Lifting Resugaring by Lazy Desugaring

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Syntactic sugar, first coined by Peter J. Landin in 1964, has proved to be very useful for defining domain specific languages and extending languages. Unfortunately, when syntactic sugar is eliminated by transformation, it obscures the relationship between the user's source program and the transformed program. Resugaring is a powerful technique to resolve this problem, which automatically converts the evaluation sequences of desugared expression in the core language into representative sugar's syntax in the surface language. However, the traditional approach relies on reverse application of desugaring rules to desugared core expression whenever possible. When a desugar rule is complex and a desugared expression is large, such reverse desugaring becomes very complex and costive.

In this paper, we propose a novel approach to resugaring by lazy desugaring, where reverse application of desugaring rules is unnecessary. We recognize a sufficient and necessary condition for a syntactic sugar to be desugared, and propose a reduction strategy, based on evaluator of the core languages and the desugaring rules, which is sufficient to produce all necessary resugared terms on the surface language. We show that this approach can be made more efficient by automatic derivation of evaluation rules for syntactic sugars. We have implemented a system based on this new approach. Compared to the traditional systems, the new system is not only more efficient, but also more powerful in that it cannot only deal with all cases (such as hygienic and simple recursive sugars) published so far, but can do more allowing more flexible recursive sugars.

Additional Key Words and Phrases: Resugaring, Syntactic Sugar, Interpreter, Domain-specific language, Reduction Semantics

1 INTRODUCTION

Syntactic sugar, first coined by Peter J. Landin in 1964 [Landin 1964], was introduced to describe the surface syntax of a simple ALGOL-like programming language which was defined semantically in terms of the applicative expressions of the core lambda calculus. It has proved to be very useful for defining domain specific languages (DSLs) and extending languages [Culpepper et al. 2019; Felleisen et al. 2018]. Unfortunately, when syntactic sugar is eliminated by transformation, it obscures the relationship between the user's source program and the transformed program.

Resugaring is a powerful technique to resolve this problem [Pombrio and Krishnamurthi 2014, 2015]. It can automatically convert the evaluation sequences of desugared expression in the core language into representative sugar's syntax in the surface language. As demonstrated in Section 2, the key idea in this resugaring is "tagging" and "reverse desugaring": it tags each desugared core term with the corresponding desugared rule, and follows the evaluation steps in the core language but keep applying the desugaring rules reversibly as much as possible to find surface-level representations of the tagged core terms.

While it is natural to do resugaring by reverse desugaring of tagged core terms, it introduces complexity and inefficiency.

- *Tricky to handle recursive sugar*. While tagging is used to remember the position of desugaring so that reverse desugaring can be done at correct position when desugared core expression is evaluated, it becomes very tricky and complex when recursive sugars are considered. Moreover, it can only handle the recursive sugar which can be written by pattern-based desugaring rules [Pombrio and Krishnamurthi 2014].

- *Complicated to handle hygienic sugar.* For reverse desugaring, we need to match part of the core expression on the RHS of the desugar rule and to get the surface term by substitution. But when a syntactic sugar introduce variable bindings, this match-and-substitute turns out to be very complex if we consider local bindings (hygienic sugars) [Pombrio and Krishnamurthi 2015].
- *Inefficient in reverse desugaring.* It need to keep checking whether reverse desugaring is applicable during evaluation of desugared expression, which is very costive. Moreover, the match-and-substitute for reverse desugaring is costive particularly when the core term is big.

In this paper, we propose a novel approach to resugaring, which does not use tagging and reverse desugaring at all. The key idea is "lazy desugaring", in the sense that desugaring is delayed so that the reverse application of desugaring rules become unnecessary. To this end, we consider the surface language and the core language as one language, and reduce expressions in such a smart way that all resugared terms can be fully produced based on the reduction rules in the core language and the desugaring rules for defining syntactic sugars. To gain more efficiency, we can compress a sequence of core expression reductions into a one-step reduction of the surface language, by automatically deriving evaluation rules of the syntactic sugars based on the syntactic sugar definition and evaluation rules of the core language.

Our main technical contributions can be summarized as follow.

- We propose a novel approach to resugaring by lazy desugaring, where reverse application of desugaring rules becomes unnecessary. We recognize a sufficient and necessary condition for a syntactic sugar to be desugared, and propose a reduction strategy, based on evaluator of the core languages and the desugaring rules, which is sufficient to produce all necessary resugared terms on the surface language. We prove the correctness of our approach.
- We show that evaluation rules for syntactic sugars can be fully derived for a wide class of desugaring rules and the evaluation rules of the core language. We design an inference automaton to capture relationship between language constructs based on the evaluation and desugaring rules, and derive evaluation rules for new syntactic sugars from the inference automaton. These evaluation rules, if derivable, can be seamlessly used with lazy desugaring to make resugaring more efficient.
- We have implemented a system based on the new resugaring approach. It is much more efficient than the traditional approach, because it completely avoids unnecessary complexity of the reverse desugaring. It is more powerful in that it cannot only deal with all cases (such as hygienic and simple recursive sugars) published so far [Pombrio and Krishnamurthi 2014, 2015], but can do more allowing more flexible recursive sugars. All the examples in this paper have passed the test of the system.

The rest of our paper is organized as follow. We start with an overview of our approach in Section 2. We then discuss the core of resugaring by lazy desugaring in Section 3, and automatic derivation of evaluation rules for syntactic sugars in Section 4. We describe the implementation and show some applications as case studies in Section 5. We discuss relative work in Section 6, and conclude the paper in Section 6.

2 OVERVIEW

In this section, we give a brief overview of our approach, explaining its difference from the traditional approach and highlighting its new features. To be concrete, we will consider the following

simple core language, defining the if expressions:

$$e ::= (if\ e\ e\ e)$$
$$|\quad \#t\ //\text{true boolean}$$
$$|\quad \#f\ //\text{false boolean}$$

The semantics of the language is very simple, consisting of the following context rule defining the computation order:

$$\frac{e \rightarrow e'}{(if\ e\ e1\ e2) \rightarrow (if\ e'\ e1\ e2)} \qquad \text{(CONTEXT RULE OF IF)}$$

and two reduction rules:

$$(if\ \#t\ e1\ e2) \rightarrow e1 \qquad \text{(REDUCTION RULE OF IFTRUE)}$$

$$(if\ \#f\ e1\ e2) \rightarrow e2 \qquad \text{(REDUCTION RULE OF IFFALSE)}$$

Assume that our surface language is defined by two syntactic sugars—*and* sugar and *or* sugar on the core language.

$$(and\ e1\ e2) \rightarrow_d (if\ e1\ e2\ \#f)$$
$$(or\ e1\ e2) \rightarrow_d (if\ e1\ \#t\ e2)$$

Now let us demonstrate how to execute (and (or #t #f) (and #f #t)), and get the following resuaring sequence.

```
      (and (or #t #f) (and #f #t))
⟶  (and #t (and #f #t))
⟶  (and #t #f)
⟶  #f
```

2.1 Traditional Approach: Tagging and Reverse Desugaring

As we discussed in the introduction, the traditional approach uses "tagging" and "reverse desugaring" to get resugaring sequences; tagging is to mark where and how the core terms are from, and reverse desugaring is to resugar core terms back to surface terms. Putting it simply, the traditional resugaring process is as follows.

```
      (and (or #t #f) (and #f #t))
⇢   { fully desugaring and tagging }
      (if-andtag (if-ortag #t #t #f) (if-andtag #f #t #f) #f)
⟶   { context rule of if, reduction rule of if-false}
      (if-andtag #t (if-andtag #f #t #f) #f)
⟶   { emit (and #t (and #f #t)) by reverse desugaring, reduction rule of if-true}
      (if-andtag #f #t #f) //check resugarable
⟶   { emit (and #f #t) by reverse desugaring, reduction rule of it-false}
      #f
```

148   In the above, the surface expression is fully desugared before resugaring. It is worth noting that
149   some desugared subexpressions (e.g., the `if-andtag` subexpression) are not touched in the first
150   two steps after desugaring, but each reverse desugaring tries on them, which is redundant and cos-
151   tive. This would be worse in practice, because we usually have lots of intermediate reduction steps
152   which will be tried by reverse desugaring (but may not succeed) during the evaluation of a more
153   complex core language. Therefore many useless resugarings on subexpressions take place in the
154   traditional approach. Moreover, reverse resugaring would introduce complexity in the resugaring
155   process, as discussed in the introduction.

2.2 Our Approach: Resugaring by lazy Desugaring

To solve the problem in the traditional approach, we propose a new resugaring approach by elimi-
nating "reverse desugaring" via "lazy desugaring", where a syntactic sugar will be desugared only
when it is necessary. We test the necessity of desugaring by a one-step try. We shall first briefly
explain our one-step try resugaring method, and then show that how the "one-step try" can be
cheaply done by derivation of evaluation rules for syntactic sugars.

```
        (resugar (and (or #t #f) (and #f #t)))
  ⇢     { a one-step try on the outermost and }
        (try (if (or #t #f) (and #f #t) #f))
  ⟶     { should reduce on subexpression (or #t #f) of and, delay desugaring of and}
        (and (resugar (or #t #f)) (and #f #t)) // no reduction
  ⇢     { a one-step try on or }
        (and (try (if #t #t #f)) (and #f #t))
  ⟶     { keep this try, finish inner resugaring, and return to the top }
        (resugar (and #t (and #f #t)))
  ⇢     { a one-step try on the outermost and }
        (try (if #t (and #f #t)))
  ⟶     { keep this try, finish inner resugaring, and return to the top }
        (resugar (and #f #t))
  ⇢     { a one-step try on the outermost and }
        (try (if #f #t #f)) // have to desugar and reduce
  ⟶ #f
```

For each step in the above, we make one reduction step and move resugaring focus if desugaring
is unnecessary. So 7 reduction steps are needed for our whole resugaring, while the traditional
approach needs 9 steps (3 in desugaring, 3 in evaluation, 3 for reverse resugaring). Note that
reverse desugaring is more complex and costive because of match and substitution. Note also that
the traditional approach would be more redundant if it works on larger expressions.

    We can go further to make our approach more efficient. As the purpose of a "one-step try"
is to determine the computation order of the syntactic sugar, we should be able to derive this
computation order through the desugar rules and the computation orders of the core language,
rather than just through runtime computation of the core expression as done in the above. As will
be shown in Section 4, we can automatically derive evaluation rules (consist of the context rules

and reductions rules) for both *and* sugar and *or*.

$$\frac{e_1 \rightarrow e_1'}{(\text{and } e_1 \ e_2) \rightarrow (\text{and } e_1' \ e_2)} \qquad (\text{and } \#t \ e2) \rightarrow e_2 \quad (\text{and } \#f \ e2) \rightarrow \#f$$

$$\frac{e_1 \rightarrow e_1'}{(\text{or } e_1 \ e_2) \rightarrow (\text{or } e_1' \ e_2)} \qquad (\text{or } \#t \ e2) \rightarrow \#t \quad (\text{or } \#f \ e2) \rightarrow e_2$$

Now with these rules, our resugaring will need only 4 steps.

```
       (and (or #t #f) (and #f #t))
  ⟶ (and #t (and #f #t))
  ⟶ (and #f #t)
  ⟶ #f
```

Two remarks are worth making here. First, we do not require a complete set of reduction/context rules for all syntactic sugars; if we have these rules, we can elaborate them to remove one-step try, and make a shortcut for a sequence of evaluation steps on core expression. For example, suppose that we have another syntactic sugar named *hard* whose evaluation rules cannot be derived. We can still do resugaring on (and (hard (and #t #t) ...) ...), as we do early. Second, our example does not show the case when a surface expression contains language constructs of the core expression. This does not introduce any difficulty in our method, as we have no reverse desugaring, so there is no worry about desugaring an original core expression to a syntactic sugar. For instance, we can deal with (and (if #t then (and #f #t) #f) #f), without resugaring it to (and (and #t (and #f #t) #f).

2.3 New Features

As will be seen clearly in the rest of this paper, our approach has the following new features.

- *Efficient.* As we do not have "tagging" and costive and repetitive "reverse desugaring", our approach is much more efficient than the traditional approach. As discussed above, by deriving reduction/context rules for the syntactic sugars, we can gain more efficiency.
- *Powerful.* As we do not have "reverse desugaring", we can avoid complicated matching when we want to deal with local bindings (hygienic sugars) or more involved recursively defined sugars (see map in Section 5.2.3).
- *Lightweight.* Our approach can be cheaply implemented using the PLT Redex tool [Felleisen et al. 2009]. This is because our "lazy" desugaring is much more simpler than "reverse desugaring" that needs careful design of patterns, and matching/substitution algorithms.

3 RESUGARING BY LAZY DESUGARING

In this section, we present our new approach to resugaring. Different from the traditional approach that clearly separates the surface and the core languages, we combine them together as one mixed language, allowing users to freely use the language constructs in both languages. We will show that any expression in the mixed language can be evaluated in such a smart way that a sequence of all expressions that are necessarily to be resugared by the traditional approach can be correctly produced.

3.1 Mixed Language for Resugaring

We will define a mixed language for a given core language and a surface language defined over the core language. An expression in this language will be reduced step by step by the reduction

$$
\begin{array}{llll}
\texttt{CoreExp} & ::= & x & \text{variable} \\
 & | & c & \text{constant} \\
 & | & (\texttt{CoreHead' CoreExp}_1 \ \ldots \ \texttt{CoreExp}_n) & \text{constructor} \\
 & | & (\texttt{CommonHead SurfExp}_1 \ \ldots \ \texttt{SurfExp}_n) & \text{selected core constructor} \\
 & & & \\
\texttt{SurfExp} & ::= & x & \text{variable} \\
 & | & c & \text{constant} \\
 & | & (\texttt{SurfHead SurfExp}_1 \ \ldots \ \texttt{SurfExp}_n) & \text{sugar expression}
\end{array}
$$

Fig. 1. Core and Surface Expressions

rules for the core language and the desugaring rules for defining the syntactic sugars in the surface language.

3.1.1 Core Language. For our host language, we consider its evaluator as a blackbox but with two natural assumptions. First, there is a deterministic stepper in the evaluator which, given an expression in the host language, can deterministically reduce the expression to a new expression. Second, the evaluation of any sub-expression has no side-effect on other parts of the whole expression.

An expression of the core language is defined in Figure 1. It is a variable, a constant, or a (language) constructor expression. Here, `CoreHead` stands for a language constructor such as `if` and `let`. To be concrete, we will use a simplified core language defined in Figure 2 to demonstrate our approach. Todo: semantic needed?

```
CoreExp  ::=  (CoreExp CoreExp ...) // apply
         |    (lambda (x ...) CoreExp) // call-by-value
         |    (lambdaN (x ...) CoreExp) // call-by-need
         |    (if CoreExp CoreExp CoreExp)
         |    (let (x CoreExp) CoreExp)
         |    (first CoreExp)
         |    (empty CoreExp)
         |    (rest CoreExp)
         |    (cons CoreExp CoreExp)
         |    (arithop CoreExp CoreExp) // +, -, *, /, >, <, =
         |    x
         |    c // boolean, number and list
```

Fig. 2. A Core Language Example

3.1.2 Surface Language. Our surface language is defined by a set of syntactic sugars, together with some basic elements in the core language, such as constant and variable. So an expression of the surface language is some core constructor expressions with sugar expressions, as defined in Figure 1.

A syntactic sugar is defined by a desugaring rule in the following form:

$$(\textsf{SurfHead } e_1 \ e_2 \ \ldots \ e_n) \rightarrow_d \textsf{Exp}$$

where its LHS is a simple pattern (unnested) and its RHS is an expression of surface language or core language, and any reducible sub-term (e.g. e_1) in LHS only appears once in RHS. For instance,

we may define syntactic sugar And by

$$(\text{And } e_1 \ e_2) \ \rightarrow_d \ (\text{if } e_1 \ e_2 \ \#f).$$

Note that if the pattern is nested, we can introduce a new syntactic sugar to flatten it. And if we need a reducible sub-term multi times in RHS, a `let` binding is needed (a normal way in syntactic sugar). We take the following sugar as example,

$$(\text{Twice } e_1) \ \rightarrow_d \ (+ \ e_1 \ e_1)$$

If we execute `(Twice (+ 1 1))`, the sugar expression will firstly desugar to `(+ (+ 1 1) (+ 1 1))`, then one step reduced to `(+ 2 (+ 1 1))`. The subexpression `(+ 1 1)` has reduced but cannot resugar to the surface, because the other `(+ 1 1)` has not reduced. It will let many intermediate steps omitted, if there are many reduction steps between reduction of them. So we just use a `let` binding to resolve it.

One may wonder why Todo: don't understand.. not restricting the RHS to be a core expression `CoreExp`, which sounds more natural. We use `surfExp` to be able to allow definition of recursive syntactic sugars, as seen in the following example.

$$(\text{Odd } e) \ \rightarrow_d \ (\text{if } (> \ e \ 0) \, (\text{Even} \, (- \ e \ 1)) \, \#f)$$
$$(\text{Even } e) \ \rightarrow_d \ (\text{if } (> \ e \ 0) \, (\text{Odd} \, (- \ e \ 1)) \, \#t)$$

We assume that all desugaring rules are not overlapped in the sense that for a syntactic sugar expression, only one desugaring rule is applicable.

```
Exp                ::=  DisplayableExp
                   |    UndisplayableExp

DisplayableExp     ::=  SurfExp
                   |    CommonExp
UndisplayableExp   ::=  CoreExp'
                   |    OtherSurfExp
                   |    OtherCommonExp

CoreExp            ::=  CoreExp'
                   |    CommonExp

CoreExp'           ::=  (CoreHead' Exp*)

SurfExp            ::=  (SurfHead DisplayableExp*)

CommonExp          ::=  (CommonHead DisplayableExp*)
                   |    c       // constant value
                   |    x       // variable

OtherSurfExp       ::=  (SurfHead Exp * UndisplayableExp Exp*)

OtherCommonExp     ::=  (CommonHead Exp * UndisplayableExp Exp*)
```

Fig. 3. Our Mixed Language

3.1.3 Mixed Language. Our mixed language for resugaring combines the surface language and the core language. The differences between terms in our core language (CoreLang) and those in our surface language (SurfLang) are identified by their Head. But there may be some terms in the core language should be displayed during evaluation, or we need some core terms to help us getting better resugaring sequences . So we defined CommonExp, which origin from CoreLang, but can be displayed in resugaring sequences. The Core'Exp terms are terms with undisplayable CoreHead (named CoreHead'). The SurfExp terms are terms with SurfHead and all subexpressions are displayable. The CommonExp terms are terms with displayable CoreLang's Head (named CommonHead), together with displayable subexpressions. There exists some other expressions during our resugaring process, which have displayable Head, but one or more subexpressions should not display. They are UndisplayableExp. We distinct the two kinds of expression for *abstraction* property (discussed in Section 3.3.2).

Take some terms in the core language in Figure 2 as examples. We may assume if, let, λ_N (call-by-name lambda calculus), empty, first, rest as CoreHead', op, λ, cons as CommonHead. Then we would show some useful intermediate steps.

Note that some expressions with CoreHead contains subexpressions with SurfHead, they are of CoreExp but not in core language, we need a tricky extension for the core language's evaluator.

3.2 Resugaring Algorithm

Our resugaring algorithm works on our mixed language, based on the evaluator of the core language and the desugaring rules for defining the surface language. Let $\rightarrow_e$ denote the one-step reduction of the core language (based on the blackbox stepper with extension), and $\rightarrow_d$ the one-step desugaring of outermost sugar. We define $\rightarrow_m$, the one-step reduction of our mixed language, as follows.

$$\frac{(\text{CoreHead } e_1 \ \ldots \ e_n) \rightarrow_e e'}{(\text{CoreHead } e_1 \ \ldots \ e_n) \rightarrow_m e'} \tag{ExtRed}$$

$$\frac{(\text{SurfHead } x_1 \ \ldots \ x_i \ \ldots \ x_n) \rightarrow_d e, \ e_i \rightarrow_m e_i''}{\exists i. \ e[e_1/x, \ldots, e_i/x_i, \ldots, e_n/x_n] \rightarrow_m e[e_1/x, \ldots, e_i'/x_i, \ldots, e_n/x_n]}{(\text{SurfHead } e_1 \ \ldots \ e_i \ \ldots \ e_n) \rightarrow_m (\text{SurfHead } e_1 \ \ldots \ e_i'' \ \ldots \ e_n)} \tag{SurfRed1}$$

$$\frac{(\text{SurfHead } x_1 \ \ldots \ x_i \ \ldots \ x_n) \rightarrow_d e}{\neg \exists i. \ e[e_1/x_1, \ldots, e_i/x_i, \ldots, e_n/x_n] \rightarrow_m e[e_1/x_1, \ldots, e_i'/x_i, \ldots, e_n/x_n]}{(\text{SurfHead } e_1 \ \ldots \ e_i \ \ldots \ e_n) \rightarrow_m e[e_1/x_1, \ldots, e_i/x_i, \ldots, e_n/x_n]} \tag{SurfRed2}$$

The CoreRed rule describes how our mixed language handles expressions with CoreHead—just leave it to the core language's evaluator with the extension. Then for the expression with SurfHead, we will firstly desugar the outermost sugar (identified by the SurfHead), then recursively executing $\rightarrow_m$. In the recursive call, if one of original subexpression e_i is reduced (SurfRed1), then the original sugar is not necessarily desugared, we should only reduce the subexpression e_i; if not (SurfRed2), then the sugar have to desugar.

Then our desugaring algorithm is defined based on $\rightarrow_m$.

393
394 $\mathrm{resugar}(e)$ =   **if** $\mathtt{isNormal}(e)$ **then** *return*
395   **else**
396   **let** $e \rightarrow_m e'$ **in**
397   **if** $e' \in \mathtt{DisplayableExp}$
398 $\mathtt{output}(e')$, $\mathrm{resugar}(e')$
399   **else** $\mathrm{resugar}(e')$

400   During the resugaring, we just call the mixed language's reduction ($\rightarrow_m$) on the input ex-
401 pression until the expression becomes a normal form. We use the DisplayableExp to restrict
402 immediate sequences to be output or not. It is more explicit compared to the traditional approach.
403 And because $\rightarrow_m$ will be executed recursively on the subexpressions, it can be optimized. (see in
404 5.1, because the current description is more easier to understand.)

405
406 ## 3.3 Correctness

407 Traditional resugaring works[Pombrio and Krishnamurthi 2014, 2015] define three properties for
408 correctness of resugaring. We think they are also reasonable to describe correctness of our ap-
409 proach. We describe the following properties in our mixed language's domain, then prove or dis-
410 cuss on them.

411   *Emulation.* For each reduction of an expression in our mixed language, it should reflect on one
412 step reduction of the expression totally desugared in the core language, or one step desugaring on
413 a syntactic sugar.

414   *Abstraction.* Only displayable expressions defined in our mixed language appear in our resugar-
415 ing sequences.

416   *Coverage.* No syntactic sugar is desugared before its sugar structure should be destroyed in core
417 language.

418
419 *3.3.1 Emulation.* It is a basic property for correctness. Since desugaring won't change an expres-
420 sion after totally desugared, what we need to prove is that a non-desugaring reduction in the mixed
421 language shows the exactly reduction which should appear after the expression totally desugared.
422 We express it by following lemma. (fulldesugar(exp) returns the expression after exp totally
423 desugared)

424   LEMMA 3.1. *For* $\mathsf{exp}=(\mathsf{SurfHead}\ e_1\ \ldots\ e_i\ \ldots\ e_n) \in \mathsf{SurfExp}$, *if* $\mathsf{exp} \rightarrow_m \mathsf{exp}'$
425 *and* fulldesugar*(exp)*≠fulldesugar*(exp')*, *then* fulldesugar(exp) $\rightarrow_c$ fulldesugar(exp')

426   DEFINITION 3.1 (EMULATION). *If the mixed language satisfies Lemma 3.1, then the resugaring*
427 *satisfies emulation property.*

428
429   LEMMA 3.2. *For* $\mathsf{exp} = (\mathsf{SurfHead}\ e_1\ \ldots\ e_i\ \ldots\ e_n)$, *if inputting* fulldesugar(exp) *to core lan-*
430 *guage's evaluator reduces the term original from* e_i *in one step, then the* $\rightarrow_m$ *will reduce* exp *at*
431 e_i.

432   PROOF OF LEMMA 3.2. For $(\mathsf{SurfHead}\ x_1\ \ldots\ x_i\ \ldots\ x_n) \rightarrow_d e$
433 if e is of normal form, the fulldesugar(exp) will not be reduced by core evaluator.
434 if e is headed with CoreHead, then according to the CoreRed rule, the $\rightarrow_e$ will execute on e
435 according to ExtRed, which will reduce the subexpression e_i according to the blackbox evalua-
436 tor with extension. Then the SurfRed2 rule will reduce e_i. Because of the extension of evaluator
437 reduces the subexpression in correct location, so it is for $\rightarrow_m$.
438 if e is headed with SurfHead, then the $\rightarrow_m$ will execute recursively on e. If the new one satisfies
439 the lemma, then it is for the former. Because any sugar expression will finally be able to desugar
440 to expression with CoreHead, it can be proved recursively.   □
441

PROOF OF LEMMA 3.1.

For SurfRed1 rule, (SurfHead e_1 ... e_i ... e_n) $\rightarrow_m$ (SurfHead e_1 ... e_i'' ... e_n), where e_i $\rightarrow_m$ e_i''. If fulldesugar(e_i)=fulldesugar(e_i''), then fulldesugar(Exp)=fulldesugar(Exp'). If not, what we need to prove is that, fulldesugar(Exp) $\rightarrow_c$ fulldesugar(Exp'). Note that the only difference between Exp and Exp' is the i-th subexpression, and we have proved the lemma 3.2 that the subexpression is the one to be reduced after the expression desugared totally, it will be also a recursive proof on the subexpression e_i.

For SurfRed2 rule, Exp' is Exp after the outermost sugar resugared. So fulldesugar(Exp)= fulldesugar(Exp').

□

So our resugaring approach satisfies evaluation property.

3.3.2 Abstraction. Abstraction is not a restrict properties, because each expression has its meaning. Users may choose what they want to output during the process. Traditional resugaring approaches use marks to determine whether to display a term generated by desugaring, or only changes on original terms will show.

We define the abstraction by catalog the expression in the mixed language, from the reason why we need resugaring—sugar expressions become unrecognizable after desugaring. So why cannot a recursive sugar's resugaring sequences show the sugars generated by itself? We think the users should be allowed to decide which terms are recognizable. Then during the resugaring process, if no unrecognizable term for the user appears in the whole expression, the expression should be shown as a step in resugaring sequences. Lazy resugaring, as the key idea of our approach, makes any intermediate steps retain as many sugar structures as possible, so the abstraction is easy.

3.3.3 Coverage. The coverage property is important, because resugaring sequences are useless if lose intermediate steps. By lazy desugaring, it becomes obvious, because there is no chance to lose. In Lemma 3.3, we want to show that our reduction rules in the mixed language is *lazy* enough. Because it is obvious, we only give a proof sketch here.

LEMMA 3.3. *A syntactic sugar only desugars when* necessary, *that means after a reduction on the fully-desugared expression, the sugar's structure is destroyed.*

DEFINATION 3.2 (COVERAGE). *If the reduction of mixed language satisfies Lemma 3.3, then the resugaring satisfies coverage property.*

PROOF SKETCH OF LEMMA 3.3. From Lemma 3.2, we know the $\rightarrow_m$ recursively reduces a expression at correct subexpression. Or the $\rightarrow_m$ will destroy the outermost sugar (of the current expression) in rule SurfRed2. Note that it is the only rule to desugar sugars directly (other rules only desugar sugars when recursively call SurfRed2), we can prove the lemma recursively if SurfRed1 is *lazy* enough.

In SurfRed2 rule, we firstly expand the outermost sugar and get a temp expression with structure of the outermost sugar. Then when we recursively call $\rightarrow_m$, the reduction result shows the structure has been destroyed, so the outermost sugar has to be desugared. Since the recursive reduction of a terminable (Some bad sugars may never stop which are pointless.) sugar expression will finally terminate, the lemma can be proved recursively. □

4 STATIC APPROACH

In this section, we introduce a static approach, which is more efficient than the one discussed above.

4.1 Inference Automaton

Based on the idea of DFA (Deterministic Finite Automaton), we designed inference automaton (IFA). An IFA describes the inference rules of a certain syntactic structure. To help readers better understand it, first we give a few examples, then we give the formal definition of IFA and proofs of theorems.

4.1.1 IFA of if. The inference rules of if are shown as AAAR1. We can observe that an if term is first evaluated for e1, and is chosen to be evaluated for e2 and e3 depending on the value of it, then the result of the evaluation of e2 or e3 is the result of the evaluation of the term. Thus, we use AAAP1 to represent the inference rules of if.

The arrow from e1 to e2 indicate that this branch will be selected when the result of the e1 evaluation is #t. The arrows between e1 and e3 are the same. The double circles of e2 and e3 denotes that their evaluation result is the result of the syntactic structure. When a term with an if syntactic structure needs to be evaluated (for example if (if #t #t #f) #f #t)), first evaluating the e1 (if #t #t #f) part. Note that in this process, evaluating a subexpression requires running another automaton based on its syntax, while the outer automaton hold the state at e1. According to the result of e1 (#f), the IFA selects the branch (e3). Then the result of e3 (#t) will be the evaluation result of the term.

4.1.2 IFA of nand. Sometimes the rules may be more complex, such as being reduced into another syntactic structure, or the term contains other syntactic structures. For example, we can express nand's inference rule in the form of AAAR2. Based on the method discussed above, we can draw nand's IFA as AAAP2.

When the automaton runs to the last node, its evaluation rule is essentially an evaluation of the if syntax structure. Thus we can replace the last node with an IFA_if and use the IFA_if termination nodes as the termination nodes of the IFA_Nand. The results are shown in AAAP3. Further decomposing the intermediate nodes, connecting the terminating node of IFA_if to the node pointed to by the original output edge, we get AAAP4.

As can be seen, the nodes of IFA in AAAP4 have only the forms e_i, v_i and values, and no other composite syntactic structure. We call such an IFbA a *standard IFA*.

4.1.3 IFA of or. We represent the inference rule of or in a more complex way, as shown in AAAR3. In this case, we use the let binding, which expresses a class of rules containing substitution. At this point, we need to record the term represented by each variable at each node, denoted by Γ. The representation of IFA_or is shown in AAAP5.

More generally, the handling of substitution tables will be more complex. We will discuss this in more detail in AAAF1.

4.1.4 Definition of IFA.

DEFINATION 4.1 (INFERENCE AUTOMATON). *An inference automaton (IFA) of syntactic structure* (Headid $e_1 \dots e_n$) *is a 5-tuple,* $(Q, \Sigma, q_0, F, \delta)$*, consisting of*

- *A finite set of nodes Q, each node contains a term and a symbol table*
- *A finite set of pattern* Σ
- *A start node* $q_0 \in Q$
- *A set of terminal nodes* $F \subseteq Q$
- *A transition function* $\delta : (Q - F) \times \Sigma' \to Q$ *where* $\Sigma' \subseteq \Sigma$

and for each node q, there is no sequence of pattern $P = (p_1, p_2, \dots, p_n) \subseteq \Sigma^*$*, which makes that after q transfers sequentially according to P, it returns q.*

540   The last constraint requires that there be no circles in our IFA.

541   In IFA, state transition does not depend on input. The only input IFA accepts is the term to
542   be evaluated with this syntactic structure. The state transition is through pattern matching on
543   the evaluation result of the term in the previous node. Note that IFA is associated with syntactic
544   structure. At Each IFA only represents the current evaluation of a syntactic structure. The state
545   indicates that some sub-expressions of the syntactic structure have been evaluated, and the rest
546   have not.

547
548   DEFINATION 4.2 (STANDARD IFA). *If the term of node in Q can only be e_i (where $i \in 1, \ldots, n$) or a*
549   *value, we name the IFA standard IFA.*

550   If an IFA is standard, it means there are no more composite syntactic structures in it. In the
551   above example, for the syntactic structure of if, we substituted the IFA of the if into nand and
552   converted it into a standard IFA. Below we will prove that it is always feasible to convert IFA to
553   standard IFA, and give the algorithm.

554
555   LEMMA 4.1. *Considering an IFA of a syntactic structure, if the standard IFAs of all syntactic struc-*
556   *tures of terms contained in the IFA are known, then the IFA can be transformed into a standard IFA.*

557   PROOF OF LEMMA.   □
558

559   ### 4.2   Convert inference rules to IFA

560   Considering the inference rules in CoreLang, which we have more strict limits on.

561   *Assumption 1.* A syntactic structure *Headid* only contains the following inference rules.

$$\frac{(\mathsf{Headid}\ v_1 \ldots v_p\ e_1 \ldots e_i \ldots e_q) \rightarrow (\mathsf{Headid}\ v_1 \ldots v_p\ e_1 \ldots e_i' \ldots e_q)}{e_i \rightarrow e_i'} \quad \text{(E-HEAD)}$$

$$(\mathsf{Headid}\ v_1 \ldots v_p\ e_1 \ldots e_q) \rightarrow e$$

$$(\mathsf{Headid}\ v_1 \ldots v_p\ e_1 \ldots e_q) \rightarrow \mathbf{let}\ x = Exp_1\ \mathbf{in}\ Exp_2$$

569   This assumption specifies the form of the inference rules to ensure that IFAs can be generated.
570   The first one is context rule, and the others are reduction rules.

571   *Assumption 2.* The syntactic structure in CoreLang is finite. Think of all syntactic structures
572   as points in a directed graph. If one of *Headid*'s inference rules can generate a term containing
573   *Headid'*, then construct an edge that points from *Headid* to *Headid'*. The directed graph generated
574   from this method has no circles.

575   IFAs are not able to construct syntactic structures that contain recursive rules now. This assump-
576   tion qualifies that we can find an order for all syntactic structures, and when we construct IFA of
577   *Headid*, IFA of *Headid'* is known.

578   *Assumption 3.* The rules satisfy the determinacy of one-step evaluation.

579   By assumption 3, we can get the following lemma, which points out the feasibility of using a
580   node in IFA to represent the evaluation process of sub-expressions.

581
582   LEMMA 4.2. *If a term* (Headid $e_1\ \ldots\ e_n$) *does a one-step evaluation by rule (E-Head) of* Headid,
583   *which is a one-step evaluation of e_i, then it will continue to use this rule until e_i becomes a value.*

584   PROOF OF LEMMA. According to Assumption 3, this lemma is trivial.   □
585

586   LEMMA 4.3. *If all syntactic structures in CoreLang satisfy Assumption 1 and Assumption 2, We can*
587   *construct standard IFAs for all syntactic structures in CoreLang.*
588

589 PROOF OF LEMMA. By Assumption 2, we get an order of syntactic structures. We generate the
590 IFA for each structure in turn.

591 We generate a node for each rule and insert them into Q. If the rule is a reduction rule, add them
592 into F as terminal nodes. Next we will connect these nodes.

593 For a term like $(\text{Headid } e_1 \ldots e_n)$, considering that $e_1 \cdots e_n$ are not value, According to Assump-
594 tion 3, we have the unique rule r of $Headid$ for one-step evaluation. Let node q corresponding to
595 r be q_0.

596 If r is a context rule for e_i, let the term of q_0 be build a new node q and add it into Q. The term of
597 q is e_i. And the symbol table is set to empty. Assume that the evaluation of e_i results in v_i, we get
598 term $(\text{Headid } e_1 \ldots e_{i-1} \ v_i \ e_{i+1} \ldots e_n)$. For each possible value of v_i, choose the rules that should
599 be used.

600 If r is a reduction rule, build a new node q and add it into Q and F. The term of q is e_i, and the
601 symbol table is set to

602 □

4.3 Convert IFA to Inference Rules

605 LEMMA 4.4. *For each IFA, it can be converted to inference rules.*

607 PROOF OF LEMMA. Give an algorithm: convert IFA to inference rules. □

4.4 Syntactic Sugar

610 With the IFA, we can easily get the inference rules for syntactic sugars.

612 DEFINATION 4.3. *Considering the following syntactic sugar*

$$(\text{SurfHead } x_1 \ldots x_n) \rightarrow_d e,$$

615 *the IFA of* SurfHead *is defined as the IFA of syntactic structure* SurfHead' *whose inference rule is*

$$(\text{SurfHead' } x_1 \ldots x_n) \rightarrow e.$$

5 IMPLEMENTATION AND CASE STUDIES

5.1 Implementation

620 Our basic resugaring approach is implemented using PLT Redex[Felleisen et al. 2009], which is an
621 semantic engineering tool based on reduction semantics[Felleisen and Hieb 1992]. The framework
622 of the implementation is as Figure 4.

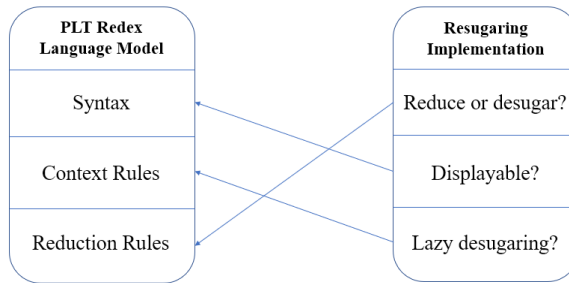
Fig. 4. framework of implementation

In the language model, desugaring rules are written as reduction rules of SurfExp. And context rules of SurfExp have no restrict (every subexpressions is reducible as a hole). Then for each resugaring step, we should choose the exact reduction which satisfies the reduction of mixed language's rule (see in Section 3.2). And one may notice the traditional resugaring approach does not need the whole evaluation rules of core language, a black-box stepper is needed instead. We have proved that our approach can also work by just given a black-box stepper, with a tricky extension. We use $\rightarrow_c$ to denote a reduction step of core language's expression in the black-box stepper, and $\rightarrow_e$ to denote a step in the extension evaluator for the mixed language. We may use $\rightarrow_m$ to denote one-step reduction in our mixed language, defined in the next section.

$$\frac{\forall\, i.\ e_i \in \mathsf{CoreExp} \qquad (\mathsf{CoreHead}\ e_1\ \ldots\ e_n)\ \rightarrow_c\ e'}{(\mathsf{CoreHead}\ e_1\ \ldots\ e_n)\ \rightarrow_e\ e'} \qquad \text{(CoreRed)}$$

$$\frac{\forall\, i.\ subst_i = (e_i \in \mathsf{SurfExp}\ ?\ \mathsf{tmpexp}\ :\ e_i),\ where\ \mathsf{tmpexp}\ is\ any\ reducible\ \mathsf{CoreExp}\qquad (\mathsf{CoreHead}\ subst_1\ \ldots\ subst_i\ \ldots\ subst_n)\ \rightarrow_c\ (\mathsf{CoreHead}\ subst_1\ \ldots\ subst_i'\ \ldots\ subst_n)}{\substack{(\mathsf{CoreHead}\ e_1\ \ldots\ e_i\ \ldots\ e_n)\ \rightarrow_e\ (\mathsf{CoreHead}\ e_1\ \ldots\ e_i'\ \ldots\ e_n)\\ where\ e_i\ \rightarrow_m\ e_i'\ if\ e_i\ \in\ \mathsf{SurfExp},\ else\ e_i\ \rightarrow_c\ e_i'}} \qquad \text{(CoreExt1)}$$

$$\frac{\forall\, i.\ subst_i = (e_i \in \mathsf{SurfExp}\ ?\ \mathsf{tmpexp}\ :\ e_i),\ where\ \mathsf{tmpexp}\ is\ any\ reducible\ \mathsf{CoreExp}\qquad (\mathsf{CoreHead}\ subst_1\ \ldots\ subst_n)\ \rightarrow_c\ e'\ /\!/\ \text{not reduced in subexpressions}}{(\mathsf{CoreHead}\ e_1\ \ldots\ e_n)\ \rightarrow_e\ e'[e_1/subst_1\ \ldots\ e_n/subst_n]} \qquad \text{(CoreExt2)}$$

For expression $(\mathsf{CoreHead}\ e_1\ \ldots\ e_n)$, replacing all subexpression not in core language with any reducible core language's term tmpexp. Then getting a result after inputting the new expression e' to the original blackbox stepper. If reduction appears at a subexpression at e_i or what the e_i replaced by, then the stepper with the extension should return $(\mathsf{CoreHead}\ e_1\ \ldots\ e_i'\ \ldots\ e_n)$, where e_i' is e_i after the mixed language's one-step reduction ($\rightarrow_m$) or after core language's reduction ($\rightarrow_c$) (the rule CoreExt1, an example in Figure 5). Otherwise, stepper should return e', with all the replaced subexpressions replacing back. (the rule CoreExt2, an example in Figure 6) The extension will not violate properties of original core language's evaluator. It is obvious that the evaluator with the extension will reduce at the subexpression as it needs in core language, if the reduction appears in a subexpression. One may notice that the stepper with extension behaves the same as mixing the evaluation rules of core language and surface language. The extension is just to make it works when the evaluator of core language is a blackbox stepper. That's why the extension is tricky.

```
(if (and e1 e2) true false)
           ⇓replace
    (if tmpe1 true false)
           ⇓blackbox
    (if tmpe1' true false)
           ⇓desugar
(if (if e1 e2 false) true false)
```

Fig. 5. CoreExt1's example

```
(if (if true ture false) (and ...) (or ...))
```
$$\Downarrow_{replace}$$
```
(if (if true ture false) tmpe2 tmpe3)
```
$$\Downarrow_{blackbox}$$
```
(if true tmpe2 tmpe3)
```
$$\Downarrow_{replaceback}$$
```
(if true (and ...) (or ...))
```

Fig. 6. CoreExt2's example

Note that in SurfRed1 rule and CoreExt1 rule, there is a recursive call on $\rightarrow_m$. We can optimize the resugaring algorithm by recursively resugaring. For example, (Sugar1 (Sugar2 e_{21} e_{22} ...) e_{11} e_{12} ...) as the input, and find the first subexpression should be reduced. We can firstly get the resugaring sequences of (Sugar2 e_{21} e_{22})

```
    (Sugar2 e_2_1 e_2_2 ...)
⟶   exp1
⤏   exp... // may be 0 or more steps
⟶   expn
```

Then a resugaring subsequence is got as

```
    (Sugar1 (Sugar2 e_2_1 e_2_2 ...) e_1_1 e_1_2 ...)
⟶   (Sugar1 exp1 e_1_1 e_1_2 ...)
⤏   (Sugar1 exp... e_1_1 e_1_2 ...) // may be 0 or more steps
⟶   (Sugar1 expn e_1_1 e_1_2 ...)
```

Thus, we will not need to try to expand the outermost sugar for each inner step (recursively resugaring for inner expression).

As for the automatic derivation of evaluation rules, it is just like what we describe. Just be careful during a merge on IFAs.

5.2 Case Studies

We test some applications on the tool as case studies. Note that we set call-by-value lambda calculus as terms in CommonExp, because we need to output some intermediate sequences including lambda expressions in some examples. It's easy if we want to skip them.

5.2.1 simple sugar. We construct some simple syntactic sugars and try it on our tool. Some sugar is inspired by the first work of resugaring[Pombrio and Krishnamurthi 2014]. The result shows that our approach can handle all sugar features of their first work.

We take a SKI combinator syntactic sugar as an example. We will show why our approach is efficient.

```
S →_d (lambdaN (x1 x2 x3) (x1 x2 (x1 x3)))
K →_d (lambdaN (x1 x2) x1)
I →_d (lambdaN (x) x)
```

Although SKI combinator calculus is a reduced version of lambda calculus, we can construct combinators' sugar based on call-by-need lambda calculus in our CoreLang. For sugar expression (S (K (S I)) K xx yy), we get the following resugaring sequences.

```
        (S (K (S I)) K xx yy)
  ⟶ (((K (S I)) xx (K xx)) yy)
  ⟶ (((S I) (K xx)) yy)
  ⟶ (I yy ((K xx) yy))
  ⟶ (yy ((K xx) yy))
  ⟶ (yy xx)
```

For the traditional approach, the sugar expression should firstly desugar to

```
((lambdaN
   (x1 x2 x3)
   (x1 x3 (x2 x3)))
 ((lambdaN (x1 x2) x1)
  ((lambdaN
    (x1 x2 x3)
    (x1 x3 (x2 x3)))
   (lambdaN (x) x)))
 (lambdaN (x1 x2) x1)
 xx yy)
```

Then in our CoreLang, the execution of expanded expression will contain 33 steps. For each step, there will be many attempts to match and substitute the syntactic sugars to resugar the expression. It will omit more steps for a larger expression.

We have described an example of and sugar and or sugar in overview. But what if the or sugar written like follows?

$$(\text{Or } e_1 \ e_2) \ \rightarrow_d \ (\text{let } (x \ e_1) \ (\text{if } x \ x \ e_2))$$

Of course, we got the same evaluation rules as the example in overview.

$$\frac{e_1 \ \rightarrow \ e_1'}{(\text{or } e_1 \ e_2) \rightarrow (\text{or } e_1' \ e_2)} \qquad (\text{or } \#t \ e2) \rightarrow \#t \quad (\text{or } \#f \ e2) \rightarrow e_2$$

Then for expressions headed with or, we won't need the one-step try to figure out whether desugaring or processing on a subexpression, which makes our approach more concise. Overall, the unidirectional resugaring algorithm makes our approach efficient, because no attempts for resugaring the expression are needed.

5.2.2 hygienic sugar. The second work[Pombrio and Krishnamurthi 2015] of traditional resugaring approach mainly processes hygienic sugar compared to first work. It use a DAG to represent the expression. However, hygiene is not hard to handle by our lazy desugaring strategy. Our algorithm can easily process hygienic sugar without special data structure.

A typical hygienic problem is as the following example.

$$(\text{Hygienicadd } e_1 \ e_2) \ \rightarrow_d \ (\text{let } (x \ e_1) \ (+ \ x \ e_2))$$

For traditional resugaring approach, if we want to get sequences of (let ((x 2)) (Hygienicadd 1 x)), it will firstly desugar to (let ((x 2)) (let ((x 1)) (+ x x))), which is awful because the two x in (+ x x) should be bind to different value. So traditional hygienic resugaring approach use abstract syntax DAG to distinct different x in the desugared expression. But for our approach based on lazy desugaring, the hygienicadd sugar does not have to desugar until necessary, so,

getting following sequences based on a rewriting system which renaming the variables during the rewriting.

```
(let ((x 2)) (Hygienicadd 1 x)
```

$\longrightarrow$ `(Hygienicadd 1 2)`

$\longrightarrow$ `(+ 1 2)`

$\longrightarrow$ `3`

The lazy desugaring is also convenient for hygienic resugaring for non-hygienic rewriting. For example, `(let ((x 1)) (+ x (let ((x 2)) (+ x 1))))` may be reduced to `(+ 1 (let ((1 2)) (+ 1 1)))` by a simple core language whose `let` expression does not handle cases like that. But by writing a simple sugar Let,

$$(\text{Let } e_1 \ e_2 \ e_3) \rightarrow_d (\text{let } ((e_1 \ e_2)) \ e_3)$$

and some simple modifies in the reduction of mixed language, we will get the following sequences in our system.

```
(Let x 1 (+ x (Let x 2 (+ x 1))))
```

$\longrightarrow$ `(Let x 1 (+ x (+ 2 1)))`

$\longrightarrow$ `(Let x 1 (+ x 3))`

$\longrightarrow$ `(+ 1 3)`

$\longrightarrow$ `4`

In practical application, we think hygiene can be easily processed by rewriting system, so we just use a rewriting system which can rename variable automatically.

And for the derivation method, there is no rewriting system at all, but the hygiene is handled more concisely. we build a hygienic sugar `Hygienicor` based the or sugar.

$$(\text{Or } e_1 \ e_2) \rightarrow_d (\text{let } (x \ e_1) \ (\text{if } x \ x \ e_2))$$
$$(\text{Hygienicor } e_1 \ e_2) \rightarrow_d (\text{let } (x \ e_1) \ (\text{or } e_2 \ x))$$

Though no need to write the sugar like that, something wrong may happen without hygienic rewriting system (`(if x x x)` appears). But by the method introduced in Todo: .., we can easily get the following rules, which will behave as it should be in resugaring.

$$\frac{e_1 \rightarrow e_1'}{(\text{Hygienicor } e_1 \ e_2) \rightarrow (\text{Hygienicor } e_1' \ e_2)} \qquad \frac{e_2 \rightarrow e_2'}{(\text{Hygienicor } v_1 \ e_2) \rightarrow (\text{Hygienicor } v_1 \ e_2')}$$
$$(\text{Hygienicor } v_1 \ \#t) \rightarrow \#t \quad (\text{Hygienicor } v_1 \ \#f) \rightarrow v_1$$

Overall, our result shows lazy desugaring is really a good way to handle hygienic sugar in any systems.

5.2.3 recursive sugar. Recursive sugar is a kind of syntactic sugars where call itself or each other during the expanding. For example,

$$(\text{Odd e}) \rightarrow_d (\text{if } (> e \ 0) \ (\text{Even } (- e \ 1)) \ \#f)$$
$$(\text{Even e}) \rightarrow_d (\text{if } (> e \ 0) \ (\text{Odd } (- e \ 1)) \ \#t)$$

are common recursive sugars. The traditional resugaring approach can't process syntactic sugar written as this (non pattern-based) easily, because boundary conditions are in the sugar itself.

Take (*Odd* 2) as an example. The previous work will firstly desugar the expression using the rewriting system. Then the rewriting system will never terminate as following shows.

```
      (Odd 2)
  ⤑ (if (> 2 0) (Even (- 2 1) #f))
  ⤑ (if (> (- 2 1) 0) (Odd (- (- 2 1) 1) #t))
  ⤑ (if (> (- (- 2 1) 1) 0) (Even (- (- (- 2 1) 1) 1) #f))
  ⤑ ...
```

Then the advantage of our approach is embodied. Our lightweight approach doesn't require a whole expanding of sugar expression, which gives the framework chances to judge boundary conditions in sugars themselves, and showing more intermediate sequences. We get the resugaring sequences of the former example using our tool.

```
      (Odd 2)
  ⟶ (Even (- 2 1))
  ⟶ (Even 1)
  ⟶ (Odd (- 1 1))
  ⟶ (Odd 0)
  ⟶ #f
```

We also construct some higher-order syntactic sugars and test them. The higher-order feature is important for constructing practical syntactic sugars. And many higher-order sugars should be constructed by recursive definition. The first sugar is `filter`, implemented by pattern matching term rewriting.

$$(\text{filter } e \text{ (list } v_1 \ v_2 \ \text{...)})$$
$$\rightarrow_d (\text{if } (e \ v_1) \text{ (cons } v_1 \text{ (filter } e \text{ (list } v_2 \ \text{...)))) (filter } e \text{ (list } v_2 \ \text{...)))}$$
$$(\text{filter } e \text{ (list)}) \rightarrow_d (\text{list})$$

and getting the following result.

```
      (filter (lambda (x) (and (> x 1) (< x 4))) (list 1 2 3 4))
  ⟶ (filter (lambda (x) (and (> x 1) (< x 4))) (list 2 3 4))
  ⟶ (cons 2 (filter (lambda (x) (and (> x 1) (< x 4))) (list 3 4)))
  ⟶ (cons 2 (cons 3 (filter (lambda (x) (and (> x 1) (< x 4))) (list 4))))
  ⟶ (cons 2 (cons 3 (filter (lambda (x) (and (> x 1) (< x 4))) (list))))
  ⟶ (cons 2 (cons 3 (list)))
  ⟶ (cons 2 (list 3))
  ⟶ (list 2 3)
```

Here, although the sugar can be processed by traditional resugaring approach, it will be redundant. The reason is that, a filter for a list of length n will match to find possible resugaring $n * (n - 1)/2$ times. Thus, lazy desugaring is really important to reduce the resugaring complexity of recursive sugar.

Moreover, just like the *Odd and Even* sugar above, there are some simple rewriting systems which do not allow pattern-based rewriting. Or there are some sugars which need to be expressed by the terms in core language as rewriting conditions. Take the example of another higher-order

sugar map as an example.

```
(map e₁ e2) →d
(let ((x e2)) (if (empty x) (list) (cons (e1 (first x)) (map e1 (rest x)))))
```

Get following resugaring sequences.

```
      (map (lambda (x) (+ x 1)) (cons 1 (list 2)))
```

⟶ `(map (lambda (x) (+ x 1)) (list 1 2))`

⟶ `(cons 2 (map (lambda (x) (+ 1 x)) (list 2)))`

⟶ `(cons 2 (cons 3 (map (lambda (x) (+ 1 x)) (list))))`

⟶ `(cons 2 (cons 3 (list)))`

⟶ `(cons 2 (list 3))`

⟶ `(list 2 3)`

Note that the let term is to limit the subexpression only appears once in RHS. In this example, we can find that the list (cons 1 (list 2)), though equal to (list 1 2), is represented by core language's term. So it will be difficult to handle such inline boundary conditions by rewriting system. But our approach is easy to handle cases like this. So our resugaring approach by lazy desugaring is powerful.

6 RELATED WORK

As discussed many times before, our work is much related to the pioneer work of resugaring in [Pombrio and Krishnamurthi 2014, 2015]. The idea of "tagging" and "reverse desugaring" is a clear explanantion of "resugaring", but it becomes very complex when the rhs of the desugaring rule becomes complex. Our approach does not need reverse desuharing, and is more lightweight, powerful and efficient. For hygienic resugaring, compared with approach of using DAG to solve the variable binding problem in [Pombrio and Krishnamurthi 2015], our approach of "lazy desugaring" is more natural, because it behaves as what the sugar ought to express.

Our work on reduction rule derivaiton for the surface language was inpired by the work of *Type resugaring* [Pombrio and Krishnamurthi 2018], which shows that it is possible to automatically construct the typing rules for the surface language by statically analyzing type inference trees. But it cannot be applied for our reduction rule derivation, because it has an assumption that there is only one rule for multi-branchs of one syntactic sugar Todo: I don't understand the meaning here., which is not the case for evaluation rules. Todo: We may explain the key idea about how we deal with this assumption.

Macros as multi-stage computations [Ganz et al. 2001] is a work related to our lazy expansion for sugars. Some other researches [Rompf and Odersky 2010] about multi-stage programming [Taha 2003] indicate that it is useful for implementing domain-specific languages. However, multi-stage programming is a metaprogramming method, which mainly works for run-time code generation and optimization. In contrast, our lazy resugaring approach treat sugars as part of a mixed language, rather than seperate them by staging. Moreover, the lazy desugaring gives us chance to derive evaluation rules of sugars, which is a new good point compared to multi-stage programming.

Our work is related to the *Galois slicing for imperative functional programs* [Ricciotti et al. 2017], a work for dynamic analyzing functional programs during execution. The forward component of the Galois connection maps a partial input x to the greatest partial output y that can be computed from x; the backward component of the Galois connection maps a partial output y to the least

partial input x from which we can compute y. This can also be considered as a bidirectional transformation [Czarnecki et al. 2009; Foster et al. 2007] and the round-tripping between desugaring and resugaring in traditional approach. In contrast to these work, our resugaring approach is basically unidirectional, with a local bidirectional step for a one-step try in our lazy desugaring. It should be noted that Galois slicing may be useful to handle side effects in resugaring in the future (for example, slicing the part where side effects appear).

Our method for derving reduction rule is influenced by work on *origin tracking* [Deursen et al. 1992], which is to track the origins of terms in rewriting system. For desugaring rules in a good form as given in Section 4, we can easily track the terms and make use of them for derivation of reduction rules. Todo: Add more related work about derivation of reductions rules by Zhichao.

Our implementation is built upon the PLT Redex [Felleisen et al. 2009], a semantics engineering tool, but it is possible to implement our approach on other semantics engineeing tools such as those in [Rosu and Serbanuta 2010; Vergu et al. 2015] which aim to test or verify the semantics of languages. The methods of these researches can be easily combined with our approach to implement more general rule derivation. *Ziggurat* [Fisher and Shivers 2006] is a semantic-extension framework, also allowing defining new macros with semantics based on existing terms in a language. It is should be useful for static analysis of macros.

7 CONCLUSION

In this paper, we purpose a lightweight, efficient and powerful resugaring approach by lazy desugaring. Essentially, we would see the derivation of rules is the abstract of the basic resugaring approach. In the basic approach, the most important part is *reduction in mixed language* (see in sec 3.2), which decides whether reducing the subexpression or desugaring the outermost sugar. Reducing subexpressions are just the same as derived context rules; desugaring the outermost sugar is similar to derived reduction rules. However, the derived evaluation rules is more convinent and efficent than the basic resugaring, because the derivation evolves a process like abstract interpretation[Cousot and Cousot 1977], then reduces many steps executed in core language. Moreover, the semantics got by derivation make it possible to do some optimization at the surface language level, which is important for implementing a DSL. In contrast, the dynamic approach is more powerful by supporting recursive sugars' resugaring. Besides, the rewriting based on reduction semantics makes the sugar represented in many ways.

The original intent of our research is finding a better method (or building a tool) for implementing DSL. We could see derived evaluation rules is better for achieving the goal, because getting the semantics of DSL (based on syntactic sugar) will be very useful for applying any other techniques on the DSL. But it will be better if the defects of expressiveness of sugar which the derivation can handle are improved. So we may be achieving a more powerful derivation which can recursive recursive sugar as a future work.

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A APPENDIX

Text of appendix …