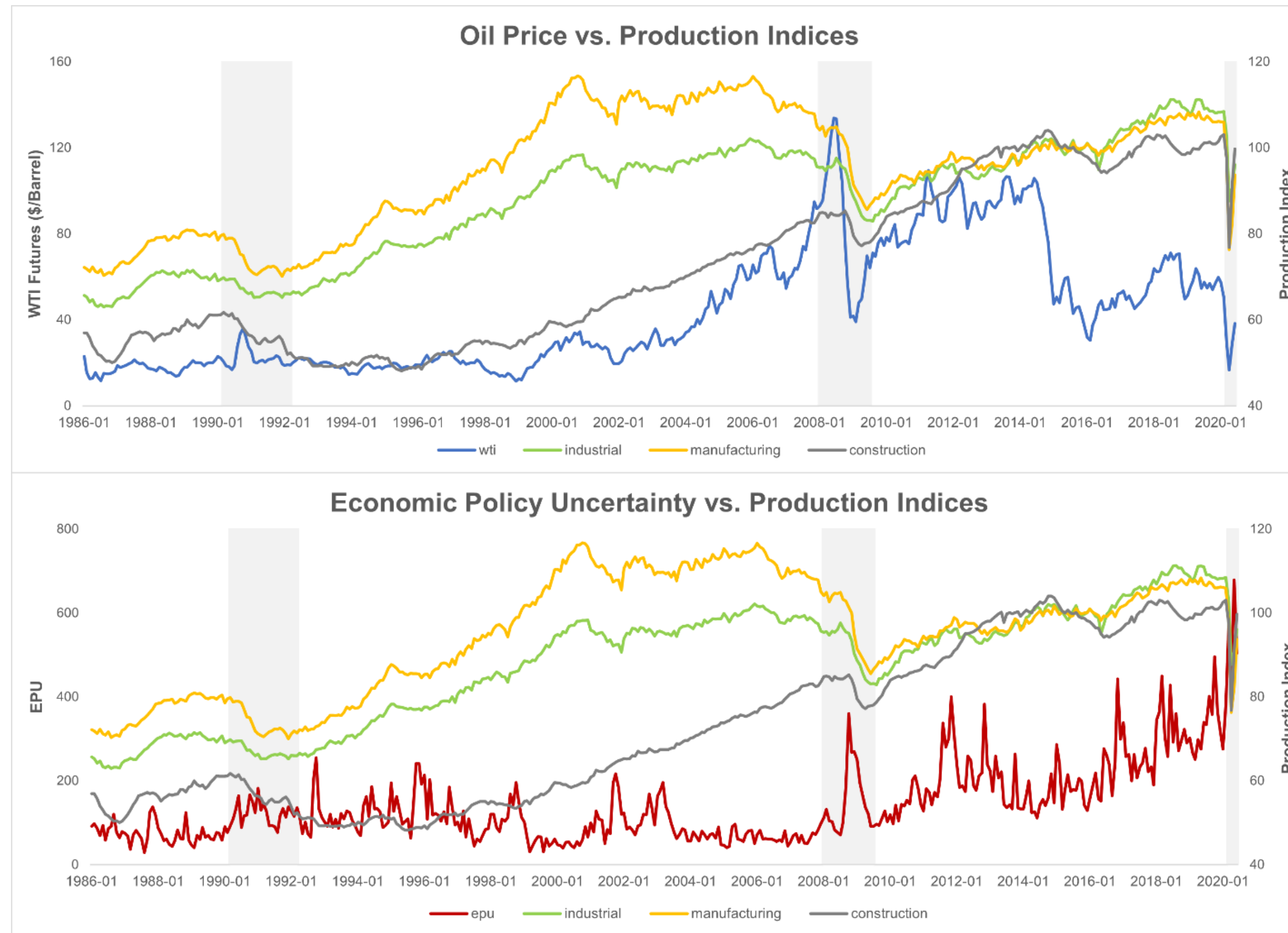


3. Data

- **Observations:** Monthly series from January 1986 to June 2020.
- **Data Source:**
 - a) Oil Price: the spot price of West Texas Intermediate (WTI) crude oil, from the *U.S. Energy Information*
 - b) Policy Uncertainty: Canadian economic policy uncertainty index, from the *Economic Policy Uncertainty* website
 - c) Real Economic Activity: production indices of Canadian industrial, manufacturing, and construction activities, from the *OECD Main Economic Indicators*

3.1 Time Series Plot



- **Trend:** each series has an overall upward trend except the oil price series.
- **Correlations:** economic policy uncertainty series seems to move in an opposite direction to other variables.
- **Cycles:** apparent cyclical patterns seems evident for each series.

3.2 Covariance Stationarity

- Augmented Dickey Fuller (ADF), Dickey Fuller GLS (DFGLS), KPSS tests
- **Null Hypotheses (H_0):**
 - a) ADF & DFGLS: the series has a unit root
 - b) KPSS: the series is covariance stationary
- I include 11 deterministic seasonal dummy variables and a linear trend in the testing equations as control variables
- I select 11 augmentation terms to ensure the validity of the tests while using monthly data.
- The critical value is based on $\alpha = 10\%$ due to the low power of the tests.

3.2 Covariance Stationarity

Series	ADF		DF-GLS		KPSS	
	Test Statistic	Crit. Val ($\alpha = 10\%$)	Test Statistic	Crit. Val ($\alpha = 10\%$)	Test Statistic	Crit. Val ($\alpha = 10\%$)
WTI	-2.096		-2.100		0.233	
EPU	-1.232		-1.352		0.429	
Industrial	-1.707	-3.130	-1.805	-2.560	0.327	0.119
Manufacturing	-1.186		-0.963		0.436	
Construction	-1.389		-1.252		0.402	

Note: The number of augmentation lags for both the ADF and the DF-GLS tests is set at 11 for each auxiliary regression. For the KPSS test, the #bandwidth is selected through using the Bartlett kernel, and is equal to 15 for EPU and 16 for the other series.

- Each of the series is **covariance non-stationary** with at least one unit root.

3.3 Seasonal Unit Roots

Frequency	WTI	EPU	Industrial	Manufacturing	Construction
0 & 2π	-1.720	-0.137	-1.665	-1.872	-0.782
$2\pi/12$ & $22\pi/12$	22.721***	25.918***	41.635***	22.168***	29.180***
$4\pi/12$ & $20\pi/12$	30.366***	39.893***	24.255***	9.192***	5.872***
$6\pi/12$ & $18\pi/12$	30.175***	55.041***	16.541***	11.692***	1.679**
$8\pi/12$ & $16\pi/12$	43.438***	27.200***	19.990***	14.291***	4.022***
$10\pi/12$ & $14\pi/12$	33.384***	22.870***	42.522***	35.132***	13.503***
π	-6.013***	-6.072***	-5.895***	-5.736***	-3.014**
All seasonal frequencies	606.388***	74.796***	30.020***	373.439***	215.603***
All frequencies	557.472***	71.682***	28.313***	348.928***	198.284***

* $p < 0.1$, ** $p < 0.05$, *** $p < 0.01$

- I undertake HEGY test to detect the presence of seasonal unit roots
- **Null Hypotheses (H_0):** the series has a unit root at the specified frequency (or degree).
- If a series has a unit root at the frequencies other than 0, we may say that the series exhibits a seasonal unit root.
- The test results indicate that all series have a **non-seasonal** unit root but no seasonal unit roots.

3.4 Cointegration Test

- I perform Johansen's (1988, 1991) maximum-eigenvalue and trace tests to explore for possible cointegrating (long-term) relationships among the series in the same system.
- Each system contain three series: the oil price, economic policy uncertainty, each production type. Therefore, I undertake the test for each considered production variable.

3.4 Cointegration Test

- **Maximum-eigenvalue Test:**

$$H_0^1: r = 0 \quad \text{vs.} \quad H_a^1: r = 1$$

$$H_0^2: r = 1 \quad \text{vs.} \quad H_a^2: r = 2$$

$$H_0^3: r = 2 \quad \text{vs.} \quad H_a^3: r = 3$$

- **Trace Test:**

$$H_0^1: r = 0 \quad \text{vs.} \quad H_a^1: r = 3$$

$$H_0^2: r = 1 \quad \text{vs.} \quad H_a^2: r = 3$$

$$H_0^3: r = 2 \quad \text{vs.} \quad H_a^3: r = 3$$

- r denotes the number of cointegrating vectors in the system.
- If we fail to reject H_0^1 , we stop testing, concluding no cointegrating relationships.

3.4 Cointegration Test

Production Series	Maximum-Eigenvalue Test		Trace Test	
	(H ₀ : r = 0 vs. H _a : r = 1)		(H ₀ : r = 0 vs. H _a : r = 3)	
	Statistic	Crit. Val ($\alpha = 5\%$)	Statistic	Crit. Val ($\alpha = 5\%$)
Industrial	4.662		8.361	
Manufacturing	5.277	21.132	9.519	29.797
Construction	11.232		17.629	

- There are **no** cointegrating relationships in each system, and using the first difference of each series in the VAR estimation seems reasonable.

3.5 VAR Diagnostics

$$Y_t = \alpha + \sum_{i=1}^p \phi_i Y_{t-i} + \sum_{j=1}^{11} \psi_j D_{t,j} + \varepsilon_t$$

- $Y_t = [\Delta wti_t, \Delta epu_t, \Delta production_t^k]'$; k = industrial, manufacturing, or construction
 - Y_{t-i} : lagged values at order i
 - Φ_i : the (3×3) matrix of reduced-form autoregressive parameters
 - $D_{t,j}$: binary variable for the j^{th} month
 - ε_t : the (3×1) vector of reduced-form error terms
-
- Based on the Akaike's (1974) Info Criterion, choose $p = 4$ for the models consisting of industrial and manufacturing productions and $p = 6$ for construction production.

3.5 VAR Diagnostics

Dependent Variable	Independent Variables	χ^2	p-value
Δ_{ind}	Δ_{wti}	26.842	0.0000
	Δ_{epu}	4.927	0.2948
	All	39.374	0.0000
Δ_{man}	Δ_{wti}	19.604	0.0006
	Δ_{epu}	7.946	0.0936
	All	35.290	0.0002
Δ_{con}	Δ_{wti}	17.976	0.0063
	Δ_{epu}	23.319	0.0007
	All	52.491	0.0001

- **Granger's (1969) non-causality test:** tests for one-period ahead predictability.
- **Null Hypothesis (H_0):** the lagged independent variable does not help explain or Granger cause the current value of the dependent variable.
- The price of crude oil Granger causes all production types, while policy uncertainty only help explain construction production.

4. Methodology

- Functional form
- Identifying restrictions

4.1 Functional Form

$$A_0 Y_t = \alpha + \sum_{i=1}^p A_i Y_{t-i} + \sum_{j=1}^{11} \gamma_j D_{t,j} + u_t$$

- A_0 : the (3×3) contemporaneous coefficient matrix between the endogenous variables
 - A_i : the (3×3) matrix comprising the structural autoregressive parameters at order i
 - u_t : the (3×1) vector of structural error terms
-
- I impose **short-run** restrictions via the error terms, as there are likely no cointegrating relationships amongst the oil price, policy uncertainty, and each real production.

4.2 Identifying Restrictions – Expressions

$$\varepsilon_t = A_0^{-1} u_t$$



$$\begin{bmatrix} \varepsilon_t^{\Delta wti} \\ \varepsilon_t^{\Delta epu} \\ \varepsilon_t^{\Delta production} \end{bmatrix} = \begin{bmatrix} a_{11} & 0 & 0 \\ a_{21} & a_{22} & 0 \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \begin{bmatrix} u_t^{\Delta wti} \\ u_t^{\Delta epu} \\ u_t^{\Delta production} \end{bmatrix}$$



$$\begin{bmatrix} \varepsilon_t^{\Delta wti} \\ \varepsilon_t^{\Delta epu} \\ \varepsilon_t^{\Delta production} \end{bmatrix} = \begin{bmatrix} a_{11} u_t^{\Delta wti} \\ a_{21} u_t^{\Delta wti} + a_{22} u_t^{\Delta epu} \\ a_{31} u_t^{\Delta wti} + a_{32} u_t^{\Delta epu} + a_{33} u_t^{\Delta production} \end{bmatrix}$$

- $u_t^{\Delta wti}$: Oil price shock
- $u_t^{\Delta epu}$: Policy uncertainty shock
- $u_t^{\Delta production}$: Shock in real activity

4.2 Identifying Restrictions – Economic Reasonings

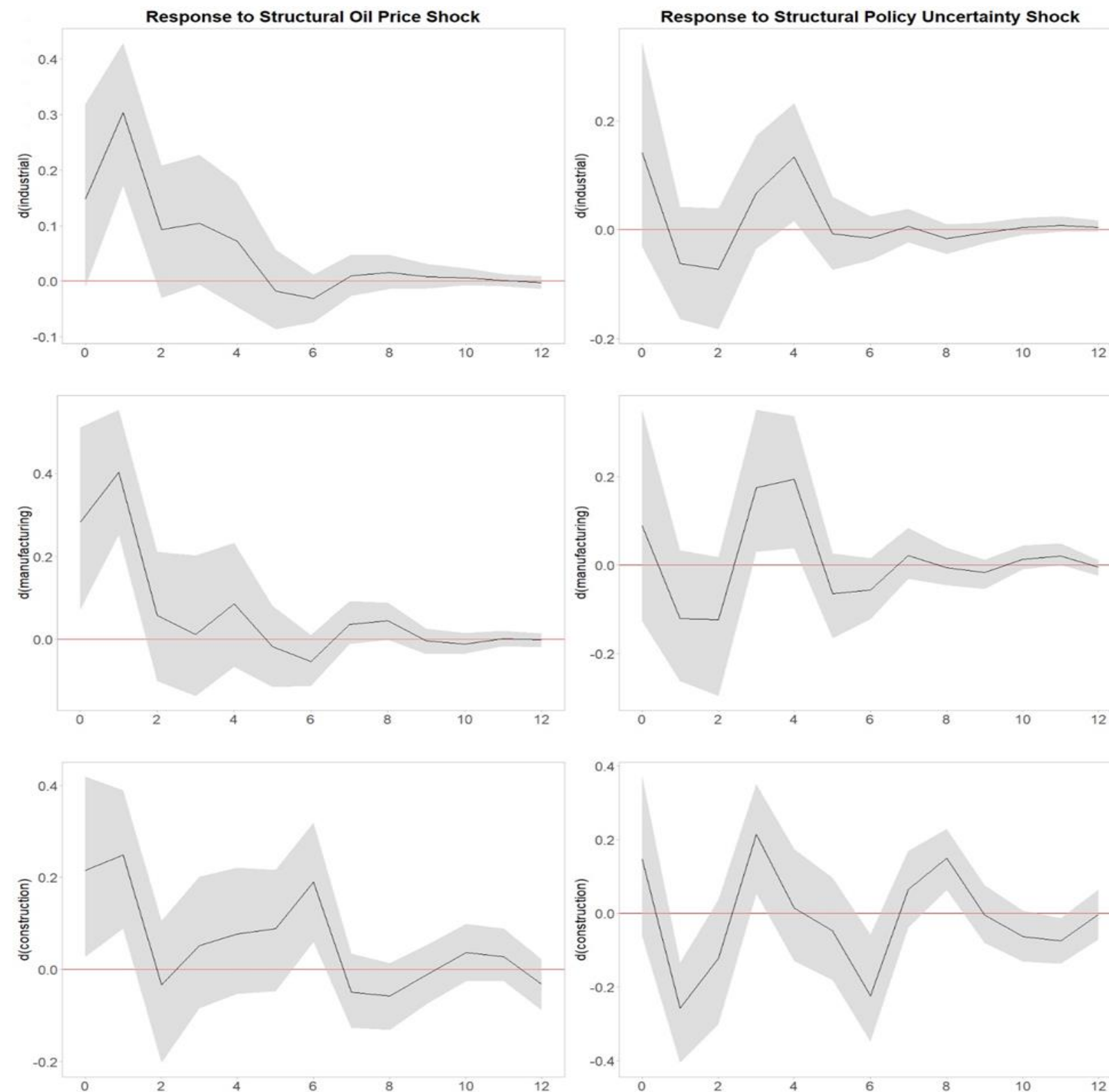
$$\begin{bmatrix} \varepsilon_t^{\Delta wti} \\ \varepsilon_t^{\Delta epu} \\ \varepsilon_t^{\Delta production} \end{bmatrix} = \begin{bmatrix} a_{11}u_t^{\Delta wti} \\ a_{21}u_t^{\Delta wti} + a_{22}u_t^{\Delta epu} \\ a_{31}u_t^{\Delta wti} + a_{32}u_t^{\Delta epu} + a_{33}u_t^{\Delta production} \end{bmatrix}$$

- a. The oil price does not respond to shocks in Canadian economic policy uncertainty and real activity because it captures the oil market price of the entire world.
- b. A change in the oil price can affect Canadian policy uncertainty, as we cannot anticipate the direction of that change.
- c. Both the world oil price and economic policy uncertainty are necessary determinants of domestic real economic activities.

5. Results

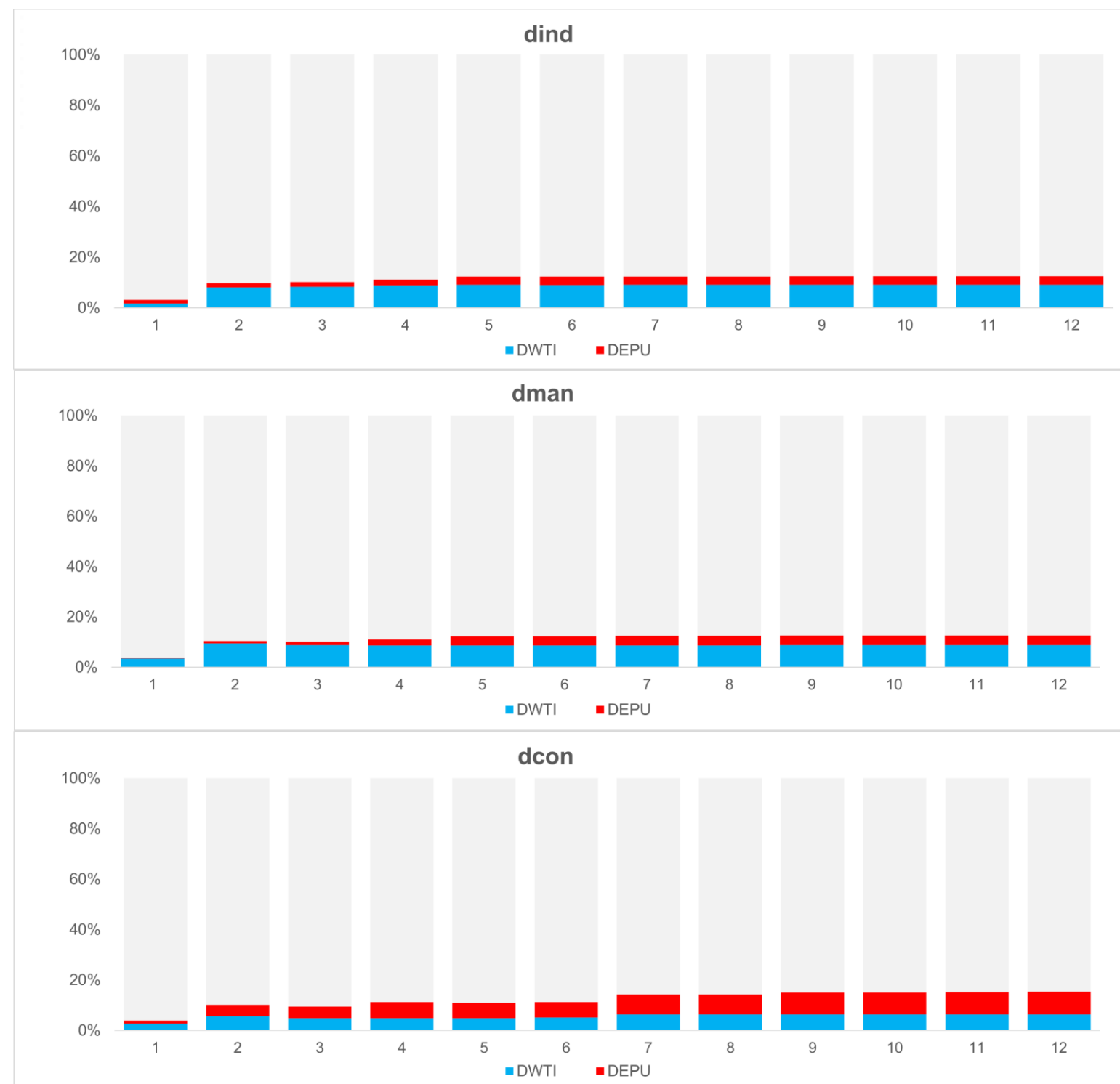
- I interpret and discuss my empirical findings based on:
 - a) Impulse response functions (IRFs)
 - b) Forecast error variance decompositions (FEVDs)

5.1 Impulse Response Analysis



- The oil price shock leads to an instantaneous **positive** response for all types of real productions, but this effect dissipates quickly.
- The policy uncertainty shock has a statistically significant impact on construction production, being negative instantaneously but becoming positive shortly thereafter.

5.2 Forecast Error Variance Decomposition



- The structural shocks to the oil price and to policy uncertainty jointly explain **15-20%** of the forecast error variance in productions.
- The oil price shock contributes a higher proportion of the variability in industrial and manufacturing productions than policy uncertainty shock; This is the inverse *w.r.t.* construction production