

Why Deep Learning rocks

A philosophical note

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No free lunch

Terminology

Machine Learning is about learning algorithms A that:

- › defined on sample set \mathcal{X} (e.g. \mathbb{R}^n) and targets \mathcal{Y} (e.g. $\{0, 1\}$);
- › take a problem (dataset) $D = (X, y) \subseteq \mathcal{X} \times \mathcal{Y}$;
- › learn relation between \mathcal{X} and \mathcal{Y} ;
- › and return prediction function:

$$\begin{aligned} A(D) &= f \\ f : \mathcal{X} &\rightarrow \mathcal{Y} \end{aligned}$$

No free lunch theorem

No free lunch theorem states that **on average** by all datasets all learning algorithms are equally bad at learning.

Examples:

- › crazy algorithm:

$$f(x) = \left\lfloor \left(\left[\sum_i x_i + \theta \right] \mod 17 + 1027 \right)^\pi \right\rfloor \mod 2$$

- › SVM

perform equally well **on average**.

No free lunch

Try to learn yourself! Predict missing y.

$$X = \begin{pmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} y = \begin{pmatrix} 0 \\ 2 \\ 3 \\ 1 \\ 1 \\ 4 \\ 3 \\ ? \end{pmatrix}$$

No free lunch

| It is binary... obviously...

$$X = \begin{pmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} y = \begin{pmatrix} 0 \\ 2 \\ 3 \\ 1 \\ 1 \\ 4 \\ 3 \\ ? \end{pmatrix}$$

$$X = \begin{pmatrix} 4 \\ 6 \\ 7 \\ 3 \\ 5 \\ 0 \\ 1 \\ 2 \end{pmatrix} y = \begin{pmatrix} 0 \\ 2 \\ 3 \\ 1 \\ 1 \\ 4 \\ 3 \\ ? \end{pmatrix}$$

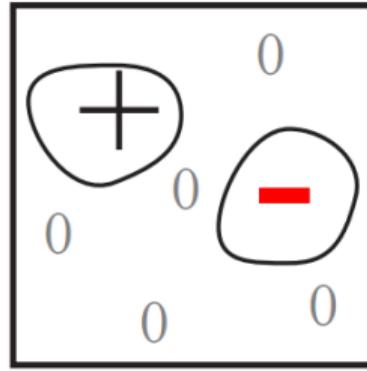
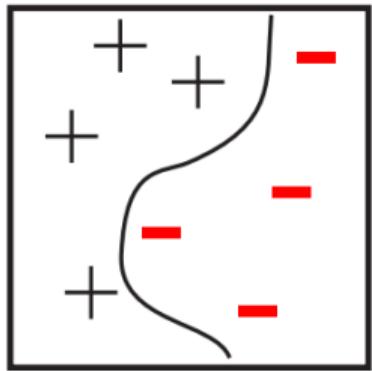
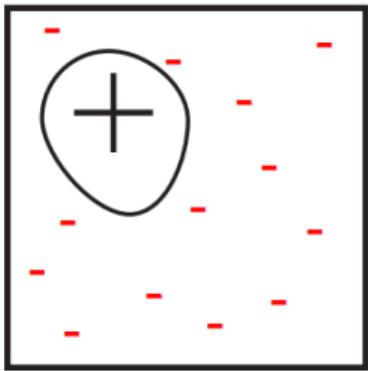
$$X = \begin{pmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{pmatrix} y = \begin{pmatrix} 4 \\ 3 \\ ? \\ 1 \\ 0 \\ 1 \\ 2 \\ 3 \end{pmatrix}$$

No free lunch

| And dependency was: $y = |x - 4|$.

$$X = \begin{pmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \quad y = \begin{pmatrix} 0 \\ 2 \\ 3 \\ 1 \\ 1 \\ 4 \\ 3 \\ 2 \end{pmatrix}$$
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No free lunch theorem



Possible learning algorithm behaviours in **problem space**:

- › **+** - better than the average;
- › **-** - worse than the average.

Are Machine Learning algorithms useless?

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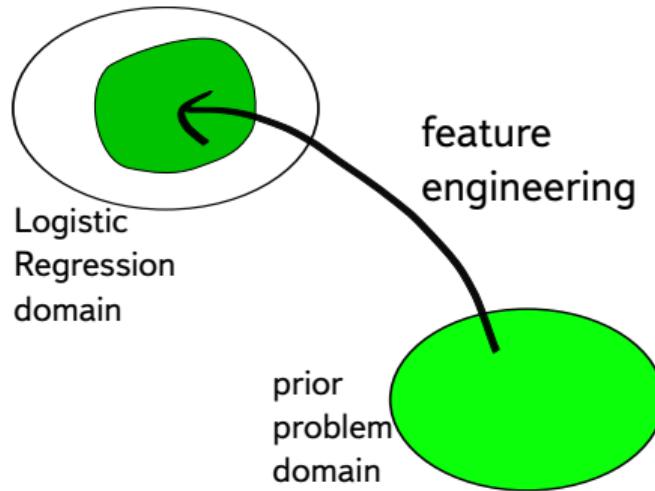
No.

Are Machine Learning algorithms useless?

- › Machine Learning algorithms have data scientists;
- › data scientists are an additional source of prior information;
- › prior information helps to bypass No Free Lunch Theorem.

Traditional Machine Learning

- › analyse the problem and make assumptions;
- › pick an algorithm from a toolkit (e.g. logistic regression);
- › provide assumptions suitable for the algorithm (**feature engineering**).



Discussion

- › this approach works well for traditional datasets with a small number of features:
- › e.g. Titanic dataset:

passenger class	name	sex	age	fare	...
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Essentially, performance of the algorithm depends data scientist's ability to generate features.

- › but our abilities are limited.

Kitten



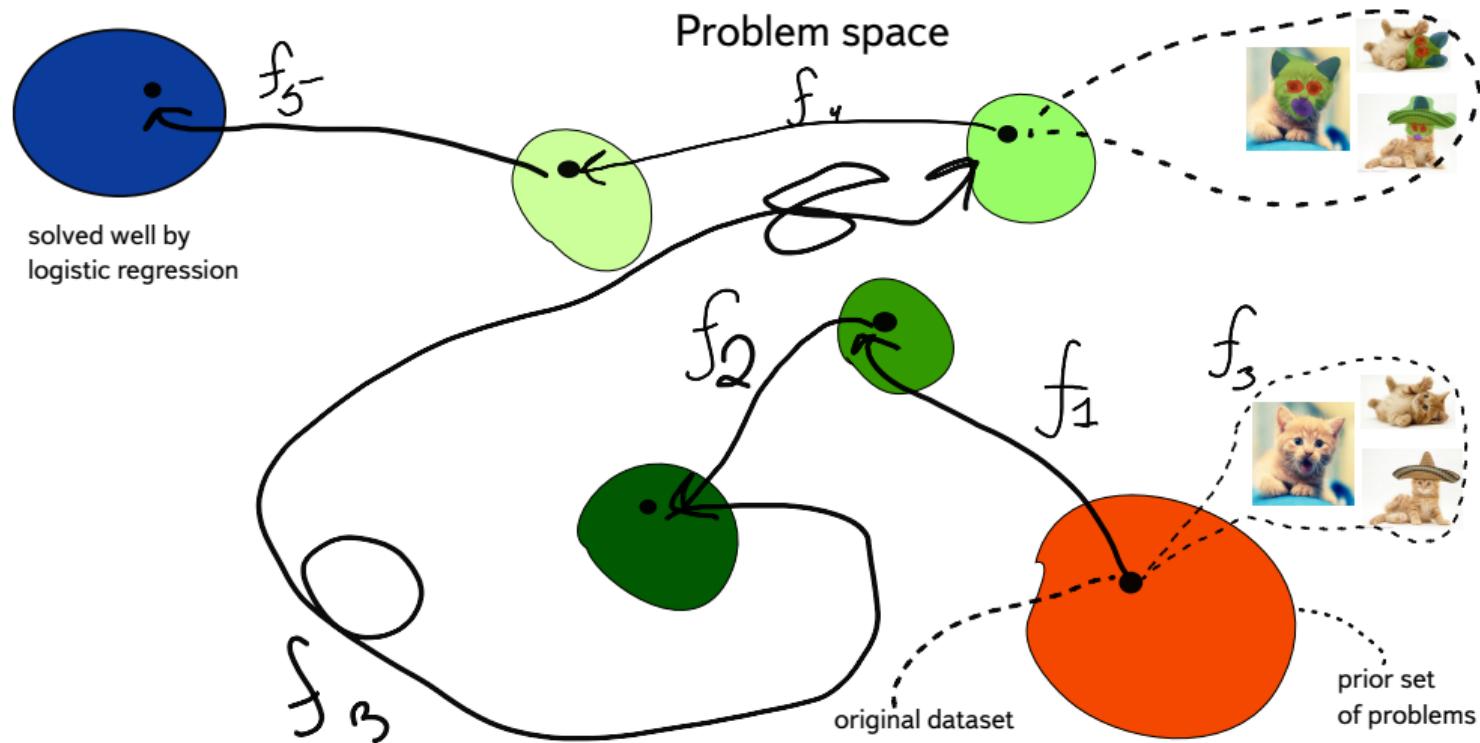
Kitten seen by a machine

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[ [ 22 25 28 32 29 ..., 58 36 35 34 34]
  [ 26 29 30 31 36 ..., 65 38 42 41 42]
  [ 27 28 31 30 40 ..., 84 58 51 52 44]
  [ 27 26 27 29 43 ..., 90 70 60 57 43]
  [ 20 26 28 28 31 ..., 83 73 62 52 45]
  ...,
  [173 187 180 183 184 ..., 170 227 244 219 199]
  [193 199 194 188 185 ..., 181 197 201 209 187]
  [175 177 156 166 171 ..., 226 215 194 185 182]
  [161 159 160 187 178 ..., 216 193 220 211 200]
  [178 180 177 185 164 ..., 190 184 212 216 189] ]
```

Solution?

- › edge detection;
- › image segmentation;
- › eyes, ears, nose models;
- › fit nose, ears, eyes;
- › average color of segments;
- › standard deviation of color segments;
- › goodness of fit for segments;
- › kitten's face model;
- › feed it to Logistic Regression

Solution?



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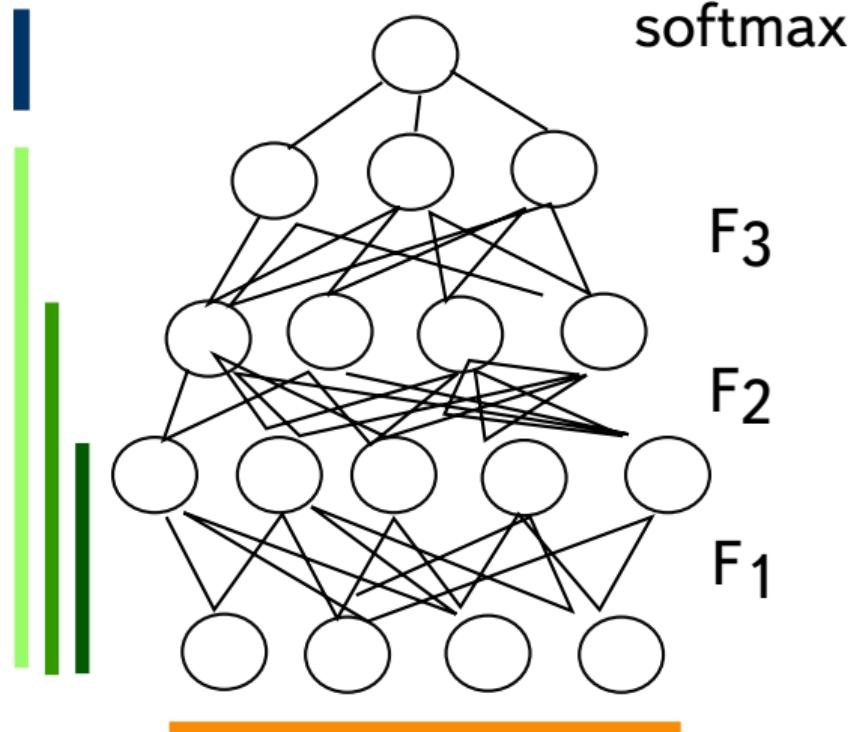
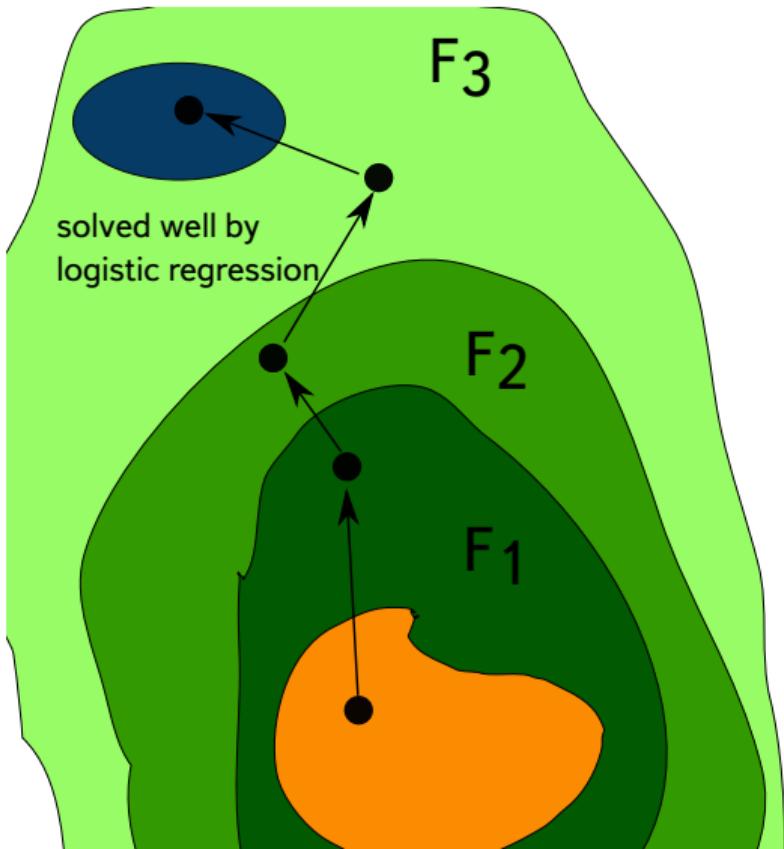
Perhaps, more Machine Learning and less Human Engineering?

Deep Learning

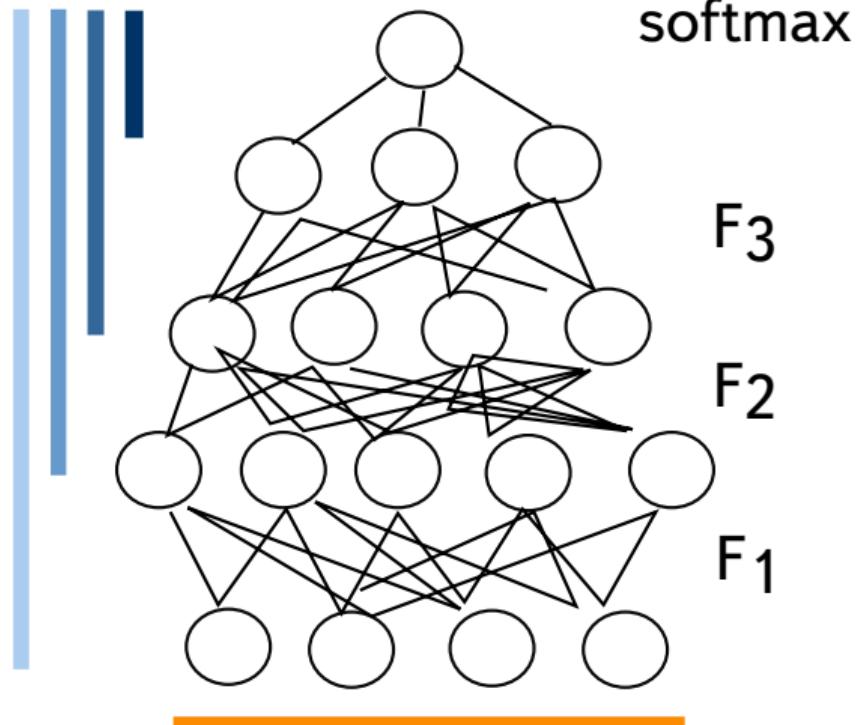
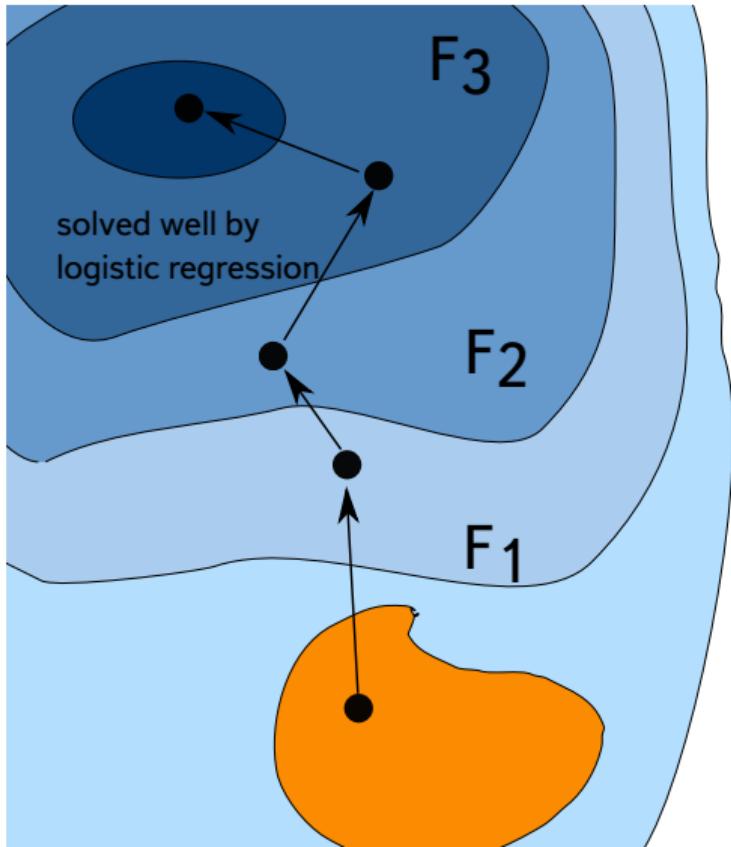
Deep Learning

Let's learn features!

Deep Learning



Deep Learning



Kitten

Traditional approach:

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Deep Learning:

- › convolutions;
- › logistic regression.

Why deep?

- › new set of features is generated from previous one by a simple learnable transformation;
- › each step increases complexity of feature generation;
- › high-level features (kitten or puppy) are complex ones thus requires a lot of steps;
- › therefore, deep.

Deep Learning

- › is not a superior algorithm;
- › is not even a single algorithm;
- › is a framework;
- › very flexible framework;
- › allows to express our assumptions in much more general way.

Why DL rocks

- › can crack much harder problems;
 - › it is easier to formulate models for features than features itself;
- › easy to construct networks:
 - › merge together;
 - › bring new objectives;
 - › inject something inside network;
 - › build networks inside networks;
 - › any differentiable magic is allowed.

Example

A problem contains groups of features:

- › velocity features, m/s ;
- › distance features, m ;
- › time features, s ;
- › acceleration features, m/s^2 .

Prior knowledge: different groups of features can not be summed.

Downsides

- › learning features requires data;
 - › big datasets;
 - › big computational resources (GPUs);
- › there is almost always a better algorithm;
 - › with hand-made features;
 - › probably constructed by a super-intelligent alien.

Summary

Summary

Deep Learning:

- › a flexible framework;
- › allows to express your knowledge easier;
- › solves much harder problems.