## **APPENDIX D**

## **SYMBOLS**

Symbol	Explanation	First page listed
•	Derivative with respect to time (before Chapter 4)	
	or conformal time (afterwards)	
$\alpha^{(2)}$	Recombination rate of hydrogen	71
β	Ionization rate of hydrogen	71
$\Gamma^{\mu}_{\alpha\beta}$	Christoffel symbol	30
$\gamma_{1,2}$	Two components of shear	300
$\frac{\gamma_{1,2}}{\Gamma}$	Parameter determining the power spectrum	205
$\delta_b$	Baryon overdensity	106
$test_i$	Estimated anisotropy in pixel i	340
$\Delta^2(k)$	Dimensionless power on scale $k$	185
δ	Dark matter overdensity	104
δ	Slow-roll parameter (Chapter 6 only)	155
$\delta^D(ec{k}-ec{k}')$	Dirac delta function in D dimensions	16
$\delta\phi$	Perturbation to the scalar field driving inflation	152
$\delta T^{\mu}_{ u}$	Perturbation to energy-momentum tensor	163
$\delta_{ij}$	Kronecker delta = $0(i \neq j)$ or $1(i = j)$	27
$\delta_H$	Amplitude of primordial perturbations at horizon	171
$\epsilon$	Slow-roll parameter	155
$\hat{\epsilon}$	Polarization unit vector	97
$\epsilon_{1,2}$	Two components of ellipticity	301
$\epsilon_0$	Ionization energy of hydrogen, 13.6 eV	70
$\eta$	Conformal time	34
$\eta_*$	Conformal time at recombination	218
$\eta_{ m eq}$	Conformal time at matter-radiation equality	213
$\eta_b$	Baryon-to-entropy ratio	62
$\eta_{ m prim}$	Conformal time at the end of inflation	149
$\eta_{\mu  u}$	Minkowski metric	26

Symbol	Explanation	First page listed
Θ	Perturbation to photon distribution	93
$\Theta_l$	Legendre moment of photon perturbation	110
$\Theta_P$	Polarization perturbation	111
$\Theta_r$	Perturbation to radiation = $\rho_{\gamma}\Theta + \rho_{\nu}N$	135
$\Theta^T$	Photon perturbation due to tensor perturbations	116
$\kappa$	Convergence	300
Λ	Cosmological constant	10
$\mu$	Cosine of the angle between $\hat{k}$ and $\hat{p}$	101
$\xi(r)$	3D correlation function	264
$\xi^0, \xi$	Generators of coordinate transformations	133
$\rho_b$	Baryon energy density	41
$ ho_{ m cr}$	Critical energy density	3
$ ho_{ m de}$	Dark energy density	50
$ ho_{ m dm}$	Dark matter energy density	123
$ ho_{ m m}$	Matter energy density	38
$\rho_{\gamma}$	Energy density of photons	40
$\rho_{ u}$	Energy density of neutrinos	46
$\rho_r$	Energy density of all radiation	38
$\sigma_T$	Thomson cross-section	72
$\tau(\eta)$	Optical depth of photons back to conformal time $\eta$	101
$\dot{\tau}$	Scattering rate	101
$\tau_n$	Neutron lifetime	67
Φ	Scalar perturbation to metric	87
$\Phi_{ m p}$	Primordial value of $\Phi$ set during inflation	183
$\phi^{(0)}$	Zero-order value of the field driving inflation	152
$\chi(z)$	Comoving distance out to redshift z	34
$\chi_{\infty}$	Comoving distance to redshift infinity	263
Ψ	Scalar perturbation to metric	87
$\psi_{ij}$	$2 \times 2$ distortion tensor	302
$\Omega_i$	Energy density in <i>i</i> th species over $\rho_{cr}$	10
$\Omega_k$	Ratio of curvature density to critical density	35
$A_{ij}$	$2 \times 2$ transformation matrix	300
a	Scale factor of the universe	2
$a_*$	Scale factor at recombination	186
$a_{ m eq}$	Scale factor at matter-radiation equality	51
$a_{ m late}$	Scale factor after which perturbations evolve as $D_1$	183
В	B-mode of polarization or weak lensing	306
$B_D$	Binding energy of deuterium	65
C	Full covariance matrix	341
$\mathcal{C}$	Band power	389
$C_l^{\mathrm{matter}}$	Angular power spectrum for matter	290

Symbol	Explanation	First page listed
$c_s$	Sound speed	82
$C_N$	Covariance matrix due to the noise	339
$C_S$	Covariance matrix due to the signal	340
$D_1$	Growth function	183
$d_A$	Angular diameter distance	35
$d_L$	Luminosity distance	36
E	E-mode of polarization or weak lensing	306
$F_{lphaeta}$	Fisher matrix	366
$\mathcal{F}$	Curvature matrix	365
f	Distribution function, often referring to photons	38
$f_{ m dm}$	Distribution function of dark matter	102
$f_e$	Distribution function of electrons	95
$f^{(0)}$	Zero-order distribution function of photons	93
$g(\eta)$	Visibility function	236
$g_*$	Effective relativistic degrees of freedom	67
$g_{\mu  u}$	Metric	25
$g_i$	Number of spin states of species $i$	38
$\overline{G}$	Newton's constant	3
$G_{\mu\nu}$	Einstein tensor	32
h	Parameter for Hubble constant	5
$\tilde{h}$	Variable tracing tensor perturbations	158
$h_{ imes}, h_{+}$	Tensor perturbations to metric	116
$\mathcal{H}$	3D matrix describing tensor perturbations	126
$\overline{H}$	Hubble rate of expansion	3
$H_0$	Hubble rate today	3
k	Wavenumber	101
$k_i = k^i$	Wavevector	101
$k_{\rm eq}$	Wavenumber crossing horizon at $a_{eq}$	194
$k_{ m nl}$	Wavenumber of nonlinearity	185
$k_{ m p}$	Location of acoustic peaks	229
Ĺ	Likelihood function	337
$\mathcal{M}$	Particle physics amplitude for a process	59
$m_e$	Electron mass	70
$m_n$	Neutron mass	64
$m_{ u}$	Neutrino mass	46
$m_{ m Pl}$	Planck mass	53
$m_p$	Proton mass	64
$N_p$	Number of pixels in an experiment	341
$n_{ m b}$	Baryon number density	62
$n_{ m dm}$	Dark matter number density	103
$n_{ m dm}^{(0)}$	Zero-order dark matter number density	104

Symbol	Explanation	First page listed
$n^{(0)}$	Equilibrium number density	61
$\mathcal{N}$	Perturbation to neutrino distribution function	111
$\mathcal{P}_l$	Legendre polynomial of order $l$	112
$\mathcal{P}$	Pressure	37
$P^{\alpha}$	4D comoving energy-momentum vector	31
p	Proper momentum	56
P(k)	Power spectrum of matter	16
$P_{\Phi}(k)$	Gravitational potential power spectrum	167
$\hat{p}^i = \hat{p}_i$	Unit direction vector	90
Q	Proton-neutron mass difference	65
$\overline{Q}$	Stokes parameter	312
r	Tensor/scalar ratio	248
$r_s$	Sound horizon	228
$R_{\mu\nu}$	Ricci tensor	32
$\mathcal{R}$	Ricci scalar = $g^{\mu\nu}R_{\mu\nu}$	32
R	Baryon-to-photon ratio, $3\rho_b/4\rho_\gamma$	82
s	Entropy density	40
t	Age of the universe	2
$T_{ m ant}$	Antenna temperature	379
T	Zero-order photon temperature	4
$T_{\mu\nu}$	Stress-energy tensor	32
U	Stokes parameter	312
$ec{v}_{ m b} = \hat{k} v_{ m b}$	Velocity of baryons	96
$\vec{v} = \hat{k}v$	Velocity of dark matter	103
$v_{ m H}$	Velocity due to Hubble expansion	261
$v_{ m pec}$	Peculiar velocity	261
$\overline{w}$	Pressure to energy-density ratio	50
$w(\theta)$	Angular correlation function	266
$X_e$	Free electron fraction	70
$X_n$	Neutron abundance	66
$X_{n, \mathrm{EQ}}$	Equilibrium neutron abundance	66
$Y_p$	Mass fraction of <sup>4</sup> He	69
$\overline{y}$	Scale factor normalized to 1 at $a_{eq}$	190
$y_H$	y when mode crosses horizon	202
$Y_{ m EQ}$	Equilibrium abundance of dark matter particles	74
$\overline{z}$	Redshift	7
$z_*$	Redshift at recombination	51
$z_{ m eq}$	Redshift at matter-radiation equality	51