

Yaniv Bronshtein HW1 Regression and Time Series

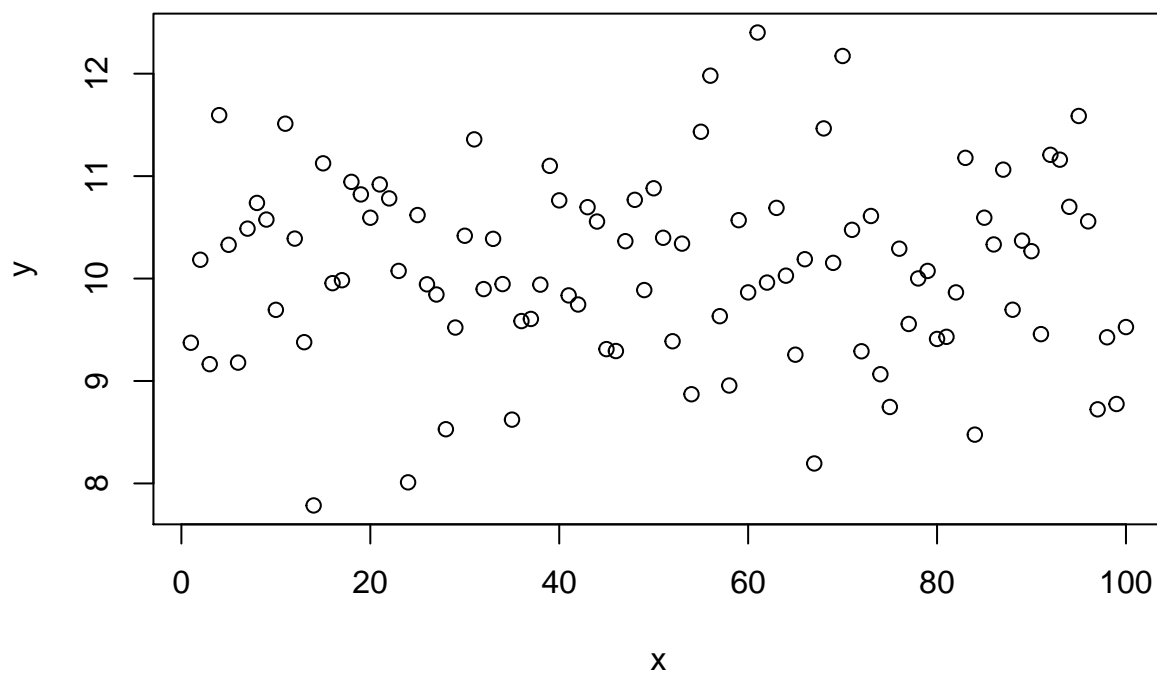
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#Question 1

(1) Create a column of y that includes 100 random sample from a normal distribution with mean=10 and sd=1

```
set.seed(1)
y <- matrix(rnorm(n=100, mean=10, sd=1))
#(2) Create a column of  $x$  that includes numbers 1 to 100
x <- matrix(1:100)
#(3) Draw a scatter plot using R. Based on the figure, do you think
# $x$  and  $y$  are correlated?
plot(x,y)
```



```
corr <- cor(x,y)
corr
```

```
##           [,1]
## [1,] -0.01456896
```

Based on the plot and the result of `cor()`, I do not believe that x and y are correlated. The value is -0.01456896 which is very close to 0

(4) Fit a regression model $y = B_0 + B_1 * x + \text{epsilon}$ and obtain the R^2 value.

```
lm_model <- lm(formula=y~x)
summary <- summary(lm_model)
r_sq <- summary$r.squared
r_sq
```

```
## [1] 0.0002122545
```

(5) Fit a regression model $y = ??x + \text{epsilon}$ and obtain the R^2 value.*

Compare this R^2 value with the one you have in (4) and **** explain which one is more reasonable.**

Which model you will recommend?

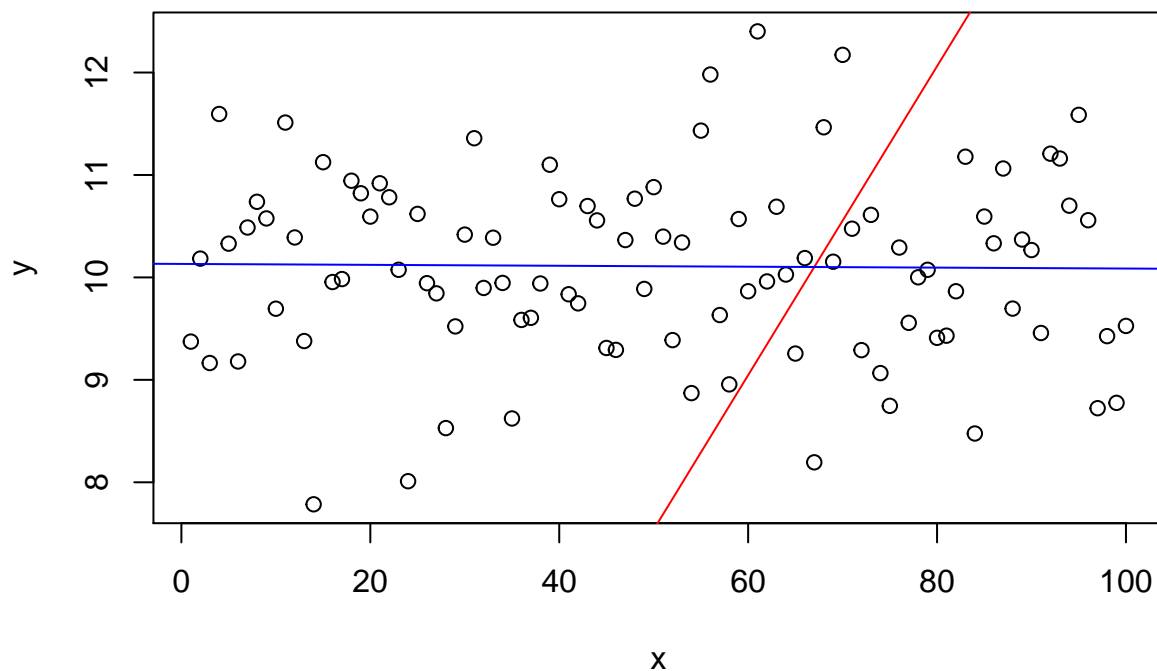
```
lm_model_2 <- lm(formula = y~x+0)
summary2 <- summary(lm_model_2)
r_sq2 <- summary2$r.squared
r_sq2
```

```
## [1] 0.7467852
```

The new R^2 is 0.7467852. The new R^2 is much higher and according to standards, is in a good range. If the R^2 had been significantly higher, it would signal likely over-fitting. I would recommend the second model as the first one suffers from under-fitting which explains why the R^2 is so low. The sum of squared distance between the points and the regression line is very high.

(6) Based on the model that you recommend in (5), is x an important factor to y ? Is this conclusion consistent with the **one** you have in (3)?**

```
plot(x,y)
#Better model
abline(lm_model_2, col='red')
#Worse model
abline(lm_model, col='blue')
```



Based on the model I recommended in (5), we still cannot tell if x is an important factor to y because R^2 for the model is high while the correlation calculated mathematically and observed visually in the plot shows inconsistency between (3) and (5)