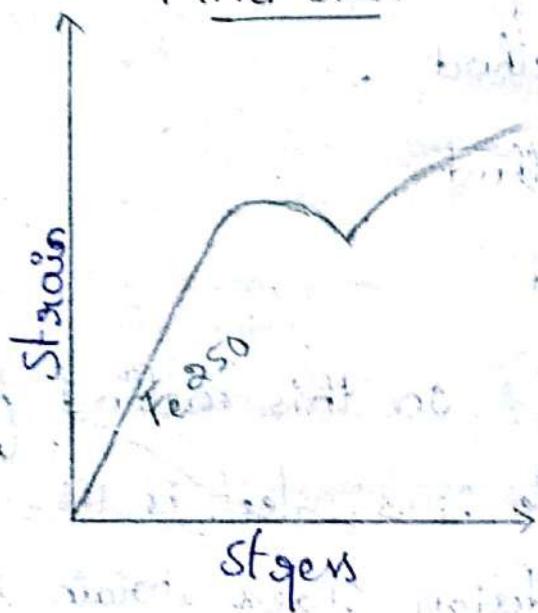
Fe \rightarrow Ferrite

250 \rightarrow yield strength (81) yield stress.

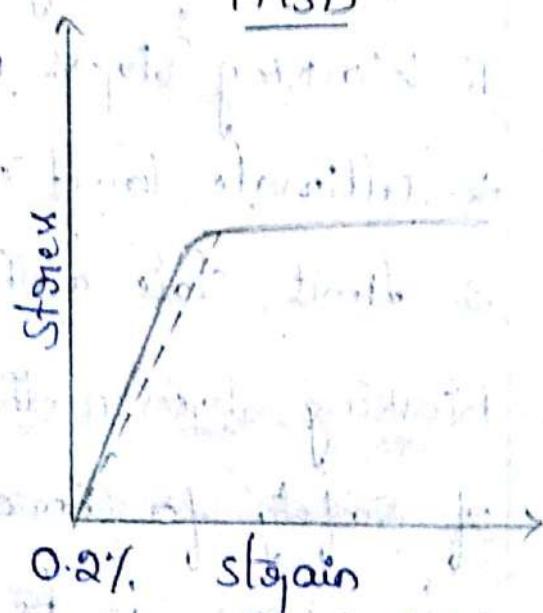
HYSO bars:

They are having high yield strength of grade Fe 415 & Fe 500.

Mild steel



HYSO



\rightarrow Yield stress is given by 0.2% of proof stress

\rightarrow The young's modulus of all types of steel

are $2 \times 10^5 \text{ N/mm}^2$.

\rightarrow Unit wt. of steel is 78.5 kN/m^3

Types of loads:

1. Dead load - Self wt (Constant)
2. Live load - moving (Assume).
3. Wind load
4. Earthquake load
5. Snow load

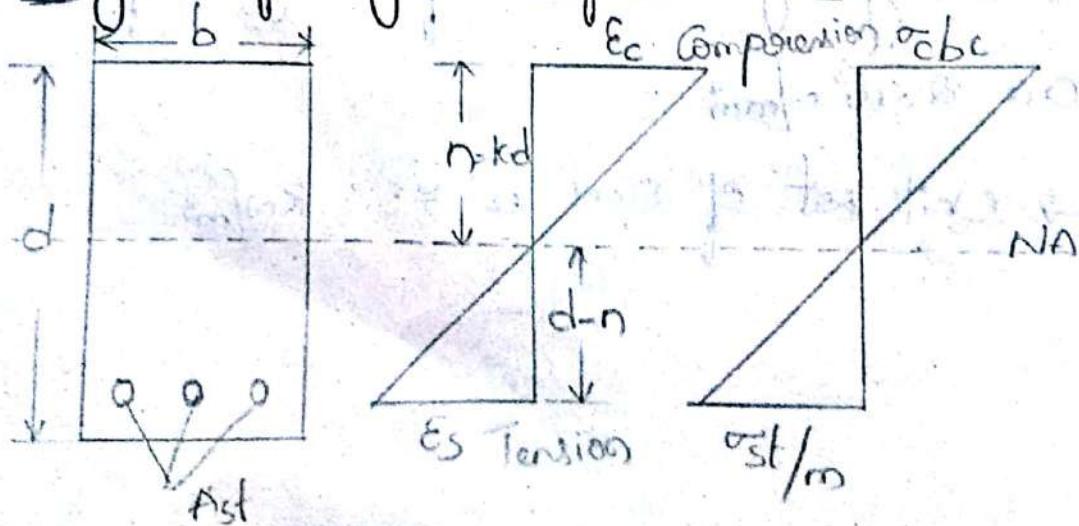
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Methods of design of reinforced Concrete:

1. Working stress method.
2. ultimate load method
3. limit state method

Working stress method: In this method factor of safety for Concrete is 3, steel is 1.5. In this only beams can be design. stress strain is linear.

Analysis of Single reinforced Sections:



If the reinforcement bars are provided only on tension side in the beam sections, it is called as single reinforced beam Sections.

- When the stresses developed in the Concrete Section are known,

Let,

σ_{bc} = Compressive stress in Concrete due to bending.

σ_s = Tensile stress in steel

A_s = Area of tension steel

ϵ_c = Maximum strain in Concrete.

ϵ_s = Maximum strain at the Centroid of steel.

d = Effective depth.

b = width of the member.

n = Depth of neutral axis = $k \cdot d$

k = Neutral axis depth factor.

m = Modulus ratio = $280 / 3\sigma_{bc}$

Since the strain in Concrete & steel are proportional to their distances from neutral axis,

$$\frac{\epsilon_e}{\epsilon_s} = \frac{n}{d-n}$$

$$\frac{d-n}{n} = \frac{\epsilon_s}{\epsilon_c}$$

$$\left(\frac{d}{n}\right) - 1 = \frac{\sigma_{st}}{E_s} \times \frac{E_c}{\sigma_{cbc}}$$

$$= \frac{\sigma_{st}}{\sigma_{cbc}} \cdot \frac{1}{m} \quad \left[\because \epsilon_s = \frac{\sigma_{st}}{E_s}; \quad E_c = \frac{\sigma_{cbc}}{E_c} \right]$$

$$\Rightarrow \left(\frac{d}{n}\right) - 1 = \frac{\sigma_{st}}{m \cdot \sigma_{cbc}} \quad \left[\therefore m = \frac{E_s}{E_c} \right] \quad \text{modular ratio}$$

$$\Rightarrow \frac{d}{n} = 1 + \frac{\sigma_{st}}{m \cdot \sigma_{cbc}} \quad \boxed{m = \frac{280}{30 \sigma_{cbc}}}$$

$$n = \left(\frac{1}{1 + \frac{\sigma_{st}}{m \cdot \sigma_{cbc}}} \right) d$$

$n = k.d$

$$\text{where } K = \frac{1}{1 + \frac{\sigma_{st}}{m \cdot \sigma_{cbc}}}$$

2. When the dimensions of the beam & the reinforcements are given:

The depth of neutral axis can be obtained by considering the equilibrium of internal forces of compression & tension

$$\text{Force of Compression} = \text{Force of Tension}$$

$$\begin{aligned}\text{Force of Compression } C &= \text{Average stress} \times \text{Area of beam in Compression} \\ &= \frac{\sigma_{cbc}}{2} \times b \times n\end{aligned}$$

$$\begin{aligned}\text{Force of tension } T &= \text{permissible stress} \times \text{Area of steel} \\ &= \sigma_{st} \times A_{st}\end{aligned}$$

$$= m \cdot \sigma_{cbc} \cdot \left(\frac{d-n}{n}\right) \times A_{st}$$

$$\Rightarrow \frac{\sigma_{cbc}}{2} \times b \times n = m \cdot \sigma_{cbc} \cdot \left(\frac{d-n}{n}\right) \cdot A_{st}$$

$$\Rightarrow \boxed{\frac{bn^2}{2} = m \cdot A_{st} (d-n)}$$

$$\cancel{\Rightarrow \frac{bn^2}{2} = m \cdot A_{st} (d-n)}$$

$$\Rightarrow \frac{bn^2}{2} + m \cdot A_{st}n - m \cdot A_{st}d = 0$$

By solving the above quadratic equation,

$$n = \frac{-m \cdot Ast + \sqrt{(m \cdot Ast)^2 - 2 \cdot b \cdot mAstd}}{b}$$

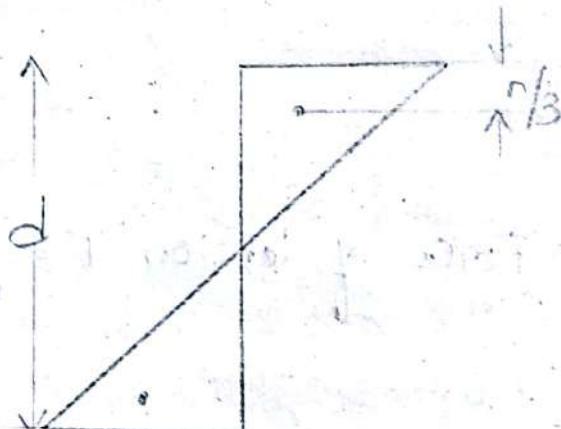
Lever arm:

The force of compression & tension form a couple. The distance between the lines of action of compression & tension forces is called as lever arm.

$$z = d - \frac{D}{3}$$

$$= d - \frac{k \cdot d}{3} \cdot d$$

$$z = d \left(1 - \frac{k}{3}\right)$$



$$z = j \cdot d$$

$$\therefore \text{Lever arm factor } j = 1 - \frac{k}{3}$$

Moment of resistance:

Moment of resistance = Total Compressive or
tension \times lever arm

$$\text{Total compressive force } C = \frac{1}{2} \times \sigma_{bc} \times b \times n$$

Total tensile force $T = \sigma_{st} \cdot A_{st}$

Moment of resistance (MR) = C · Q

$$= \frac{1}{2} \cdot \sigma_{cbc} \times b \times n \times (j.d)$$

$$= \frac{\sigma_{cbc}}{2} \times b \times k_d \times j.d$$

$$= \frac{1}{2} k_j \cdot \sigma_{cbc} \cdot b d^2$$

$$\boxed{MR = Q \cdot b d^2}$$

Q = moment of resistance Constant

m, k, j, Q are also design constants.

Types of section:

1. Balanced section.
2. under reinforced section.
3. over reinforced section

Balanced section:

A reinforced concrete section in which steel & concrete reach their maximum allowable stresses simultaneously is called balanced or critical section. Neutral axis corresponding to balanced section is called as critical neutral axis.

The percentage steel corresponding to balanced section is called critical percentage of steel.

Under reinforced Section:

A section in which the area of steel reinforcement provided is less than that is required for a balanced section is called as under reinforced section.

$$\text{Moment of resistance} = \sigma_{sf} \cdot A_{sf} \left(d - \frac{\rho_a}{3} \right)$$

Over reinforced Section:

A section in which the area of steel reinforcement provided is more than that is required for a balanced section is called as over reinforced section.

$$MR = \frac{1}{2} \sigma_{cbc} \times b \times n_a \left(d - \frac{\rho_a}{3} \right)$$

- A reinforced concrete beam 250mm wide, 475mm overall depth is reinforced with 3 bars of 16mm at an effective cover of 50mm using M₂₀ grade Concrete & Fe 415 steel. Find the depth of NA.

of Given data,

$$b = 880 \text{ mm}$$

$$d = 475 - 50$$

$$= 425 \text{ mm}$$

$$A_{st} = 3 \times \frac{\pi}{4} (16)^2$$

$$A_{st} = 603.19 \text{ mm}^2$$

$$\sigma_{cbc} = 7 \text{ N/mm}^2 \quad [\because \text{From table no: 21 for M}_20 \text{ grade}]$$

$$\sigma_{st} = 230 \text{ N/mm}^2$$

[\because From table no: 22]

$\frac{bn^2}{2}$ Depth of ^{actual} neutral axis (n_a):-

$$\frac{bn^2}{2} = m \cdot A_{st} (d - n)$$

$$\frac{250 \times n^2}{2} = 13.33 \times 603.19 (425 - n)$$

$$n^2 = 64.32 (425 - n)$$

$$n^2 - 8733.78 + 64.32n = 0$$

$$\therefore \boxed{n_a = 136.88 \text{ mm}}$$

- Q. A reinforced concrete beam of 300mm wide by 550mm overall depth is reinforced with 4 bars of 20mm ϕ at an effective depth of 50mm

using M₂₀ grade Concrete & Fe 415 steel. Estimate
the moment of resistance of the section.

EoF

Given data,

$$b = 300\text{mm}$$

$$D = 550\text{mm}$$

$$\text{Effective depth } d = 550 - 50 \\ = 500\text{mm}$$

$$\text{Area of tension steel } A_{st} = 4 \times \frac{\pi}{4} (20)^2 \\ = 1256.6\text{mm}^2$$

$$\sigma_{st} = 230 \text{ N/mm}^2$$

$$\sigma_{cbc} = 7 \text{ N/mm}^2$$

Design Constant for M₂₀ & Fe 415

$$m = \frac{280}{3\sigma_{cbc}} = 13.33$$

Critical depth of neutral axis,

$$n_c = k \cdot d$$

$$k = \frac{1}{1 + \frac{\sigma_{st}}{m \times \sigma_{cbc}}}$$

$$= \frac{1}{1 + \frac{230}{13.33 \times 7}}$$

$$k = 0.859$$

$$\therefore n_c = k \cdot d$$

$$= 0.859 \times 500$$

$$\therefore \boxed{n_c = 444.5 \text{ mm}}$$

Depth of actual neutral axis (n_a):

$$\frac{b n^2}{2} = m \cdot A_{st} (d - n_a)$$

$$\frac{300n^2}{2} = 13.33 \times 1256.6 (500 - n_a)$$

$$\boxed{n_a = 187 \text{ mm}}$$

$n_a < n_c \rightarrow$ under-reinforced

$n_a > n_c \rightarrow$ Over-reinforced

$$\boxed{n_a > n_c}$$

\therefore The section is over-reinforced.

$$\text{Moment of resistance (MR)}: \frac{1}{2} \sigma_{bc} b c \times b \times n_a \left(d - \frac{n_a}{3} \right)$$

$$\Rightarrow \frac{1}{2} \times 2 \times 300 \times 187 \left(500 - \frac{187}{3} \right)$$

$$\boxed{MR = 85.9 \text{ kN-m}}$$

3. A Reinforced Concrete beam 300mm x 600mm, over all depth is reinforced with 4 bars of 20mm at an effective cover of 50mm. What uniformly distributed load of this beam can carry excluding self wt, over a S.S span of 5m. Assume M₂₅ grade & Fe 415 steel.

Ans

Given data,

$$b = 300\text{mm}$$

$$D = 600\text{mm}$$

$$\text{Effective Cover } d = 600 - 50 \\ = 550\text{mm}$$

$$\text{Area of tension steel } A_{st} = 4 \times \frac{\pi}{4} (20)^2 \\ = 1256.6 \text{mm}^2$$

$$\sigma_{st} = 230 \text{N/mm}^2 \quad (\because \text{From table 22})$$

$$\sigma_{cbc} = 8.5 \text{N/mm}^2 \quad (\because \text{from Pg: no 81} \\ \text{Table 21})$$

Design Constant of M₂₅ grade & Fe 415

$$m = \frac{280}{3\sigma_{cbc}} = \frac{280}{3 \times 8.5} = 0.98$$

Critical depth of neutral axis;

$$n_c = k \cdot d$$

$$k = \frac{1}{1 + \frac{\sigma_{st}}{m \sigma_{cbc}}} = \frac{1}{1 + \frac{230}{0.98 \times 8.5}}$$

$$k = 0.28$$

$$n_c = 0.28 \times 550$$

$$\boxed{n_c = 158.76 \text{ mm}}$$

Depth of actual neutral axis (n_a):

$$\frac{bn^2}{a} = m \cdot A_{sf} (d - n_a)$$

$$\frac{300n^2}{2} = 10.98 \times 1256.6 (550 - n_a)$$

$$\boxed{n_a = 183.59 \text{ mm}}$$

$$n_a > n_c$$

∴ The section is over reinforced section.

$$MR = \frac{1}{2} \times \sigma_{cbc} \times b \times n_a \left(d - \frac{n_a}{3} \right)$$

$$> \frac{1}{2} \times 8.5 \times 300 \times 183.59 \left(550 - \frac{183.59}{3} \right)$$

$$\boxed{MR = 114.42 \text{ kN-m}}$$

Maximum load:

Let w (kn/m) be the uniformly distributed load beam can carry.

$$\text{Max BM} = \frac{\omega l^2}{8} \Rightarrow \frac{\omega \times 5^2}{8} = 3.125\omega$$

$$MR = \text{max. BM}$$

$$114.42 = 3.125 w$$

$$w = 36.51 \text{ [including self wt]}$$

$$\text{Self wt. of the beam} = 0.3 \times 0.6 \times 1 \times 25 \\ = 4.5 \text{ kN/m}$$

Uniformly distributed load excluding self wt.

$$= 36.51 - 4.5$$

$$= 32.01 \text{ kN/m}$$

Q. Design a RCC beam 230mm wide to resist a BM of 30 kN-m. Use M₂₀ & Fe 415.

Ans

Given data,

$$b = 230 \text{ mm}$$

$$\text{BM} = 30 \text{ kN-m}$$

$$\sigma_{st} = 230 \text{ N/mm}^2$$

$$\sigma_{cbc} = 7 \text{ N/mm}^2$$

Design Constants for M₂₀ grade & Fe 415 steel

$$m = \frac{280}{3\sigma_{cbc}} = \frac{280}{3 \times 7} = 13.33$$

$$k = \frac{1}{1 + \frac{\sigma_{st}}{m \cdot \sigma_{cbc}}} = \frac{1}{1 + \frac{230}{13.33 \times 7}} = 0.289$$

$$k = 0.289$$

$$j = 1 - \frac{k}{3}$$

$$= 0.904$$

$$\begin{aligned} Q &= \frac{1}{\alpha} \sigma_{bc} \times k \times j \\ &= \frac{1}{\alpha} \times 7 \times 0.289 \times 0.904 \\ &= 0.914 \end{aligned}$$

Depth required,

$$MR = Qbd^2$$

$$d = \sqrt{\frac{BM}{Q \times b}}, \quad [\because MR = \text{max. BM}]$$

$$= \sqrt{\frac{80 \times 10^6}{0.914 \times 230}}$$

$$d = 377.8 \text{ mm} \approx 380 \text{ mm}$$

Area of tensile steel A_{st} :

$$MR = A_{st} \cdot \sigma_{st} \times j \cdot d$$

$$30 \times 10^6 = A_{st} \times 230 \times 0.904 \times 380$$

$$30 \times 10^6 = 79009.6 A_{st}$$

$$A_{st} = 379.7 \text{ mm}^2$$

$$d = 379.8 \approx 380\text{mm}$$

$$D = 380 + 40$$

$$= 420\text{mm} \quad [\because \text{Assume } 40\text{mm}]$$

Let,

Assume 12mm ϕ bars to find out the no. of bars.

$$A_{st} = \text{No. of bars} \times \frac{\pi}{4} (12)^2$$

$$379.9 = 113.09 \times \text{No. of bars}$$

$$\text{No. of bars} = \frac{379.9}{113.09}$$

$$= 3.35 \approx 4 \text{ bars}$$

$$\therefore \text{No. of bars} = \underline{\underline{4}}$$

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5. Double reinforced beam is to be design having an overall c/s dimensions of 850mm x 400mm with an effective span of 4m. The beam has to support and uniformly distributed dead load of 2.5 kN/m together with a live load of 80kN/m in addition to its self wt adopting M₂₀ grade Concrete & Fe 455. Design suitable reinforcement in the beam

Effective span $L = 4\text{m}$

Breadth of beam $b = 250\text{mm}$

Overall depth $D = 400\text{mm}$

dead load = 2.5 kN/m

Live load = 20 kN/m

M₂₀ grade Concrete & Fe 415 HYSI bars,

$$\sigma_{cbc} = 7 \text{ N/mm}^2$$

$$Q = 0.91$$

$$j = 0.90$$

$$\sigma_t = 230 \text{ N/mm}^2$$

$$m = \frac{250}{3\sigma_{cbc}} = \frac{250}{3 \times 7} = 13.33$$

$$Q = \frac{1}{3} \times \sigma_{cbc} \times b \times j$$

~~$\sigma_t \times 230$~~

$$K = \frac{1}{1 + \frac{\sigma_t}{m \cdot \sigma_{cbc}}} = \frac{1}{1 + \frac{230}{13.33 \times 7}}$$

$$\boxed{K = 0.289}$$

$$j = 1 - \frac{K}{3}$$

$$= 1 - \frac{0.289}{3}$$

$$j = 0.904$$

$$Q = \frac{1}{2} \times 3 \times 0.269 \times 0.904 \\ = 0.914$$

Depth required

~~MR = Qd²~~

Load:

$$\text{Self wt. of beam} = 0.25 \times 0.4 \times 25$$

$$W = 25 \text{ kN/m}$$

$$\text{Dead Load} = 2.5$$

$$\text{Live Load} = 20.00$$

$$\text{Total load } W = 25 \text{ kN/m}$$

Adopt an effective cover of 50mm

$$\text{Effective depth} = 400 - 50$$

$$d = 350 \text{ mm}$$

Bending moments & shear force

$$M = \frac{wl^2}{8} = \frac{25 \times 4^2}{8} = 50 \text{ kN-m}$$

Depth required.

$$MR = Qbd^2$$

$$= 0.914 \times 0.25 \times (3.5 \times 10^9)$$

$$MR = 27.8 \text{ kN-m} \rightarrow M_1$$

M_1 greater than M . so, it is design by doubly reinforced section.

$$\text{Balance moment } M_2 = M - M_1$$

$$= 50 - 27.8$$

$$= 22.2 \text{ kN-m}$$

Tension steel required for balanced singly reinforced section,

$$A_{st1} = \frac{M_1}{\sigma_{st} \cdot j \cdot d} \Rightarrow \frac{27.8 \times 10^6}{230 \times 0.904 \times 350} \\ = 382 \text{ mm}^2$$

Additional tension steel for balanced moment,

$$A_{st2} = \frac{M_2}{\sigma_{st}(d - d_c)} \\ = \frac{22.2 \times 10^6}{230 \times (350 - 50)} \\ = 321.7 \approx 322 \text{ mm}^2$$

Total tensile steel bars,

$$A_{st} = A_{st1} + A_{st2}$$

$$A_{st} = 328 + 381$$

$$\Rightarrow 703 \text{ mm}^2$$

Provide 4 bars of 16mm diameter

Companion reinforcement.

$$A_{sc} = \frac{m \cdot A_{st} \cdot (d - n_c)}{(1.5m - 1)(n_c - d_c)}$$



$$n_c = 0.289 d$$

$$= 0.289 \times 350$$

$$\approx 99.05 \quad 101.15 \quad 1.22 \times 10^6 \quad 1.223 \times 10^6$$

$$A_{sc} = \frac{13.33 \times 328 \left(350 - \frac{101.15}{1.223 \times 10^6} \right)}{(1.5 \times 13.33 - 1) \left(\frac{101.15}{1.223 \times 10^6} - 50 \right) \times 10^6}$$

$$\approx 1096.8 \text{ mm}^2$$

Assume 16mm φ bars to find out the no of bars

$$A_{sc} = \text{No. of bars} \times \frac{\pi}{4} (16)^2$$

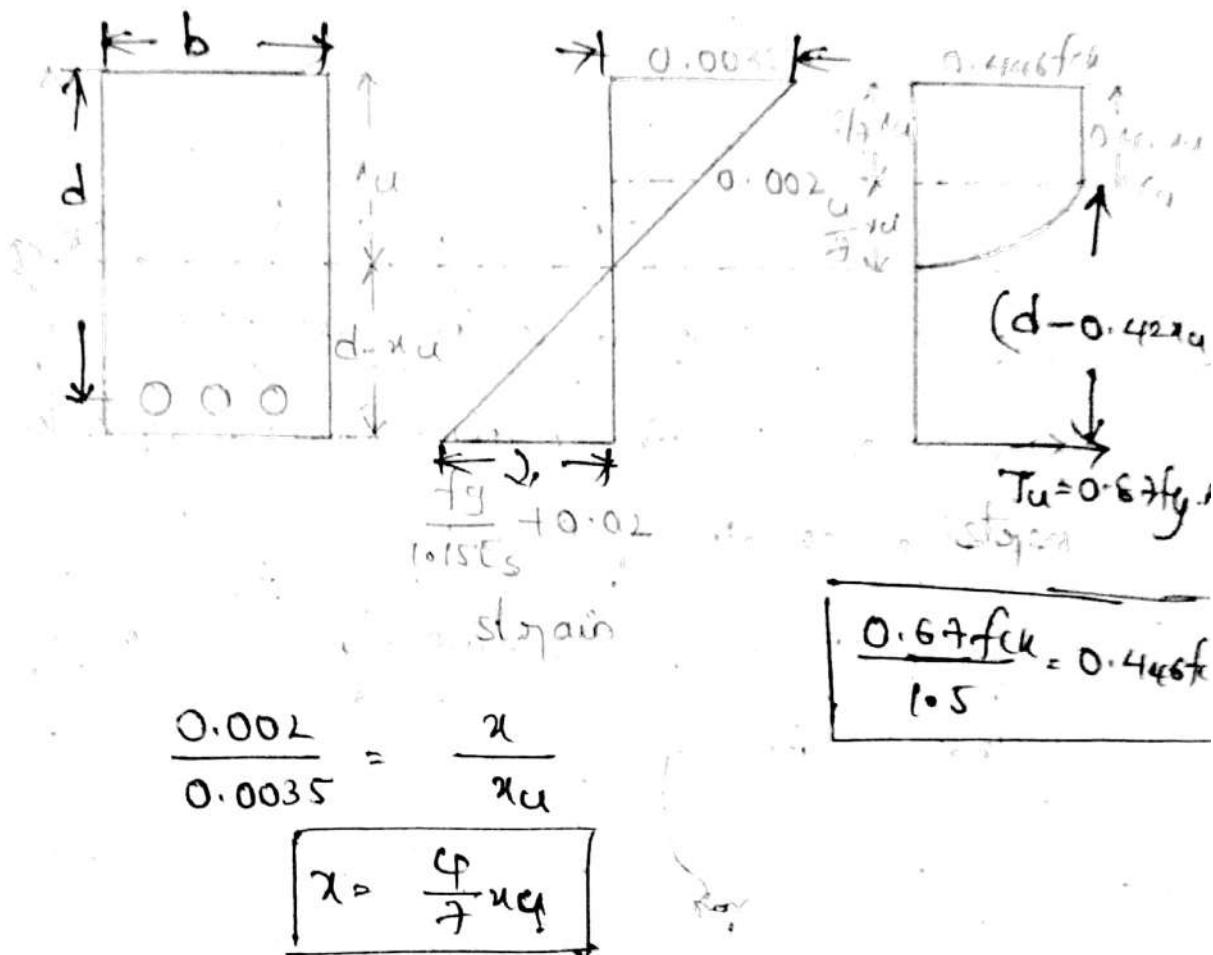
$$1096.8 = \text{No. of bars} \times 201.06$$

$$\text{No. of bars} = 5.46 \approx 6 \text{ bars}$$

8, 12, 20, 16, 18, 22, 24, 25, 32, 36 - φ

UNIT-II

Limit state Method



$$\frac{0.002}{0.0035} = \frac{x}{x_u}$$

$$x = \frac{4}{7} x_u$$

Area of Concrete = parabolic + rectangle

$$= \frac{2}{3} b h + \frac{3}{7} x_u \times 0.446 f_{ck}$$

$$= \left(\frac{2}{3} \times \frac{4}{7} x_u \times 0.446 f_{ck} \right)$$

$$+ \frac{3}{7} x_u \times 0.446 f_{ck}^{0.1911}$$

$$= 0.36 f_{ck} \cdot x_u$$

Distance of Centroid of stem block from the top fibre:

$$x_c = \left(\frac{3}{7} x_u \times 0.446 f_{ck} \right) \left(\frac{1}{2} \times \frac{3}{7} x_u \right) +$$

$$+ \left(\frac{2}{3} \times \frac{4}{7} x_u \times 0.466 f_{ck} \right) \left(\frac{3}{8} \times \frac{4}{7} x_u + \frac{3}{7} x_u \right)$$

$$\boxed{x_c = 0.42 x_u}$$

Stress Block parameters:

Stress-strain Curve at the crushing of concrete is assumed to be parabolic shape upto 0.002 strain & then constant upto the maximum strain of 0.0035.

The strain varies linearly across the depth of the section.

Depth of Neutral axis (x_u):

Force of Compression = Force of Tension

$$0.36 f_{ck} b \cdot x_u = 0.87 f_y \cdot A_{st}$$

$$\boxed{x_u = \frac{0.87 f_y \cdot A_{st}}{0.36 f_{ck} \cdot b}}$$

Moment of resistance of section

Moment = Force x distance

Stress = $\frac{\text{Force}}{\text{Area}}$

Moment = Stress x Area x distance

- (i) For balanced reinforced section,
- $x_u = x_{\max}$
- In this Concrete & steel both are failed

So, Dead loading of 159 mmt.

$$M_R = 0.36 f_{ck} g_b \times x_u (d - 0.42 x_u)$$

→ for Concrete.

for steel,

$$M_R = 0.87 f_y A_{st} (d - 0.42 x_u)$$

- (ii) For under-reinforced section

$x_u < x_{\max}$

$$M_R = 0.87 f_y A_{st} (d - 0.42 x_u)$$

Steel fails in this section

(iii) for Over reinforced Section ($x_u > x_{umax}$)

In this section Concrete fails.

So, the moment of resistance is,

$$MR = 0.36 f_{ck} \cdot x_u \cdot \max \times b (d - 0.42 x_{umax})$$

x_u = Actual depth of Neutral axis,

x_{umax} = Max. depth of Neutral axis.

⇒ From pg: 70 in Code book:

f_g	x_{umax}/d
250	0.53
415	0.48
500	0.46

for Fe 250 steel, $x_{umax} = 0.53d$

for Fe 415 steel, $x_{umax} = 0.48d$

for Fe 500 steel, $x_{umax} = 0.46d$.

Limiting value of $M_{u,lim}$ (Mu,limit)

Since the maximum depth of NA is limited to avoid brittle failure, the maximum value of moment of resistance is also limited.

$M_{u,lim}$

$$M_{u,R} = 0.36 f_{ck} \times b \times x_u (d - 0.42 x_u)$$

for Fe 250 steel

$$x_{u,max} = 0.53d \quad [\text{from Code book}]$$

$M_{u,lim}$

$$M_{u,R} = 0.36 f_{ck} \times b (0.53d) (d - (0.42 \times 0.53d))$$

$M_{u,lim}$

$$M_{u,R} = 0.148 f_{ck} b d^2$$

for Fe 415 steel, $x_{u,max} = 0.48d$ [from Code book].

$M_{u,lim}$

$$M_{u,R} = 0.36 f_{ck} \times b \times x_u (d - 0.42 x_u)$$

$$= 0.36 f_{ck} \times b \times 0.48d (d - 0.42(0.48d))$$

$$M_{u,lim} = 0.138 f_{ck} b d^2$$

for Fe 500 steel, $x_{u,max} = 0.46d$

$$M_{u,lim} = 0.36 f_{ck} \times b \times 0.46d (d - 0.42(0.46d))$$

$$= 0.133 f_{ck} b d^2$$

10. Find the moment carrying a singly reinforced beam of $230\text{mm} \times 480\text{mm}$ effective depth reinforced with 3 bars of 20mm diameter. Concrete is of M₂₀ grade & Fe 415 steel.

Lof

Given data,

$$b = 230\text{mm}$$

$$d = 480\text{mm}$$

$$f_{ck} = 20\text{N/mm}^2$$

$$f_y = 415\text{N/mm}^2$$

$$A_{st} = \frac{\pi}{4}(20)^2 \times 3$$

$$A_{st} = 942.47\text{mm}^2$$

Depth of Neutral axis:

$$0.87 f_y \cdot A_{st}$$

$$0.87 f_{ck} \cdot b$$

$$= \frac{0.87 \times 415 \times 942.47}{0.36 \times 20 \times 230}$$

$$x_u = 205.48\text{mm}$$

$$x_{u\max} = 0.48d \quad [\text{for Fe 415 steel}]$$

$$= 0.48(480)$$

$$\therefore x_u \max = 230.4 \text{ mm}$$

$$\therefore x_u < x_u \max$$

So, the section is under ~~under~~ reinforced.

Moment of resistance:

$$M_R = 0.87 f_y A_{st} (d - 0.42 x_u)$$

$$= 0.87 \times 415 \times 942.47 (480 - 0.42(205.4))$$

$$M_R \approx 183.96 \times 10^6 \text{ N-mm}^2$$

$$M_R = 183.96 \times 10^6 \text{ N-mm} \times 10^3 \text{ kN}$$

$$= 183.96 \text{ kNm} \times 10^3$$

2. Find the ultimate moment of resistance of singly reinforced beam 280mm x 400mm effective depth reinforced with 5 bars of 20mm dia. Concrete is of M20 grade & steel Fe 250.

Sol

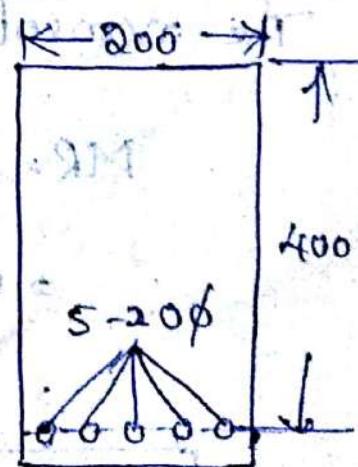
Given data;

$$(1) \text{ Width } b = 200 \text{ mm}$$

$$(2) d = 400 \text{ mm} \times 0.8 \times 28.0$$

$$f_{ck} = 20 \text{ N/mm}^2 \text{ (P. 1)}$$

$$f_y = 415 \text{ N/mm}^2$$



$$A_{st} = 5 \times \frac{\pi}{4} (20)^4$$

$$A_{st} = 1570.79 \text{ mm}^2$$

Depth of Neutral axis:

$$x_u = \frac{0.87 f_y \cdot A_{st}}{0.36 f_{ck} k_b}$$

$$x_u = \frac{(0.87) \times 250 \times 1570.79}{0.36 \times 20 \times 200}$$

$$x_u = 237.25 \text{ mm}$$

$$x_{u,\max} = 0.53 d \left[f_a / f_e \right] \text{ [Steel]}$$

$$= 0.53 \times 400 \text{ mm}$$

$$x_{u,\max} = 212 \text{ mm}$$

$$x_u > x_{u,\max}$$

So, the section is over reinforced.

The moment of resistance is:

$$M_R = 0.36 f_{ck} x_{u,\max} b (d - 0.42 x_{u,\max})$$

$$= 0.36 \times 20 \times 212 \times 200 (400 - (0.42 \times 212))$$

$$= 94.92 \times 10^6 \text{ N-mm}$$

$$M_R = 94.92 \text{ kN-m}$$

Max. permissible Ast (Concrete beam)

To determine the Ast dimensions of the beam

& MR is given

$$M_u = 0.87 f_y \cdot A_{st} (d - 0.92 x_0)$$

$$= 0.87 f_y \cdot A_{st} (d - 0.42 \left(\frac{0.87 f_y \cdot A_{st}}{0.36 f_{ck} b} \right))$$

$$\therefore M_u = 0.87 f_y \cdot A_{st} \cdot d \left[1 - \frac{f_y \cdot A_{st}}{f_{ck} \cdot b \cdot d} \right]$$

3. A reinforced concrete beam has a section of 200 x 500 mm overall. It is subjected to a factored moment of 80 kN-m. Design the reinforcement using Fe 250 steel & M20 grade concrete. The effective cover over concrete is 50 mm

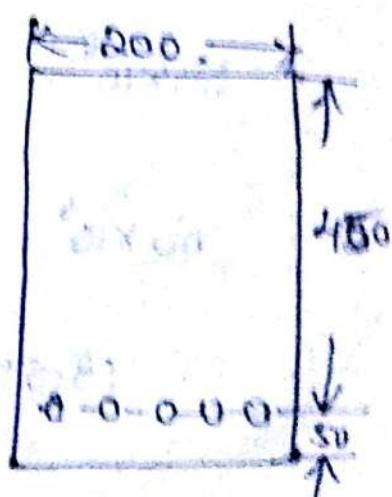
Ex:

Given data,

$$b = 200 \text{ mm} \quad \text{factored } M_u = 80 \text{ kNm}$$

$$d = 500 - 50 \\ = 450 \text{ mm}$$

$$M_u = 80 \text{ kNm}$$



$M_u < M_{ulimit} \rightarrow$ Single reinforced beam

$M_u > M_{u, \text{limit}}$ [Doubly Reinforced beam]

$$f_y = 250 \text{ N/mm}^2$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$M_{u, \text{limit}} = 0.148 f_{ck} b d^2$$

$$= 0.148 \times 20 \times 800 \times 450^2$$

$$= 119.88 \times 10^6 \text{ N-mm}$$

$$= 119.88 \text{ kN-m}$$

$\therefore M_u < M_{u, \text{limit}}$ (Single Reinforced)

$$M_u = 0.87 f_y A_{st} d \left[1 - \frac{f_y A_{st}}{f_{ck} b d} \right]$$

$$80 \times 10^6 = 0.87 \times 250 \times A_{st} \times 450 \left[1 - \frac{250 \times A_{st}}{80 \times 800 \times 450} \right]$$

$$80 \times 10^6 = 97875 A_{st} \left[1 - 1.388 \times 10^{-4} A_{st} \right]$$

$$80 \times 10^6 = 97875 A_{st} - 13.593 A_{st}^2$$

$$13.593 A_{st}^2 - 97875 A_{st} + 80 \times 10^6 = 0$$

$$\boxed{A_{st} = 940.2 \text{ mm}^2}$$

Provide 20mm φ for finding no. of bars

$$A_{st} \rightarrow \text{No. of bars} \times \frac{\pi}{4} (d_0)^2$$

$$940.2 = \text{No. of bars} \times 314.15$$

$$314.15 \times \text{No. of bars} = 940.2$$

$$\text{No. of bars} = 2.99 \approx 3$$

$$\therefore \boxed{\text{No. of bars} \approx 3}$$

Design
General Considerations for beam:

1. Effective span: The effective span of S.S. beam shall be taken as clear span plus effective depth of the beam (or) Centre to Centre distance b/w the supports which ever is less

2. Limiting stiffness: $\left(\frac{l}{d}\right)$ ratio

Cantilever - 7

l = Effective span

Simply Supported - 20. d = effective depth

Continuous - 26.

3. Minimum reinforcement = $\frac{A_{st\min}}{bd} \frac{0.85}{f_y}$

4. Maximum reinforcement = $0.04 bD$

Q. A singly reinforced concrete beam section 200x450mm is reinforced with 4 bars of 20mm ϕ with an effective cover of 40mm. The beam is S.S over a span of 4m. Find the safe uniform distributed load the beam can carry. Use M₂₀ grade concrete & Fe 415, steel.

Ans

Given data:

$$b = 200 \text{ mm}$$

$$d = 450 - 40$$

$$\therefore d = 410 \text{ mm}$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

$$\begin{aligned} A_{st} &= 4 \times \frac{\pi}{4} (20)^2 \\ &= 1256.6 \text{ mm}^2 \end{aligned}$$

Depth of Neutral axis:

$$\begin{aligned} x_u &= \frac{0.87 f_y \cdot A_{st}}{0.86 f_{ck} \cdot b} \\ &= \frac{0.87 \times 415 \times 1256.6}{0.86 \times 20 \times 200} \end{aligned}$$

$$x_u = 315.1 \text{ mm}$$

$$x_{u\max} = 0.48d \quad [\text{for Fe 415 steel}]$$

$$= 0.48 \times 410$$

$$\Rightarrow 196.8 \text{ mm}$$

$$x_{u\max} = 196.8 \text{ mm}$$

$$x_u > x_{u\max}$$

∴ So, the Section is Over reinforced.

Moment of resistance: (MR)

$$MR = 0.36 \cdot f_{ck} \cdot x_{u\max} \cdot b \cdot (d - 0.42 x_{u\max})$$

$$= 0.36 \times 20 \times 196.8 \times 200 (410 - 0.42 (196.8))$$

$$= 92.76 \times 10^6 \text{ N-mm}$$

$$M_u = 92.76 \text{ kN-m}$$

Safe load:

$$BM = \frac{wl^2}{8} = \frac{w(4)^2}{8} = 2w$$

$$\text{Equate } BM = M_u$$

$$2w = 92.76$$

$$w = \frac{92.46}{2}$$

$$w = 46.38 \text{ kN/m}$$

Safe working load, $w = \frac{\text{Bending moment (act)}}{\text{load factor}}$

$$\Rightarrow \frac{46.38}{1.5}$$

$\therefore 30.92 \text{ kN/m}$ (including
(act) contribution for the self wt.)

Self wt. of the beam $= 0.2 \times 0.45 \times 25$

$$= 2.25 \text{ kN/m}$$

\therefore Net superimposed load $= 30.92 - 2.25$

$$\therefore \underline{28.67 \text{ kN/m}}$$

3/17

General Design requirements for beams:

5. Gage Spacing of bars: The horizontal distance between two parallel main reinforcement bars shall usually be ^{not} less than the greatest of the following.

$\therefore \underline{2.67 \text{ inches}}$

- (a). Diameter of the bars if the diameters are equal.
- (b) Diameters of the largest bars if the bars are unequal.
- (c) 5mm more than the normal max. size of the aggregate.

Design procedure: (l, f_{ck}, f_y, b)

1. Assuming $\frac{l}{d}$ ratio (40 to 15)

Assume $b = 230\text{mm}$

2. Effective span : $l_a + l_b$

a) clear span + d

b) clear span + $\frac{b}{2} + \frac{b}{2}$ } ~~max min~~

3. Calculation of loads & BM

Self weight = volume of beam \times density
of Concrete

$$= b \times d \times 1 \times 25$$

$$BM = \frac{w l^2}{8}$$

factored BM, $M_u = 1.5 \times BM$

$$RCC = 25 \text{ kN/m}^3$$

$$PCC = 24 \text{ kN/m}^3$$

4. Check of depth required,

M_ulimit is equating to M_u ($M_u = M_{ulim}$)

for Fe 415, $M_{ulim} = 0.138 f_{ck} b d^2$

$$d = \sqrt{\frac{M_{ulim}}{0.138 f_{ck} \cdot b}}$$

5. Calculated area of reinforcement

$$M_u = 0.8 f_y A_{st} \times d \left(1 - \frac{f_y A_{st}}{f_{ck} b d} \right)$$

$$A_{st} = ?$$

$$A_{stmin} < A_{st} < A_{stmax}$$

6. check for deflection,

5. Design a rectangular S-S reinforced concrete beam over a clear span of 4m. If the super imposed load is 20kN/m, and support width is 300mm each. Use M₂₀ and Fe 415 steel. Check for deflection also.

Ref

Given data,

$$\text{Clear span } L = 4\text{m} \Rightarrow 4000\text{mm}$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

$$b = 300\text{mm}$$

Super imposed load $> 20 \text{ kN/m}$

(i) Assuming $\frac{l}{d} = 12$ based on

Stiffness d - $\frac{40000}{12}$ $\frac{40000}{d} = 12$
 $12d = 4000$
 $d = 333.33 \text{ mm} \approx 350 \text{ mm}$ $d = \frac{4000}{12}$

$$\boxed{d = 350 \text{ mm}}$$

(ii) Effective Cover assuming = 50mm

Overall depth = 50 + 350

$$\boxed{D = 400 \text{ mm}}$$

(iii) Effective Span:

It is the least of the following

(i) Centre to Centre - clear span + $\frac{b}{2} + \frac{b}{2}$
 $\Rightarrow 4000 + \frac{300}{2} + \frac{300}{2}$
 $= 4300 \text{ mm} \Rightarrow 4.3 \text{ m}$

(ii) Clear span + d = $4000 + 350$
 $= 4350 \text{ mm}$
 $= 4.35 \text{ m}$

\therefore Hence effective span $l = 4.3 \text{ m}$

(iii) Calculation of Loads & BM

$$\text{Self wt} = 0.3 \times 0.4 \times 1 \times 25$$

dead load $= 3 \text{ kN/m}$

$$BM = \frac{wl^2}{8}$$

Superimposed load $= 20 \text{ kN/m}$

$$\therefore \text{Total load} = 20 + 3 \\ = 23 \text{ kN/m}$$

$$\therefore \text{Total load} = 23 \text{ kN/m}$$

$$BM = \frac{23 \times 4.3^2}{8}$$

$$\boxed{BM = 53.15 \text{ kN-m}}$$

factored BM, $\approx 4.5 \times BM$

$$M_u = 1.5 \times BM$$

$$= 1.5 \times 53.15$$

$$\boxed{M_u = 79.74 \text{ kN-m}}$$

Step 4: check of depth required.

$$M_u = M_{ulimit}$$

for Fe 415, $M_{ulimit} = 0.138 f_{ck} b d^2$

$$d = \sqrt{\frac{M_{ulimit}}{0.138 f_{ck} b}}$$

$$\sqrt{\frac{79.34 \times 10^6}{0.138 \times 20 \times 300}}$$

$$d = 310.32 \text{ mm} < d \text{ provided } (d = 350 \text{ mm})$$

Hence provided depth is adequate

Step 5: Area of reinforcement,

$$M_u = 0.87 f_y A_{st} \times d \left(1 - \frac{f_y A_{st}}{f_{ck} b \times d} \right)$$

$$79.34 \times 10^6 = 0.87 \times 415 \times A_{st} \times 350 \left[1 - \frac{415 A_{st}}{20 \times 300 \times 350} \right]$$

$$79.46 \times 10^6 = 126.36 \times 10^3 A_{st} \left[1 - 1.976 \times 10^{-9} A_{st} \right]$$

$$79.46 \times 10^6 = 126.36 \times 10^3 A_{st} - 19.97 A_{st}^2$$

$$19.97 A_{st}^2 - 126.36 \times 10^3 A_{st} + 79.46 \times 10^6 = 0$$

$$A_{st} = 735.8 \text{ mm}^2$$

Provide 4 bars of 16 mm ϕ for finding no. of bars

$$A_{st} = \text{No. of bars} \times \frac{\pi}{4} (16)^2$$

$$735.8 = \text{No. of bars} \times 201.06$$

$$201.06 \text{ No. of bars} = 735.8$$

$$\therefore \text{No. of bars} = \frac{0.6735 \times 80}{0.2 \times 201.06 \times 0}$$

$$= 3.65 \approx 4 \text{ bars.}$$

$$\therefore \text{No. of bars} = 4 \text{ bars.}$$

Minimum reinforcement: (Pg: 47)

$$\Rightarrow \frac{A_{st\min}}{bd} = \frac{0.85}{f_y} = \frac{0.85}{415} = 0.00204$$

$$\left[\frac{A_{st\min}}{0.2 \times 300 \times 0.06} = \frac{0.85 bd}{415 f_y} = \frac{0.85 \times 300 \times 300}{415 \times 415} = 0.00204 \right]$$

$$\left[\frac{A_{st\min}}{0.2 \times 300 \times 0.06} = \frac{0.85 \times 300 \times 300}{415} = 0.00204 \right]$$

$$\therefore A_{st\min} = 0.00204 \times 300 \times 0.06 = 36.06 \text{ mm}^2$$

Maximum reinforcement:

$$A_{st\max} = 0.04 \times bD$$

$$\left[\frac{A_{st\max}}{0.2 \times 300 \times 0.06} = \frac{0.04 \times 300 \times 400}{0.06} = 400 \right]$$

$$\left[\frac{A_{st\max}}{0.2 \times 300 \times 0.06} = \frac{0.04 \times 300 \times 400}{0.06} = 400 \right]$$

$$\therefore A_{st\max} = 400 \text{ mm}^2$$

$$2 \times 16 \text{ mm}^2 = 32 \text{ mm}^2 < 400 \text{ mm}^2$$

Ast required = 1935.8 mm²

$$\text{Ast provided} = \frac{\pi}{4}(16)^2 \times 4$$

$$= 804.24 \text{ mm}^2$$

So

6. Check for deflection (Stiffness)

For S.S beam basic value ($\frac{l}{d} = 20$)

In code book, pg: no - 38

Modification factor for tension reinforcement,

$$f_s = 0.58 f_y \times \frac{\text{Area of c/s of Ast required}}{\text{Area of c/s of Ast provided}}$$

$$= 0.58 \times 415 \times \frac{1935.8}{804.24}$$

$$\boxed{f_s = 220.22 \text{ N/mm}^2}$$

$$\% \text{ of steel} = \frac{\text{Ast provided}}{bd} \times 100$$

$$\frac{804.24}{300 \times 350} \times 100$$

$$= 0.76\%$$

From Fig. 4 of IS: 456, modification factor = 1.15

Max. permitted deflection ratio = 1.5% K20

$$\frac{l}{d} \text{ provided} = \frac{4300}{360}$$

(min.) $15.28 < 23$ ~~is safe~~

∴ Hence deflection is safe.

6. Design a rectangular beam for effective span 4m. which is subjected to dead load of 15kN/m and live load of 12kN/m. use M15 & Fe 400 grade steel. Assume $b = 250\text{mm}$

Ref

Given data,

Effective

Clear Span $l = 4\text{m} \Rightarrow 4000\text{mm}$

$$f_{ck} = 15\text{N/mm}^2$$

$$f_y = 250\text{N/mm}^2$$

$$b = 250\text{mm}$$

$$\text{Dead Load} = 15\text{kN/m}$$

$$\text{Live Load} = 12\text{kN/m}$$

(i) Assuming $\frac{l}{d} = 10$ based on

stiffened = $\frac{4000}{10}$

$$d = 400 \text{ mm}$$

Assuming effective cover = 50mm.

Overall depth = 500 + 400

$$D = 450 \text{ mm}$$

(ii) Effective span, $l = 9000 \text{ mm}$

(iii) Calculation of loads & BM

$$\begin{aligned} \text{Self wt.} &= 0.25 \times 0.45 \times 1 \times 25 \\ &= 2.8125 \text{ kN/m} \end{aligned}$$

BRK

Dead load = 15 kN/m

Live load = 18 kN/m

$$\begin{aligned} \text{(i) Total load} &= 15 + 12 + 2.8125 \\ &= 29.81 \text{ kN/m} \end{aligned}$$

\therefore Total load = 29.81 kN/m

$$BM = \frac{29.81 \times 4^2}{8}$$

$$BM = 59.62 \text{ kN/m}$$

Factored Bending moments

$$M_u = 1.5 \times BM$$

$$\Rightarrow 1.5 \times 59.62$$

$$\therefore M_u = 89.43 \text{ kN-m}$$

Step 4: Depth required,

$$M_u = M_{u\text{ limit}}$$

for Fe 250 steel, $M_{u\text{ limit}} = 0.148 f_{ck} b d^2$

$$d = \sqrt{\frac{M_u}{0.148 f_{ck} b}}$$
$$= \sqrt{\frac{89.43 \times 10^6}{0.148 \times 15 \times 250}}$$

$$d = 401.4 \text{ mm} > d = 400$$

from Code book procedure $\frac{l}{d}$ ratio (10 to 1)

Take, $\frac{l}{d}$ ratio = 9

So, procedure will be redesigned

(i) Assuming $\frac{l}{d} = 9$ based on

$$\text{stiffness } d = \frac{4000}{9}$$

$$d = 444.4 \text{ mm} \approx 450 \text{ mm}$$

$$\boxed{d = 450 \text{ mm}}$$

Assuming effective Cover = 50mm

$$D = 450 + 50$$

$\rightarrow 500 \text{ mm}$: $M_u < M_{\text{ult}} - \text{singly}$

$$\boxed{D = 500 \text{ mm}}$$

$M_u < M_{\text{ult}} - \text{Doubly}$

(ii) Effective Span $l = 4000 \text{ mm}$

(iii) Calculation of load & BM:

$$\text{Self wt} = 0.25 \times 0.5 \times 1 \times 25.$$

$$\text{Dead load} = 3.125 \text{ kN/m}$$

$$\text{Live load} = 12 \text{ kN/m}$$

$$\text{Total load} = 3.125 + 15 + 12$$

$$= 30.125 \text{ kN/m}$$

$$\text{BM} = \frac{30.125 \times 4^2}{8}$$

$$\boxed{\text{BM} = 60.25 \text{ kNm}}$$

Factored Bending moment,

$$M_u = 1.5 \times 60.25$$

$$\therefore M_u = 90.375 \text{ kN-m}$$

Step 4: Depth required,

$$M_u = M_u \text{ limit}$$

for Fe 250 steel, $M_u \text{ limit} = 0.148 f_{ck} b d^2$

$$d = \sqrt{\frac{M_u \text{ limit}}{f_{ck} \times 0.148 \times b}}$$

$$= \sqrt{\frac{90.375 \times 10^6}{15 \times 0.148 \times 250}}$$

$$d = 240.353 \text{ mm} < 450 \text{ mm}$$

Hence provided depth is adequate.

Step 5: Area of reinforcement,

$$M_u = 0.87 f_y \cdot A_{st} \times d \left[1 - \frac{f_y \cdot A_{st}}{f_{ck} \cdot b \cdot d} \right]$$

$$= 0.87 \times 250 \times A_{st} \times 450 \left[1 - \frac{1250 A_{st}}{15 \times 250 \times 450} \right]$$

$$\Rightarrow 97.875 \times 10^3 A_{st} - 14.5 A_{st}^2 = 0$$

$$14.5 A_{st}^2 - 97.875 \times 10^3 A_{st} + 90.375 \times 10^6 = 0$$

$$A_{st} = 1103.9 \text{ mm}^2 \quad] \text{ required}$$

Provide 16 mm φ for finding no. of bars

$$A_{st} = \text{no. of bars} \times \frac{\pi}{4} (16)^2$$

$$201.06 \text{ No. of bars} = 1103.9$$

$$\text{No. of bars} = \frac{1103.9}{201.06}$$

$$= 5.49 \approx 6 \text{ bars}$$

$$\therefore [\text{No. of bars} = 6]$$

$$A_{st} \text{ provided} = \frac{\pi}{4} (16)^2 \times 6$$

$$= 201.06 \times 6$$

$$= 1206.37 \text{ mm}^2$$

$$[A_{st} \text{ provided} = 1206.37 \text{ mm}^2]$$

6. Check for deflection : (stiffness)

For S.S beam basic value ($\frac{l}{d}, \alpha_0$)

in Code book pg: no-38

Modification for tension reinforcement,

$$f_s = 0.58 f_y \times \frac{\text{Area of c/s of Ast required}}{\text{Area of c/s of Ast provided}}$$

$$f_s = 0.58 \times 250 \times \frac{1103.9}{1206.37}$$

$$f_s = 138.68 \text{ N/mm}^2$$

% of steel = $\frac{A_{st} \text{ provided}}{bd} \times 100$

$$= \frac{1206.37}{250 \times 400} \times 100$$

$$= 10.42\%$$

From fig. 4 of IS: 456, modification

$$\text{fact}(S) = 1.5$$

$$\text{Max. permitted } \frac{l}{d} \text{ ratio} = 1.5 \times 20 \\ = 30$$

$$\frac{l}{d} \text{ provided} = \frac{4000}{400} \\ = 10 < 30$$

\therefore Hence deflection control is safe.

Min reinforcement: step 5:-

$$\frac{A_{st\min}}{bd} = \frac{0.85}{f_y}$$

$$A_{st\min} = \frac{0.85 \times 250 \times 400}{350}$$

$$A_{st\min} = 340 \text{ mm}^2$$

Max. reinforcement:

$$A_{st\ max} = 0.04 \times bD$$

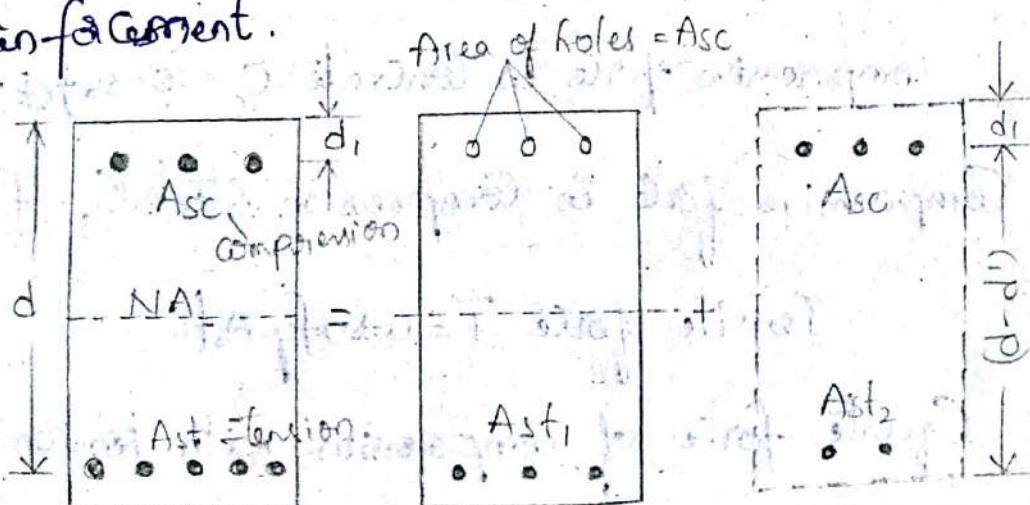
$$= 0.04 \times 250 \times 450$$

$$\boxed{A_{st\ max} = 4500 \text{ mm}^2}$$

15/2/17

Doubly reinforced beams:

Beams which are reinforced in both compression & tension sides are called as doubly reinforced beam. These beams are generally provided when the dimensions of the beam are restricted & it is required to resist moment higher than the limiting moment of resistance of a singly reinforced section. The additional moment of resistance required can be obtained by providing compression reinforcement & additional tension reinforcement.

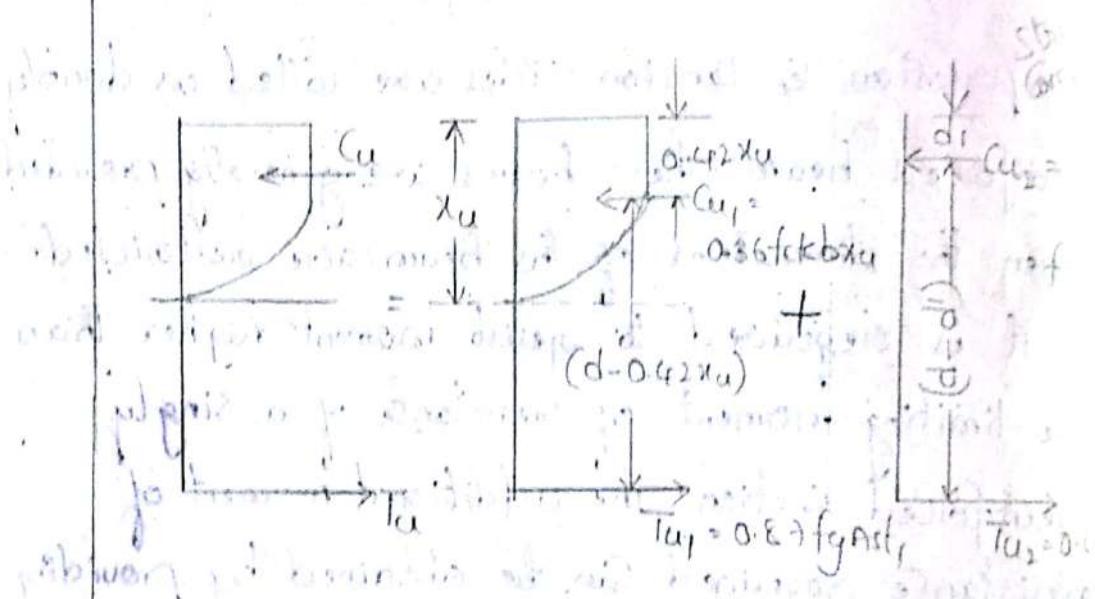


Section Subjected to moment M_u Section-I: Resisting moment $M_{u1} = M_{ulim}$ Section-II: Resisting balance moment $M_{u2} = M_u - M_{ulim}$

This doubly reinforced section can be considered to be composed of two sections as given below.

- (a). A singly reinforced section with M_u , i.e.
- (b) A section with compression steel & additional tension steel to resist additional moment

$M_{u2} = M_u - M_{u,lim}$ i.e., a steel beam without concrete.



1. Depth of Neutral axis:

Compressive force in Concrete $C_c = 0.36 f_{ck} \cdot b \cdot r_u$

Compressive force in Compression Steel $C_s = f_{sc} \cdot A_s$

Tensile force $T = 0.87 f_y A_{st}$

Equate force of compression with tension

$$C_c + C_s = T$$

$$0.36 f_{ck} \cdot b \cdot x_u + f_{sc} \cdot A_{sc} = 0.87 f_y \cdot A_{st}$$

$$x_u = \frac{0.87 f_y \cdot A_{st} - f_{sc} \cdot A_{sc}}{0.36 f_{ck} \cdot b}$$

~~17.5 ft~~

2. ultimate moment of resistance:

The ultimate moment of resistance of doubly reinforced is given by,

$$M_u = M_{u1} + M_{u2}$$

$$= 0.36 f_{ck} \cdot b \cdot x_u (d - 0.42 x_u) + f_{sc} \cdot A_{sc} (d - d')$$

where,

$x_u > x_{u,\max}$, x_u is limited to $x_{u,\max}$.

$$\boxed{M_u = 0.36 f_{ck} \cdot b \cdot x_{u\max} (d - 0.42 x_{u\max}) + f_{sc} \cdot A_{sc} (d - d')}$$

3. Area of Compression steel:

Additional moment of resistance M_{u2} ,

$$M_{u2} = f_{sc} \cdot A_{sc} (d - d')$$

$$\boxed{A_{sc} = \frac{M_{u2}}{f_{sc} (d - d')}}$$

The maximum area of compression reinforcement shall not exceed $0.04bd$ i.e., 4% of gross area.

4. Area of Tension steel: The limiting moment of resistance of singly reinforced section is given by,

$$M_{u, \text{lim}} = 0.87 f_y \cdot A_{st_1} (d - 0.42 x_{u, \text{max}})$$

$$A_{st_1} = \frac{M_{u, \text{lim}}}{0.87 f_y (d - 0.42 x_{u, \text{max}})}$$

Additional area of tensile steel (A_{st_2}) can be calculated by equating the compressive force in compression steel & tensile force in additional tension steel.

$$0.87 f_y \cdot A_{st_2} = f_{sc} \cdot A_{sc}$$

$$A_{st_2} = \frac{f_{sc} \cdot A_{sc}}{0.87 f_y}$$

A_{st_2} can also be calculated by using,

$$M_{u_2} = 0.87 f_y \cdot A_{st_2} (d - d')$$

$$A_{st_2} = \frac{M_{u_2}}{0.87 f_y (d - d')}$$

Total area of tension steel $A_{st} = A_{st1} + A_{st2}$

Stress in Comprehension steel (f_{sc}) based on d'/d

Table 3.5

Stress in Comprehension steel. f_{sc} , N/mm² in doubly reinforced beam with cold worked bars.

(Table-F in SP16) when $d'/d < 0.2$

Grade of steel	d'/d			
	0.05	0.10	0.15	0.20
Fe 415	355	353	342	329
Fe 500	424	412	395	370

For $d'/d < 0.2$, f_{sc} for mild steel is $0.87f_y$.

7. Calculate the ultimate moment of resistance of an R.C beam of rectangular section 300mm wide & 400mm deep. Area of steel consists of 6 Nos 18φ in tension side & 3 Nos 18φ in compression side. Assume steel of grade Fe 415 & concrete of grade M₂₀ & an effective cover 35mm on both sides.

8of

Given data,

$$b = 300\text{mm}$$

$$d = 400 - 35 \\ = 365\text{mm}$$

$$d' = 35 \text{ mm}$$

$$f_{ck} = 40 \text{ N/mm}^2$$

$$f_g = 4115 \text{ N/mm}^2$$

$$A_{st} = 6 \times \frac{\pi}{4} (18)^2 = 1526.8 \text{ mm}^2$$

$$A_{sc} = 8 \times \frac{\pi}{4} (18)^2 = 5089 \text{ mm}^2$$

1. Stresses in Compression steel:

$$\frac{d'}{d} = \frac{35}{365} = 0.09$$

$$\frac{d'}{d} = 0.09 < 0.2$$

from ~~text~~ book table 3.5.

$$0.05 - 355$$

$$0.10 - 353$$

$$0.09 - ?$$

$$\Rightarrow 355 - \left(\frac{355 - 353}{0.10 - 0.05} \right) (0.09 - 0.05)$$

$$f_{sc} = 353.4 \text{ N/mm}^2$$

2. Depth of Neutral Axis:

$$x_a = \frac{0.5 + f_g \cdot A_{st} - f_{sc} \cdot A_{sc}}{0.36 f_{ck} \times b}$$

$$0.87 \times 415 \times 1526.8 - (353.4 \times 508.91)$$

$$0.36 \times 20 \times 300$$

$$x_u = 171.94 \text{ mm}$$

Limiting depth of neutral axis:-

$$x_{\max} = 0.48d$$

$$= 0.48 \times 365$$

$$= 175.2 \text{ mm}$$

$$\therefore x_u < x_{\max}$$

So, the section is under-reinforced.

3. Moment of resistance :-

$$M_u = 0.36 f_{ck} b x_u (d - 0.42 x_u) + f_{sc} A_{sc} (d - d_i)$$

$$\Rightarrow 0.36 \times 20 \times 300 \times 171.94 (365 - (0.42 \times 171.94))$$

$$+ (353.4 \times 508.91) (365 - 35)$$

$$\Rightarrow 167.62 \times 10^6 \text{ N-mm}$$

$$M_u = 167.62 \times 10^6 \text{ N-mm}$$

$$= 167.62 \text{ kN-mm}$$

19/2/18

8. A rectangular beam is 200mm wide & 400mm deep if it is reinforced beam & has a concrete cover of 40mm. In compression with an effective cover of 30mm. Determine the area of tension reinforcement to make the beam section fully effective. Then calculate the moment of resistance.
- (Concrete = Fe 405 steel.)

Ans

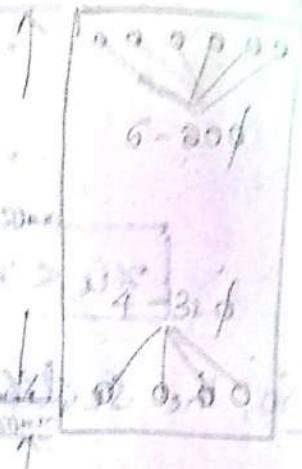
Given data,

$$b = 200\text{mm}$$

$$d = 400 - 40 = 360\text{mm}$$

$$= 320\text{mm}$$

$$D = 500\text{mm}$$



$$A_{sc} = 6 \times \frac{\pi}{4} (20)^2 \Rightarrow 1884.95\text{mm}^2$$

(b) Standard concrete $f_{ck} = 30\text{N/mm}^2$

$$f_y = 415\text{N/mm}^2$$

$$d' = 50\text{mm}$$

A_{st} is provided based on Muslimi

$$\text{Muslimi} = 0.138 f_{ck} b d^2$$

$$= 0.138 \times 30 \times 200 \times 450^2$$

$$= 117.8 \times 10^6 \text{N-mm}$$

$$= 117.78 \text{KN-m}$$

$$A_{st} = \frac{M_u}{0.87 f_y (d - 0.42 x_{u, \max})}$$

$$x_{u, \max} = 0.48 d$$

$$= 0.48 \times 450$$

$$= 216 \text{ mm}$$

$$\therefore A_{st_1} = \frac{111.78 \times 10^6}{0.87 \times 415 (450 - 0.42(216))}$$

$$A_{st_1} = 861.21 \text{ mm}^2$$

$$A_{st_2} = \frac{f_{sc} \cdot A_{sc}}{0.87 f_y}$$

for f_{sc} value, $\frac{d_1}{d} = \frac{50}{450} = 0.11$

$$\frac{d_1}{d} = \frac{50}{450} = 0.11$$

from table,

$$0.10 - 353$$

$$0.15 - 342$$

$$f_{sc} = 353 - \left(\frac{353 - 342}{0.15 - 0.10} \right) (0.10 - 0.10)$$

$$f_{sc} = 350.8 \text{ N/mm}^2$$

$$A_{st_2} = \frac{f_{sc} \cdot A_{sc}}{0.87 f_y}$$

$$= \frac{350.8 \times 1889.95}{0.87 \times 415}$$

$$= 1831.43 \text{ mm}^2$$

$$\boxed{A_{st_2} = 1831.43 \text{ mm}^2}$$

$$A_{st} = A_{st_1} + A_{st_2}$$

$$= 861.31 + 1831.43$$

$$= 2693.14 \text{ mm}^2$$

$$\boxed{A_{st} = 2693.14 \text{ mm}^2}$$

$$x_u = \frac{0.87 f_y \cdot A_{st} - f_{sc} \cdot A_{sc}}{0.36 f_{ck} \times b}$$

no. of bars $\times \frac{\pi}{4}$
bars

$$= \frac{0.87 \times 415 \times 2693.14 - (350.8 \times 1889.95)}{0.36 \times 20 \times 200}$$

$$x_u = 216.05 \text{ mm}$$

$$\therefore x_u = x_{u\max}$$

∴ the section is balanced section.

$$M_u = 0.36 f_{ck} \times b \times x_{u, max} (d - 0.42 x_u) + f_{sc} \cdot A_{sc} (d - d')$$

$$= 0.36 \times 20 \times 200 \times 246 (450 - 0.42(246))$$

$$+ (350.8 \times 1884.95) (450 - 50)$$

$$= 376.24 \times 10^6 \text{ N-mm}$$

$$M_u = 376.24 \text{ kN-m}$$

9. Determine the main tensile & compression reinforcement required for a rectangular beam with a following data. Overall size of the beam

$$= 250 \times 550 \text{ mm}$$

Given data = M_u

F_y = 415 steel

Factored moment = 800 kN-m

Effective Cover = 50mm

Given data,

$$b = 250 \text{ mm}$$

$$d = 500 \text{ mm}$$

$$D = 550 \text{ mm}$$

$$d' = 50 \text{ mm}$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

$$M_u = 200 \text{ kN-m}$$

1. Limiting moment of resistance of the given section as singly reinforced section:

$$M_{u,lim} = 0.138 f_c k_b d^2$$

$$= 0.138 \times 20 \times 280 \times 500^2$$

$$= 178.5 \times 10^6 \text{ N-mm}$$

$$\boxed{M_{u,lim} = 178.5 \text{ kN-m}}$$

$$\therefore \boxed{M_u > M_{u,lim}}$$

So, the section should be designed as doubly reinforced section.

2. Area of tension steel corresponding to $M_{u,lim}$

$$A_{st,1} = \frac{0.88 M_{u,lim}}{0.87 f_y (d - 0.42 x_{max})}$$

$$x_{max} = 0.41 d$$

$$= 0.41 \times 500$$

$$= 205 \text{ mm}$$

$$A_{st} = \frac{172.5 \times 10^6}{0.87 \times 415 (500 - (0.42 \times 240))}$$

$$A_{st} = 1196.82 \text{ mm}^2$$

$$3. M_{u_2} = M_u - M_{ulim}$$

$$= 200 - 172.5$$

$$M_{u_2} = 27.5 \text{ kNm}$$

$$M_{u_2} = f_{sc} \cdot A_{sc} (d - d')$$

$$\frac{d'}{d} = \frac{50}{500} = 0.1$$

from table 3.5

$$0.10 - 353$$

$$\text{So, } f_{sc} = 353 \text{ N/mm}^2$$

$$M_{u_2} = 353 \times A_{sc} (500 - 50)$$

$$27.5 \times 10^6 = 158.85 \times 10^3 A_{sc}$$

$$158.85 \times 10^3 A_{sc} = 27.5 \times 10^6$$

$$A_{sc} = \frac{27.5 \times 10^6}{158.85 \times 10^3}$$

$$A_{sc} = 173.11 \text{ mm}^2$$

Required.

4. Additional tensile stress (A_{st2}):

$$A_{st2} = \frac{f_{sc} \cdot A_{sc}}{0.87 f_y}$$

$$= \frac{353 \times 173.1}{0.87 \times 415}$$

$$A_{st2} = 169.24 \text{ mm}^2$$

∴ Total tension steel,

$$A_{st} = A_{st1} + A_{st2}$$

$$= 1196.82 + 169.24$$

$$A_{st} = 1366.06 \text{ mm}^2 \quad \text{Required}$$

Assume 20mm ϕ to finding no. of bars

$$A_{st} = \text{No. of bars} \times \frac{\pi}{4} (20)^2$$

$$1366.06 = \text{No. of bars} \times 314.15$$

$$314.15 \text{ No. of bars} = 1366.06$$

$$\text{No. of bars} = 4.3 \approx 5 \text{ bars}$$

$$A_{st} = 5 \times \frac{\pi}{4} (20)^2$$

$$= 1570.7 \text{ mm}^2$$

$$A_{st} \text{ provided} = 1570.07 \text{ mm}^2$$

Provide 12mm φ to find out no. of bars in compression.

$$A_{sc} = \text{No. of bars} \times \frac{\pi}{4} (12)^2$$

$$173.11 = 113.09 \text{ No. of bars}$$

$$\text{No. of bars} = 1.53 \approx 2$$

$$\therefore \text{No. of bars} = 2$$

$$A_{sc} = 2 \times \frac{\pi}{4} (12)^2$$

$$= 226.18 \text{ mm}^2$$

$$\therefore \text{Provided } A_{sc} = 226.18 \text{ mm}^2$$

Design of shear: [Pg: NO - 72, 73]

τ_v = nominal shear stress

τ_c = shear strength resistance by concrete [from table No: 19]

τ_{max} = Max. shear stress [Table no: 20]

$$\tau_v = \frac{V}{bd}; V = \text{shear force}$$

$\tau_v > \tau_c$ = provided shear reinforcement

Shear reinforcement has to be provided against diagonal tensile stresses caused by the shear force. The longitudinal bars do not prevent the diagonal tension failure.

The inclined shear crack starts at the bottom near the support and extend toward compression zone. The shear reinforcement can be provided in any of the following forms.

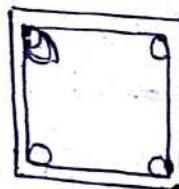
(a). Vertical stirrups.

(b). Bent up bars along with stirrups.

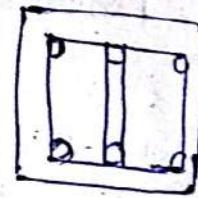
(c) Inclined stirrups.



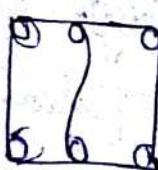
One legged
stirrup



Two legged
stirrup



Four legged
stirrup



Three legged
stirrup

22/7/17 $\tau_c < \tau_v \rightarrow$ minimum reinforcement is to be provided.

from Code book - Table no:19 - τ_c value.

$\tau_{c\max}$ - Table no:20.

10. A simply supported R.C.C beam 250mm x 450mm (effective) is reinforced with 4 nos of 18mm Ø bars. Design the shear reinforcement if M₂₀ grade Concrete & Fe 415 steel is used if beam is subjected to a force of 150kN at service load

Given data,

$$b = 250 \text{ mm}$$

$$d = 450 \text{ mm}$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

$$\text{Shear force} = 150 \text{ kN}$$

$$\begin{aligned}\text{Factored shear force } V_u &= 1.5 \times 150 \\ &= 225 \text{ kN}\end{aligned}$$

$$\tau_v = \frac{V_u}{bd} = \frac{225 \times 10^3}{250 \times 450} = 2 \text{ N/mm}^2$$

from Code book table no:19

$$A_{st} = \frac{4 \times \pi}{4} (18)^2 \\ = 1017.8 \text{ mm}^2$$

$$\% \text{ of steel} = \frac{1017.8}{250 \times 450} \times 100 \\ = 0.9047$$

from table no: 19

$$0.75 - 0.56$$

$$1.00 - 0.62$$

$$0.9047 - ?$$

$$\tau_c = 0.56 + \left(\frac{0.56 - 0.62}{1.00 - 0.75} \right) (0.9047 - 0.75)$$

$$\tau_c = 0.52 \text{ N/mm}^2, \tau_{cmax} = 2.8 \text{ N/mm}^2$$

$$\boxed{\tau_v > \tau_c} \quad \text{Shear reinforcement has } \tau_{vmax} = 2.8 \text{ N/mm}^2 \quad \text{to be designed}$$

(ii) Design of shear reinforcement:

$$V_{ac} = \tau_c \cdot b d \Rightarrow 0.52 \times (250 \times 450) \\ \Rightarrow 58500 \text{ N.} \Rightarrow 58.5 \text{ kN}$$

$$V_{us} = V_u - V_{ac}$$

$$\Rightarrow 225 - 58.5 \Rightarrow 166.5 \text{ kN}$$

Design of vertical stirrups:
Spacing of 2-legged 10mm stirrup stirrups

$$A_{sv} = 2 \times \frac{\pi}{4} (10)^2 \\ = 157.07 \text{ mm}^2$$

Spacing of stirrups:

$$1. 0.75 \times 450 + 0.75 \times 450 = 337.5 \text{ mm}$$

2. 300 2. 300mm whichever is less.

3. For vertical stirrups:

$$V_{us} = \frac{0.87 f_y \cdot A_{sv} \cdot d}{s_v}$$

$$s_v = \frac{0.87 f_y \cdot A_{sv} \cdot d}{V_{us}}$$

$$\frac{0.87 \times 415 \times 157.07 \times 450}{166.5}$$

$$s_v = 168.56 \times 10^3 \text{ mm}$$

$$s_v = 153.85 \text{ mm} \approx 165 \text{ mm}$$

from code book pg: 48.

26.5.1.6 - main shear reinforcement

$$\frac{A_{sv}}{b s_v} \geq \frac{0.4}{0.87 f_y}$$

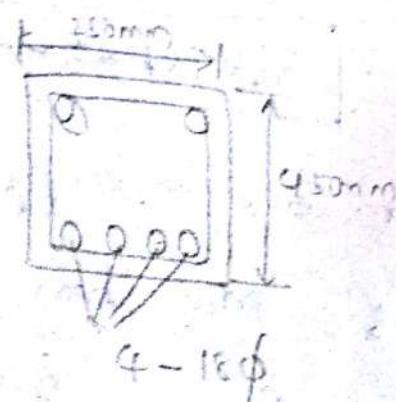
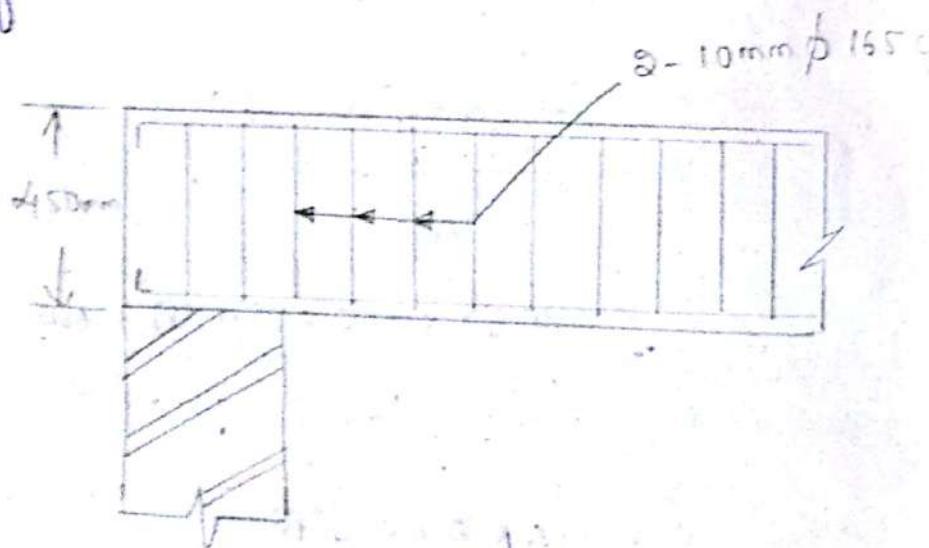
$$\frac{A_{sv}}{b \cdot s_v} = \frac{0.4}{0.87 f_y}$$

$$s_v = \frac{0.87 f_y \cdot A_{sv}}{0.4 \times b}$$

$$= \frac{0.87 \times 415 \times 157.07}{0.4 \times 280}$$

$$[s_v = 567.10 \text{ mm}]$$

Provide 10mm ϕ stirrups with a spacing of 165mm



4-10φ

24/7/17

11. A S.S R.C.C beam of 200mm x 400mm (effective) is reinforced with 4 bars of 22mm ϕ on tension side. The beam is carrying a udl of 10kN/m over a clear span of 8m. Design the shear reinforcement by using M₂₀ grade concrete & Fe 415 steel.

sol

Given data,

$$b = 200\text{mm}$$

$$d = 400\text{mm}$$

$$\text{load} = 10\text{kN/m}$$

$$l = 8\text{m}$$

$$f_{ck} = 20\text{N/mm}^2$$

$$f_y = 415\text{ N/mm}^2$$

$$D = 400 + 50$$

$$= 450\text{ mm}$$

$$\begin{aligned}\text{Self wt.} &= 25 \times 0.45 \times 0.2 \\ &= 2.25\text{ kN/m}\end{aligned}$$

$$\begin{aligned}\text{Total load} &= 2.25 + 10 \\ &= 12.25\text{ kN/m}\end{aligned}$$

$$\begin{aligned}\text{Factored load } w_u &= 12.25 \times 1.5 \\ &= 18.375\text{ kN/m}\end{aligned}$$

$$\text{Factored shear force} = \frac{W_u d}{2}$$

$$= \frac{18.375 \times 8.2}{2}$$

$$V_u = 75.33 \text{ kN.}$$

$$\text{Effective span} = 8 + \frac{0.2}{2} + \frac{0.2}{2}$$

$$l = 8.2 \text{ m}$$

1. Monomial shear stresses:

$$\tau_v = \frac{V_u}{bd} \Rightarrow \frac{75.33 \times 10^3}{200 \times 400}$$

$$\tau_v = 0.942 \text{ N/mm}^2$$

$$A_{st} = 4 \times \frac{\pi}{4} (22)^2$$

$$A_{st} = 1520.5 \text{ mm}^2$$

$$\% \text{ of steel} = \frac{1520.5}{200 \times 400} \times 100 \\ \Rightarrow 1.9\%$$

from table no: 19

$$1.75 \rightarrow 0.75$$

$$2.00 \rightarrow 0.79$$

$$1.9 \rightarrow ?$$

$$\tau_c = 0.75 + \left(\frac{0.79 - 0.75}{2.00 - 1.75} \right) (1.9 - 1.75)$$

$$\boxed{\tau_c = 0.774 \text{ N/mm}^2}$$

$$\tau_{c\max} = 2.8 \text{ N/mm}^2$$

$$\boxed{\tau_v > \tau_c}$$

Shear reinforcement has to be designed

(ii) Design of shear reinforcement:

$$V_{uc} = \tau_c \cdot b d \rightarrow 0.774$$

$$= 0.774 \times 200 \times 400$$

$$\rightarrow 16920 \text{ N} / 61920 \text{ N}$$

$$\boxed{V_{uc} = 61.92 \text{ kN}}$$

$$V_{us} = V_u - V_{uc}$$

$$= 75.33 - 61.92$$

$$= 13.41 \text{ kN}$$

$$\boxed{V_{us} = 13.41 \text{ kN}}$$

(iii) Design of vertical stirrups,

Spacing of 2-legged comn stirrups.

$$A_{sv} = \frac{2 \times \pi}{4} (10)^2$$

$$= 157.08 \text{ mm}^2$$

Spacing of stirrups:

$$1. 0.75d \Rightarrow 0.75 \times 400$$

$$= 300.0 \text{ mm}$$

2. 300mm which ever is less.

3. For vertical stirrups,

$$V_{us} = \frac{0.87 f_y A_{sv} d}{S_V}$$

$$S_V = \frac{0.87 \times 415 \times 157.08 \times 400}{V_{us}}$$

$$= \frac{0.87 \times 415 \times 157.08 \times 400}{13.41}$$

$$= 1691.57 \times 10^3 \text{ mm}$$

$$= 1691.57 \text{ mm} \approx 1700 \text{ mm}$$

from Code book pg: 48

8.6.5.4.6 - Minimum shear reinforcement.

$$\frac{A_{sv}}{b s_V} \geq \frac{0.4}{0.87 f_y}$$

$$A_{sv} = \frac{2 \times \pi}{4} (10)^2$$

$$= 157.07 \text{ mm}^2$$

Spacing of stirrups:

$$1. 0.75d \Rightarrow 0.75 \times 400$$

$$= 300.0 \text{ mm}$$

2. 300mm which every is less

3. For Vertical stirrups,

$$V_{us} = \frac{0.87 f_y A_{sv} d}{S_V}$$

$$S_V = \frac{0.87 \times 415 \times 157.07 \times 400}{V_{us}}$$

$$= \frac{0.87 \times 415 \times 157.07 \times 400}{13.41}$$

$$= 1691.57 \times 10^3 \text{ mm}$$

$$= 1691.57 \text{ mm} \approx 1700 \text{ mm}$$

from Code book pg: 208

26.5.5.6 - Minimum shear reinforcement.

$$\frac{A_{sv}}{b s_V} \geq \frac{0.4}{0.87 f_y}$$

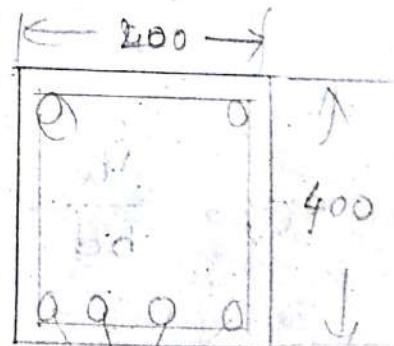
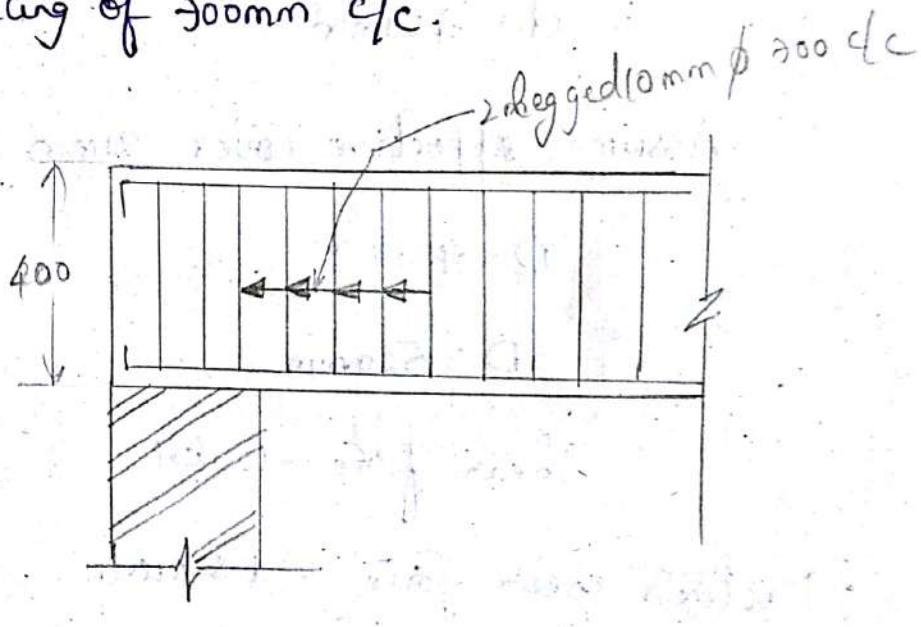
$$S_v = \frac{0.87 f_y A_{sv}}{0.4 \times b}$$

$$\Rightarrow \frac{0.87 \times 415 \times 152.07}{0.4 \times 200}$$

$$= 708.88 \text{ mm} \approx 700 \text{ mm}$$

$$S_v = 700 \text{ mm}$$

Hence provide 2-legged - 10mm ϕ stirrups with a spacing of 700mm c/c.



4- 12φ

12. A R.C.C beam has an effective depth 450mm & breadth of 300mm it contains of 20mm ϕ bars. Mild steel out of which 2 bars are curtailed at a section where force is 100kN at service load. Design reinforcement if the concrete is M₂₀

Ex

Given data,

$$b = 300\text{mm}$$

$$d = 450\text{mm}$$

Assume effective Cover = 50mm

$$D = 450 + 50$$

$$D = 500\text{mm}$$

Shear force = 100kN

Factored shear force = 1.5×100

$$V_u = 150\text{kN}$$

$$\tau_v = \frac{V_u}{bd} = \frac{150 \times 10^3}{300 \times 450} = 1.11 \text{N/mm}^2$$

$$A_{st} = 3 \times \frac{\pi}{4} (20)^2 \rightarrow 1570.8 \text{mm}^2 \text{ or } 942.4 \text{mm}^2$$

$$\% \text{ of steel} = \frac{942.47}{300 \times 450} \times 100 \\ = 0.698\%$$

$$0.50 \rightarrow 0.48 \\ 0.75 \rightarrow 0.56$$

from table no: 19

$$0.698 \rightarrow ?$$

$$\tau_c = 0.48 + \left(\frac{0.56 - 0.48}{0.75 - 0.50} \right) (0.698 - 0.50)$$

$$\tau_c = 0.543 \text{ N/mm}^2$$

$$\tau_{\max} = 2.8 \text{ N/mm}^2$$

$$\boxed{\tau_v > \tau_c}$$

Shear reinforcement has to be designed.

(ii) Design of shear reinforcement:

$$V_{uc} = \tau_c \times b \times d \Rightarrow 0.543 \times 300 \times 450$$

$$V_{uc} = 73305 \text{ kN}$$

$$\boxed{V_{uc} = 73.305 \text{ kN}}$$

$$V_{us} = V_u - V_{uc}$$

$$= 150 - 73.305$$

$$\boxed{V_{us} = 76.695 \text{ kN}}$$

(iii) Design of Vertical stirrups:

spacing of 2-legged 8mm stirrups,

$$A_{sv} = 2 \times \frac{\pi}{4} (8)^2 \Rightarrow 100.53 \text{ mm}^2$$

Spacing of stirrups:

(i) $0.75 \times d \Rightarrow 0.75 \times 400 = 337.5 \text{ mm}$

(ii) 300mm which ever is less

(iii) for vertical stirrups;

$$V_{us} = \frac{0.87 f_y A_{sv} \cdot d}{S_v}$$

$$S_v = \frac{0.87 f_y A_{sv} \cdot d}{V_{us}}$$

$$\geq \frac{0.87 \times 250 \times 100.53 \times 400}{76.695}$$

$$\Rightarrow 128.29 \times 10^3 \text{ mm}$$

$$S_v = 128.29 \text{ mm}$$

$$S_v = 130 \text{ mm}$$

from Code book pg: 48

26.5.1.6 - Min. shear reinforcement

$$\frac{A_{sv}}{bsv} \geq \frac{0.4}{0.87 f_y}$$

$$\frac{A_{sv}}{b \times s_v} = \frac{0.4}{0.87 f_y}$$

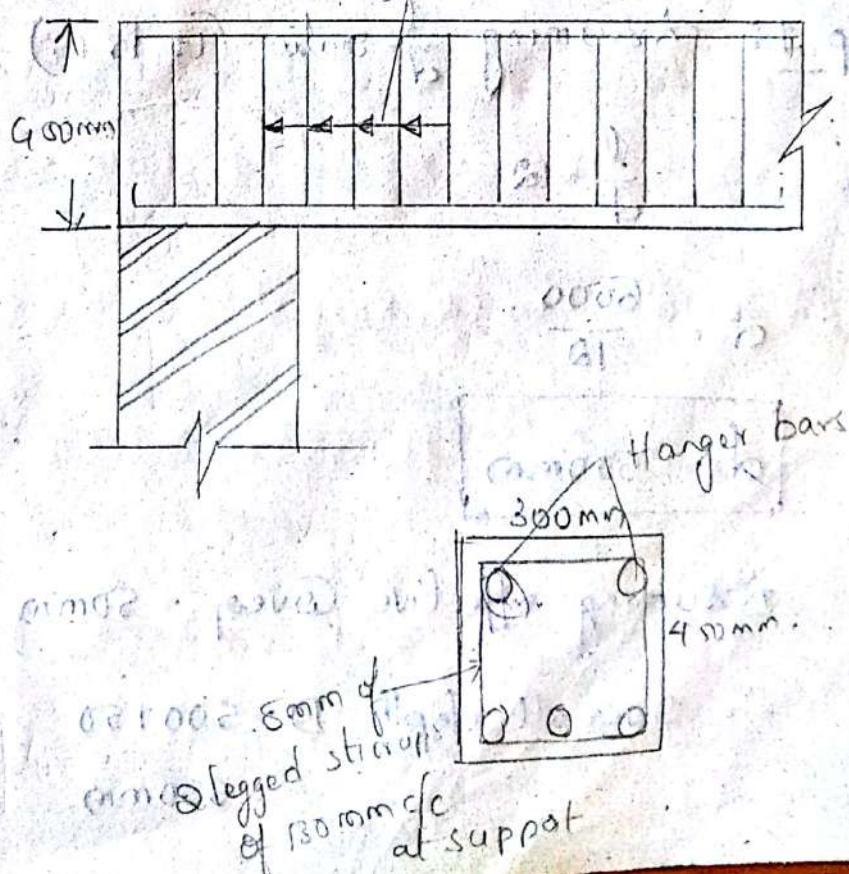
$$s_v = \frac{0.87 f_y \cdot A_{sv}}{0.4 \times b}$$

$$= \frac{0.87 \times 250 \times 100.53}{0.4 \times 300}$$

$$s_v = 182.21 \text{ mm}$$

Provide 8mm ϕ of 2-legged stirrups with
of spacing of 130mm.

2-8mm ϕ 130 c/c



26/7/17
13. A rectangular concrete beam is S.S on two masonry walls 230mm thick, 6m apart (Centre Centre) the beam is carrying an imposed load 15kn/m. Design the beam with all necessary checks. Use M₂₅ Concrete & Fe 415 steel. sketch the details of reinforcement

sol

Given data,

$$b = 230\text{mm}$$

$$\text{imposed load} = 15\text{kn/m}$$

$$f_y = 415\text{N/mm}^2$$

$$f_{ck} = 25\text{N/mm}^2$$

$$l = 6\text{m} \quad (\text{Centre to Centre})$$

Step 1: Assuming $\frac{l}{d}$ ratio (10 to 15)

$$\frac{l}{d} = 12$$

$$d = \frac{6000}{12}$$

$$d = 500\text{mm}$$

Assuming effective Cover = 50mm

$$\therefore \text{Overall depth } D = 500 + 50 \\ = 550\text{mm}$$

(ii) Effective span $l = 6000\text{mm}$

(iii) Calculation of loads & BM

$$\text{Self wt} = 0.23 \times 0.55 \times 1 \times 85 \\ = 3.1625 \text{ kN/m}$$

Imposed load = 15 kN/m

Total load = 15 + 3.1625

$$= 18.1625 \text{ kN/m}$$

$$BM = \frac{\omega d^2}{8} \rightarrow \frac{18.1625 \times 6^2}{8}$$

$$BM = 81.73 \text{ kN/m}$$

factored bending moment,

$$M_u = 1.5 \times BM$$

$$= 1.5 \times 81.73$$

$$M_u = 122.6 \text{ kN/m}$$

Step 4:- Depth required,

$$M_u = M_{ulimit}$$

for $f_{ck} 415$ steel, $M_{ulimit} = 0.138 f_{ck} b d^2$

$$d = \sqrt{\frac{M_{ulimit}}{0.138 f_{ck} \cdot b}} = \sqrt{\frac{122.6 \times 10^6}{0.138 \times 415 \times 230}}$$

$$d = 393.07 \text{ mm} \approx 400 \text{ mm} < 500 \text{ mm}$$

Hence provided depth is adequate.

$$M_{\text{allow}} = 0.138 \cdot f_{ck} \cdot b \cdot d^2$$

$$= 0.138 \times 25 \times 230 \times 500^2$$

$$= 198.37 \text{ kN-m}$$

$$M_u < M_{\text{allow}}$$

\therefore So, the section is singly reinforced.

Step 5:- Area of reinforcement,

$$M_a > 0.87 \cdot f_y \cdot A_{st} \cdot d \left[1 - \frac{f_y \cdot A_{st}}{f_{ck} \cdot b \cdot d} \right]$$

$$122.6 \times 10^6 > 0.87 \times 415 \times A_{st} \times 500 \left[1 - \frac{415 A_{st}}{25 \times 230 \times 500} \right]$$

$$122.6 \times 10^6 = 180.525 \times 10^3 A_{st} \left[1 - 1.443 \times 10^{-9} A_{st} \right]$$

$$122.6 \times 10^6 = 180.525 \times 10^3 A_{st} - 26.058 A_{st}^2$$

$$26.058 A_{st}^2 - 180.525 \times 10^3 A_{st} + 122.6 \times 10^6 = 0$$

$$A_{st} = 763.2 \text{ mm}^2$$

Provide 16mm φ for finding no. of bars

$$A_{st} = \text{No. of bars} \times \frac{\pi}{4} (16)^2$$

$$763.21 = 118.09 \text{ No. of bars}$$

$$118.09 \text{ No. of bars} = 763.21$$

18
16
20

$$\text{No. of bars} = 3.79 \approx 4 \text{ bars}$$

$$\therefore \text{No. of bars} = 4$$

$$A_{st} \text{ required} = 763.21 \text{ mm}^2$$

$$A_{st} \text{ provided} = 4 \times \frac{\pi}{4} (16)^2$$

$$\approx 804.24 \text{ mm}^2$$

Min. Reinforcement:

$$\rightarrow \frac{A_{st \min}}{bd} = \frac{0.85}{f_y}$$

$$A_{st \min} = \frac{0.85 bd}{f_y}$$

$$= \frac{0.85 \times 230 \times 500}{215}$$

$$\therefore A_{st \min} = 235.5 \text{ mm}^2$$

Max. Reinforcement:

$$A_{st \max} = 0.04 \times bD$$

$$= 0.04 \times 230 \times 550$$

, 5060

$$A_{st\ max} = 5060 \text{ mm}^2$$

Step 5:- check for deflection (stiffness)

~~For S.S beam basic value~~ ($\frac{l}{320}$)

$$\& \tau_v < \tau_{c\ max}$$

$$\tau_v < \tau_c - \text{min. reinforcement}$$

$\tau_v > \tau_c \& \tau_v < \tau_{c\ max}$ - design design
shear reinforcement

$\tau_v > \tau_c \& \tau_v > \tau_{c\ max}$ - redesign
beam.

Step 6:- check for shear reinforcement

$$\tau_v = \frac{V_u}{bd} \Rightarrow \frac{81.73}{230 \times 550} \rightarrow 7.106 \times 10^{-3}$$

$$\tau_v = 7.106 \times 10^{-3} \text{ N/mm}^2$$

$$\boxed{\tau_{c\ max} = 3.1 \text{ N/mm}^2}$$

$$\% \text{ of steel} = \frac{A_{st}}{bd} \times 100$$

$$= \frac{804.24}{230 \times 500} \times 100$$

$$\therefore 0.699$$

from Code book table no:19, τ_c value

for 0.699

$$0.50 - 0.49$$

$$0.75 - 0.52$$

$$0.699 - ?$$

$$\tau_c = 0.49 + \left(\frac{0.52 - 0.49}{0.75 - 0.50} \right) (0.699 - 0.50)$$

$$\therefore 0.55$$

$$\tau_c = 0.55 \text{ N/mm}^2$$

$$\tau_{c\max} = 3.1 \text{ N/mm}^2$$

from table no:20

$$\tau_c \leq \tau_{c\max}$$

$\tau_v > \tau_c$ & $\tau_v < \tau_{c\max} \rightarrow$ So design
design shear reinforcement.

Design of shear reinforcement:

Hence provided 6mm ϕ of 2 legged stirrups 220 mm c/c.

Check for deflection:-

for s.s beam basic value ($\frac{l}{d} = 20$)

In Code book, pg. no - 38.

modification factor for tension reinforcement

$$f_s = 0.58 f_y \times \frac{\text{Area of c/s of Ast required}}{\text{Area of c/s of Ast provided}}$$

$$\Rightarrow 0.58 \times 455 \times \frac{763.21}{804.24}$$

$$f_s = 228.42 \text{ N/mm}^2$$

$$\% \text{ of steel} = \frac{\text{Ast provided}}{bd} \times 100$$

$$\Rightarrow \frac{804.24}{230 \times 500} \times 100$$

$$= 0.699\%$$

from fig. 4 of IS:456, modification

$$\text{factor} = 1.2$$

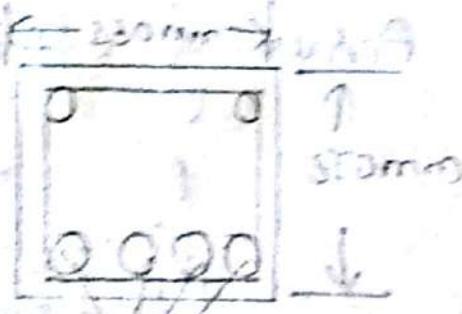
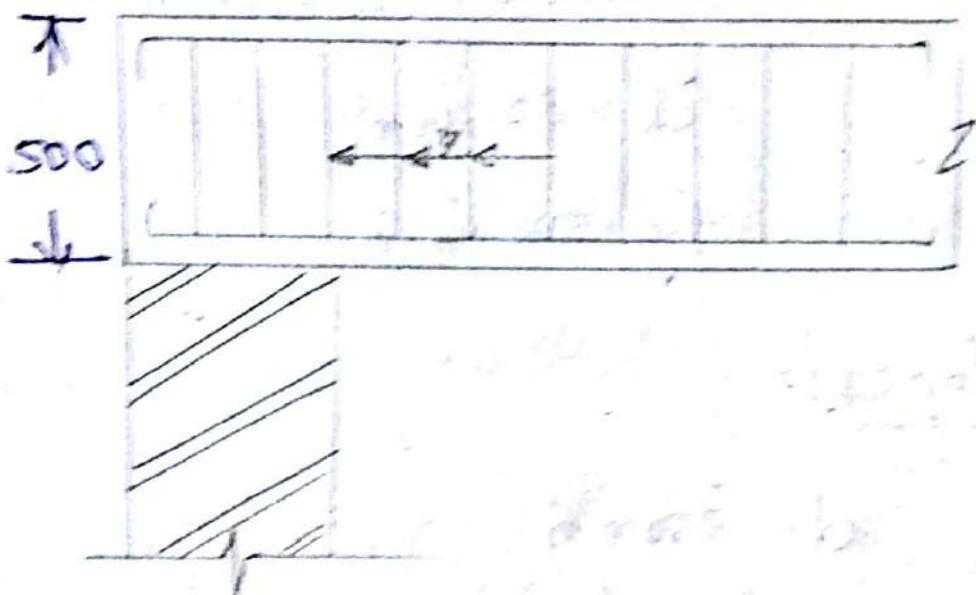
Max. permitted $\frac{l}{d}$ ratio = $\frac{1.2}{0.02} = 60$

$$\frac{l}{d} \text{ provided} = \frac{6000}{500}$$

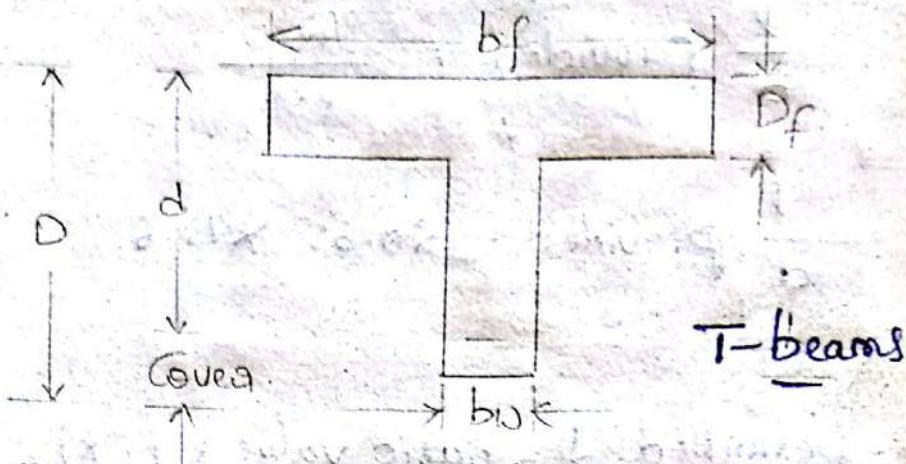
$$\frac{l}{d} \text{ provided} = 12 < 60$$

∴ Hence deflection control is safe.

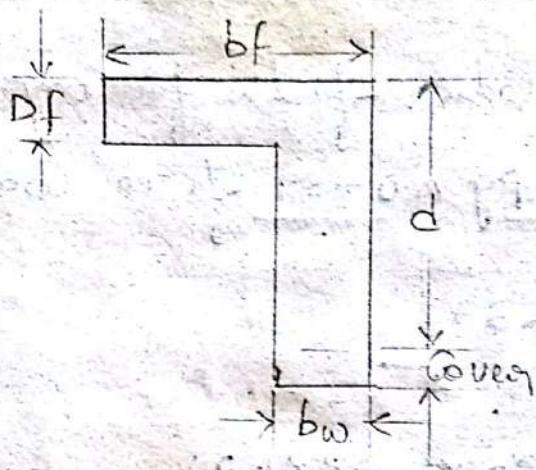
6mm ϕ 2-legged @ 220 qc



T-Beams:



T-beams



L-beams

F8. T-beams:

$$b_f = \frac{l_0}{6} + b_w + 6D_f$$

F9. L-beams:

$$b_f = \frac{l_0}{12} + b_w + 3D_f$$

→ When the slab occurs on both the sides of the beam (intermediate beams), the beam is known as T-beam.

→ When the slab is only on one side of the beam (end beams), the beam is known as "L-beam"

Advantages of T-beams

1. As the slab being monolithic with the beam is also compressed & shares the compressive force with the beam, which significantly increases the moment of resistance of the beam.
2. As most of the compressive force is shared by the flange, the depth of the beam required is less and hence the maximum deflections are also less.

For isolated beams, the effective width shall be obtained as given below but in no case greater than the actual width (b)

$$\text{For T-beams } b_f = \frac{l_0}{\left(\frac{l_0}{b} + 4\right)} + b_w$$

$$\text{For L-beams } b_f = \frac{0.5 l_0}{\left(\frac{l_0}{b} + 4\right)} + b_w$$

Where,

b_f = effective width of flange

l_0 = distance b/w points of zero moment
in the beam.

$b_{w\bar{b}}$ = breadth of web.

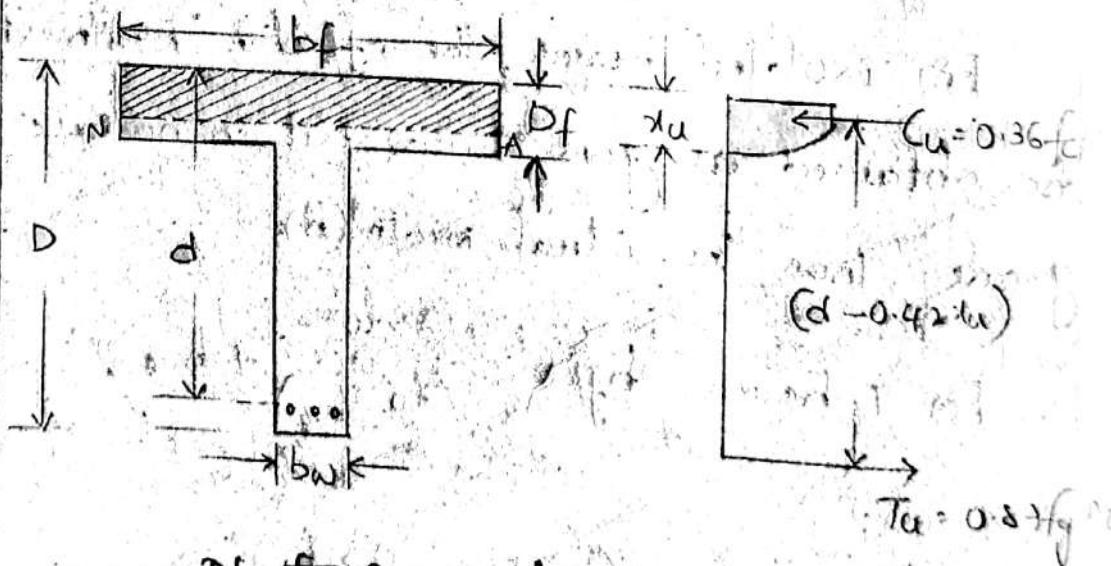
D_f = thickness of flange.

b = Actual width of the flange.

x_1, x_2 = half the clear distance b/w two
adjacent beams.

Analysis of T-beams:-

Case 1: Neutral axis is with in the flange
 $(x_u \leq D_f)$



Neutral axis lying inside the
flange.

When the NA falls with in the flange as
shown, the T-beam can be treated as a normal

rectangular beam of width b & depth d . The moment of resistance of the section can be calculated by the same procedure as that of rectangular section of width b & depth d :

$$C = 0.36 f_{ck} \cdot b_f \cdot x_u$$

$$T = 0.87 f_y \cdot A_{st}$$

1. Depth of Neutral axis

$$C = T$$

$$0.36 f_{ck} \cdot b_f \cdot x_u = 0.87 f_y \cdot A_{st}$$

$$x_u = \frac{0.87 f_y \cdot A_{st}}{0.36 f_{ck} \cdot b_f}$$

2. Moment of resistance:

$$M_u = 0.36 f_{ck} b_f \cdot x_u (d - 0.42 x_u) - \text{Concrete}$$

$$M_u = 0.87 f_y \cdot A_{st} (d - 0.42 x_u) - \text{Steel}$$

Case II: Neutral axis is below the flange ($x_u > D_f$)

i.e., in the web and $D_f/d \leq 0.2$

10. Find the moment of resistance of T-beam.

Section having $b_w = 300$, $b_f = 1650\text{mm}$, $D_f = 150\text{mm}$, $d = 550\text{mm}$. The open face consists of 6 bars of $20\text{mm} \times 20\text{mm}$. Use M₂₀ Concrete & Fe 415 Steel.

Given

Given data,

$$b_w = 300\text{mm}$$

$$b_f = 1650\text{mm}$$

$$D_f = 150\text{mm}$$

$$d = 550\text{mm}$$

$$\text{No. of bars} = 6$$

$$\text{Dia.} = 20\text{mm}$$

$$f_{ck} = 20\text{N/mm}^2$$

$$f_y = 415\text{N/mm}^2$$

$$A_{st} \rightarrow \frac{\pi}{4} \times (20)^2 \times 6 = 1884.9\text{mm}^2$$

Step 1:-

Assuming depth of N.A. is in the flange

$$x_a = \frac{0.87 f_y A_{st}}{0.36 f_{ck} b_f}$$

$$= \frac{0.87 \times 415 \times 1884.9}{0.36 \times 20 \times 1650}$$

$$x_u = 57.28 \text{ mm} \leq D_f$$

$$x_{u,\max} = 0.44d \Rightarrow 0.44 \times 550 \\ = 264 \text{ mm}$$

$$x_u < x_{u,\max}$$

So, the beam is under-reinforced section.

Moment of resistance:

$$M_u = 0.87 f_y A_{st} (d - 0.42 x_u)$$

$$= 0.87 \times 415 \times 1884.9 (550 - 0.42(57.28)) \\ \rightarrow 357.92 \times 10^6 \text{ N-mm}$$

$$M_u = 357.92 \text{ kNm}$$

2/8/13

- Q. Find the moment of resistance of a T-beam having $b_w = 300\text{mm}$, $b_f = 165\text{mm}$, $D_f = 120\text{mm}$, $d = 510\text{mm}$. The reinforcement consists of 4 bars of $25\text{mm } \phi$. use M₂₀ Concrete & Fe 415 steel.

Ex

Given data,

$$b_w = 300\text{mm}$$

$$b_f = 165\text{mm}$$

$$D_f = 120 \text{ mm}$$

$$d = 510 \text{ mm}$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

$$A_{st} = \frac{\pi}{4} (25)^2 \rightarrow 1963.49 \text{ mm}^2$$

Step 1:

Assuming depth of N.A is in the flange

$$\chi_u = \frac{0.87 f_y \cdot A_{st}}{0.36 f_{ck} \cdot B_f}$$

$$= \frac{0.87 \times 415 \times 1963.49}{0.36 \times 20 \times 1650}$$

$$\boxed{\chi_u = 59.67 \text{ mm}} \leq D_f$$

$$\chi_{u\max} = 0.48 d \Rightarrow 0.48(510)$$

$$= 244.8 \text{ mm}$$

$$\boxed{\chi_u < \chi_{u\max}}$$

So, the beam is under reinforced section.

Moment of resistance:

$$M_u = 0.87 f_y \cdot A_{st} (d - 0.42 x_u)$$

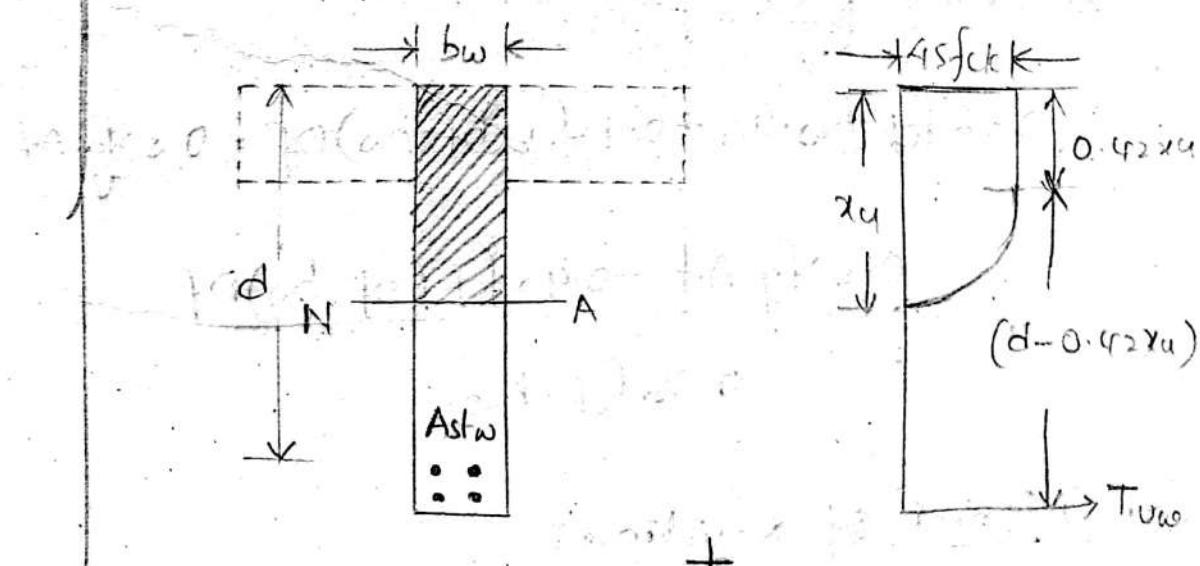
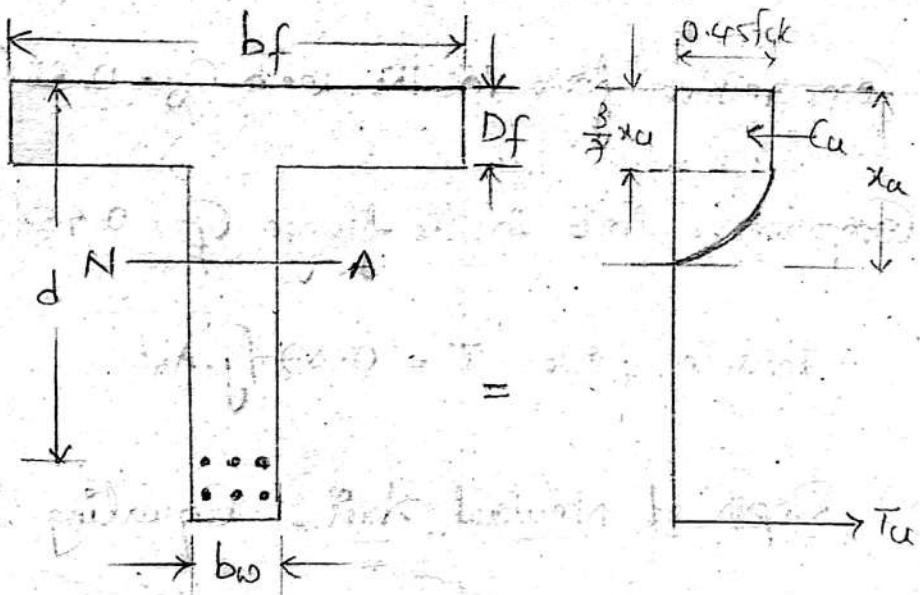
$$= 0.87 \times 415 \times 1963.49 (510 - (0.42 \times 59.6))$$

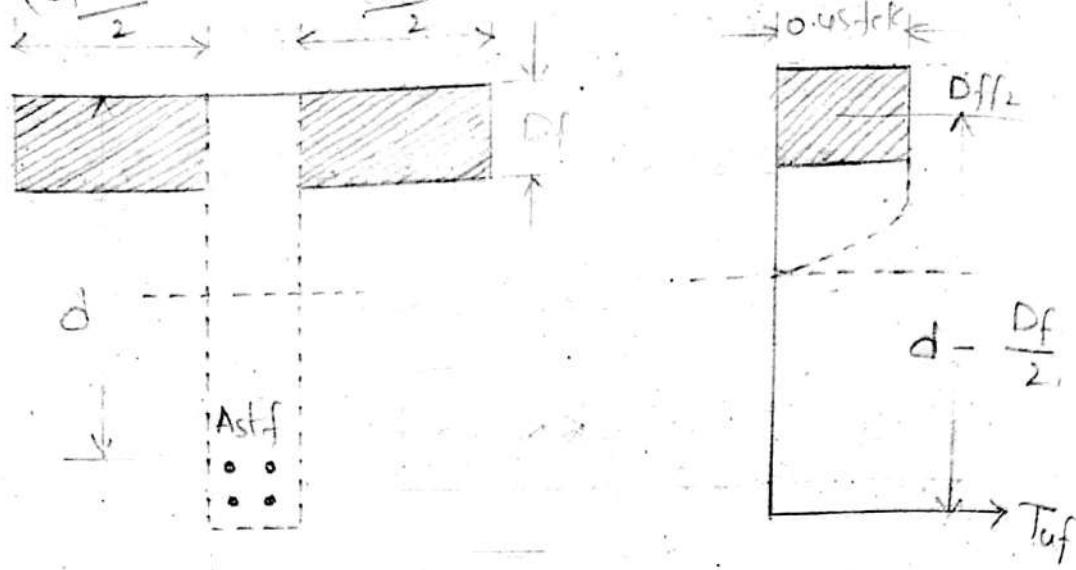
$$= 343.78 \times 10^6 \text{ N-mm}$$

$$\boxed{M_u = 343.78 \text{ kN-m}}$$

Case 2: Neutral Axis is below the flange

($x_u > D_f$) i.e., in the web & $D_f/d \leq 0.2$





Neutral Axis is below the flange if

$$\frac{Df}{d} \leq 2$$

Compressive force in the web $C_w = 0.36 f_{ck} \cdot b_w \cdot x_u$

Compressive force in the flange $C_f = 0.45 f_{ck} (b_f - b_w)$

$$\text{Tensile force } T = 0.87 f_y \cdot A_{st}$$

(a). Depth of Neutral Axis: Equating compression & tension force.

$$0.36 f_{ck} \cdot b_w \cdot x_u + 0.45 f_{ck} (b_f - b_w) D_f = 0.87 f_y \cdot A_{st}$$

$$x_a = \frac{0.87 f_y \cdot A_{st} - 0.45 f_{ck} (b_f - b_w) D_f}{0.36 f_{ck} \cdot b_w}$$

(b). Moment of Resistance

$$M_u = M_{u,\text{web}} + M_{u,\text{flange}}$$

$$M_u = C_w(d - 0.42x_u) + C_f\left(d - \frac{D_f}{2}\right)$$

Substituting the values of C_w & C_f

$$M_u = 0.36 f_{ck} \cdot b_w \cdot x_u (d - 0.42x_u) + 0.45 f_{ck} (b_f - b_w) D_f \left[d - \frac{D_f}{2}\right]$$

3. Calculate the moment of resistance of the T-beam with the following data.

Width of the flange = 800mm = b_f

Thickness of slab = 160mm = D_f

Width of rib = 300mm = b_w

Effective depth = 600mm = d

Area of tension steel = 2800mm² = A_{st}

Characteristic strength of concrete = 20N/mm² = f_{ck}

Characteristic strength of steel = 415N/mm² = f_y

Step 1: Assuming x_u is within in the flange:

$$x_u = \frac{0.87 f_y \cdot A_{st}}{0.36 f_{ck} \cdot b_f}$$

$$\Rightarrow \frac{0.87 \times 415 \times 2800}{0.36 \times 20 \times 800}$$

$$x_u = 156.7 \text{ mm} > D_f$$

∴ Our assumption is wrong. So, the N.A lies in the web.

$$\frac{D_f}{d} = \frac{110}{600} = 0.18 < 0.2$$

So, it is Case - 2

Step 2:

Actual depth of N.A

$$x_a = \frac{0.87 f_y A_{st} - 0.45 f_{ck} (b_f - b_w) D_f}{0.36 f_{ck} b_w}$$

$$= \frac{0.87 \times 415 \times 2000 - 0.45 \times 20 (800 - 300) 110}{0.36 \times 20 \times 300}$$

$$\boxed{x_a = 188.72 \text{ mm}}$$

$$x_{u\max} = 0.48 d$$

$$= 0.48 \times 600$$

$$= 288$$

$$\boxed{x_a < x_{u\max}}$$

∴ The section is under overficed section.

3. step : Moment of resistance:

$$M_u = 0.36 f_{ck} \cdot b_w \cdot x_u (d - 0.42 x_u) + 0.45 f_{ck} (b_f - b_w) b_f \\ \left(d - \frac{D_f}{2} \right)$$

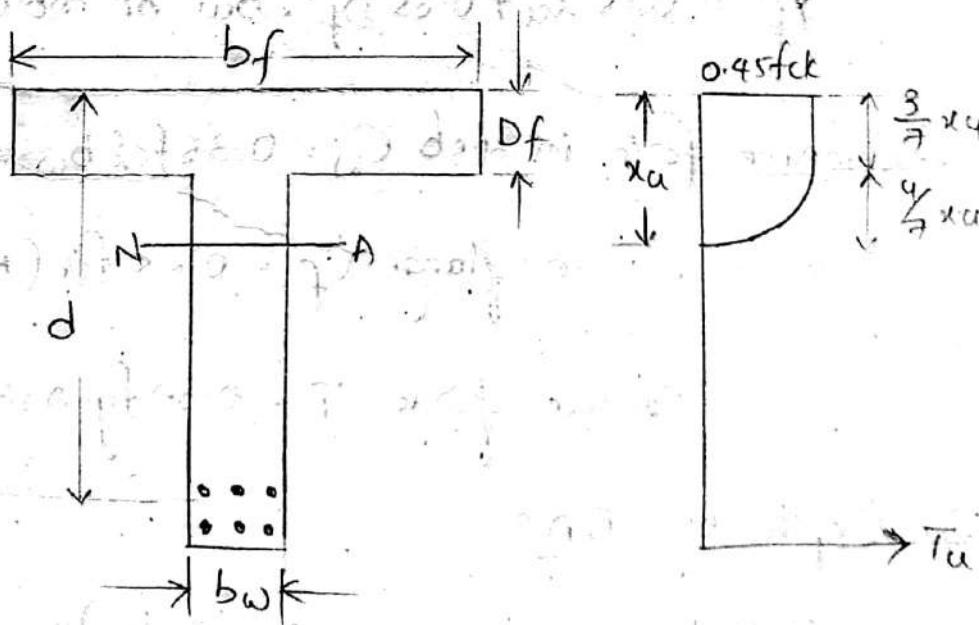
$$\Rightarrow 0.36 \times 20 \times 300 \times (88.72) \left(600 - (0.42 \times 188.72) \right) \\ + 0.45 \times 20 \left(800 - 300 \right) 110 \times \left(600 - \frac{110}{2} \right)$$

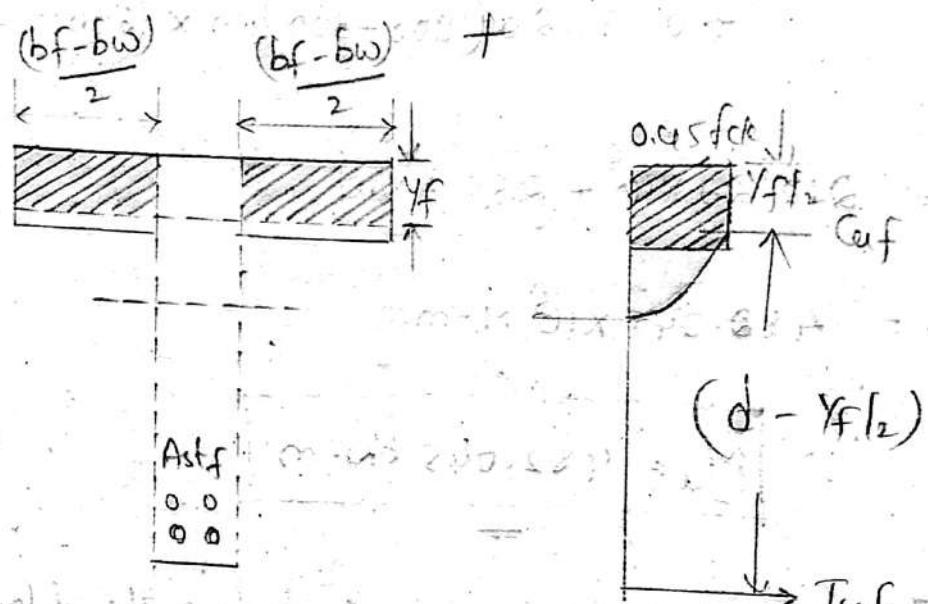
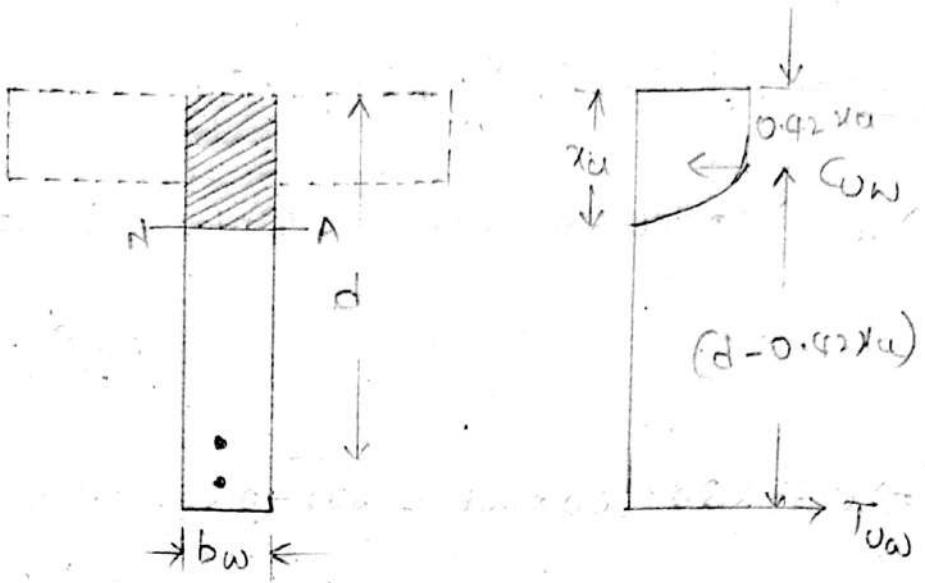
$$\Rightarrow 212.27 \times 10^6 + 269.7 \times 10^6 \\ = 482.045 \times 10^6 \text{ N-mm}$$

$$\therefore M_u = 482.045 \text{ kNm}$$

Case III: Neutral axis is below the flange

($x_u > D_f$) i.e., in the web & $D_f/d > 0.2$





Modified thickness of flange = y_f

$$y_f = 0.65 x_u + 0.65 D_f, \text{ but not more than } D_f$$

Comparative force in web $C_W = 0.36 f_{ck} b_w \cdot x_u$

" " in flange $C_f = 0.45 f_{ck} (b_f - b_w) y_f$

Tensile force $T = 0.8 f_y A_{st}$

(a) Depth of N.A:

$$0.36 f_{ck} \cdot b_w \cdot x_u + 0.45 f_{ck} (b_f - b_w) y_f = 0.8 f_y A_{st}$$

$$x_u = \frac{0.87 f_y A_{st} - 0.45 f_{ck} (b_f - b_w) y_f}{0.36 f_{ck} b_w}$$

(b) Moment of resistance:

$$M_u = c_w (d - 0.42 x_u) + c_f \left(d - \frac{y_f}{2} \right)$$

$$M_u = 0.36 f_{ck} \cdot b_w \cdot x_u (d - 0.42 x_u) + 0.45 f_{ck} (b_f - b_w) y_f \left(d - \frac{y_f}{2} \right)$$

Footings.

Types of footings:-

1. Isolated footing
2. Combined footing.
3. Strip footing.
4. Raft or mat footing

Design procedure:-

1. Size of the footings:

Area of the footing required,

$$A = \frac{1.1P}{SBC \text{ of soil}}$$

where P = working load

SBC = Safe bearing capacity.

2. Determine the uprooted soil reaction for the factored load:

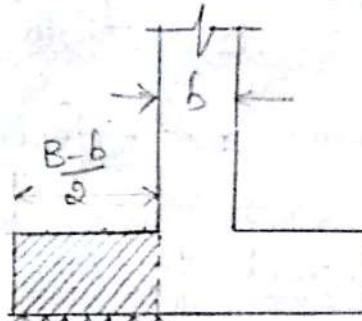
$$q_u = \frac{P_u}{A}$$

$$= \frac{1.5P}{A}$$

3. Determine the min. depth required to resist bending moment:

Projection of the footing

$$= \frac{(B-b)}{2}$$



The B.M about x-x is (as a cantilever slab, $\frac{q_u l^2}{2}$)

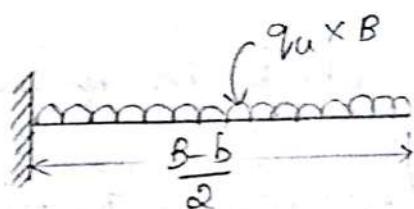
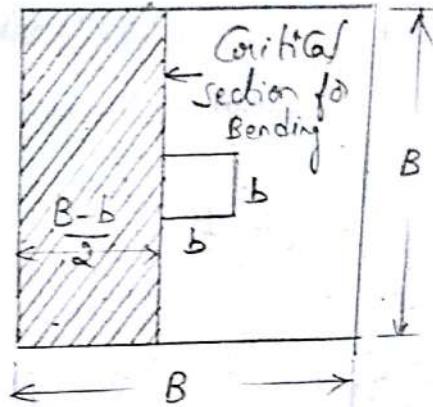
$$M_u = \frac{q_u \cdot B \left(\frac{B-b}{2} \right)^2}{2}$$
$$= q_u \cdot \frac{B(B-b)^2}{8}$$

where q_u = upstand soil

pressure

B = width of footing,

b = width of column.



4. Determine the area of reinforcement required in width B using,

$$M_u = 0.87 \times f_y \times d \times A_{st} \left[1 - \frac{f_y \cdot A_{st}}{f_{ck} \cdot B \cdot d} \right]$$

using the bars of diameter not less than 10mm,
find the spacing of bars.

$$\text{Spacing} = \frac{B \cdot a_{st}}{A_{st}}$$

where, a_{st} = area of bar used

A_{st} = total area of steel required.

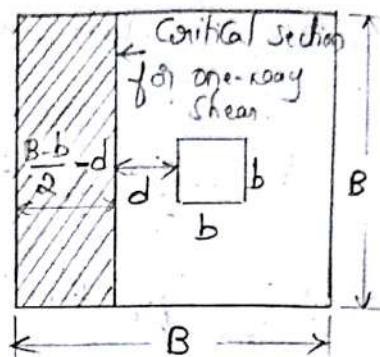
B = width of the footing

d = effective depth.

5. check for one way shear:

v_u = Soil pressure from the shaded area.

$$= q_u \cdot B \left[\frac{B-b}{2} - d \right]$$



$$\tau_v = \frac{v_u}{Bd} < \tau_c, \text{ permissible shear stress in Concrete.}$$

6. check for two way shear: (Punching shear).

Perimeter of the punching

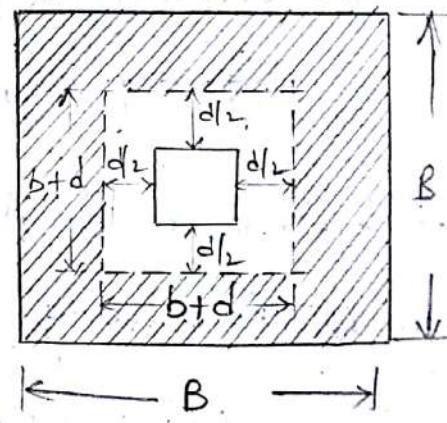
$$\text{area} = 4(b+d)$$

Area of Concrete resisting

Punching force = perimeter

of Punching x depth

$$A = 4(b+d)d$$



Force of punching $S = q_u \times \text{shaded Area}$

$$= q_u [B^2 - (B+d)^2]$$

Punching shear stress.

$$\tau_p = \frac{S}{A} < \text{permissible value.}$$

Permissible value of punching shear stress is,

$$\tau_p = 0.85 \sqrt{f_{ck}}$$

& check for Bond Length:

$$L_d = \frac{0.87 f_y \phi}{\tau_{bd}}$$

Design of staircase:

(1) Assuming $\frac{x}{y}$ ratio (20 to 25).

a. Effective span:

x	y	Span in m
< 1m	< 1m	$G_i + x + y$
< 1m	> 1m	$G_i + x + f$
> 1m	< 1m	$G_i + y + f$
> 1m	> 1m	$G_i + f + f$

3. Loads on stairs:

live load if crowded - 5 kN/m^2

if not - 3 kN/m^2

Dead load:

Thickness of riser slab = D

(a) weight of riser slab per unit horizontal

area,

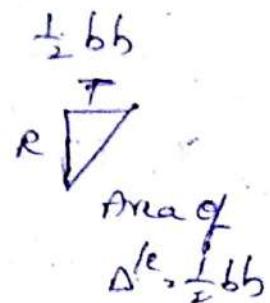
$$w_1 = \frac{D\sqrt{R^2 + T^2}}{T} \times 25$$

$$= D\sqrt{1 + \left(\frac{R}{T}\right)^2} \times 25$$

(b) no. of steps per unit horizontal Area,

$$\cdot \frac{\frac{1}{\alpha} \times R \times f \times 25}{8}$$

$$= \frac{1}{\alpha} R \times 25$$



where R is metre.

Finishing load (0.5 to 1 kN/m²) may be added to the above values.

Ques

4. Determine the max. bending moment,

$$M_u = \frac{w u l^2}{8}$$

5. Determine the min. depth required to resist the bending moment by equating,

$$M_u = M_{ulim} = k \cdot f_{ck} \cdot b d^2$$

$b = 1000\text{mm}$, $k = 0.138$ for Fe 415 steel & 0.148 for mild steel.

Provided depth should be more than this value.

Otherwise increase the depth.

6. Calculate the area of steel per metre width of slab by using,

6. Calculate

$$M_a = 0.87 f_y A_{st} d \left[1 - \frac{f_y A_{st}}{f_{ck} b d} \right]$$

7. Find the spacing of bars using,

$$S = \frac{1000 \times a_{st}}{A_{st}}$$

where,

a_{st} = area of bar used.

A_{st} = total area of steel required.

Spacing should not be more than 3d or 300mm
which ever is less.

8. providing distribution reinforcement proportional
to the span direction at 0.12% (for HRSB bars)
gross c/c area & find the spacing of these bars.
if mild steel bars are used, provide 0.15% of
gross area as distribution steel.

9. Design a doglegged staircase for a building in
which the height of floors is 3.3m. Adopt size
of flight of each step are 150mm & 225mm
respectively. The stair hall is 2.5m x 4.5m. Live
load may be taken as 3kN/m². use M20 grade
concrete & Fe 415 grade steel. Assume the stairs
are supported on 230mm walls at the ends of

Outer edges of landing slabs.

1. proportioning of stairs:

Dimensions of stair hall = $8.5m \times 4.5m$

height of the floor = $3.3m$

height of one flight = $\frac{3.3}{2} \Rightarrow 1.65m$
 $\Rightarrow 1650mm$

Rise, R = $150mm$

Tread, T = $225mm$

No. of steps = $\frac{\text{height of one flight}}{\text{Rise}}$

$$\Rightarrow \frac{1650}{150}$$

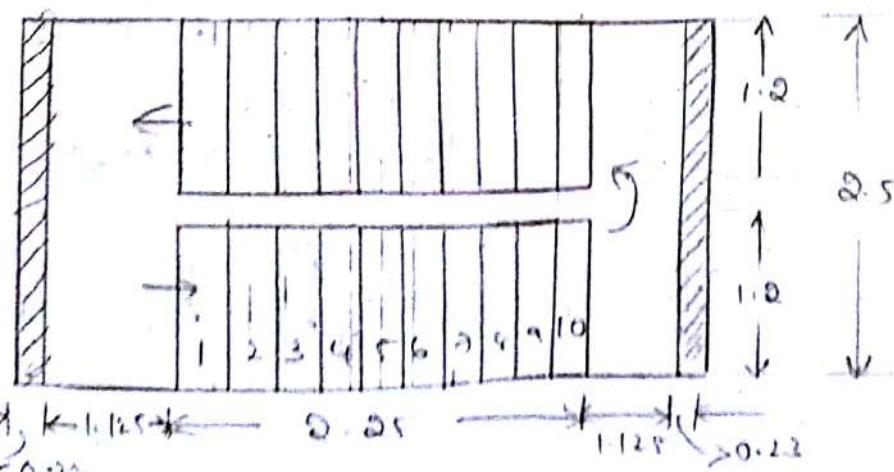
$$= 11$$

Hence, no. of treads = $11 - 1 \Rightarrow 10$

Adopt width of stair = $1.2m$

For 10 threads, the length required = 10×0.025
 $= 0.25m$

width of landing = $(\frac{4.5 - 0.25}{2}) \Rightarrow 1.125m$



2. Effective span:

As the stair slab is spanning longitudinally,

Effective span = Centre to centre distance of walls.

$$= 4.5 + 0.23$$

$$\boxed{l = 4.73 \text{ m}}$$

3. Thickness of slab:

Assume effective depths

$$d = \frac{\text{Span}}{25} \Rightarrow \frac{4730}{25} = 189.2 \text{ mm}$$

$$d = 190 \text{ mm}$$

$$D = 220 \text{ mm}$$

4. Loads: Loads per m² per horizontal width of stairs are as follows.

$$\text{wt. of waist slab} = D \sqrt{1 + \left(\frac{R}{T}\right)^2} \times 25$$

$$= 0.22 \sqrt{1 + \left(\frac{0.15}{0.225}\right)^2} \times 25$$

$$= 6.61 \text{ kN/m}^2$$

$$\text{wt. of steps} = \frac{\left(\frac{1}{2} RT\right)}{T} \times 25 \Rightarrow R \times \frac{25}{2}$$

$$\Rightarrow 0.15 \times \frac{25}{2}$$

$$\Rightarrow 1.875 \text{ kN/m}^2$$

live load $\Rightarrow 3 \text{ kN/m}^2$

Floor finish $\Rightarrow 0.6 \text{ kN/m}^2$

Total load $\Rightarrow 12.1 \text{ kN/m}^2$

Factored load $w_u = 1.5 \times 12.1$

$$\Rightarrow 18.15 \text{ kN/m}^2$$

5. Factored BM

$$M_u = \frac{w_u l^2}{8} \Rightarrow \frac{18.15 \times (4.73)^2}{8}$$

$$M_u = 50.76 \text{ kN-m}$$

$$= 50.76 \times 10^6 \text{ N-mm}$$

6. Min. depth required

$$M_u = 0.138 f_{ck} b d^2$$

$$50.76 \times 10^6 = 0.138 \times 20 \times 1000 \times d^2$$

$$d = \sqrt{\frac{50.76 \times 10^6}{0.138 \times 20 \times 1000}}$$

$$d = 135.6 \text{ mm} < 190 \text{ mm, provided depth}$$

Hence provided depth is adequate

7. Tension reinforcement:

$$M_u = 0.87 f_y A_{st} d \left[1 - \frac{f_y A_{st}}{f_{ck} b d} \right]$$

$$50.76 \times 10^6 = 0.87 \times 415 \times A_{st} \times 190 \left[1 - \frac{415 A_{st}}{80 \times 1000 \times 190} \right]$$

$$50.76 \times 10^6 = 68.6 \times 10^3 A_{st} - 7.49 A_{st}^2$$

$$7.49 A_{st}^2 - 68.6 \times 10^3 A_{st} + 50.76 \times 10^6 = 0$$

$$A_{st} = 812 \text{ mm}^2$$

using 12mm ϕ bars, spacing of bars,

$$S = \frac{A_{st}}{A_{st}} \times 1000$$

$$\Rightarrow \frac{\pi}{4} \times 12^2 \times \frac{1000}{812}$$

$$\Rightarrow 139.3 \text{ mm}$$

Provide 12mm bars @ 130mm c/c.

8. Distribution reinforcement:

$A_{st} = 0.12\%$ of gross area

$$\Rightarrow 0.12 \times 1000 \times \frac{220}{100}$$

$$A_{st} = 264 \text{ mm}^2$$

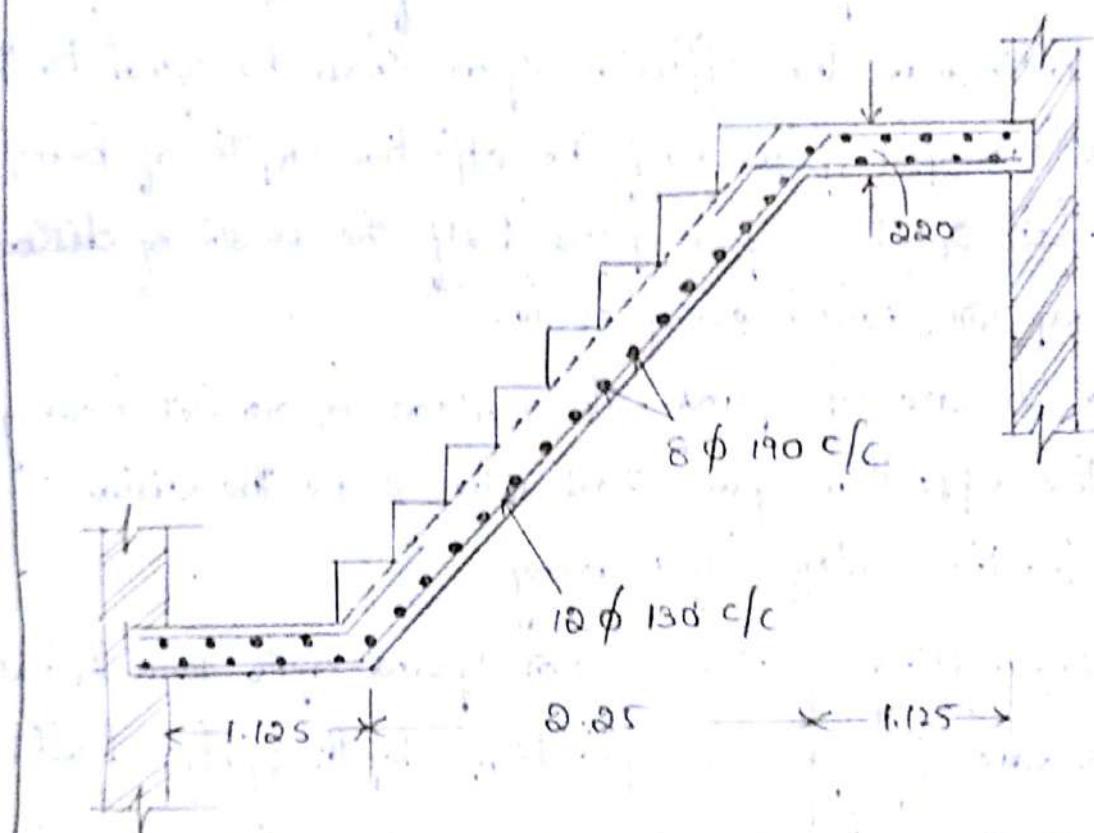
using 8mm bars, Spacing

$$S = \frac{\pi}{4} \times k^2 \times \frac{1000}{264}$$

$$\approx 190.4 \text{ mm}$$

Hence, provide 8mm bars @ 190 mm c/c

The details of reinforcement are shown in fig 4.21



19/9/17

Continuous Beams :-

- i) Effective span: if the width of the support is less than $\frac{1}{12}$ of clear span; The effective span shall be as per simply supported beam

(i) width of support < $\frac{1}{12}$ of clear span

(ii) width of support > $\frac{1}{12}$ of clear span (3) 600mm

which ever is less, the effective span shall be as follows.

- For end spans with one end free & the other continuous or for intermediate spans, the effective span shall be the clear span b/w the supports.
- For end spans with one end free & the other continuous, the effective span shall be equal to the clear span plus half the effective depth of beam/slab or clear span plus half the width of continuous support, which ever is less.
- In case of spans with rollers or rocket bearings, the effective span shall always be the distance b/w the centers of bearing.

2. Limiting stiffness: For spans upto 10m, the basic value of span to effective depth ratio should not exceed 26. Depending up on the area & type of tension steel the span to depth ratio may be multiplied by the modification factors.

In general, Continuous beams carry heavy load & consequently the span/depth ratio recommended in practical design is normally in between 15 to 20

22/9/17
3. Bending moments & shear forces of needs rigorous structural analysis to get the design

moments & shear forces. However IS: 456-2000 permits use of design coefficients shown in table 4.1 & 4.2 (Table 18 & 19 of IS: 456-2000) subjected to the following conditions:

- there are three or more spans.
- spans don't differ by 15% of the longest.
- loads are predominantly uniformly distributed loads.

4. Reinforcements

Same rules apply as for simply supported beams/slabs.

1. Mid span reinforcement
2. Support reinforcement.
3. Design a singly reinforced Continuous RC rectangular beam for flexure for the following conditions. use M20 grade Concrete & Fe 415 steel.

No. of spans = 3

Clear distance b/w supports = 3600mm

Width of the support = 300mm

Imposed load (not fixed) = 5 kN/m²

Imposed load (fixed) = 4.5 kN/m (excluding self wt).

Partial fixity may be expected at the discontinuous edge.

Given data,

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

$$b = 300 \text{ mm}$$

$$\text{width} = 300 \text{ mm}$$

$$\text{No. of spandrel} = 3$$

$$\text{Clear span } L = 3.6 \text{ m}$$

i. Depth of the beam:

Selecting the depth in range of $\frac{l}{15}$ to $\frac{l}{20}$ based on stiffness

Assume $\frac{l}{d}$ ratio as 15

$$\frac{l}{d} = 15$$

$$d = \frac{3600}{15}$$

$$= 240 \text{ mm}$$

Adopt $d = 250 \text{ mm}$

Assume effective Cover = 50 mm

$$D = 250 + 50$$

$$\boxed{D = 300 \text{ mm}}$$

ii. Effective Span:

$$(i) \text{ clear span} + d \Rightarrow 3.6 + 0.25 \\ = 3.85 \text{ m}$$

$$\begin{aligned}
 \text{(ii) clear span} &+ \frac{b}{2} + \frac{b}{2} \\
 &= 3.6 + \frac{0.43}{2} + \frac{0.43}{2} \\
 &= 3.85 \text{ m}
 \end{aligned}$$

Effective span $l = 3.85 \text{ m}$

3. Loads:-

$$\begin{aligned}
 \text{Self wt. of the beam} &= 0.3 \times 0.3 \times 1 \times 25 \\
 &= 2.25 \text{ kN/m}^2
 \end{aligned}$$

$$\text{Imposed load, fixed} = 7.5 \text{ kN/m}^2$$

$$\text{Total load fixed} = 9.75 \text{ kN/m}^2$$

$$\text{Imposed load, not fixed} = 5 \text{ kN/m}^2$$

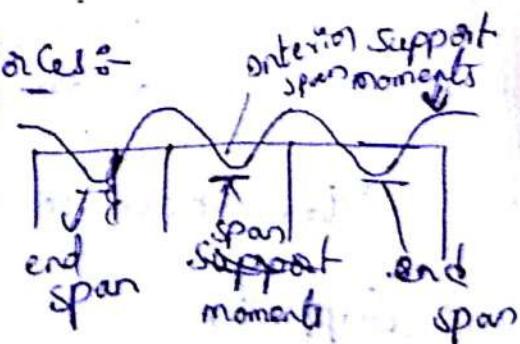
Factored loads:

$$\begin{aligned}
 \text{factored fixed load, } w_{ud} &= 1.5 \times 9.75 \\
 &= 14.63 \text{ kN/m}
 \end{aligned}$$

$$\begin{aligned}
 \text{not fixed wdl} &= 1.5 \times 5 \\
 &= 7.5 \text{ kN/m}
 \end{aligned}$$

4. Bending moments & shear forces:-

Span moments: (At the middle of end spans).



$$M_u = \left(\frac{1}{12}\right) \times 14.63 \times 3.85^2 + \left(\frac{1}{10}\right) \times 7.5 \times 3.85^2$$

$$= 18.07 + 10.61 \text{ kNm}$$

$$= 29.2 \text{ kNm}$$

At the middle of interior Span.

$$M_u = \left(\frac{1}{16}\right) \times 14.63 \times 3.85^2 + \left(\frac{1}{12}\right) \times 7.5 \times 3.85^2$$

$$= 13.55 + 9.26$$

$$= 22.81 \text{ kNm}$$

Support moments :- (At support next to the end Support).

Max. shear force at the end of beam.

$$M_u = \left(\frac{1}{10}\right) \times 14.63 \times 3.85^2 + \left(\frac{1}{9}\right) \times 7.5 \times 3.85^2$$

$$= 21.68 + 12.35$$

$$= 34.03 \text{ kNm}$$

At other interior Support,

$$M_u = \left(\frac{1}{12}\right) \times 14.63 \times 3.85^2 + \left(\frac{1}{9}\right) \times 7.5 \times 3.85^2$$

$$= 18.07 + 12.35$$

$$= 30.42 \text{ kNm}$$

Max. shear force at support next to the end Support,

$$V_{u,\max} = (0.6 \times 14.63 \times 3.85) + (0.6 \times 7.5 \times 3.85)$$

$$= 63.27 \text{ kN}$$

4. Depth required:-

$$M_u = 0.138 f_{ck} b d^2$$

$$34.03 \times 10^6 = 0.138 \times 20 \times 300 \times d^2$$

$$d = \sqrt{\frac{34.03 \times 10^6}{0.138 \times 20 \times 300}}$$

$$d = 202.72 < 250 \text{ mm}$$

Hence provided depth is adequate.

5. Reinforcement at supports:

$$M_u = 0.8 f_y A_{st} d \left[1 - \frac{f_y A_{st}}{f_{ck} b d} \right]$$

$$34.03 \times 10^6 = 0.8 \times 415 \times A_{st} \times 250 \left[1 - \frac{415 A_{st}}{20 \times 300 \times 250} \right]$$

$$34.03 \times 10^6 = 90.26 \times 10^3 A_{st} - 24.97 A_{st}^2$$

$$24.97 A_{st}^2 - 90.26 \times 10^3 A_{st} + 34.03 \times 10^6 = 0$$

$$A_{st} = 427.6 \text{ mm}^2$$

Provide, 12mm ϕ to finding no. of bars

$$\text{No. of bars} = \frac{A_{st}}{\frac{\pi}{4} (12)^2}$$

$$\frac{427.6}{\frac{\pi}{4} (12)^2}$$

$$\approx 3.78 \approx 4 \text{ bars}$$

Hence provide 4 bars of 18mm Ø

$$A_{st} \text{ provided} = 4 \times \frac{\pi}{4} (12)^2$$

$$\therefore = 452.4 \text{ mm}^2$$

6. Reinforcement at mid spans:-

$$M_u = 0.87 \cdot f_y \times A_{st} \times d \left[1 - \frac{f_y \cdot A_{st}}{f_{ck} \cdot b \cdot d} \right]$$

$$29.2 \times 10^6 = 0.87 \times 415 \times A_{st} \times 250 \left[1 - \frac{415 A_{st}}{20 \times 300 \times 250} \right]$$

$$29.2 \times 10^6 = 90.26 \times 10^3 - 24.97 A_{st}^2$$

$$24.97 A_{st}^2 - 90.26 \times 10^3 + 29.2 \times 10^6 = 0$$

$$A_{st} = 359.2 \text{ mm}^2$$

Assume 18mm Ø bars,

$$\text{No. of bars} = \frac{359.2}{\frac{\pi}{4} (12)^2} \Rightarrow 3.17 \approx 3 \text{ bars.}$$

Hence provide 3 bars of 18mm Ø,

$$A_{st} \text{ provided} = 3 \times \frac{\pi}{4} (12)^2$$

$$\therefore 339.3 \text{ mm}^2$$

7. Design of shear reinforcement:

$$T_v = \frac{V_u}{bd} = \frac{63.22 \times 10^3}{300 \times 250} = 0.84 \text{ N/mm}$$

$$\text{percentage of steel Pt} = \frac{\frac{O_t}{bd}}{100} \times 100$$

$$= \frac{628.3 \times 100}{300 \times 200} = 1.04\%$$

Referring to the table -19 of IS: 456, shear strength of concrete is

$$1.00 - 0.62$$

$$1.25 - 0.67$$

$$1.04 - ?$$

$$\tau_c = 0.67 + \left(\frac{0.67 - 0.62}{1.25 - 1.00} \right) (1.04 - 1.00) \rightarrow 0.67 \text{ N/mm}$$

max. shear stress in concrete τ_c max from table 20 of IS 456 (Page NO: 73)

$$\tau_{c \text{ max}} = 2.8 \text{ N/mm}^2$$

as $\tau_v > \tau_c$, shear reinforcement has to be designed

shear resistance of concrete $V_{ac} = \tau_c \cdot b d$

$$= 0.67 \times 300 \times 200$$

$$= 40200 \text{ N}$$

$$= 40.2 \text{ kN}$$

shear to be resisted by shear reinforcement

(vertical stirrups)

$$\begin{aligned} V_{as} &= V_u - V_{ac} \\ &= 49.15 - 40.2 \\ &= 8.95 \text{ kN} \end{aligned}$$

using 6mm, 2 legged Fe 415 steel

$$A_{sv} = 2 \times \frac{\pi}{4} (6)^2 \Rightarrow 56.55 \text{ mm}^2$$

$$\text{Spacing } S_v = \frac{0.87 f_y \cdot A_{sv} \cdot d}{V_{us}} \Rightarrow \frac{0.87 \times 415 \times 56.55 \times 35}{89.50}$$
$$= 456.25 \text{ mm}$$

max. allowed spacing $0.75d \Rightarrow 0.75 \times 200 \approx 150 \text{ mm}$,
a 300mm which even is less.

Hence, provide 2 legged 6mm stirrups @ 100 mm c/c

check for deflection: (Def. Stiffness)

$$\frac{l}{d} > 26 \text{ (for continuous)}$$

$$\% \text{ of steel} @ \text{mid span} = \frac{603.18 \times 100}{300 \times 200} = 1.00$$

$$f_s = 0.58 \times 415 \times \frac{456.25}{603.18} \Rightarrow 161.99 \text{ N/mm}^2$$

from fig. 4 of IS: 456

modification factor = 1.3

$$\text{max. permitted } \frac{l}{d} \text{ ratio} = 1.3 \times 26$$
$$= 33.8$$

$$\frac{l}{d} \text{ provided} = \frac{3800}{200}$$

$$= 19 < 33.8$$

∴ hence deflection control is safe.

=

Columns

Clause - 25

Limit state of collapse: compression.

Axial moment

Biaxial moment

Based on reinforcement

Tied column,

Spiral column.

Composite column.



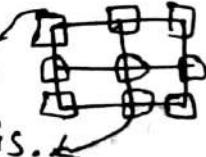
Based on the loading.

i) Axially loaded.

ii) Eccentrically loaded

 i) Ecc. " " in one axis.

 " " " " double axis.



iii) Based on slenderness ratio

 i) Short column.

$$\frac{l}{b} \leq 12.$$

 ii) long or slender column. $\rightarrow \frac{l}{b} > 12.$

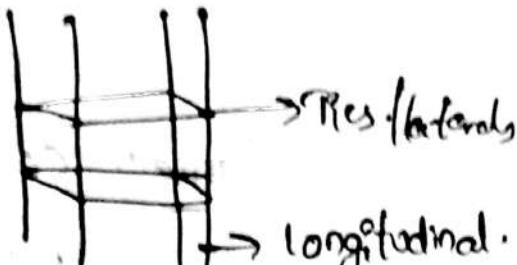
Columns

Form

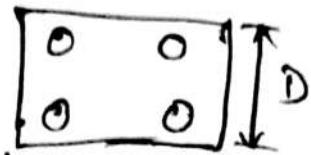
1) Circular

2) Rectangular

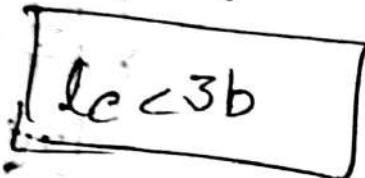
3) Square.



$$P = \frac{A_{st}}{bD} \times 100$$



$\therefore D = \text{gross area. (total)}$



Q5.12

it is column : if not pedestal.

Q5.41

$$e = \frac{l}{500} + \frac{b}{30}$$

Q5.4

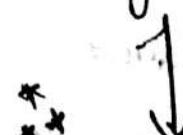
subjected to min of 20mm

$$e_{\min} = 20\text{mm.}$$

Pg.no - 48 , 26.5.3. , 26.5.3.1

↓
Columns

↓
longitudinal reinforcement



0.8% to 6%

for circular - min 6 bars

Other - min 4 bars.

Pg No - 49 :- c) Pitch & diameter of the lateral ties.

\downarrow
spacing

S_{max}

i) b

ii) 16 times the small diameter of length

iii) 300 mm.

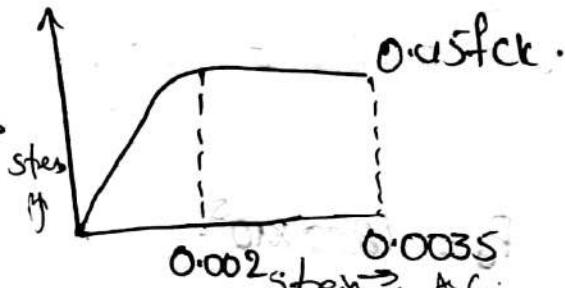
which ever is less.

2) diameter :-

$d = \frac{1}{4} \times \phi \rightarrow$ largest longitudinal bar dia.
 $< 16 \text{ mm.}$

Pg No - 70

axial compression is
0.002.

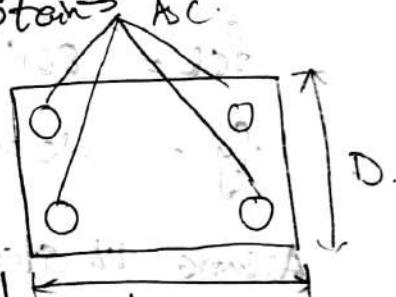


Cls of the column.

$$A_c = (bD) A_{cs} - A_{sc}$$

$P_u =$ load carried by concrete +

load carried by steel.

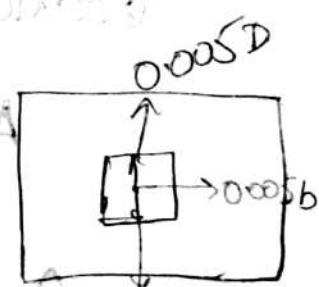


$$= A_c (0.45 f_{ck}) + A_{sc} (0.75 f_y)$$

$$= 0.9 (0.45 f_{ck} A_c + 0.75 f_y A_{sc})$$

$$= 0.405 f_{ck} A_c + 0.675 f_y A_{sc}$$

$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$$



$$P_u = 0.4f_{ck} + A_c + 0.67 f_y A_{sc}$$

$$A_{sc} = 4 \times \frac{\pi}{4} \times 18^2 = 1059.38$$

$$f_{ck} = 20 N/mm^2, f_y = 415 N/mm^2$$

$$A_c = (250 \times 300) - 1059.38$$

$$= 74547.62$$

$$P_u = 0.4 \times 20 \times 74547.62 + 0.67 \times 415 \times 1059.38$$

$$= 596 \text{ kN} + 125 \text{ kN}$$

$$= 722.165 \text{ kN}$$

Design a square column for the design load of 1200
kN. Use M20 Concrete, Fe415 steel.

$$P_u = 1200 \times 10^3$$

$$f_{ck} = 20 N/mm^2$$

$$f_y = 415 N/mm^2$$

Assume 1% steel $A_{sc} = 1\% \text{ of } A_c$

$$\approx 0.01 \times A_c$$

$$1200 \times 10^3 = 0.4 \times 20 \times A_c + 0.67 \times 415 \times 0.01 A_c$$

$$A_c = \frac{1200 \times 10^3}{10.78} = 111312 \text{ mm}^2$$

$$A_c = 111312 \text{ mm}^2$$

$$b = \sqrt{111312} \text{ for square.}$$

$$= 333.6$$

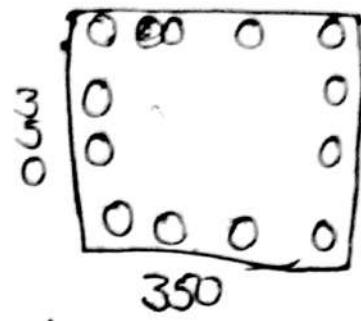
\therefore provide $350 \times 350 \text{ mm}^2$

$$A_{SC} = 0.01 \times (350 \times 350)^2$$

$$= 1225 \text{ mm}^2$$

$$12 \text{ Q} - 10.83.$$

$$16 \text{ Q} = 6.09$$



Provide 12 - 12Q as longitudinal reinforcement

Provide 8 - 16Q as longitudinal rft.

$$P = \frac{A_{SC}}{bd} \times 100.$$
$$= \frac{8 \times \frac{\pi}{4} \times 16^2}{350 \times 350} \times 100$$

$$= 1.3 \%$$

Hence Ok.

Lateral ties:-

$$\text{Diameter } d = \frac{1}{4} \times 16$$

$$= 4 \text{ mm}$$

Hence provide 6 mm ϕ (m/s) bar.

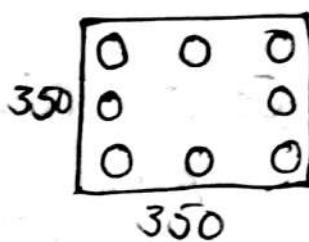
spacing. least of

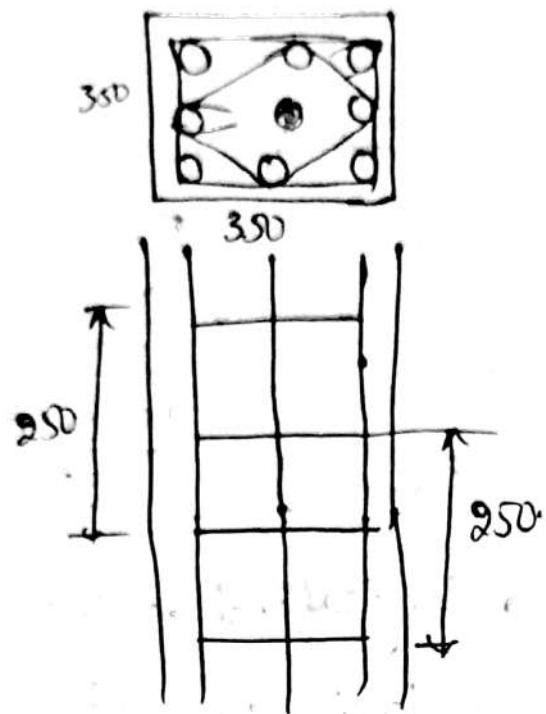
$$350 \text{ mm}$$

$$16 \text{ } \phi = 16 \times 16 = 256 \text{ mm}$$

$$300 \text{ mm}$$

Provide 6mm ϕ @ 250 mm c/c.





Center Columns:- P_u



Axial :- P_u, M_u



Biaxial :- P_u, M_{ax}, M_{ay}



Design a ^{short} axially loaded tied column pinned at both ends with an unsupported length of 3.5 mts. for carrying a characteristic load of 1500 kN. Use M20, Fe 415 steel.

Given data;

$$f_{ck} = 20 \text{ N/mm}^2$$

$$P = 1500 \text{ kN.}$$

$$f_y = 415 \text{ N/mm}^2$$

$$l = 3500 \text{ mm}$$

Pinned-pinned.

Design load $P_0 = 1.5 \times 1500 = 2250 \text{ kN}$.

Eff length $l_e = l = 3500 \text{ mm}$.

For short column $\frac{l_e}{D} = 12$.

$$\frac{3500}{12} = D.$$

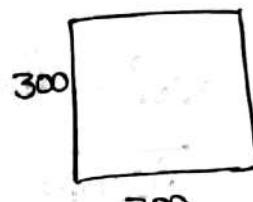
$$D = 291.67 \text{ mm.}$$

Assume col. section $300 \times 300 \text{ mm}^2$.

$$e_{\min} = \frac{l}{500} + \frac{D}{30}.$$

$$= \frac{3500}{500} + \frac{300}{30}$$

$$= 17 < 20 \text{ mm.}$$



$$\frac{l}{D} = \frac{3500}{300}$$

$$= 11.67 < 12.$$

$$A_g = 300 \times 300 = 90000 \text{ mm}^2.$$

Area of steel $A_{sc} = ?$

$$A_c = A_g - A_{sc} = 90000 - A_{sc}.$$

$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}.$$

$$2250 \times 10^3 = 0.4 \times 20 \times (90000 - A_{sc}) + 0.67$$

$$2250 \times 10^3 = 720000 - 8A_{sc} + 278.05 A_{sc}.$$

$$= 720000 - 270.05 A_{sc}.$$

$$A_{sc} = 5665.61 \text{ mm}^2$$

$$\% \text{ steel} = \frac{A_{sc}}{bd} \times 100 = \frac{5665.61}{300 \times 300} \times 100 \\ = 6.29\%$$

$$A_{sc} = 5665.61 \text{ mm}^2.$$

25 Q.

$$A_n = \frac{5665.61}{490.8} \\ = 11.54 \text{ b.m} \approx 12 \text{ b.m.}$$

12/9/05
Revise the section

Assume 375x375mm

140

$$\frac{le}{D} = \frac{3500}{375} = 9.33 < 12$$

~~140625~~

$$A_g = 375 \times 375 = 140625 \text{ mm}^2$$

$$A_c = A_g - A_{sc} = 140625 - A_{sc}.$$

$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$$

$$2250 \times 10^3 = 0.4 \times 20 \times (140625 - A_{sc}) + 0.67 \times 415 \times A_{sc}$$

$$A_{sc} = 4165.89 \text{ mm}^2.$$

$$\% \text{ of steel p} = \frac{A_{sc}}{bd} \times 100$$

$$= \frac{4165.89}{375 \times 375} \times 100 = 2.96\%$$

$$A_{sc} = 4165.89 \text{ mm}^2.$$

Assume 25 Ø $A\phi = \frac{\pi}{4} \times 25^2 = 490.87 \text{ mm}^2$

$$n = \frac{116589}{490.87}$$

$$= 8.48$$

Provide $10 \times 25\text{ Ø}$

$$\% \text{ steel provided} = \frac{10 \times \frac{\pi}{4} \times 25^2}{375 \times 375} \times 100 = 34.9\%$$

Lateral ties:

$$d = \frac{\phi}{4} = \frac{25}{4} = 6.25 \text{ mm.}$$

Provide 8mm Ø.

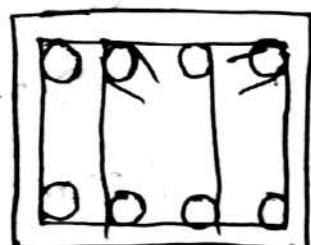
Spacing:

i) 375mm.

ii) $16\phi = 16 \times 25 = 400 \text{ mm.}$

iii) 300 mm.

Ties 8Ø @ 300 c/c. 375



- ① Design a circular column to carry an axial load of 1000kN using lateral ties. Use M20, Fe415 steel.

$$P = 1000 \text{ kN.}$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2.$$

$$\begin{aligned} \text{Design load } P_0 &= 1.5 \times P = 1.5 \times 1000 \\ &= 1500 \text{ kN.} \end{aligned}$$

$$A_{SC} = 1452.20 \text{ mm}^2$$

(3)

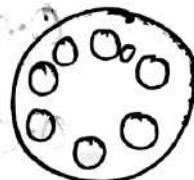
Assume 16 Φ $A\phi = 201.06$

$$\eta = \frac{1452.20}{201.06}$$
$$= 7.22 \text{ bars.}$$

provide 8 bars 16 Φ .

$$A_{SC, provided} = 1608.49.$$

$$A_{SC, provided} = \frac{1608.49 \times 100}{\pi \times D^2}$$
$$= 11.64$$



lateral ties;

$$Diameter d = \frac{\phi}{4} = \frac{16}{4} = 4 \text{ mm.}$$

Provide 6mm ϕ (M.S.).

spacing

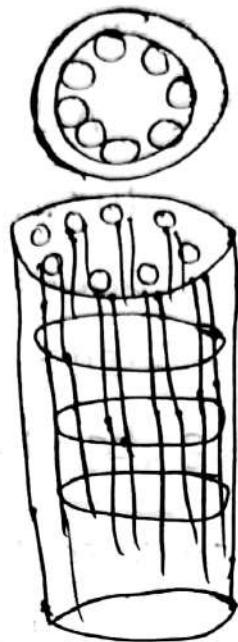
$$i) 430 \text{ mm}$$

$$ii) 16 \times 16 = 256 \text{ mm.}$$

$$iii) 300 \text{ mm.}$$

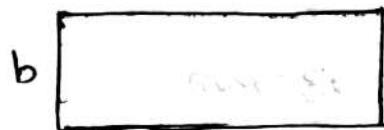
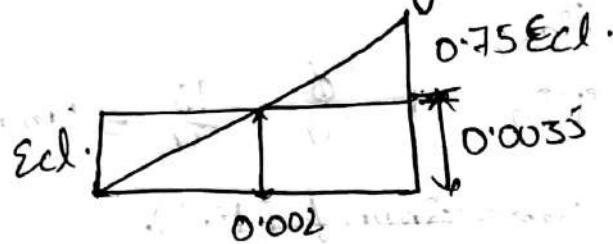
Provide 6mm ϕ @ 3250 mm c/c.

(a)



0.002 for axial load.

0.0035 for bending.



D

$$Ecl = 0.0035 - 0.75 Ecl.$$

Design of columns having axial load & moment (P_0, M_0)

$M_0 = 0$ then it is a axially loaded column.

$P_0 = 0$, then pure bending case

$P_0 \& M_0$ are present for uniaxial column.

Design a column for the following data.

Axial load $P_0 = 1200 \text{ kN}$.

B.M $M_0 = 250 \text{ kN-m}$.

Unsupported length $l = 3200 \text{ mm}$.

Clear cover 40mm.

pinned-pinned case.

Given data:-

$P_0 = 1200 \text{ kN}$.

$M_0 = 250 \text{ kN-m}$.

$f_{ck} = 20 \text{ N/mm}^2$

$f_y = 415 \text{ N/mm}^2$

C.C = 40mm

$l = 3200 \text{ mm}$.

Pinned-pinned.

Effective length $l_e = l = 3200 \text{ mm}$.

$$e = \frac{l}{500} + \frac{D}{30}$$



$$= \frac{3800}{500} + \frac{400}{30}$$

$$= 19.73 < 20\text{mm.}$$

$$e_{min} = 20\text{mm.}$$

$$M_0 = P_0 \times e \Rightarrow e = \frac{M_0}{P_0} = \frac{250 \times 10^6}{1200 \times 10^3}$$

$$= 208.33$$

allowable

$e > e_{min}$
Design for bending.

$$\frac{P_u}{f_{ck} b D} = \frac{1200 \times 10^3}{20 \times 300 \times 400} \\ = 0.5$$

$$\frac{M_0}{f_{ct} b D^2} = \frac{250 \times 10^6}{20 \times 300 \times 400} \\ = 0.5026$$

$$d = 40\text{mm} + \frac{\phi}{2} \\ = 50\text{mm}$$

$$\frac{d}{D} = \frac{50}{400} = 0.125$$

From SP-16, Chart 33, $f_y = 415 \text{N/mm}^2$

$$\frac{P}{f_{cb}} = \frac{0.24}{80} \times 90 \\ = 4.8$$

De-tailing.

$$P_u = 48\%$$

$$A_{SC} = \frac{41.8}{100} \times 300 \times 400$$

$$= 5760 \text{ mm}^2$$

$$20 \text{ Q } A\phi = 310 \text{ mm}^2$$

$$= \frac{5760}{310} = 18.31 \text{ bars}$$

Provide. 20 bars

25 Q.

$$= \frac{5760}{25}$$

$$= 12 \text{ bars.}$$

$$= 300 - 40 - 40 - \frac{25}{2} - \frac{25}{2}$$

$$= 195$$

$$= \frac{195}{5} = 39 \text{ mm.}$$

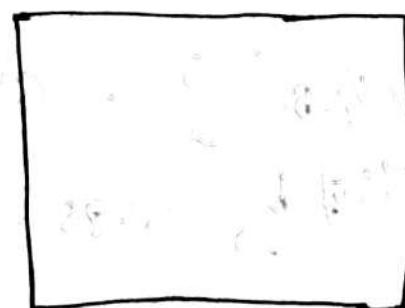
$$\Rightarrow 39 - \frac{25}{2} - \frac{25}{2}$$

$$= 14 \text{ mm} < 25 \text{ mm.}$$

Revise the section;

$$\frac{P_u}{f_{ckbd}} = \frac{1200 \times 10^3}{20 \times 350 \times 450} = 0.38 \quad 350$$

$$\frac{M_o}{f_{ckbd}^2} = \frac{200 \times 10^6}{20 \times 350 \times 450^2} = 0.176 \quad 450$$



$$d' = 40 + \frac{25}{2}$$

$$= 52.5$$

$$\frac{d'}{D} = 0.15$$

Chart-33, SP-16

$$\frac{P}{f_{ck}} = 0.135$$

$$P = 2.7\%$$

$$A_{sc} = \frac{2.7}{100} \times 350 \times 400 \\ = 4252.5 \text{ mm}^2$$

$$\text{Assume } 25 \Phi = A_\phi = 490.87 \text{ mm}^2$$

$$n = 8.66$$

10x25 Φ.

Detailing:-

C/c of outer bars.

$$350 - 40 - 40 - \frac{25}{2} - \frac{25}{2}$$

$$= 245$$

$$\text{C/c of I.B. } \frac{245}{2} = 61.25 \text{ mm.}$$

$$\text{C/c of b} \Rightarrow 61.25 - \frac{25}{2} - \frac{25}{2}$$

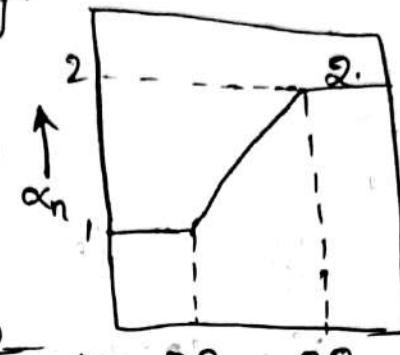
$$= 36.25 \text{ mm.}$$

Biaxial columns

Procedure: P_u, M_{ux}, M_{uy} .

1) Assume cross section. (b, D)

Assume % of steel. (ρ).



Step-2 Find $\frac{P}{f_{ck}}, \frac{P_u}{f_{ck}bd^2}, \frac{M_{ux}}{f_{ck}bd^2} \rightarrow \frac{P_u}{P_u}$
 $\frac{M_{uy}}{f_{ck}bd^2} \rightarrow & \text{ find } M_{uy}$

Step-3 find $\frac{P}{f_{ck}}$; $\frac{M_{uy}}{f_{ck}bd^2} \rightarrow M_{uy}$.

$$\left(\frac{M_{ux}}{M_{ux}}\right)^{\alpha_n} + \left(\frac{M_{uy}}{M_{uy}}\right)^{\alpha_n} \leq 1.$$

Rectangular column with biaxial bending.

Determine the rft to be provided in a column subjected to biaxial bending with the following data

Size of column $400 \times 500 \text{ mm.}$

Concrete mix $M20.$

Characteristic strength of rft 415 N/mm^2

Factored load = 1200 kN.

Factored moment acting II to the larger dimension 100 kN-m.

Factored moment acting II to the shorter dimension
= 80 kNm

clear cover = 40 mm.

Given;

$$P_u = 1200 \text{ kN}$$

$$M_{ux} = 100 \text{ kNm}$$

$$M_{uy} = 80 \text{ kNm}$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

Sized column = 400 x 500 mm.

Assume % of steel as $P = 1.6x$.
Moment carrying capacity

$$\frac{P}{f_{ck} b D} = \frac{1.6}{20} = 0.08$$

$$\frac{P_u}{f_{ck} b D} = \frac{1200 \times 10^3}{20 \times 400 \times 500}$$

chart

$$= 0.3$$

$$\frac{d'}{D} = \frac{52.5}{500} = 0.105$$

Chart - 44.

$$\frac{M_{ux_1}}{f_{ck} b D^2} = \frac{M_{ux}}{20 \times 400 \times 500^2} = \frac{0.105}{0.12} = 0.105$$
$$= \frac{5 \times 10^{-10}}{M_{ux_1}}$$

$$M_{ux_1} = 0.105 \text{ kNm}$$

0.91

$$\frac{d'}{b} = \frac{52.5}{400} = 0.13125$$

$$\frac{M_{Uy_1}}{f_{ck} b D^2} = \frac{M_{Uy_1}}{20 \times 500 \times 400^2}$$

chart 45

$$\frac{M_{Uy_1}}{f_{ck} b D^2} = 0.11$$

$$M_{Uy_1} = 176 \text{ kNm}$$

$$\left(\frac{M_{Ua_1}}{M_{Uy_1}} \right)^{\alpha_n} + \left(\frac{M_{Uy}}{M_{Uy_1}} \right)^{\alpha_n} \leq 1$$

$$\alpha_n = \frac{P_u}{P_2}$$

$$P_2 = 0.45 f_{ck} \phi A_c + 0.75 f_y A_{sc}$$

$$A_{sc} = \frac{1.6}{100} \times 400 \times 500 \\ = 3200 \text{ mm}^2$$

$$A_g = 400 \times 500 = 200000 \text{ mm}^2$$

$$A_c = A_g - A_{sc} \\ = 200000 - 3200 \\ = 196800$$

$$P_{u2} = 0.45 \times 20 \times 196800 + 0.75 \times 415 \times 3200 \\ = 2767200$$

$$\frac{P_u}{P_{u2}} = \frac{1200 \times 10^3}{2767200} \\ = 0.4336$$

$$\frac{107 \times 10^6}{212 \times 10^6} = 1.28$$

$$\left(\frac{8 \times 10^6}{116 \times 10^6} \right) = 0.38$$

$$= \frac{298}{0.38} + 0.336$$

~~0.408~~ < 0.634 $\leq 1.$ Hence Ok.

Assume 25 Φ .

$$= \frac{3900}{490.87}$$

$$= 6.519$$

Provide $8 \times 25 \Phi$.

$$\text{Lateral ties} = \frac{1}{6} = \frac{25}{6} = 6.25$$

Provide 8 mm bars.

Spacings / pitch.

i) 400 mm.

$$(i) 16\phi = 16 \times 25 = 400$$

ii) 300 mm

Provide 8 Φ @ 300 mm c/c.

Circular column with
Design a reinforced column 400 mm square
to carry an ultimate load of 1000 kN at an
eccentricity of 160 mm. Use M20, Fe 250

$$P_u = 1000 \text{ kN}$$

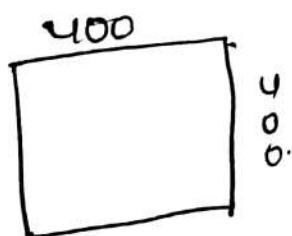
$$E = 160 \text{ mm}$$

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 250 \text{ N/mm}^2$$

$$b = 400 \text{ mm}$$

$$D = 400 \text{ mm}$$



$$M_u = P_u \times E = 160 \text{ kN-m}$$

Assume % of steel = 1.6%.

$$\frac{P}{f_{ck}} = \frac{1.6}{20} = 0.08$$

$$\frac{P_u}{f_{ck} b D} = \frac{1000 \times 10^3}{20 \times 400 \times 400} = 0.3125$$

$$\frac{d'}{d} = \frac{50}{400} = 0.125$$

$$\frac{P \cdot M_u}{f_{ck} b D^2} = \frac{160 \times 10^6}{20 \times 400 \times 400^2} = 0.125$$

Design a short circular column of 500mm dia with the following data.

Factored load = 800kN.

Factored moment = 162.5 kN-m.

Provide Hoop reinforcement. Take M20, Fe415 steel.

$$D = 500\text{mm}.$$

$$P_0 = 800\text{kN}.$$

$$M_u = 162.5 \cdot \text{kN-m}.$$

$$f_{ck} = 20\text{N/mm}^2$$

$$f_y = 415\text{N/mm}^2.$$

$$d' = 40 + \frac{80}{2} = 50\text{ mm (Assume } 20\Phi)$$

$$\frac{d'}{D} = \frac{50}{500} = 0.1$$

$$\frac{P_0}{f_{ck} D^2} = \frac{800 \times 10^3}{20 \times 500^2} = 0.16.$$

$$\frac{M_u}{f_{ck} D^3} = \frac{162.5 \times 10^3}{20 \times 500^3} = 0.065.$$

Chart-56 $\frac{P}{f_{ck}} = 0.05$

$$P = 0.05 \times 20 = 1\text{.}$$

$$\Phi = 1\text{.}$$

$$\begin{aligned} A_{SC} &= \frac{1}{100} \times \frac{\pi \times 500^2}{4} \\ &= 1963\text{ mm}^2. \end{aligned}$$

$$20\bar{R} = A\phi = 31.6 \text{ mm}^2$$

$$n = 6.25$$

$$7 \times 20\bar{R}$$

lateral ties

$$d = \frac{20}{4} = 5 \text{ mm}$$

Provide 6ϕ

spacing i) 500 mm

ii) $16 \times 20 = 400 \text{ mm}$

iii 300 mm .

Provide $6 \text{ mm} \phi @ 300 \text{ mm c/c.}$

b = 250 mm

$$P_u = 600 \text{ kN-m.}$$

$$M_{UD} = 60 \text{ kN-m.}$$

$$M_{Uy} = 40 \text{ kN-m.}$$

$$f_y = 415 \text{ N/mm}^2$$

$$f_{ck} = 30 \text{ N/mm}^2.$$

Assume $P = 3y$.

$$\frac{P}{f_{ck}} = \frac{3y}{30} = 0.1$$

$$\frac{P_u}{f_{ck} b D} = \frac{600 \times 10^3}{30 \times 250 \times 250}$$

$$= 0.32.$$

$$\frac{M_{u1}}{f_{ck} b D^2} = ? = 0.11.$$

$$40 + \frac{10}{2} = 50$$

$$\frac{d}{D} = \frac{50}{200} = 0.2.$$

$$M_{u1} = 51.5625 \text{ kNm}.$$

Assume $P = @42$,

$$\frac{P}{f_{ct}} = \frac{42}{30} = 0.14.$$

$$\frac{M_{u1}}{f_{ck} b D^2} = 0.14.$$

$$M_{u1} = 65.625 \text{ kNm}.$$

$$M_{uy1} = 65.625 \text{ kNm}.$$

~~$$P_{ez} A_g = 250 \times 250 = 62500 \text{ mm}^2.$$~~

$$A_{sc} = \frac{P b D}{100} = 2625 \text{ mm}^2$$

$$A_c = 59875 \text{ mm}^2$$

$$P_{uz} = 0.45 f_{ck} A_c + 0.75 \times f_y \times A_{sc}$$

$$= 16253 \text{ kN}$$

$$\frac{P_0}{P_2} = \frac{600 \times 10^3}{16253 \text{ kN}}$$

$$= 0.369$$

$$0.2 \rightarrow 1$$

$$0.8 \rightarrow 2.$$

$$0.369 \rightarrow ?$$

$$1 + \frac{(2-1)}{(0.8-0.2)} (0.369 - 0.2)$$

$$= 1.281$$

$$= \left(\frac{60}{65.625} \right)^{1.28} + \left(\frac{40}{65.625} \right)^{1.28}$$

$$= 0.891 + 0.53$$

$$= 1.42.$$

$$M_{u1} = 0.16 \times 30 \times 300^3$$

$$= 75000 \text{ m.}$$

$$A_g = 3000$$

$$A_c = 59500$$

$$\Delta g = 62500.$$

$$P_{u2} = 1737000$$

$$\rho_{\alpha_n} = 0.345$$

$$0.34$$

$$1 + \frac{(0.1)}{(0.8 - 0.2)} (0.34 - 0.2)$$

$$= 1.93.$$

$$= 0.75 + 0.46.$$

$$1.21.$$

5.4

$$\frac{P}{P_{ct}} = 0.018$$

0.17

79.6887500

3375

59125

$$P_{U2} = 1848656.25$$

$$P_U = 0.324$$

$$\left(\frac{60}{79.688} \right)^{1.206} + \left(\frac{40}{79.688} \right)^{1.206}$$

$$0.711 + 0.435$$

$$= 1.14$$

$$G = 0.2$$

$$0.19 \times 89062500$$

$$= 3250$$

$$58750 \quad P_f = 1960312.5$$

$$= 0.306.$$

$$\therefore 1.16$$

$$= \left(\frac{60}{89.0625} \right)^{1/16} + \left(\frac{40}{89.0625} \right)^{1/16}$$

$$= 0.622 + 0.37$$

$$= 0.9.$$

Spiral column:-

Design a short circular column 500 dia

factored load = 800 kN

factored moment = 162.5 kNm

provide ^{Helical} Hoop reinforcement. Take M20, Fe415 std.

P_U = 800 kN

M_U = 162.5 kNm.

f_{ck} = 41.5 N/mm².

f_y = 415 N/mm².

$$\left(\frac{P_U}{f_{ck} D^2} \right)_{\text{Hoop}} = 0.16.$$

$$\left(\frac{P_U}{f_{ck} D^2} \right)_{\text{Helical}} = 0.152.$$

$$\left(\frac{M_u}{f_{ck} D^3} \right)_{Hoop} = 0.065$$

$$\left(\frac{M_u}{(f_{ck} D^3)} \right)_{Helical} = 0.061$$

$$\frac{P}{f_{ck}} = 0.04 \Rightarrow P = 0.04 \times 20 \\ = 0.8.$$

$$\therefore \text{Area of steel} = \frac{\pi}{100} \times \frac{P}{f_{ck}} \times D^2 \\ = 1570 \text{ mm}^2.$$

Assume 20 TMT.

~~provide 6 x 20 TMT.~~

$$P = \frac{6 \times \frac{\pi}{100} \times 20^2}{\frac{\pi}{100} \times 500^2} \times 100$$

$$= 0.96.$$

~~Let us use 8mm dia mild steel bar for helical reinforcement.~~

$$\therefore \text{Core dia; } D_c = 500 - 2 \times 40 + 2 \times 8 \\ = 438 \text{ mm.}$$

$$\therefore \text{Core area} = \frac{\pi}{4} \times D_c^2$$

$$V_c = A_c = 109301 \text{ mm}^2$$

$$\therefore \frac{A_g}{A_c} = \frac{\frac{\pi}{4} \times 500^2}{436^2} = 1.3151$$



500 - 2x40 + 2x8

$$0.36 \left(\frac{A_g}{A_c} - 1 \right) f_{ck} / f_{yh}$$

$$0.36 \left(1.315 - 1 \right) \frac{20}{450}$$

$$= 0.00907$$

Dia. of core upto center of helics.



$$500 - 2 \times 40 + 8 = 428 \text{ mm.}$$

Let the pitch of the spiral be S mm
volume of spiral for 1mm length of column.

$$V_H = \frac{\pi d}{s} \times \frac{\pi}{4} \times \frac{d^2}{3}$$

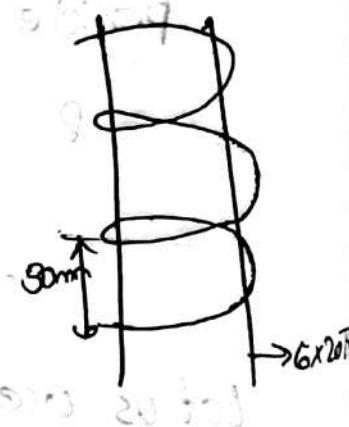
$$= \frac{\pi \times 428}{s} \times \frac{\pi}{4} \times 8^2$$

$$= \frac{67587}{s}$$

$$\frac{V_H}{V_C} = \frac{67587}{s}$$

$$V_C = 149301$$

$$= \frac{0.452}{s}$$



$$\frac{V_H}{V_C} = 0.36 \rightarrow 0.36 \left(\frac{A_g}{A_c} - 1 \right) \frac{f_{ck}}{f_{yh}} = 0.00907$$

$$\frac{0.452}{s} = 0.00907 \cdot 149.9 \text{ mm.}$$

$$s = 50 \text{ mm}$$

pitch should not more than

i) 75mm.

ii) $\frac{1}{6} D_c = \frac{1}{6} \times 0.36$
 $= 72.67$

Pitch should not be less than = $3 \times d_s$
 $= 3 \times 8 = 24\text{mm}$

Hence pitch 50mm is 'OK'

Long columns:-

$$M_{bax} = \frac{P_o D}{2000} \left(\frac{e_{ax}}{D} \right)^2$$

we have

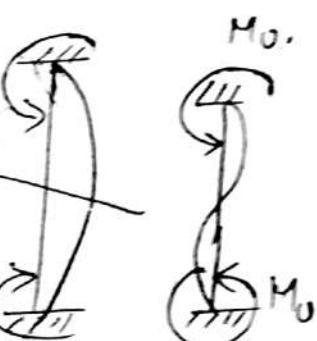
$$M_{bax} = P_o e_{ax}$$

$$\therefore e_{ax} = \frac{D}{2000} \left(\frac{l_{ex}}{D} \right)^2$$

$$M_{bay} = \frac{P_o b}{2000} \left(\frac{l_{ey}}{b} \right)^2$$

$$M_{uxl} = 0.6 M_2 + 0.4 M_1$$

$$P_o = \left(k_1 + k_2 + \frac{P}{f_{ck}} \right) f_{ck} b D$$



Design a slender braced circular column under axial bending with the following data.

Size of column - 400mm.

M_{20} concrete
Fe 415 steel.

Effective length 6mts, unsupported length 7mts.

factored load $P_o = 1200\text{ kN}$.

moment $M_{uxl} = 75\text{ kNm}$ at top & 50 kNm at bottom. Assume column is bent in single curvature.

$$\frac{l_{ex}}{D} = \frac{6000}{400} = 15 > 12.$$

Hence it is long column.

Additional moments

$$\begin{aligned} e_{ax} &= \frac{D}{2000} \left(\frac{l_{ex}}{D} \right)^2 \\ &= \frac{400}{2000} (15)^2 \\ &= 45 \text{ mm.} \end{aligned}$$

$$\begin{aligned} M_{ax} &= P_u \times e_{ax} \\ &= 1800 \times \frac{45}{1000} \\ &= 54 \text{ kNm.} \end{aligned}$$

Calc: of k_a

$$\underline{k_a} = \frac{P_{uz} - P_u}{P_{uz} - P_b}$$

$$P_b = \left(k_1 + k_2 \frac{P}{f_{ck}} \right) f_{ck} D^2$$

$$P_z = 25\%$$

$$\frac{d'}{D} = \frac{50}{400} = 0.125$$

$$\text{Table 60; } k_1 = 0.155$$

$$k_2 = 0.266$$

$$= \left(0.155 + 0.266 \times \frac{2.5}{20} \right) 20 \times 400^2$$

$$= \cancel{1747800} = 601 \text{ kN.}$$

$$K = \frac{P_{UZ} - P_u}{P_{UZ} - P_b} \leq 1$$

$$A_g = \frac{\pi}{4} \times D^2 = \frac{\pi}{4} \times 400^2 = 125663.7 \text{ mm}^2.$$

$$A_s = \frac{\rho}{100} \times \frac{\pi}{4} \times D^2 = \frac{2.5}{100} \times \frac{\pi}{4} \times 400^2 = 3141.59 \text{ mm}^2.$$

$$A_c = 122522.1 \text{ mm}^2$$

$$P_{UZ} = 0.85 f_{ck} A_c + 0.75 f_y A_s c$$

$$= 0.45 \times 20 \times 122522.1 + 0.75 \times 415 \times 3141.59.$$

$$= 2080518.854 \text{ N-m}$$

$$\underbrace{K = \frac{2080518854 + 1200 \times 10^3}{2080518.854 - 600 \times 10^3}}_{\approx 0.596 < 1}$$

Assume 20Ω .

$$= \frac{3141.59}{314} = 10.005 \text{ bars}$$

Provide $10 \times 20\Omega$.

\therefore Reduced Additional moment.

$$\underline{M'a = k Ma.}$$

$$= 0.59 \times 5u.$$

$$= 31.86 \text{ kNm}$$

Slabs

Slabs:- Flexure, shear.

$$M = \frac{w l e^2}{8} = \frac{W l c}{8}$$

$$V = \frac{W l c}{8} = \frac{W}{8}$$

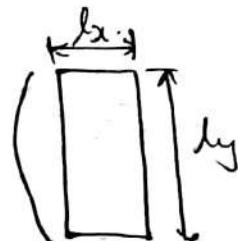
$$W = w l e$$

l_{eff} is the least of

- i) clearspan + d.
- ii) c/c of supports.

Slab types:-

- 1) One-way slab $\rightarrow \frac{ly}{lx} > 2$.
- 2) Two-way slab.
- 3) Flat slab
- 4) Flat plate.



IS 875 (Part 182).

Finishes and Partitions 1.5 kN/m^2 .

For roofs:-

1.5 kN/m^2 with access.

0.75 kN/m^2 with out access

For floors:-

2.0 kN/m^2 for residential buildings.

3 kN/m^2 for office building.

Effective span:-

'eff' small of

i) C/c of supports.

ii) C.s + d.

minimum 'eff' for slabs $\sim 0.12\%$

Minimum t. of steel:-

0.12% for Hysd

0.15% for mild steel.

Design of One-way slab:-

Design a simply supported R.C.C. slab for a roof a house 3.5 mts x 8 mts (inside dimensions). With 25 mm walls all around. Assume a live load of 4 kN/m² and finishing load 1 kN/m². Use M20 & Fe 450 Steel.

Step 1 Given data:-

Hall = 3.5 m x 8 m

width of masonry = 250 mm

live load = 4 kN/m²

finishing = 1 kN/m²

f_ck = 20 N/mm²

f_y = 415 N/mm²

Step 1 Cal. of factored loads.

Assume $\frac{l}{d} = \frac{3500}{25} = 140\text{mm}$.

$$\text{do } \frac{l}{d} = 25 \\ d = \frac{l}{25}.$$

Overall depth $D = d + c.c + \frac{\phi}{2}$

$$= 140 + 15 + \frac{10}{2}$$

$$D = 160\text{mm.}$$

Dead load;

i) Slab = $25 \times 0.16 = 4\text{kN/m}^2$.

ii) Finishish = 1kN/m^2

Total dead load = 5kN/m^2 .

Live load = 4kN/m^2 .

Total load $w = D.L + L.L = 5 + 4 = 9\text{kN/m}^2$.

Factored load $w_f = 1.5 \times w$

$$= 1.5 \times 9 = 13.5\text{kN/m}^2$$

Step-2 Calc. of effective span.

l_{eff} is the least of

i) C/c of supports.

$$= 3.5 + 0.25$$

$$= 3.75\text{m.}$$

ii) C.s + d = $3.5 + 0.1u$.

$$= 3.6\text{m.}$$

Step 3

Factored BM & SF.

$$\begin{aligned}\text{Factored BM } (M_0) &= \frac{w_{\text{left}}^2}{8} \\ &= \frac{13.5 \times 3.6 u^2}{8} \\ &= 22.35 \text{ kNm} \\ \text{Factored SF } (v_0) &= + \frac{w_{\text{left}}}{2} \\ &= 24.5 \text{ kN/m.}\end{aligned}$$

Step 4 Check for depth.

$$M_u = 0.138 f_{ck} b d^2$$

$$\begin{aligned}d &= \sqrt{\frac{M_u}{0.138 f_{ck} b}} \\ &= \sqrt{\frac{22.35 \times 10^6}{0.138 \times 20 \times 1000}} \\ &= 90 \text{ mm} < 140 \text{ mm.}\end{aligned}$$

Step 5 Calc. of steel area.

$$\begin{aligned}\frac{a}{d} &= 1.2 - \sqrt{1.04 - \frac{6.6 M_0}{f_{ck} b d^2}} \\ \frac{6.6 M_0}{f_{ck} b d^2} &= \frac{6.6 \times 22.35 \times 10^6}{20 \times 1000 \times 140^2} \\ &= 0.376\end{aligned}$$

$$\frac{a}{d} = 0.168$$

$$\frac{a}{d} = 0.168 < \left(\frac{d_{\text{min}}}{d} = 0.18 \right)$$

Hence it is under reinforced section.

$$\text{lever arm } r = d \left(1 - 0.02 \frac{\sigma}{d}\right)$$

$$= 140 \left(1 - 0.02 \times 0.16\right)$$

$$= 130.19 \text{ mm.}$$

$$\text{Area of steel } A_{st} = \frac{M_u}{0.85 f_y^2}$$

$$= 475.7 \text{ mm}^2$$

$$\text{Assume } 107 \text{ MTS } A\phi = \frac{\pi}{4} \times 10^2 = 78.53 \text{ mm}^2$$

$$\text{No of bars } n = \frac{A_{st}}{A\phi}$$

$$= \frac{475.7}{78.53}$$

$$= 6.05$$

$$\text{Spacing } s = \frac{1000}{n}$$

$$= \frac{1000}{6.05}$$

$$= 165.28 \text{ mm.}$$

Max. Spacing (s_{max}) ~~is~~

$$i = 3d = 3 \times 140 = 420 \text{ mm.}$$

i.e. 300 mm

$$s_{max} = 300 \text{ mm}$$

Provide 107MT @ 160 mm c/c.

Step-7 Check for deflection

for simply supported case basic value $\frac{l}{d} = 20$.
% of tensile steel at midspan.

$$A_{st\ provided} = \frac{1000}{5} \cdot \frac{\pi}{4} d^2$$

$$= \frac{1000}{180} \times \frac{\pi}{4} \times 10^2$$

$$= 490.8 \text{ mm}^2$$

$$A_{st\ req} = 475 \text{ mm}^2$$

$$f_s = 0.58 f_y \cdot \frac{A_{st\ req}}{A_{st\ provided}}$$

$$= 0.58 \times 415 \times \frac{475}{490.8}$$

$$= 232.9 \text{ mm}^2$$

$$\text{Modi \% of steel} = \frac{5490.8}{1000 \times 160} \times 100 = 0.35$$

$$\frac{l}{d} = 20 \times 1$$

$$\frac{l}{d} = \frac{3300}{160} = 25$$

Hence deflection limit exceeds so change spacing of the main steel. ie, Assume $s = 150 \text{ mm}$ instead of 160 mm .

$$f_s = A_{st\ provided} = \frac{1000}{150} \times \frac{\pi}{4} \times 10^2$$

$$= 523.5 \text{ mm}^2$$

$$0.58 \times 415 \times \frac{475}{523.5} = 1.55$$

$$\frac{l}{d} = 20 \times 1.55$$

$$= 31.$$

$$\left(\frac{l}{d}\right)_{\text{provided}} = \frac{3500}{100} = 25$$

Hence ok.

Step-8 Check for shear (optional).

$$V_U = 24.5 \text{ kN}$$

$$f_v = \frac{V_U}{bd} = \frac{24.5 \times 10^3}{1000 \times 160} = 0.175 \text{ N/mm}^2$$

Calc. of f_c .

$$50\% \quad P_f = \frac{0.37}{2} = 0.185\% \quad (\text{at supports})$$

$$\text{from Table 19} \quad f_c = 0.285 \text{ N/mm}$$

$f_c > f_v$ Hence ok.

Step-9 Summary of design.

Depth of slab $D = 160 \text{ mm}$

Cover = 15 mm.

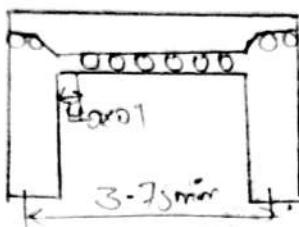
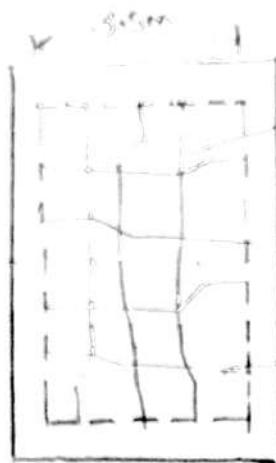
M₂₀ Concrete = M₂₀.

Steel Fe415.

Primary 10TMT @ 150 mm c/c.

8 TMT @ 260 mm c/c

Step-10 Detailing:-



Moments developed in Two way slabs (simply supported case).

$$\Delta_{\text{max.}} = \frac{5}{384} \frac{q_a l_a^4}{EI}$$

$$\Delta_{\text{min.}} = \frac{5}{384} \frac{q_y l_y^4}{EI}$$

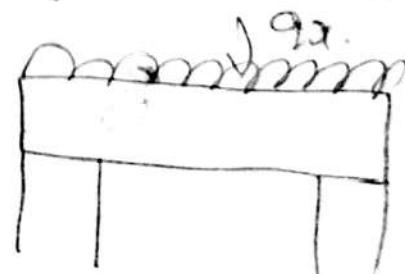
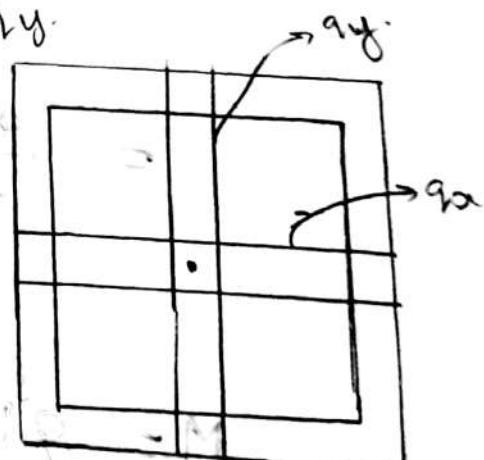
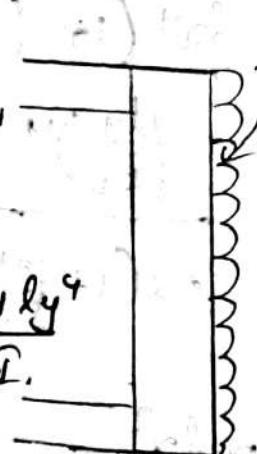
$$\frac{5}{384} < \frac{q_a l_a^4}{EI} = \frac{5}{384} \frac{q_y l_y^4}{EI}$$

$$q_a = q_y \left(\frac{l_y}{l_a} \right)^4$$

$$q_y = q_a \left(\frac{l_a}{l_y} \right)^4$$

$$q = q_a + q_y$$

$$q = q_a + q_a \left(\frac{l_a}{l_y} \right)^4 + q_a$$



$$q_x = \frac{q}{\left(\frac{ly}{lx}\right)^4 + 1}$$

$$q_x = \frac{q \times ly^4}{lx^4 + ly^4}$$

$$q_y = \frac{q lx^4}{lx^4 + ly^4}$$

$$\begin{aligned} M_x &= \frac{q a l a^2}{8} \\ &= \frac{q ly^4}{8(lx^4 + ly^4)} \times lx^2 \end{aligned}$$

$$\begin{aligned} &= \frac{q}{8} \frac{ly^4}{lx^4 \left(1 + \left(\frac{ly}{lx}\right)^4\right)} lx^2 \\ &= \frac{q}{8} \frac{\left(\frac{ly}{lx}\right)^4}{lx \left(1 + \left(\frac{ly}{lx}\right)^4\right)} \end{aligned}$$

$$M_b = q B_a \cdot lx^2$$

$$B_a = \frac{\left(\frac{ly}{lx}\right)^4}{8 \left(1 + \left(\frac{ly}{lx}\right)^4\right)}$$

$$M_y = \frac{qy ly^2}{8} \\ = \frac{q l a^4}{8 l a^4 + l y^4} l y^2.$$

$$= \frac{q \cdot l a^4}{8(l a^4(1 + P(\frac{l y}{l a})^4))} l y^2$$

$$= \frac{q \cdot l y^2}{8(1 + (\frac{l y}{l a})^4)}$$

$$= \frac{q}{8(1 + (\frac{l y}{l a})^4)} \cdot \frac{l y^2}{l a^2}$$

$$M_y = q B_y l a^2$$

$$B_y = \frac{\left(\frac{l y}{l a}\right)^2}{8\left(1 + \left(\frac{l y}{l a}\right)^4\right)}$$

$$d = \frac{\text{Span}}{25 \text{ to } 30}$$

Design of Simply supported two-way slab:

Design a reinforced concrete slab 5.5 mts x 4 mts.

Simply supported on all the four sides it has to carry a characteristic live load of 8 kN/m² M25, Fe415 exposure condition mild.

Given data.

Room Dimensions : 4 m x 5.5 m.

Concrete $f_{ck} = 25 \text{ N/mm}^2$

Steel $f_y = 415 \text{ N/mm}^2$

Table 16 mild exposure = 20 mm

Calc. of Depth of the slab.

$$l_y = 5.5 \text{ m}$$

$$l_x = 4 \text{ m.}$$

$$\frac{l_y}{l_x} = \frac{5.5}{4} = 1.375 < 2.$$

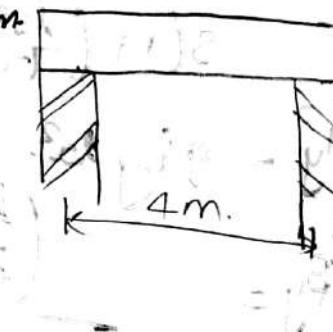
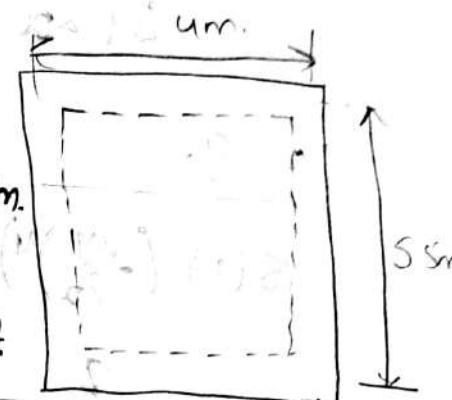
Hence it is two way slab.

$$l_x = 4000 \text{ mm.}$$

$$\text{Total depth } D = \frac{l_x}{24} = \frac{4000}{24} = 166.67 \text{ mm.}$$

$$= 166.67 \text{ mm.}$$

$$= 166 \text{ mm.}$$



Take $D = 170\text{ mm}$.

$$\begin{aligned}\text{Effective depth } d &= D - CC - \frac{\phi}{2} \\ &= 170 - 20 - \frac{10}{2}, \quad (\text{10 TMT bars}) \\ &= 145\text{ mm.}\end{aligned}$$

Step-2 Design load.

i) Dead load =

- 1) Self weight of slab = $0.17 \times 25 = 4.25\text{ kN/m}^2$
- 2) Finishing load (25 mm thick) = 0.5 kN/m^2 .
 $\frac{25}{1000} \times 250$
- 3) Plastering load (6 mm) = $\frac{6}{1000} \times 25 = 0.15\text{ kN/m}^2$

$$\text{Total dead load} = 4.894\text{ kN/m}^2$$

ii) Live load = 8 kN/m^2 .

$$\text{Total load} = DL + LL$$

$$= 4.89 + 8$$

$$= 12.89\text{ kN/m}^2$$

$$\begin{aligned}\text{Design load} &= 1.5\omega = 1.5 \times 12.89 \\ &= 19.341\text{ kN/m}^2\end{aligned}$$

Step-3 Design moment and S.F.

$$\omega_u = 19.341\text{ kN/m}^2$$

$$\text{Moment} = P_x = 4000$$

$$l_y = 5500\text{ mm.}$$

$$\frac{l_y}{d_x} = 1.375$$

Table 27:

$$\frac{I_y}{I_x} = 1.3 \quad \alpha_a = 0.093.$$

$$\frac{I_y}{I_x} = 1.4 \quad \alpha_a = 0.099$$

$$0.093 + \frac{(0.099 - 0.093)}{(1.4 - 1.375)} (1.375 - 1.3)$$

$$= 0.0975$$

$$\frac{I_y}{I_x} = 1.3 \quad 0.055$$

$$\frac{I_y}{I_x} = 1.4 \quad 0.051$$

$$\alpha_y = 0.052$$

$$M_a = \alpha_a w b \alpha^2$$

$$= 0.0975 \times 19.341 \times u^2$$

$$= 30.17 \text{ kNm}$$

$$M_y = \alpha_y w b \alpha^2 = 0.052 \times 19.341 \times u^2$$

$$= 16.09 \text{ kNm}$$

Step 4 Check for depth.

$$M_{max} = 30.17 \text{ kNm}$$

$$\text{For Fe415 } M_o = 0.138 f_{ck} b d^2$$

$$d = \sqrt{\frac{M_o}{0.138 f_{ck} b}} = \sqrt{\frac{30.17 \times 10^6}{0.138 \times 25 \times 100}}$$

$$= 93 \text{ mm}$$

$$d_{cal} = 93 < (d_{max} = 105 \text{ mm}),$$

flange ok.

Step-5 Primary steel.

$$M_a = 30.17 \text{ kNm.}$$

$$M_u = 0.87 f_y A_{st} d \left(1 - \frac{f_y A_{st}}{f_{ck} b d} \right)$$

$$\frac{a}{d} = 1.2 - \sqrt{1.44 - \frac{6.6 M_u}{f_{ck} b d^2}}$$

$$= 1.2 \sqrt{1.44 - \frac{6.6 M_u}{f_{ck} b d^2}}$$

$$\frac{6.6 M_u}{f_{ck} b d^2} = 0.378$$

$$\frac{a}{d} = 0.169 < 0.48$$

It is a under reinforced.

$$\text{lever arm} = 105 (1 - 0.416 \times 0.169)$$

$$= 134.8 \text{ mm.}$$

Area of steel.

$$\frac{M_u}{0.87 f_y 2} = \frac{30.17 \times 10^6}{0.87 \times 415 \times 134.8} \\ = 620 \text{ mm}^2.$$

10 TMT bars

$$A\phi = \frac{\pi}{4} \times 10^2 = 78.5 \text{ mm}^2$$

$$n = \frac{A_t}{A\phi} = \frac{620}{78.5} = 7.89$$

$$\text{Spacing } s = \frac{1000}{n} = \frac{1000}{7.89} = 126 \text{ mm}$$

max. spacing is the least of

$$i) 3d = 3 \times 145 = 435 \text{ mm.}$$

$$ii) 300 \text{ mm.}$$

$$S_{\text{max}} = 300 \text{ mm.}$$

10 TMT @ 180 mm clc.

$$A_{st} \text{ provided} = \frac{1000}{S} A_{st}$$

$$= \frac{1000}{120} \times \frac{\pi}{4} \times 10^2 = 650 \text{ mm}^2.$$

$$\% \text{ of steel} = \frac{A_{st}}{bt} \times 100$$

$$= \frac{650}{1000 \times 145} \times 100 = 0.45 \%$$

Step 6 Secondary steel.

$$M_{\text{allow}} = 1.2 - \sqrt{1.00 - \frac{6.6 M_0}{f_{ck} b d^2}}$$

$$\frac{a}{d} = 0.08 < 0.48$$

Hence. Ok.

$$\text{less arm } z = d \left(1 - 0.416 \times \frac{a}{d} \right)$$

$$= 318.3 \text{ mm.}$$

Assume 10 TMT.

$$A_{st} = 788$$

$$n = \frac{A_{st}}{A_{st}} = 1.05$$

$$S = \frac{1000}{n} = 246 \text{ mm} \quad (d = 135 \text{ mm})$$

$$\text{Span } 8) 3d = 3 \times 135 \\ = 405 \text{ mm.}$$

(i) 180 mm.

Provide 10 TMT @ 220 mm c/c.

$$\text{Ast provide} = \frac{1000}{S} A\phi$$

$$= \frac{1000}{220} \times 78.5$$

$$= 356.9 \text{ mm}^2.$$

$$\% \text{ of steel} = \frac{356.9}{1000 \times 135} \times 100 = 0.24\%$$

$$\left(\frac{356.9}{1000 \times 135} \times 100 \right) \\ = 0.26$$

Check for deflection.

For simply supported case $\frac{l}{d} = 20$.

$$M_{25} f_s = 0.58 f_y \times 0.58 \times 115 \times \frac{620}{654} \\ = 228.18 \text{ N/mm}^2$$

Modification factor = 1.5.

$$\left(\frac{l}{d}\right)_{max} = 20 \times 1.5 = 30$$

$$\left(\frac{l}{d}\right)_{provide} = \frac{1000}{145} = 27.6 < 30$$

Hence OK.

Summary :-

Depth of slab = 170 mm

C.C = 20 mm.

Primary 10 TMT @ 120 mm c/c.

Secondary 10 TMT @ 220 mm c/c.