## Hill Climbing Robot System Specifications

State: 
$$\begin{bmatrix} x \\ y \end{bmatrix}$$

Control: 
$$\begin{bmatrix} u \\ \theta \end{bmatrix}$$

**System Dynamics:** 

Hill Terrain: 
$$h(x, y) = 3y + \sin(x + xy)$$

$$\theta_{heading} = \theta + \arctan\left(\frac{\partial h/\partial y}{\partial h/\partial x}\right)$$

$$\Delta h = h\left(x + \cos\theta_{heading}, y + \sin\theta_{heading}\right) - h(x, y)$$

$$\begin{bmatrix} \dot{x} \\ \dot{y} \end{bmatrix} = \begin{bmatrix} u \cdot \frac{\cos\theta_{heading}}{\sqrt{1 + \Delta h^2}} \\ u \cdot \frac{\sin\theta_{heading}}{\sqrt{1 + \Delta h^2}} \end{bmatrix}$$