## 7-5: Probabilistic Matrix Factorization

#### Introduction

- Linear algebra isn't the only matrix factorization basis
- This lecture: matrix factorization approaches with a probabilstic basis

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## Probabilistic Modeling

- Many interesting algorithms are based on probabilistic models
- Basic idea:
  - Assume that data is generated by random process (with known structure)
  - Learn parameters that would generate data that looks like what you have

## Popularity Model

- Non-personalized probabilistic model
- P(I) is # of times i was bought, scaled to probability
  - Divide by total # of purchases

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#### Personalized

- Goal: compute P(i|u)
  - Probability that user u will select item i
- Problem: many, many parameters
- Also, we don't know for items the user hasn't bought!

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#### PLSI and LSI (SVD)

- Probabilistic has same form as SVD
  - $M = U\Sigma V^T$
- Left and right vectors are stochastic, not orthogonal
  - That is, they encode probability distributions
- Learned with expectation maximization

## Probabilistic Latent Semantic Analysis

- Goal: estimate P(i|u)
  - Probability that user u will select item i
- Decompose with latent factors

$$P(i|u) = \sum_{z} P(i|z)P(z|u)$$

- P(z|u) user picks a random feature
- P(i|z) user picks movie for feature
- User preference broken down to feature preference

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#### PLSI with Ratings

- Basic idea: model ratings as a distribution (e.g. gaussian)
- Distribution parameters determined by item, user, and/or latent feature

#### **PMF**

- Alternate formulation of probabilistic factorization of ratings matrix
- Models ratings as drawn from normal distributions
  - Mean determined by user and item via features
  - Not simple probability matrices like PLSI
- Faster to train than PLSI

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#### Further Reading

- Matrix factorization, both probabilistic and not, is core to many current algorithms
- Other latent feature models
  - Restricted Boltzman machines
  - Neural nets generally

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