

AI and Human Capital Accumulation: Aggregate and Distributional Implications*

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Abstract

This paper develops a model to analyze the effects of AI advancements on human capital investment and their impact on aggregate and distributional outcomes in the economy. We construct an incomplete markets economy with endogenous asset accumulation and general equilibrium, where households decide on human capital investment and labor supply. Anticipating near-term AI advancements that will alter skill premiums, we analyze the transition dynamics toward a new steady state. Our findings reveal that human capital responses to AI amplify its positive effects on aggregate output and consumption, mitigate the AI-induced rise in precautionary savings, and stabilize the adjustments in wages and asset returns. Furthermore, while AI-driven human capital adjustments increase inequalities in income, earnings, and consumption, they unexpectedly reduce wealth inequality.

Keywords: AI, Job Polarization, Human Capital, Inequality

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¹ 1 Introduction

² The distinctive nature of AI advancements lies in their ability to perform cognitive,
³ non-routine tasks that previously required significant education and expertise, fun-
⁴ damentally differentiating its impact on the labor market and economy from that
⁵ of general automation. For example, AI tools in medical diagnostics now assist ra-
⁶ diologists in analyzing medical images, potentially reducing demand for entry-level
⁷ radiologists while simultaneously increasing the productivity of senior professionals.
⁸ More generally, AI could shift the premium associated with various skills levels, de-
⁹ valuing middle-level skills while increasing the demand for high-level expertise. In
¹⁰ anticipation of these changes, households are likely to adjust their human capital
¹¹ investments.

¹² The average worker in low-skilled occupations also obtains a significant wage
¹³ premium from working in a more innovative firm Aghion *et al.*, (2019)

¹⁴ Recent labor market data highlight the disproportionate impact of AI on entry-
¹⁵ level employment opportunities. According to Revelio Labs¹, postings for entry-level
¹⁶ jobs in the US declined by about 35% since January 2023, with roles more exposed
¹⁷ to AI experiencing even steeper reductions. Bloomberg² reports that, in the words
¹⁸ of Matt Sigelman, president of the Burning Glass Institute, “Demand for junior hires
¹⁹ in many college-level roles is already declining, even as demand for experienced hires
²⁰ in the same jobs is on the rise.”

²¹ Experimental evidences reviewed by Calvino *et al.*, (2025) suggest two seemingly
²² contradictory findings in productivity gains between experienced and less experi-
²³ enced workers. On the one hand, AI can help to narrow the gap between low- and
²⁴ high-skilled workers given the same task. On the other hand, higher digital profi-
²⁵ ciency or task-specific experience can positively affect the returns to AI’s use. The
²⁶ rational for these contradictory findings is that less experienced users may see greater
²⁷ improvements in simpler tasks, where current AI excels. For tasks that AI may not
²⁸ be capable of performing effectively, successful use of AI requires more advanced skills
²⁹ and experience that involves understanding AI’s capabilities and limitations.

³⁰ Asam and Heller (2025) find that GitHub Copilot helps software startups raise
³¹ their initial funding 19% faster with 20% fewer employed developers. Moreover, the
³² productivity gains is disproportionately larger for startups with more experienced
³³ founders.

³⁴ Souza (2025) find that AI used in Brazilian firms reduces employment and wages
³⁵ for middle-wage office workers whereas increases employment of low-skilled produc-
³⁶ tion workers.

¹<https://www.reveliolabs.com/news/macro/is-ai-responsible-for-the-rise-in-entry-level-unemployment/>

²<https://www.bloomberg.com/news/articles/2025-07-30/ai-s-takeover-of-entry-level-tasks-is-making-college-grads-job-hunt-harder>

37 According to the National Center for Education Statistic,³ college enrollment in
38 the U.S. has been declining since 2010. The National Student Clearinghouse Re-
39 search Center reports that the undergraduate college enrollment decline has acceler-
40 ated since the pandemic began, resulting in a loss of almost 6% of total enrollment
41 between fall 2019 to fall 2023, while graduate enrollment has risen by about 5%.⁴
42 These shifts, regardless of their causes, highlight evolving patterns in human capital
43 investment.

44 This paper develops a model to study the effects of AI advancements on human
45 capital investment and their subsequent impact on aggregate and distributional
46 outcomes of the economy. We posit an economy consisting of three sectors, requiring
47 low, middle and high levels of skill (human capital) with increasing sectoral labor
48 productivity. Households can invest in their human capital to move up to more
49 productive sectors. But if they do not invest, their human capital depreciates and,
50 over time, they will move down to less productive sectors. We model human capital
51 investment at two levels, a low level attainable on the job and a high level requiring
52 full-time commitment, such as pursuing higher education. Households are subject
53 to uninsurable idiosyncratic risk in terms of productivity shocks that affect both
54 labor productivity and effectiveness in human capital investment.

55 The interaction between human capital investment and labor supply presents a
56 tradeoff at the household level between current wage earning and future wage gains.
57 At aggregate level, the interaction implies that when individuals transition from
58 the middle to the high sector, they may temporarily exit the workforce to upskill,
59 reducing immediate labor supply but improving future labor productivity.

60 Add interaction between human capital and saving.

61 We model AI advancements as increasing the productivity for the low and high
62 sectors but not for the middle sector so that the skill premium of the middle sector
63 decreases and the skill premium of the high sector increases. Allowing for human
64 capital adjustments not only alters AI's economic implications quantitatively, it also
65 makes a qualitative difference.

66 If the skill distribution is fixed, AI will unambiguously improve the labor pro-
67 ductivity of the whole economy. However, allowing human capital to adjust enables
68 workers to upskill or downskill. The response of overall labor productivity could be
69 enhanced, or dampened, or even reverted depending on whether workers move to
70 more or less productive sectors.

71 Using a two-period model, we show how households' labor supply and human
72 capital investment are affected by their productivity shocks, asset holdings and
73 stocks of human capital. The effects of AI, in this partial equilibrium analysis, are
74 shown to discourage human capital investment for households in the low sector and

³https://nces.ed.gov/programs/digest/d22/tables/dt22_303.70.asp

⁴<https://public.tableau.com/app/profile/researchcenter/viz/CTEEFall2023dashboard/CTEEFall2023>

75 encourage human capital investment for households in the middle sector, thereby
76 increasing human capital inequality. In addition, AI worsens consumption inequality
77 for households with low levels of human capital and reduces consumption inequality
78 for those with high levels of human capital.

79 At the economy level, the effects of AI advancements depend on the sectoral
80 distribution of households and the general equilibrium effects via wage and capital
81 return responses. We quantify these effects using a fully-fledged dynamic quanti-
82 tative model that incorporates an infinite horizon, endogenous asset accumulation,
83 and general equilibrium. The model is calibrated to reflect key features of the U.S.
84 economy, capturing realistic household heterogeneity. The steady state distribution
85 of human capital without AI advancements pins down the sectoral distribution of
86 households. We then introduce fully anticipated AI advancements happening in the
87 near future and study the transition dynamics from the current state of the economy
88 to the eventual new steady state.

89 We find that aggregate human capital rises sharply even before AI introduction,
90 indicating that a substantial portion of workers, anticipating changes in skill pre-
91 mium, leave the labor force early to accumulate human capital. The economy also
92 experiences AI-induced job polarization, with a notable reallocation of workers from
93 the middle sector to either low or high sectors.

94 Building on these labor dynamics, our model examines how AI influences both
95 the aggregate and distributional outcomes of the economy, including output, con-
96 sumption, investment, employment, income inequality, consumption inequality, and
97 wealth inequality. Our focus is on how human capital adjustments reshape AI's
98 effects on each of these outcomes. Specifically, we examine two primary chan-
99 nels through which human capital adjustments operate: the redistribution channel,
100 which reallocates workers across skill sectors, and the general equilibrium channel,
101 which operates through wages and capital return changes.

102 Our findings reveal that human capital responses to AI amplify its positive effects
103 on aggregate output and consumption, mitigate the AI-induced rise in precautionary
104 savings, and stabilize the adjustments in wages and asset returns. Furthermore,
105 while AI-driven human capital adjustments increase inequalities in income, earnings,
106 and consumption, they unexpectedly reduce wealth inequality. We also show that
107 the redistribution channel is the dominant factor in the effects of human capital
108 adjustments, whereas the general equilibrium channel, via wage and capital return
109 changes, plays a comparatively minor role.

110 INTRODUCING PRECAUTIONARY SAVING MOTIVE IN THE WAGE PO-
111 LARIZATION INVESTIGATION Autor *et al.*, (2006)Autor and Dorn (2013)

112 1.1 *Related Literature*

113 This paper relates to the literature examining how technological advancements, in-
114 cluding AI, have significantly contributed to job polarization. Goos and Manning
115 (2007) show that since 1975, the United Kingdom has experienced job polarization,
116 with increasing employment shares in both high- and low-wage occupations. Autor
117 and Dorn (2013) expanded on this by providing a unified analysis of the growth of
118 low-skill service occupations, highlighting key factors that amplify polarization in
119 the U.S. labor market. Empirical evidence from Goos *et al.*, (2014) further confirms
120 pervasive job polarization across 16 advanced Western European economies. In the
121 U.S., Acemoglu and Restrepo (2020) show that robots can reduce employment and
122 wages, finding robust negative effects of automation on both in various commuting
123 zones.

124 The introduction of AI and robotics has had adverse effects on labor markets,
125 with significant implications for employment and labor force participation. Lerch
126 (2021) highlights that the increasing use of robots not only displaces workers but
127 also negatively impacts overall labor force participation rates. Similarly, Faber *et al.*,
128 (2022) demonstrate that the detrimental effects of robots on the labor market have
129 resulted in a decline in job opportunities, particularly in sectors where automation
130 is prevalent. These findings suggest that while technological advancements bring
131 productivity gains, they simultaneously reduce employment prospects and partici-
132 pation in the labor market, exacerbating economic challenges for certain groups of
133 workers.

134 The introduction of AI and robotics also influences human capital accumulation
135 as workers respond to technological disruption. Faced with the employment risks
136 brought about by automation, many exposed workers may invest in additional ed-
137 ucation as a form of self-insurance, rather than relying on increases in the college
138 wage premium (Atkin, 2016; Beaudry *et al.*, 2016). Empirical evidence supports this
139 response. Di Giacomo and Lerch (2023) find that for every additional robot adopted
140 in U.S. local labor markets between 1993 and 2007, four individuals enrolled in col-
141 lege, particularly in community colleges, indicating a rise in educational investments
142 triggered by automation. Similarly, Dauth *et al.*, (2021) show that within German
143 firms, robot adoption has led to an increase in the share of college-educated workers,
144 as firms prioritize higher-skilled employees over those with apprenticeships.

145 The response of human capital accumulation to technological disruption could
146 also go to the other extreme. A 2022 report by Higher Education Strategy Associates
147 finds that following decades of growth, dropping student enrollment has become a
148 major trend in higher education in the Global North.⁵ In the U.S., the public across
149 the political spectrum has increasingly lost confidence in the economic benefits of

⁵<https://higheredstrategy.com/world-higher-education-institutions-students-and-funding/>

150 a college degree. Pew Research Center reports that about half of Americans say
151 having a college degree is less important today than it was 20 years ago in a survey
152 conducted in 2023.⁶ A 2022 study from Public Agenda, a nonpartisan research
153 organization, shows that young Americans without college degrees are most skeptical
154 about the value of higher education.

155 The rise of AI and automation also plays a significant role in exacerbating gen-
156 eral inequality, particularly through its impact on education and wealth distribution.
157 Prettner and Strulik (2020) present a model showing that innovation-driven growth
158 leads to an increasing proportion of college graduates, which in turn drives higher
159 income and wealth inequality. As technology advances, workers with higher educa-
160 tional attainment benefit disproportionately, widening the gap between those with
161 and without advanced skills. Sachs and Kotlikoff (2012) also explore this dynamic,
162 providing a model within an overlapping generations framework that examines the
163 interaction between automation and education. They demonstrate how automation
164 can further entrench inequality by favoring workers with higher levels of educa-
165 tion, as those without adequate skills are more likely to be displaced or see their
166 wages stagnate. This interaction between technological change and educational at-
167 tainment not only amplifies economic inequality but also perpetuates disparities in
168 wealth across generations.

169 The rest of the paper is organized as follows. Section 2 describes the model
170 environment. Section 3 solves the household’s problem using a two-period version
171 of the model. Section 4 solves the fully-fledged quantitative model and calibrates it
172 to fit key features of the U.S. economy, including employment rate, human capital
173 investment, and household heterogeneity. Section 5 incorporates AI into the quanti-
174 tative model and examines its economic impact on both aggregate and distributional
175 outcomes. Section 6 analyzes how human capital adjustments change the economic
176 impact of AI advancements. Section 7 concludes.

177 2 Model Environment

178 Time is discrete and infinite. There is a continuum of households. Each household
179 is endowed with one unit of indivisible labor and faces idiosyncratic productivity
180 shock, z , that follows an AR(1) process in logs:

$$\ln z' = \rho_z \ln z + \varepsilon_z, \varepsilon_z \stackrel{\text{iid}}{\sim} N(0, \sigma_z^2) \quad (1)$$

181 The asset market is incomplete following Aiyagari (1994), and the physical capital,
182 a , is the only asset available to households to insure against this idiosyncratic risk.
183 Households can also invest in human capital, h , which allows them to work in sectors

⁶<https://www.pewresearch.org/social-trends/2024/05/23/public-views-on-the-value-of-a-college-degree/>

¹⁸⁴ with different human capital requirement.

¹⁸⁵ 2.1 Production Technology

¹⁸⁶ The production technology in the economy is a constant-returns-to-scale Cobb-
¹⁸⁷ Douglas production function:

$$F(K, L) = K^{1-\alpha} L^\alpha \quad (2)$$

¹⁸⁸ K represents the total physical capital accumulated by households, while L denotes
¹⁸⁹ the total effective labor supplied by households, aggregated across three sectors: low,
¹⁹⁰ middle, and high. The marginal products of capital and effective labor determine
¹⁹¹ the economy-wide wage rate, w , and interest rate, r .

¹⁹² These sectors differ in their technologies for converting labor into effective labor
¹⁹³ units and in the levels of human capital required for employment. The middle sector
¹⁹⁴ employs households with human capital above h_M and converts one unit of labor
¹⁹⁵ to one effective labor unit. The high sector, requiring human capital above h_H ,
¹⁹⁶ converts one unit of labor to $1 + \lambda$ effective units, while the low sector, with no
¹⁹⁷ human capital requirement, converts one unit into $1 - \lambda$ effective units. This implies
¹⁹⁸ a sectoral labor productivity $x(h)$ that is a step function in human capital:

$$x(h) = \begin{cases} 1 - \lambda & \text{low sector if } h < h_M \\ 1 & \text{middle sector if } h_M < h < h_H \\ 1 + \lambda & \text{high sector if } h > h_H \end{cases} \quad (3)$$

¹⁹⁹ A household i who decides to work thus contributes $z_i x(h_i)$ units of effective labor,
²⁰⁰ where z_i is his idiosyncratic productivity. Denote $n_i \in \{0, 1\}$ as the indicator that
²⁰¹ takes one if the household works and zero if the household does not. The aggregate
²⁰² labor is

$$L = \int n_i z_i x(h_i) di, \quad (4)$$

²⁰³ assuming perfect substitutability of effective labor across the three sectors.

²⁰⁴ 2.2 Household's Problem

²⁰⁵ Households derive utility from consumption, incur disutility from labor and effort of
²⁰⁶ human capital investment. A household maximizes the expected lifetime utility by
²⁰⁷ optimally choosing consumption, saving, labor supply and human capital investment
²⁰⁸ each period, based on his idiosyncratic productivity shock z_t :

$$\max_{\{c_t, a_{t+1}, n_t, e_t\}_{t=0}^{\infty}} E_0 \left[\sum_{t=0}^{\infty} \beta^t (\ln c_t - \chi_n n_t - \chi_e e_t) \right] \quad (5)$$

209 where c_t represents consumption, a_{t+1} represents saving, $n_t \in \{0, 1\}$ is labor supply,
 210 and e_t is the effort of human capital investment.

211 If a household decides to work in period t , he will be employed into the appropriate
 212 sector according to his human capital h_t and receive labor income $w_t z_t x(h_t)$.
 213 The household's budget constraint is

$$c_t + a_{t+1} = n_t(w_t z_t x(h_t)) + (1 + r_t)a_t \quad (6)$$

$$c_t \geq 0 \text{ and } a_{t+1} \geq 0 \quad (7)$$

214 We prohibit households from borrowing $a_{t+1} \geq 0$ to simplify analysis.⁷

215 Human capital investment can take three levels of effort: $\{0, e_L, e_H\}$. A non-
 216 working household is free to choose any of the three effort levels but a working
 217 household cannot devote the highest level of effort e_H , reflecting a trade-off between
 218 working and human capital investment. Hence:

$$e_t \in \{0, e_L, (1 - n_t)e_H\}. \quad (8)$$

219 Its contribution to next-period human capital is subject to the productivity shock:

$$h_{t+1} = z_t e_t + (1 - \delta)h_t \quad (9)$$

220 where δ is human capital's depreciation rate.

221 3 Household Decisions in a Two-Period Model

222 In this section, we solve the household's problem with two periods to gain intuition.

223 **Period-2 decisions** Households do not invest in human capital or physical capital
 224 in the last period. The only relevant decision is whether to work.

225 The household works $n = 1$ if and only if $z \geq \bar{z}(h, a)$, with $\bar{z}(h, a)$ defined as

$$\ln(w\bar{z}(h, a)x(h) + (1 + r)a) - \chi_n = \ln((1 + r)a) \quad (10)$$

226 The household faces a trade-off between earning labor income and incurring the
 227 disutility of working. Given the sector-specific productivity $x(h)$ specified in (3),

⁷According to Aiyagari (1994), a borrowing constraint is necessarily implied by present value budget balance and nonnegativity of consumption. Since the borrowing limit is not essential to our analysis, we set it to zero for simplicity.

²²⁸ the threshold for idiosyncratic productivity, $\bar{z}(h, a)$, takes on three possible values:

$$\bar{z}(h, a) = \begin{cases} \bar{z}(a)^{\frac{1}{1-\lambda}} & \text{if } h < h_M \\ \bar{z}(a) & \text{if } h_M \leq h < h_H \\ \bar{z}(a)^{\frac{1}{1+\lambda}} & \text{if } h > h_H \end{cases} \quad (11)$$

$$\text{where } \bar{z}(a) := \frac{(\exp(\chi_n) - 1)(1 + r)a}{w} \quad (12)$$

²²⁹ Households with higher human capital is more likely to work, whereas households
²³⁰ with higher physical capital is less likely to work.

²³¹ **Period-1 decisions** In addition to labor supply, period-1 decisions include saving
²³² and human capital investment, both of which are forward-looking and affected by
²³³ the idiosyncratic risk associated with the productivity shock z' . Our model also
²³⁴ features a trade-off between human capital investment and labor supply as a working
²³⁵ household cannot devote the highest level of effort e_H in human capital investment.
²³⁶ Therefore, human capital investment grants households the possibility of a discrete
²³⁷ wage hike in the future but may entail a wage loss in the current period.

²³⁸ To see the implication of this trade-off and how it interacts with uninsured
²³⁹ idiosyncratic risk, we proceed in two steps. We first derive the period-1 decisions
²⁴⁰ without uncertainty by assuming that z' is known to the household at period 1 and
²⁴¹ z' is such that the household will work in period 2. We then reintroduce uncertainty
²⁴² in z' and compare the decision rules with the case without uncertainty.

²⁴³ 3.1 Period-1 Labor Supply and Human Capital Investment

²⁴⁴ 3.1.1 Consumption and saving without uncertainty

²⁴⁵ The additive separability of household's utility implies that labor supply n and
²⁴⁶ human capital investment e enters in consumption and saving choices only via the
²⁴⁷ intertemporal budget constraint:

$$c + \frac{c'}{1+r'} = (1+r)a + n(wzx(h)) + \frac{w'z'x(h')}{1+r'} \\ \text{with } h' = ze + (1-\delta)h.$$

²⁴⁸ The log utility in consumption implies the optimality condition:

$$c' = \beta(1+r')c. \quad (13)$$

²⁴⁹ Combining it with the budget constraint, we obtain the optimal consumption as a
²⁵⁰ function of labor supply n and human capital investment e :

$$c(n, e) = \frac{1}{1 + \beta} \left[(1 + r)a + n(wzx(h)) + \frac{w'z'x(h' = ze + (1 - \delta)h)}{1 + r'} \right]. \quad (14)$$

²⁵¹ 3.1.2 Labor supply and human capital investment

²⁵² The optimal consumption rules in (14) and (13) allow us to express the household's
²⁵³ problem as the maximization of an objective function in labor supply n and human
²⁵⁴ capital investment e :⁸

$$\max_{n, e} (1 + \beta) \ln c(n, e) - \chi_n n - \chi_e e \quad (15)$$

²⁵⁵ This maximization depends critically on the household's current human capital and
²⁵⁶ achievable next-period human capital. Accordingly, we partition households into
²⁵⁷ five ranges of h : $[0, h_M]$, $[h_M, h_M(1 - \delta)^{-1}]$, $[h_M(1 - \delta)^{-1}, h_H]$, $[h_H, h_H(1 - \delta)^{-1}]$,
²⁵⁸ and $[h_H(1 - \delta)^{-1}, h_{\max}]$.

²⁵⁹ We now derive the decision rules for households $h \in [h_M, h_M(1 - \delta)^{-1}]$ in detail,
²⁶⁰ as the decision rules for the other four ranges are similar. For households with
²⁶¹ $h < h_M(1 - \delta)^{-1}$, we define two cutoffs in z :

$$\underline{z}_M(h) := \frac{h_M - (1 - \delta)h}{e_H}; \bar{z}_M(h) := \frac{h_M - (1 - \delta)h}{e_L} \quad (16)$$

²⁶² These cutoffs divide households into three groups based on their ability to be em-
²⁶³ ployed in the middle sector in the next period.

²⁶⁴ **Non-learners** are households with $z < \underline{z}_M(h)$. They cannot achieve $h' > h_M$
²⁶⁵ with either e_L or e_H level of human capital investment today. As a result, they will
²⁶⁶ choose not to invest in human capital, $e = 0$, and their future sectoral productivity
²⁶⁷ will be $x(h') = 1 - \lambda$. These non-learners work $n = 1$ if and only if $z \geq \bar{z}_{non}^L(a)$:

$$\bar{z}_{non}^L(a) = \frac{\left(\exp\left(\frac{\chi_n}{1+\beta}\right) - 1\right)[(1 + r)a + \frac{w'z'(1-\lambda)}{1+r'}]}{w} \quad (17)$$

²⁶⁸ **Slow learners** are households with $z \in (\underline{z}_M(h), \bar{z}_M(h))$. These households can
²⁶⁹ reach $h' > h_M$ in the next period only by investing $e = e_H$ today. Their choice
²⁷⁰ is restricted to $e = 0$ or $e = e_H$, since selecting $e = e_L$ incurs a cost without any
²⁷¹ future benefit. Slow learners must trade off between working and human capital
²⁷² investment: choosing $e = e_H$ requires not working today ($n = 0$), while opting to

⁸This follows since $c' = \beta(1 + r')c$, so $\ln c' = \ln \beta + \ln(1 + r') + \ln c$.

²⁷³ work means forgoing investment in human capital ($n = 1, e = 0$).⁹

²⁷⁴ Slow learners prefer ($n = 1, e = 0$) to ($n = 0, e = e_H$) if and only if $z \geq \bar{z}_{slow}^L(a)$:

$$\bar{z}_{slow}^L(a) = \frac{(\exp(\frac{\chi_n - \chi_e e_H}{1+\beta}) - 1)[(1+r)a + \frac{w' z'}{1+r'}] + \lambda \frac{w' z'}{1+r'}}{w} \quad (18)$$

²⁷⁵ **Fast learners** are households with $z > \bar{z}_M(h)$. They can achieve $h' > h_M$ in
²⁷⁶ the next period if they invest $e = e_L$ today. In this case, there is no need to exert
²⁷⁷ high effort e_H in human capital investment. The fast learners choose among three
²⁷⁸ options: ($n = 1, e = 0$), ($n = 1, e = e_L$), and ($n = 0, e = e_L$).¹⁰

²⁷⁹ The decision rule for fast learners are as follows:

$$n(z, h, a), e(z, h, a) = \begin{cases} n = 1, e = 0 & \text{if } z \geq \bar{z}_{fast}^L(a) \\ n = 1, e = e_L & \text{if } \underline{z}_{fast}^L(a) \leq z < \bar{z}_{fast}^L(a) \\ n = 0, e = e_L & \text{if } z < \underline{z}_{fast}^L(a) \end{cases} \quad (19)$$

²⁸⁰ where

$$\bar{z}_{fast}^L(a) = \frac{\left\{ \exp(\frac{\chi_e e_L}{1+\beta}) \lambda \left[\exp(\frac{\chi_e e_L}{1+\beta}) - 1 \right]^{-1} - 1 \right\} \frac{w' z'}{1+r'} - (1+r)a}{w} \quad (20)$$

²⁸¹

$$\underline{z}_{fast}^L(a) = \frac{(\exp(\frac{\chi_n}{1+\beta}) - 1)[(1+r)a + \frac{w' z'}{1+r'}]}{w} \quad (21)$$

²⁸² We set up our model so that $\bar{z}_{fast}^L(a) > \underline{z}_{fast}^L(a)$.¹¹

²⁸³ **Decision rule diagram:** Figure 1 illustrates the decision rule (n, e) as a function
²⁸⁴ of states (z, h, a) for households with $h_M \leq h < h_M \frac{1}{1-\delta}$. The human capital h
²⁸⁵ changes along the horizontal line and the idiosyncratic productivity z changes along
²⁸⁶ the vertical line. The two diagonal lines, $\bar{z}_M(h)$ and $\underline{z}_M(h)$ defined in (16), separate
²⁸⁷ the state space into three areas: the unshaded area represents the non-learners,
²⁸⁸ the lightly-shaded area represents the slow learners, and the darkly-shaded area
²⁸⁹ represents the fast learners. The areas are divided by four dashed horizontal lines
²⁹⁰ associated with cutoffs $\bar{z}_{non}^L(a)$, $\bar{z}_{slow}^L(a)$, $\underline{z}_{fast}^L(a)$, and $\bar{z}_{fast}^L(a)$ that are functions of
²⁹¹ capital holding a and defined in (17), (18), (21), and (20).

²⁹² This decision rule diagram is representative for households in other four ranges

⁹The choice between $(n = 0, e = e_H)$ and $(n = 0, e = 0)$ does not depend on z . For e_H to be relevant, λ must be large enough so that $(n = 0, e = e_H)$ is preferred to $(n = 0, e = 0)$. See the Appendix for details on the lower bound for λ .

¹⁰Similar to the case of slow learners, the choice between $(n = 0, e = e_L)$ and $(n = 0, e = 0)$ does not depend on z . Moreover, since our model is set up so that $(n = 0, e = e_H)$ dominates $(n = 0, e = 0)$, it implies that $(n = 0, e = e_L)$ dominates $(n = 0, e = 0)$.

¹¹Appendix A.2 provides the parameter restrictions such that the condition for $(n = 0, e = e_H)$ to dominate $(n = 0, e = 0)$ is sufficient for $\bar{z}_{fast}^L(a) > \underline{z}_{fast}^L(a)$.

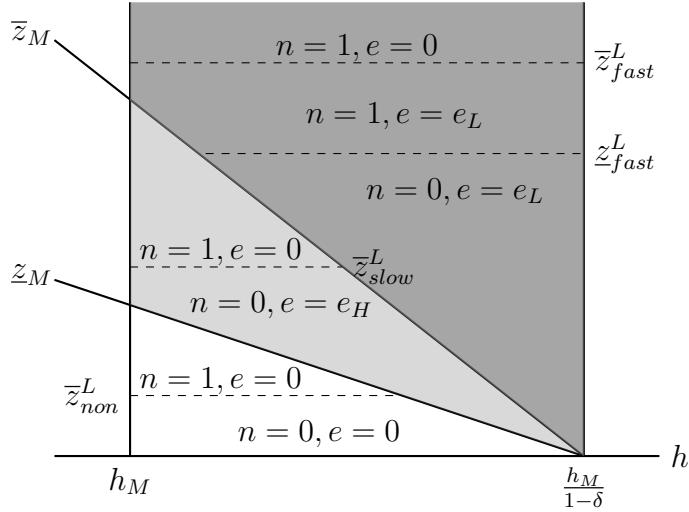


Figure 1: Decision Rule Diagram for $h_M \leq h < h_M(1 - \delta)^{-1}$

The human capital h changes along the horizontal line and the idiosyncratic productivity z changes along the vertical line. The two diagonal lines, $\bar{z}_M(h)$ and $\underline{z}_M(h)$, separate the state space into three areas: the unshaded area represents the non-learners, the lightly-shaded area represents the slow learners, and the darkly-shaded area represents the fast learners. The areas are divided by four dashed horizontal lines associated with cutoffs \bar{z}_{non}^L , \bar{z}_{slow}^L , \underline{z}_{fast}^L , and \bar{z}_{fast}^L that are functions of capital holding a .

of human capital. Figure 2 illustrates the regions in which households make positive human capital investments. Striped shading highlights where investment occurs, with dark areas denoting fast learners and light areas representing slow learners.

For households with $h < h_M$, $\bar{z}_M(h)$ and $\underline{z}_M(h)$ continue to be the boundaries that separate non-learners, slow learners and fast learners, but the four cutoffs are $\bar{z}_{non}^L \frac{1}{1-\lambda}$, $\bar{z}_{slow}^L \frac{1}{1-\lambda}$, $\underline{z}_{fast}^L \frac{1}{1-\lambda}$, and $\bar{z}_{fast}^L \frac{1}{1-\lambda}$.

For households with $h_M \frac{1}{1-\delta} \leq h < h_H \frac{1}{1-\delta}$, the boundaries for state space division change to $\bar{z}_H(h)$ and $\underline{z}_H(h)$:

$$\underline{z}_H(h) := \frac{h_H - (1 - \delta)h}{e_H}; \quad \bar{z}_H(h) := \frac{h_H - (1 - \delta)h}{e_L} \quad (22)$$

If $h_M \frac{1}{1-\delta} \leq h < h_H$, the four cutoffs that partition the decision regions for households are denoted as $\bar{z}_{non}^M(a)$, $\bar{z}_{slow}^M(a)$, $\underline{z}_{fast}^M(a)$, and $\bar{z}_{fast}^M(a)$ (see Appendix A.1 for the explicit formulae).¹² If $h_H \leq h < h_H \frac{1}{1-\delta}$, the analogous cutoffs are given by $\bar{z}_{non}^M \frac{1}{1+\lambda}$, $\bar{z}_{slow}^M \frac{1}{1+\lambda}$, $\underline{z}_{fast}^M \frac{1}{1+\lambda}$, and $\bar{z}_{fast}^M \frac{1}{1+\lambda}$.

Households with $h \geq h_H \frac{1}{1-\delta}$ are always non-learners, since their human capital guarantees high-sector employment next period without further investment. For them, only the cutoff $\bar{z}_{non}^H(a) \frac{1}{1+\lambda}$ matters.

¹²Appendix A.2 provides parameter restrictions for $\bar{z}_{fast}^M(a) > \underline{z}_{fast}^M(a)$.

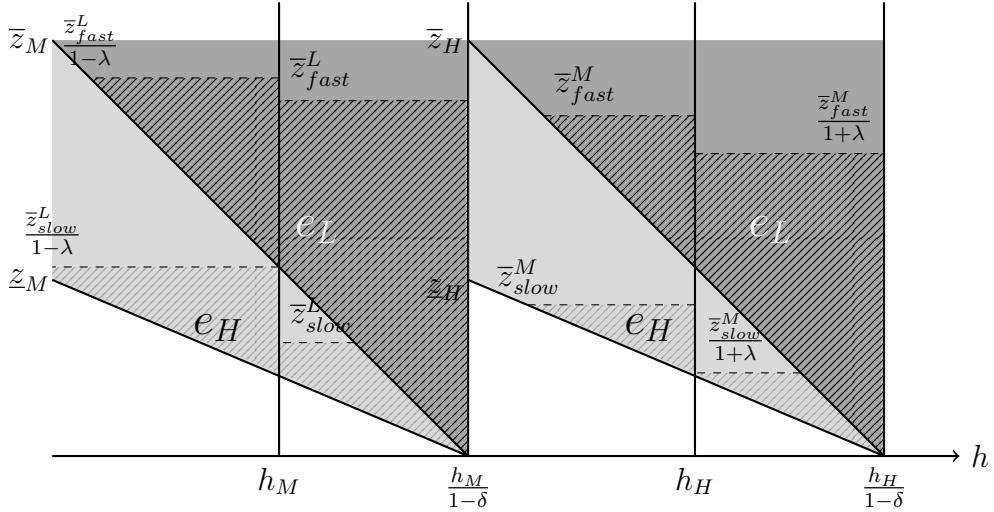


Figure 2: State Space for Human Capital Investment

The darkly-shaded striped areas indicate the state space for human capital investment equal to e_L by the fast learners. The lightly-shaded striped areas indicate the state space for human capital investment equal to e_H by the slow learners.

308 3.2 The Effects of Uninsured Idiosyncratic Risk

309 We now reintroduce the idiosyncratic risk to households in period 1 by assuming
310 that z' follows a log-normal distribution with mean \bar{z}' and variance σ_z^2 .

311 Our previous analysis without uncertainty is a special case with $\sigma_z^2 = 0$. The
312 effects of uninsured idiosyncratic risk can be thought as how households' decisions
313 change when the distribution of z' undergoes a mean-preserving spread in the sense
314 of second-order stochastic dominance.

315 From a consumption-saving perspective, the uncertain z' is associated with future
316 labor income risk. It is well understood in the literature that idiosyncratic future
317 income risk raises the expected marginal utility of future consumption for households
318 with log utility and makes them save more. In our model, households can also supply
319 more labor to mitigate the effect of idiosyncratic income risk on the marginal utility
320 of consumption.

321 From the perspective of human capital investment, the uncertain z' is associated with risk in the return to human capital. Conditional on working, households'
322 income increases with z' : $c' = (1 + r')a' + w'x(h')z'$. $\ln(c')$ is increasing and concave
323 in z' , and a higher $x(h')$ increases the concavity.¹³ Consider two levels of h' , $\bar{h}' > \underline{h}'$,

¹³The marginal effect of z' on $\ln(c')$ is

$$\frac{\partial \ln(c')}{\partial z'} = \frac{w'x(h')}{(1 + r')a' + w'x(h')z'} > 0$$

The second derivative is

$$\frac{\partial^2 \ln(c')}{(\partial z')^2} = - \left[\frac{w'x(h')}{(1 + r')a' + w'x(h')z'} \right]^2 < 0$$

325 a mean-preserving spread of z' distribution reduces the expected utility at both
 326 levels of h' but the reduction is larger for the higher level \bar{h}' . Hence, the expected
 327 utility gain of moving from h' to \bar{h}' is smaller due to the idiosyncratic risk. Human
 328 capital investment is discouraged.

329 Taking into account endogenous labor supply reinforces the discouragement of
 330 human capital investment by the idiosyncratic risk. Recall from Section 3 that
 331 households with z' lower than a cutoff do not work. The endogenous labor supply
 332 therefore provides insurance against the lower tail risk of the idiosyncratic z' . More-
 333 over, the cutoff in z' is lower for those with higher human capital h' . This makes
 334 households with higher h' more exposed to the lower tail risk than those with lower
 335 h' , further reducing the gain of human capital investment.

336 **Proposition 1.** *The uninsured idiosyncratic risk in z' makes households in period
 337 1 save more, work more and invest less in human capital.*

338 3.3 Period-1 Saving and Human Capital Investment

339 In this section, we study the impact of endogenous human capital investment on
 340 households' saving decisions. Specifically, we compare optimal saving behavior in
 341 two scenarios: one in which households can choose to invest in human capital, and
 342 an alternative scenario in which human capital is exogenously fixed. To facilitate the
 343 comparison, we assume in this section that there is no human capital depreciation.¹⁴

344 When the optimal choice of human capital investment is zero, optimal saving is
 345 identical in both scenarios. When the optimal human capital investment is either e_L
 346 or e_H , we compare the household's optimal saving to the case where human capital
 347 investment is exogenously fixed at zero, i.e., $(n = 1, e = 0)$.¹⁵

348 To make the human capital relevant, we assume that $n' = 1$ in period 2. The
 349 additive separability of work and human capital investment effort from consumption
 350 allows us to consider the optimal saving conditional on a given choice of labor supply
 351 and human capital investment.

352 In particular, the household maximizes expected lifetime utility:

$$\max_{a'} : \ln(c) + \beta \mathbb{E}_{z'} [\ln(c')], \quad (23)$$

and is more negative if $x(h')$ is higher.

¹⁴If depreciation is allowed, the analysis proceeds similarly but involves more comparison pairs.

¹⁵Why not compare to $(n = 0, e = 0)$? Such a comparison is not meaningful when considering $(n = 1, e = e_L)$ because the two scenarios involve different state spaces. To see it, suppose conditions are such that $(n = 1, e = e_L)$ is optimal. If we were to fix $e = 0$ exogenously, the household's lifetime income would fall, and as a result the household would have a greater incentive to work. Thus, it is not possible for the household to deviate from choosing $n = 1$ when human capital is held fixed at $e = 0$. The comparison between $(n = 0, e = 0)$ and $(n = 0, e = e_L \text{ or } e_H)$ is similar to the comparison between $(n = 1, e = 0)$ to $(n = 1, e = e_L)$, since human capital investment does not affect period-1 labor income in either case.

³⁵³ subject to the budget constraints

$$c + a' = (1 + r)a + n(wzx(h)), \quad (24)$$

$$c' = (1 + r')a' + w'z'x(h'), \quad (25)$$

$$\text{with } h' = ze + (1 - \delta)h, e \in \{0, e_L, (1 - n)e_H\} \quad (26)$$

³⁵⁴ **3.3.1 Effect of on-job-training on saving**

³⁵⁵ We now compare the optimal saving between $(n = 1, e = e_L)$ and $(n = 1, e = 0)$,
³⁵⁶ where e_L allows households to move to a higher sector in period 2 with higher
³⁵⁷ sectoral productivity $x(h')$.

³⁵⁸ To simplify the notation while maintaining the key economic forces, we normalize
³⁵⁹ $(1 + r) = (1 + r') = 1$, $w = w' = 1$, the period-1 productivity shock $z = 1$ and the
³⁶⁰ period-2 productivity shock z' to $\ln z' \sim \mathcal{N}(0, \sigma_z^2)$. The budget constraints become:

$$c + a' = a + x, \quad c' = a' + txz' \quad (27)$$

³⁶¹ where $t \geq 1$ represents the effect of human capital investment on period-2 income:
³⁶² $t > 1$ if $e = e_L$; $t = 1$ if $e = 0$.

³⁶³ The optimal saving is determined by the FOC:

$$\frac{1}{a + x - a'} = \beta \mathbb{E}_{z'} \left(\frac{1}{a' + txz'} \right) \quad (28)$$

³⁶⁴ Denoting the mean and variance of z' as μ and Σ , respectively:

$$\mu \equiv \mathbb{E}[z'] = e^{\sigma_z^2/2}, \quad \Sigma \equiv \text{Var}(z') = e^{\sigma_z^2}(e^{\sigma_z^2} - 1). \quad (29)$$

³⁶⁵ The second-order approximate solution to the FOC is:

$$a'^*(x, a; t) = \underbrace{\frac{\beta(a + x) - tx\mu}{1 + \beta}}_{\text{CE}} + \underbrace{\frac{t^2 x^2 \Sigma}{\beta(a + x + tx\mu)}}_{\text{Precautionary}} \quad (30)$$

³⁶⁶ The first term is the *certainty-equivalent* saving, which reflects the consumption
³⁶⁷ smoothing motive, increasing in the period-1 resources $a + x$ and decreasing in the
³⁶⁸ period-2 expected labor income $tx\mu$. The second term is the *precautionary* saving,
³⁶⁹ which is increasing in the variance of period-2 labor income $t^2 x^2 \Sigma$ and decreasing in
³⁷⁰ the expected total resources $a + x + tx\mu$.

³⁷¹ The effect of on-job-training on saving can be decomposed into two components:

$$\frac{\partial a'^*}{\partial t}(x, a; t) = -\frac{x\mu}{1 + \beta} + \frac{x^2 \Sigma}{\beta} \frac{t[2(a + x) + tx\mu]}{(a + x + tx\mu)^2}. \quad (31)$$

³⁷² The first term being negative captures the *crowd-out* effect on saving via consumption-

373 smoothing motive as on-job-training increases the expected period-2 labor income
 374 $tx\mu$. The second positive term captures the *crowd-in* effect via precautionary saving
 375 motive as on-job-training exposes households to larger future income risk.

376 To capture the overall impact of on-job-training on saving, we define:

$$\Delta_{\text{on-job}}(x, a; t) = a'^*(x, a; t) - a'^*(x, a; 1) = \int_1^t \frac{\partial a'^*}{\partial u}(x, a; u) du, \quad (32)$$

377 where $a'^*(x, a; t)$ is the optimal saving when households undertake on-job-training,
 378 and $a'^*(x, a; 1)$ is the optimal saving when human capital is kept exogenously fixed.

379 Whether on-job-training increases or decreases saving ultimately depends on
 380 the balance between the crowd-out effect (via higher expected future income) and
 381 the precautionary crowd-in effect (via heightened future income risk). The next
 382 proposition demonstrates that these effects can dominate differently depending on
 383 skill, so that the overall impact of on-job-training on saving can differ between low-
 384 and high-skilled households.

385 **Proposition 2.** *When the idiosyncratic shock is large enough, i.e., $\frac{\Sigma}{\mu} > \underline{\sigma}(t)$, on-
 386 job-training crowds out saving for low-skilled households and crowds in saving for
 387 high-skilled households: for $x < x^*(a, t)$, $e = e_L$ lowers saving $\Delta_{\text{on-job}}(x, a; t) < 0$;
 388 for $x > x^*(a, t)$, $e = e_L$ raises saving $\Delta_{\text{on-job}}(x, a; t) > 0$.*

389 *Proof.* See Appendix B. □

390 3.3.2 Effect of full-time training on saving

391 We next compare the optimal saving between $(n = 0, e = e_L \text{ or } e_H)$ and $(n =$
 392 $1, e = 0)$. Note that full-time training requires the households to give up their labor
 393 income in period 1, which is not the case for on-job-training. Following the same
 394 normalization and notation as in the previous subsection, we can write the budget
 395 constraints with full-time training and without training as:

$$e = e_H : c + a' = a, \quad c' = a' + txz' \quad (33)$$

$$e = 0 : c + a' = a + x, \quad c' = a' + xz' \quad (34)$$

396 where $t > 1$ captures the effect of full-time training on period-2 income.

397 The second-order approximate solution to the optimization problem is:

$$e = e_H : a'_{e_H}^*(x, a; t) = \underbrace{\frac{\beta a - tx\mu}{1 + \beta}}_{\text{CE}} + \underbrace{\frac{t^2 x^2 \Sigma}{\beta(a + tx\mu)}}_{\text{Precautionary}} \quad (35)$$

$$e = 0 : a'^*(x, a; 1) = \underbrace{\frac{\beta(a + x) - x\mu}{1 + \beta}}_{\text{CE}} + \underbrace{\frac{x^2 \Sigma}{\beta(a + x + x\mu)}}_{\text{Precautionary}} \quad (36)$$

³⁹⁸ so that the total effect of full-time training on saving is:

$$\Delta_{\text{full-time}}(x, a; t) = a'_{e_H}(x, a; t) - a'^*(x, a; 1) \quad (37)$$

$$= \Delta_{\text{on-job}}(x, a; t) - x \frac{\beta}{1 + \beta} + \frac{t^2 x^2 \Sigma}{\beta} \frac{x}{(a + x + tx\mu)(a + tx\mu)} \quad (38)$$

³⁹⁹ Compared to the effect of on-job-training, represented by $\Delta_{\text{on-job}}(x, a; t)$ defined in
⁴⁰⁰ (32), full-time training introduces two additional effects on saving. First, it further
⁴⁰¹ reduces saving because households forgo their period-1 labor income, as reflected
⁴⁰² in the second term. Second, it increases precautionary saving, since having lower
⁴⁰³ current resources leaves households less able to self-insure against idiosyncratic risk
⁴⁰⁴ in period 2, which is captured by the third term. Denote the net additional effect
⁴⁰⁵ of full-time training on saving as:

$$\Delta_H(x, a; t) \equiv x \left[-\frac{\beta}{1 + \beta} + \frac{\Sigma}{\beta} \frac{t^2 x^2}{(a + x + tx\mu)(a + tx\mu)} \right] \quad (39)$$

⁴⁰⁶ so that $\Delta_{\text{full-time}}(x, a; t) = \Delta_{\text{on-job}}(x, a; t) + \Delta_H(x, a; t)$. The next proposition shows
⁴⁰⁷ that the net additional effect is negative and stronger for higher skilled households.

⁴⁰⁸ **Proposition 3.** *When the idiosyncratic shock is not too large, i.e., $\frac{\Sigma}{\mu} < \bar{\sigma}(t)$, full-
⁴⁰⁹ time training crowds out more saving than on-job-training, $\Delta_H(x, a; t) < 0$. More-
⁴¹⁰ over, the crowding-out effect is stronger for higher skilled households: $\Delta_H(x, a; t)$ is
⁴¹¹ decreasing in x .*

⁴¹² *Proof.* See Appendix B. □

⁴¹³ 3.4 The Effects of an Anticipated Period-2 AI Shock

⁴¹⁴ Suppose that an AI shock is anticipated to occur in period 2 and to increase the
⁴¹⁵ labor productivity for the low sector and the high sector but not the middle sector.
⁴¹⁶ The effect of AI shock on the sectoral productivity is captured by γ with $0 < \gamma < 1$:

$$x(h') = \begin{cases} 1 - \lambda + \gamma\lambda & \text{low sector if } h' < h_M \\ 1 & \text{middle sector if } h_M < h' < h_H \\ 1 + \lambda + \gamma\lambda & \text{high sector if } h' > h_H \end{cases} \quad (40)$$

⁴¹⁷ In other words, the AI shock increases average labor productivity, reduces the earn-
⁴¹⁸ ings premium for the middle sector, and enlarges the earnings premium for the high
⁴¹⁹ sector relative to the middle sector.

⁴²⁰ 3.4.1 Effects on human capital investment

⁴²¹ The AI shock lowers the incentive to work in the middle sector in period 2. Con-
⁴²² sequently, households with $h < h_M/(1 - \delta)$ reduce their human capital investment,

423 while those with $h > h_M/(1 - \delta)$ increase it. More specifically, the upper bounds
 424 that determine whether households undertake positive human capital investment –
 425 denoted by \bar{z}_{slow}^L and \bar{z}_{fast}^L for $h < h_M/(1 - \delta)$, and \bar{z}_{slow}^M and \bar{z}_{fast}^M for $h > h_M/(1 - \delta)$
 426 – respond in opposite directions to the anticipated shock: the former decrease with
 427 γ and the latter increase. This relationship is formalized below.

428 **Proposition 4.** *An anticipated AI shock decreases human capital investment among
 429 households with $h < h_M/(1 - \delta)$, but increases it among those with $h > h_M/(1 - \delta)$.
 430 Specifically, \bar{z}_{slow}^L and \bar{z}_{fast}^L decrease with γ , while \bar{z}_{slow}^M and \bar{z}_{fast}^M increase with γ .*

431 *Proof.* See Appendix B. □

432 3.4.2 Effects on labor supply

433 **via income:** The AI shock raises period-2 labor income for households who will
 434 work in the low or high sector, leading to a positive income effect that reduces their
 435 labor supply in period 1.

436 **via full-time training:** Because full-time training and labor supply compete for
 437 time, the AI shock affects their tradeoff through its impact on human capital invest-
 438 ment incentives. For $h > h_M/(1 - \delta)$, where AI makes investing in additional skills
 439 more attractive, households are more likely to engage in full-time training and thus
 440 reduce period-1 labor supply. In contrast, for $h < h_M/(1 - \delta)$, where the AI shock
 441 lowers the payoff to investing in skills, households shift away from full-time training
 442 and supply more labor in the first period.

443 3.4.3 Effects on saving

444 The AI shock increases sectoral labor productivities for the low and high sectors in
 445 period 2, while leaving the middle sector's labor productivity unchanged. Its effect
 446 on saving can be analyzed as if we are varying the parameter t in the functions
 447 $\Delta_{on-job}(x, a; t)$, defined in (32), and $\Delta_H(x, a; t)$, defined in (39).

448 **Proposition 5.** $\Delta_{on-job}(x, a; t)$ is convex in t . $\Delta_H(x, a; t)$ is increasing in t .

- 449 • If $\Delta_{on-job}(x, a; t) > 0$ and $t > 1$, $\Delta_{on-job}(x, a; t') > \Delta_{on-job}(x, a; t)$ for $t' > t > 1$.
- 450 • If $\Delta_{on-job}(x, a; t) > 0$ and $t < 1$, $\Delta_{on-job}(x, a; t') < \Delta_{on-job}(x, a; t)$ for $1 > t' > t$.

451 *Proof.* See Appendix B. □

452 **Households who stay in the same sector** For middle-sector households, the
 453 AI shock leaves both their incomes and saving unchanged.

454 By contrast, low-sector and high-sector households experience an increase in
 455 period-2 labor income x' as a result of the AI shock. If they remain in the same

456 sector without needing additional human capital investment or on-the-job training,
457 their saving behavior in the absence of the AI shock can be compared to the scenario
458 with fixed human capital. Following the AI shock, however, their situation resembles
459 one with on-the-job training that enhances x' (i.e., $t > 1$). Thus, the effect of the
460 AI shock on saving is captured by the on-the-job training impact, $\Delta_{\text{on-job}}(x, a; t)$.

461 As shown in Proposition 2, $\Delta_{\text{on-job}}(x, a; t)$ has opposite signs for low-skill and
462 high-skill households. This implies that the AI shock *crowds out* saving among
463 low-sector households, while it *crowds in* saving for high-sector households.

464 For households who must undertake full-time training to remain in the high
465 sector, $\Delta_H(x, a; t)$ captures the additional effect of such training on saving. In this
466 case, a higher x' —brought about by the AI shock—corresponds to an increase in t ,
467 further boosting $\Delta_H(x, a; t)$ (Proposition 5). Consequently, the AI shock *crowds in*
468 saving for high-sector households in this scenario as well.

469 **Households who upskill** For low-sector households, saving behavior remains
470 unchanged, as the AI shock does not affect their future productivity after upskilling.

471 For the middle-sector households who upskill via on-job-training, the AI shock
472 boosts their future productivity gain from λ to $(1 + \gamma)\lambda$, which corresponds to a
473 higher t in $\Delta_{\text{on-job}}(x, a; t)$ with $t > 1$. According to Proposition 5, if the pre-shock
474 effect of on-the-job training on saving is positive, the AI shock will *raise* saving.
475 However, if this effect is negative, the overall impact of the AI shock on saving
476 becomes ambiguous.

477 For the middle-sector households who upskill via full-time training, there is an
478 *additional positive effect* of the AI shock on their saving, because a higher x' increases
479 $\Delta_H(x, a; t)$ (Proposition 5).

480 **Households who downskill** Downsampling, which reflects human capital depre-
481 ciation, does not require any new investment in skills. For high-sector households
482 who transition downward, the AI shock leaves their future productivity – and thus
483 their saving – unchanged.

484 For middle-sector households who downskill to the low sector, their saving differs
485 from the fixed human capital scenario by $\Delta_{\text{on-job}}(x, a; t)$ with $t < 1$. The AI shock
486 mitigates their future productivity loss by reducing it from λ to $(1 - \gamma)\lambda$, effectively
487 increasing t to a new value $t' < 1$. According to Proposition 5, if the pre-shock effect
488 $\Delta_{\text{on-job}}(x, a; t)$ is positive, the AI shock will *reduce* saving. If this effect is negative,
489 however, the overall impact of the AI shock on saving is ambiguous.

490 3.5 Limitations of the two-period model

491 Up to this point, our analysis has focused on how AI influences household-level
492 decisions regarding human capital investment, labor supply, and saving within the

493 framework of a two-period model. While this provides valuable insights into individual
494 behavioral responses, understanding the broader, economy-wide implications
495 of AI requires moving to a more comprehensive setting – a quantitative model with
496 an infinite time horizon, endogenous asset accumulation, and general equilibrium
497 feedback.

498 **General equilibrium (GE) effects** When households adjust their investment in
499 human capital, labor supply, and savings in response to AI, these changes aggregate
500 up to affect the total supply of effective labor and capital in the economy. As these
501 aggregates shift, they exert downward or upward pressure on the wage rate and
502 the interest rate, feeding back into each household’s optimization problem. Thus,
503 general equilibrium effects capture the intricate loop by which individual decisions
504 shape, and are shaped by, the macroeconomic environment.

505 **Composition effects** Endogenizing human capital investment injects dynamism
506 into how households sort themselves among the three skill sectors. When an AI shock
507 occurs, individuals may choose to retrain, upskill, or even move to lower-skilled work,
508 reshaping the distribution of labor across sectors. This shifting composition changes
509 the relative size of each sector, with significant consequences for both aggregate
510 outcomes and the distributional effects of AI.

511 4 A Quantitative Model

512 We now solve the full dynamic model with infinite horizon, endogenous asset accumulation,
513 and general equilibrium. We calibrate the model to reflect key features of
514 the U.S. economy, capturing reasonable household heterogeneity.

515 4.1 Calibration

516 We calibrate the model to match the U.S. economy. For several preference parameters,
517 we adopt values commonly used in the literature. Other parameters are
518 calibrated to align with targeted moments. The model operates on an annual time
519 period. Table I summarizes the parameter values used in the benchmark model.

520 The time discount factor, β , is calibrated to match an annual interest rate of 4 percent.
521 We set χ_n to replicate an 80 percent employment rate. We calibrate χ_e to match the fact that around 30 percent of the population invests in human capital.
523 The borrowing limit, \underline{a} , is set to 0.

524 We calibrate parameters regarding labor productivity process as follows. We
525 assume that x follows the AR(1) process in logs: $\log z' = \rho_z \log z + \epsilon_z$, where
526 $\epsilon_z \sim N(0, \sigma_z^2)$. The shock process is discretized using the Tauchen (1986) method,
527 resulting in a transition probability matrix with 9 grids. The persistence parameter

Table I: Parameters for the Calibration

Parameter	Value	Description	Target or Reference
β	0.91795	Time discount factor	Annual interest rate
ρ_z	0.94	Persistence of z shocks	See text
σ_z	0.287	Standard deviation of z shocks	Earnings Gini
\underline{a}	0	Borrowing limit	See text
χ_n	2.47	Disutility from working	Employment rate
χ_e	1.48	Disutility from HC effort	See text
\bar{n}	1/3	Hours worked	Average hours worked
e_H	1/3	High level of effort	Average hours worked
e_L	1/6	Low level of effort	See text
h_M	0.41	Human capital cutoff for M	See text
h_H	0.96	Human capital cutoff for H	See text
λ	0.2	Skill premium	Income Gini
α	0.36	Capital income share	Standard value
δ	0.1	Capital depreciation rate	Standard value

528 $\rho_z = 0.94$ is chosen based on estimates from the literature. The standard deviation
529 σ_z , is chosen to match the earnings Gini coefficient of 0.63.

530 We deviate from the two-period model by assuming that the labor supply is a
531 discrete choice between 0 and $\bar{n} = 1/3$. This change only rescales the two-period
532 model without altering the trade-off facing the households. But such rescaling facil-
533 itates the interpretation that households are deciding whether to allocate one-third
534 of their fixed time endowment to work. The high-level human capital accumulation
535 effort, e_H is assumed to equal \bar{n} . The low-level effort, e_L is set to half of e_H . The skill
536 premium across sectors, λ , is set at 0.2 to match the income Gini coefficient. Human
537 capital cutoffs, h_M and h_H , are set so that the population shares in low, middle, and
538 high sectors are, respectively, 20, 40, and 40 percent. This population distribution
539 roughly matches the fractions of U.S. workers in 2014 who are employed in routine
540 manual occupations (low sector), routine cognitive and non-routine manual (middle
541 sector), and non-routine cognitive (high sector) (Cortes *et al.*, 2017).

542 On the production side, we set the capital income share, α , to 0.36, and the
543 depreciation rate, δ , to 0.1.

544 4.2 Key Moments: Data vs. Model

545 In Table II, we present a comparison of key moments between the model and the
546 empirical data. The model does an excellent job of replicating the 80% employment
547 rate observed in the data. In this context, employment is defined as having positive
548 labor income in the given year, consistent with the common approach used in the
549 literature. According to OECD (1998), the share of the population investing in
550 human capital—those who are actively engaged in skill acquisition or education—is

Table II: Key Moments

Moment	Data	Model
Employment rate	0.80	0.80
Human capital investment ratio	0.29	0.29
Gini coefficient for wealth	0.78	0.76
Gini coefficient for earnings	0.63	0.62
Gini coefficient for income	0.57	0.58

551 approximately 30%, a figure well matched by the model’s predictions. This is an
 552 important metric because it reflects the model’s capacity to capture the dynamics
 553 of human capital formation, which plays a critical role in shaping long-run earnings
 554 and income inequality. Additionally, the model accurately captures the distribution
 555 of income and earnings, aligning closely with observed data. This suggests that the
 556 model effectively incorporates the key mechanisms driving labor market outcomes
 557 and the corresponding distributional aspects of earnings. Although the model does
 558 not explicitly target the wealth Gini coefficient, it achieves a close match to the
 559 data: the empirical wealth Gini is 0.78, while the model produces a value of 0.76.
 560 This highlights the model’s ability to capture substantial wealth inequality in the
 561 economy.

562 4.3 Steady-state Distribution

563 Table III presents the steady-state distribution of population, employment, and
 564 assets across sectors. The population shares are calibrated to 20%, 40%, and
 565 40% by adjusting the human capital thresholds that define sectors. The shares
 566 of employment and assets are endogenously determined by households’ labor supply
 567 and savings decisions. Notably, the high sector accounts for 46% of total employ-
 568 ment—exceeding its population share—indicating that a disproportionate number
 569 of households choose to work in that sector. Asset holdings are even more skewed:
 570 the high sector holds 68% of total assets, while the low sector holds only 8%.

Table III: Distribution of Population, Employment and Assets

Sectors	Pop. Share (%)	Emp. Share (%)	Assets Share (%)
Low	20.76	18.58	8.07
Middle	38.87	35.35	23.92
High	40.35	46.07	68.01

Note: Human capital cutoffs, h_H and h_M , determine the population share across sectors. Employment share and assets share are implied by households labor supply decisions and saving decisions.

571 5 AI’s Impact on Human Capital Adjustments

572 We now introduce AI technology into the quantitative model, assuming that it will
 573 be implemented in 10 years and that households have full information about its

Figure 3: Steady-state Human Capital Distribution

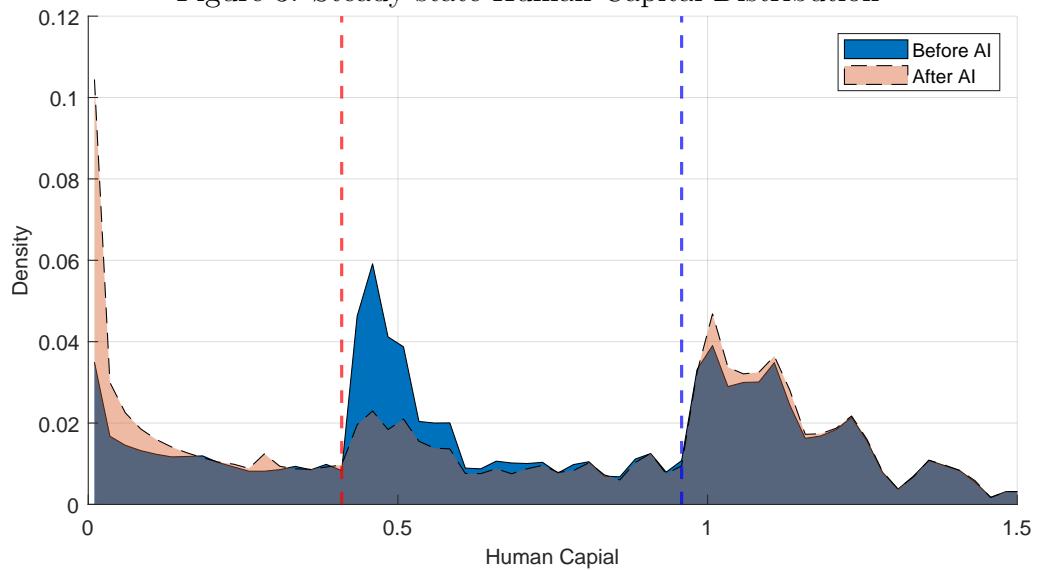
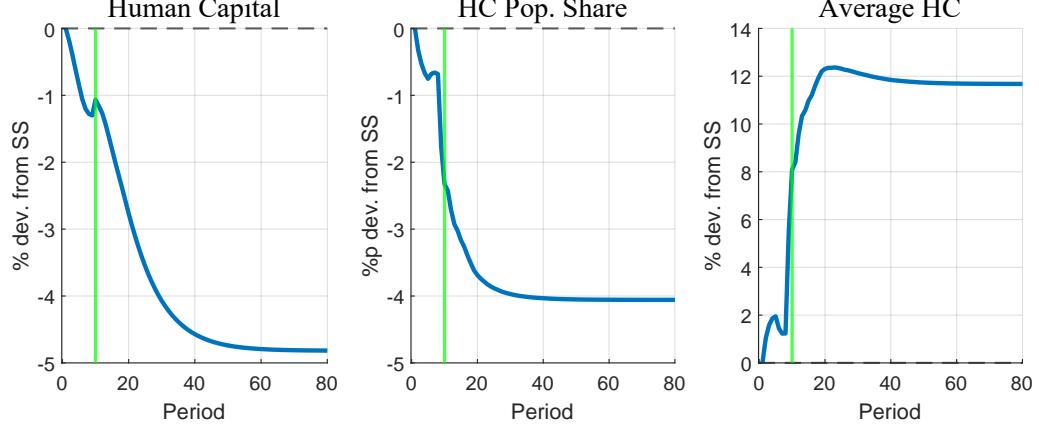


Figure 4: Transition Path for Human Capital Investment



574 arrival. We examine both the transition dynamics and the differences between the
575 initial and new steady states. This framework allows us to analyze how the economy
576 adjusts in anticipation of, and in response to, the adoption of AI.

577 The effect of AI on the sectorial productivity is modeled as in (40) with $\gamma = 0.3$.
578 That is, AI boosted the productivity of the low sector workers by 7.5% and the
579 productivity of the high sector workers by 5%, leaving the middle sector intact.
580 It captures the key idea that AI increases average labor productivity (Acemoglu
581 and Restrepo, 2019), but reduces the earning premium for the middle sector, and
582 enlarges the earning premium for the higher sector relative the middle sector.

583 *5.1 Human Capital Adjustments*

584 Given the employment distribution in the initial steady state, AI is projected to
585 increase the economy's labor productivity by 4% on average, assuming households
586 do not alter their decisions in response. However, changes in earning premiums
587 incentivize households to adjust their human capital investments.

588 **Steady-state human capital distribution:** Figure 3 illustrates how households
589 reallocate across sectors in the new steady state relative to the initial one. The x-axis
590 denotes the level of human capital, while the y-axis indicates the mass of households
591 at each human capital level. The red vertical line marks the cutoff between the low
592 and middle sectors, and the blue vertical line marks the cutoff between the middle
593 and high sectors.

594 The gray shaded area shows the overlap between the two steady-state distri-
595 butions. Within each sector, the distribution of households is skewed to the left,
596 reflecting the tendency for human capital investment to be concentrated among
597 those near the sectoral cutoffs. As shown in the decision rule diagram in Figure 2,
598 some households seek to upgrade their skills, while others aim to remain in more
599 skilled sectors. The blue shaded area highlights the mass of households who have
600 exited the middle sector following the AI shock. The pink areas represent the addi-
601 tional mass of households in the new steady-state distribution, concentrated at the
602 lower end of the low sector and the lower end of the high sector.

603 **Transition path** Figure 4 reports the transition dynamics of aggregate human
604 capital from the initial to the new steady state. The figure also displays its extensive
605 margin (the share of households making positive human capital investments) and
606 intensive margin (average human capital per household among those who invest).

607 As households reallocate from the middle sector to the low and high sectors, the
608 net effect is a gradual decline in aggregate human capital along the transition path.
609 This mirrors the steady-state change observed in Figure 3, where the increased mass
610 at the lower end of the low sector outweighs the increase in the high sector.

611 Additionally, human capital accumulation becomes increasingly concentrated
612 among a smaller share of the population. The proportion of households making
613 positive human capital investments steadily declines, ultimately stabilizing at a level
614 4% lower than in the initial steady state. Meanwhile, the average human capital
615 among those who invest rises, reaching a level 12% higher than the initial steady
616 state in the long run.¹⁶

617 5.2 *Job Polarization*

618 An important implication of human capital adjustments to the AI shock is job
619 polarization. Figure 5 illustrate the transition paths of population shares and em-
620 ployment rates in each sector. Notably, the middle sector experiences a significant
621 decline, with its population share decreasing by approximately 13%. Additionally,
622 employment within this sector plummets to a level 16% lower than the initial steady
623 state. In contrast, both the low and high sectors see increases in their population
624 shares and employment rates. These dynamics indicate a reallocation of *workers*
625 from the middle sector to the low and high sectors following the introduction of AI.

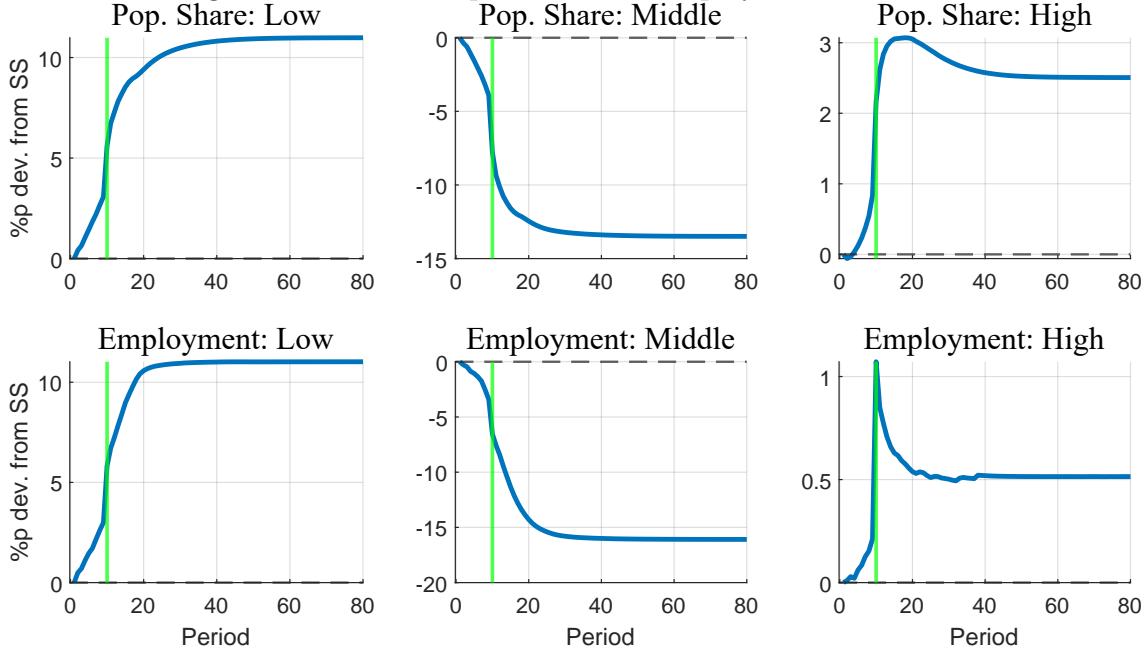
626 **Voluntary job polarization** This worker reallocation aligns with the phenomenon
627 of “job polarization”(Goos *et al.*, 2014), where AI and automation technologies dis-
628 proportionately replace tasks commonly performed by middle-skilled workers. How-
629 ever, our model introduces a complementary mechanism to the conventional under-
630 standing of this reallocation. Specifically, households in our model voluntarily exit
631 the middle sector even before AI implementation by adjusting their human capital
632 investments – many middle-sector workers opt for non-employment to invest in skills
633 that will better position them for the post-AI labor market. To emphasize this key
634 difference, our model deliberately abstracts from any direct negative effect of AI on
635 middle-sector workers.

636 **Employment flows more towards the low sector** Another intriguing finding
637 in our model is the more pronounced employment effect in the low sector compared
638 to the high sector. In the new steady state, the employment rate in the low sector
639 increases by 12%, whereas in the high sector, it rises by only 0.5%. This asymmetry
640 in employment rate changes suggests an unbalanced reallocation of workers from the
641 middle sector, with a greater flow toward the low sector.

642 This disparity arises from two key factors. First, AI enhances the productivity of
643 low-sector workers by 7.5% and high-sector workers by 5%. However, this produc-
644 tivity differential alone does not fully account for the significant asymmetry. The
645 second factor is the variation in labor supply elasticity across sectors. Compared to

¹⁶The only exception to those patterns occurs at period 10 when the positive effects of AI on sectoral productivity are realized.

Figure 5: Sectoral Population and Employment Transition



Note: The transition paths within each sector. The x-axis represents years, and the y-axis shows the percentage (or percentage point) deviation from the initial steady state. AI introduction is assumed to occur in period 10. “Pop. Share” denotes the population share within each sector. “Employment” is the percentage of households who are employed in each sector.

the high sector, the low sector exhibits higher labor supply elasticity, meaning that the same change in labor earnings triggers larger labor supply responses. This is because households in the low sector have lower consumption levels, making their marginal utility of consumption more sensitive to changes in their budget. Consequently, a greater proportion of households in the low sector are at the margin between employment and non-employment (Chang and Kim, 2006).

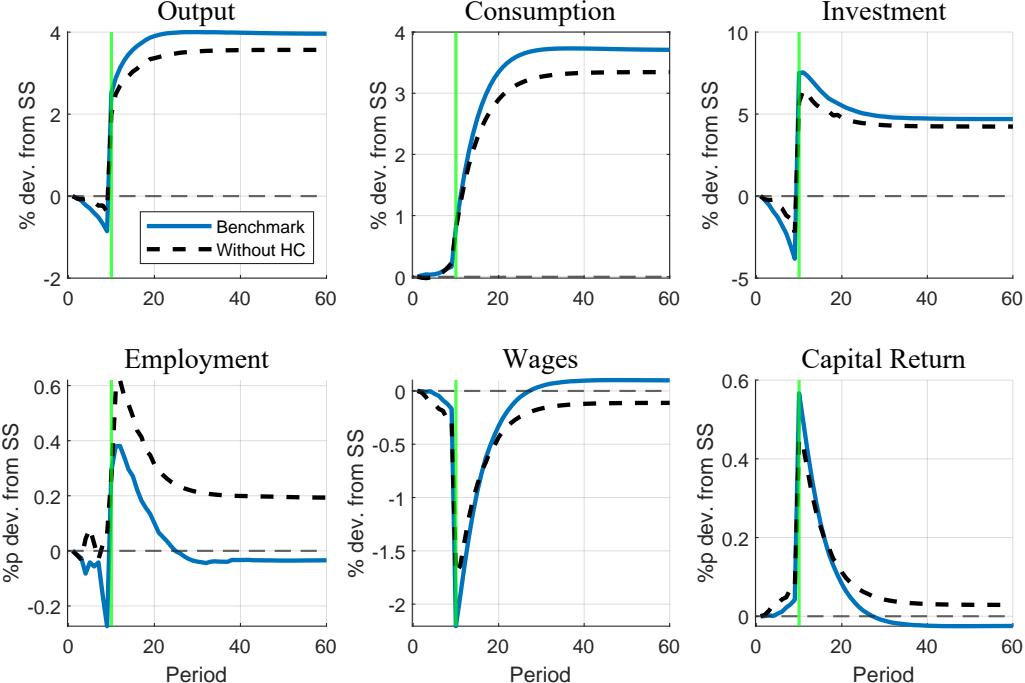
6 The Aggregate and Distributional Effects of AI

The aggregate and distributional effects of AI are shaped by both its direct impact on sectoral productivity and the endogenous response of human capital accumulation. By altering sectoral productivity, AI changes labor earnings, which in turn influences labor supply decisions and savings through income effects. Consequently, AI directly affects the supply of labor and capital, generating aggregate economic responses. Because AI’s productivity effects are heterogeneous across sectors, its impact is inherently distributional.

These sectoral differences also induce human capital adjustments, as households reallocate across sectors in response to changing incentives. This reallocation not only shifts the distribution of labor productivity and aggregate productivity, but also directly shapes distributional outcomes, as households’ relative positions in the income and asset distributions are altered by their movement across sectors.

In this section, we examine the importance of endogenous human capital ad-

Figure 6: Transition Path of Aggregate Variables: Benchmark vs. No HC Models.



Note: The transition paths of aggregate variables: benchmark vs. No HC models. The x-axis represents years, and the y-axis shows the percentage deviation from the initial steady state. AI introduction is assumed to occur in period 10. The No HC model is an economy in which workers maintain their initial steady-state level of human capital throughout the AI implementation until the new steady state is reached.

justment in shaping both the transitional and long-run effects of AI. To do so, we compare the benchmark economy – where households endogenously adjust their human capital – with an alternative scenario in which households are held fixed at their initial steady-state human capital during the AI transition (“No HC model”). In both cases, households make endogenous decisions about consumption, savings, and labor supply.

By contrasting the transition dynamics across these two economies, we can disentangle the direct and indirect effects of AI. The transition path in the No-HC-model isolates the direct impact of AI on aggregate and distributional outcomes, as it abstracts from any human capital adjustments. The difference in outcomes between the benchmark and the No-HC-model then reveals the indirect effects of AI that operate through households’ adjustments in human capital. This decomposition allows us to assess the relative importance of human capital dynamics in driving both the aggregate and distributional consequences of AI.

6.1 Aggregate Implications

Figure 6 shows the transition paths of key macroeconomic variables—output, consumption, investment, and employment—as well as factor prices, including the wage rate and capital return. The blue solid lines depict results from the benchmark model with endogenous human capital adjustment, while the black dashed lines represent the No-HC model in which human capital is held fixed.

686 **6.1.1 AI's direct impacts**

687 The No-HC-model isolates the direct effects of AI. In the long run, the introduction
688 of AI leads to higher output, consumption, investment, and employment. However,
689 in anticipation of AI (prior to period 10), output and investment decline, while
690 consumption and employment remain stable.

691 Before the implementation of AI, sectoral productivity is unchanged; the only
692 difference is households' awareness of future increases in productivity in the low and
693 high sectors beginning in period 10. This anticipation raises households' expected
694 lifetime income, prompting them to save less and consume more ahead of the actual
695 productivity gains. As a result, aggregate capital stock falls, which lowers output and
696 reduces the marginal product of labor while raising the marginal product of capital.
697 Employment remains largely unchanged in this period, as sectoral productivity has
698 not yet shifted.

699 Following the AI shock, sectoral productivity in the low and high sectors rises,
700 boosting labor income, employment, and output in these sectors. Because produc-
701 tivity gains are labor-augmenting, the supply of efficient labor units rises sharply,
702 causing wages to decline and capital returns to increase. Employment and invest-
703 ment both adjust to dampen these factor price changes. In the new steady state, the
704 wage rate is slightly below its initial level, while the return to capital is marginally
705 higher.

706 **6.1.2 AI's indirect impacts via endogenous human capital adjustments**

707 The difference between the No-HC model and the benchmark model captures the
708 indirect effects of AI operating through endogenous human capital adjustments.
709 Among all macroeconomic variables, this indirect effect is most pronounced for em-
710 ployment.

711 In anticipation of AI, employment declines as some households temporarily exit
712 the labor market to invest in human capital and prepare for the post-AI economy.¹⁷
713 During this period, labor productivity remains unchanged, so the decline in em-
714 ployment directly translates to a reduction in output. Consistent with standard
715 consumption-smoothing behavior, this reduction is mainly absorbed by lower in-
716 vestment. Meanwhile, the drop in employment mitigates the direct effects of AI on
717 both wages and capital returns prior to the AI implementation.

718 After AI is introduced, employment rebounds as sectoral productivity increases.
719 However, continued human capital investment by middle-sector households keeps
720 employment lower than in the No-HC model, resulting in an almost neutral long-
721 run effect of AI on employment. Despite this, output, consumption, and investment
722 are all higher in the benchmark model because human capital adjustments reallocate

¹⁷Empirical studies, such as Lerch (2021) and Faber *et al.*, (2022), support the short-term adverse effects of AI adoption on labor markets.

723 more labor to the low and high sectors, thereby better capturing the productivity
724 gains from AI.

725 This reallocation also reverses the steady-state comparison of factor prices: en-
726 dogenous human capital adjustment transforms the negative direct effect of AI on
727 the wage rate into a positive net effect, and the positive direct effect on capital
728 returns into a negative net effect.

729 *6.2 Distributional Implications*

730 The findings above underscore the importance of accounting for human capital ad-
731 justments when assessing the aggregate impact of AI, as households actively adapt
732 to a rapidly evolving labor market. When it comes to economic inequality, endoge-
733 nously adjusting human capital plays an even more significant role.

734 Figure 7 shows the transition paths of Gini coefficients for earnings (labor in-
735 come), total income (capital and labor income), consumption, wealth (asset hold-
736 ings), and human capital. The black dashed lines represent results from the No-HC
737 model, capturing the direct impact of AI without human capital adjustment. In
738 contrast, the blue solid lines reflect the benchmark model, where human capital re-
739 sponds endogenously to both anticipated and realized changes in the skill premium
740 induced by AI.

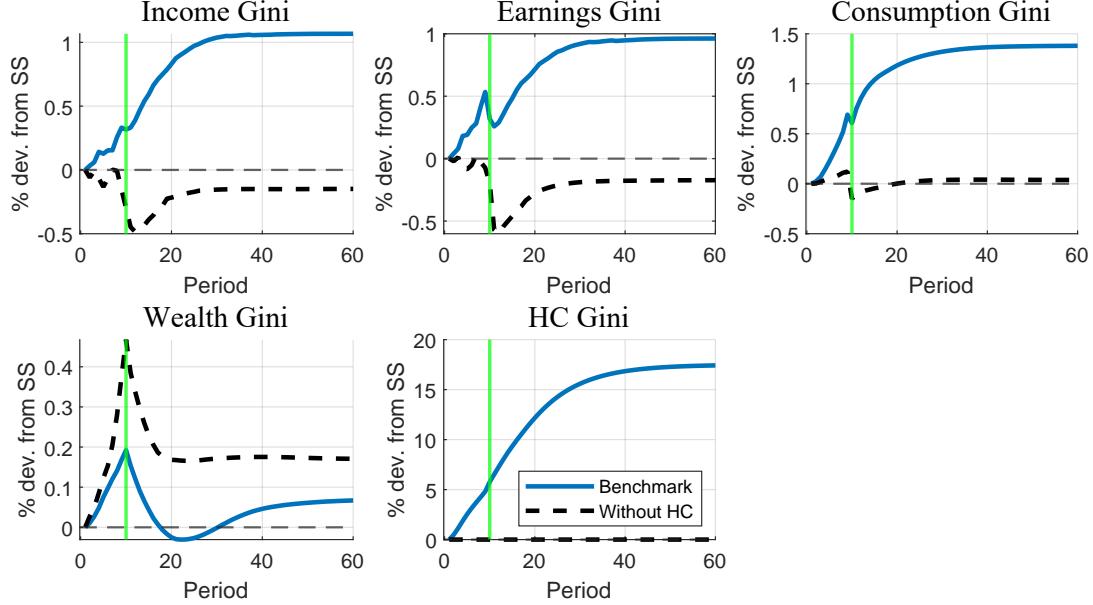
741 **6.2.1 Income, earnings, and consumption inequalities**

742 The comparison of transition paths between the No-HC model and the benchmark
743 model reveals that endogenous human capital adjustments fundamentally alter the
744 impact of AI on income, earnings, and consumption inequalities.

745 **AI's direct impacts:** Without any human capital adjustments, AI's impact on
746 inequalities is primarily driven by productivity gains in the low and high sectors
747 – 7.5% and 5%, respectively. As a result, there is little direct impact on income
748 and earnings Gini coefficients in anticipation of AI before period 10. After AI is
749 implemented, both income and earnings inequality decline: higher labor productivity
750 raises earnings in the low sector, while wage declines in the middle sector compress
751 the distribution. Consumption inequality remains largely unchanged throughout
752 the transition.

753 **Effects of AI-induced human capital adjustments:** Allowing human capital
754 to adjust endogenously, however, leads to pronounced job polarization, as shown in
755 Section 5.2. Households who would have qualified for middle-sector jobs now tran-
756 sition to either the low or high sector. Those moving to the low sector see reduced
757 labor earnings, while those shifting to the high sector enjoy increased earnings. This

Figure 7: Transition Path of Inequality Measures: Benchmark vs. No HC Models.



Note: The transition paths of inequality measures: benchmark vs. No HC models. The x-axis represents years, and the y-axis shows the percentage deviation from the initial steady state. AI introduction is assumed to occur in period 10. The No HC model is an economy in which workers maintain their initial steady-state level of human capital throughout the AI implementation until the new steady state is reached.

758 polarization drives up earnings and income inequality, both before and after AI is
759 implemented. As income disparities widen, consumption inequality also increases.

760 6.2.2 Wealth inequality

761 In stark contrast to the effects on income and earnings inequality, allowing for en-
762 dogenous human capital adjustment mitigates the negative direct impact of AI on
763 wealth inequality. While AI's direct effect would otherwise widen disparities, human
764 capital responses help dampen the increase in wealth inequality, underscoring the
765 stabilizing role of human capital adjustments in the wealth distribution.

766 **AI's direct impacts:** Without any human capital adjustment, AI's impact on
767 households' saving works purely through income effect. In both the low and high
768 sectors, households reduce their savings in anticipation of AI, expecting higher life-
769 time labor income. After AI is implemented at period 10, their savings increase
770 alongside rising labor incomes. In contrast, households in the middle sector, antici-
771 pating a negative income effect from AI due to a lower wage rate, increase their
772 savings prior to period 10. Once AI is introduced and the wage rate recovers,
773 middle-sector households reduce their savings.

774 These shifts in sectoral saving patterns sharply increase wealth inequality before
775 period 10, as low-sector households – typically the least wealthy – reduce their asset
776 holdings. After AI is implemented and saving rates in the low sector recover, the
777 wealth Gini coefficient declines from its peak and stabilizes at a level about 0.2%
778 higher than its initial steady state.

779 **Effects of AI-induced human capital adjustments:** Endogenous human cap-
780 ital responses introduce an additional channel. AI-induced changes in the skill
781 premium motivate more households in the middle and high sectors to undertake
782 full-time training, either to move into or remain in the high sector. This extensive
783 margin adjustment requires these households to forgo labor income and rely on their
784 assets to finance consumption, thus reducing their ability to accumulate additional
785 savings during the transition. Meanwhile, low-sector households reduce their full-
786 time investment in human capital, freeing up resources to save more. As a result,
787 this endogenous response of human capital dampens the rise in wealth inequality
788 that would otherwise occur, helping to stabilize the wealth distribution even as AI
789 reshapes the labor market.

790 I cannot really explain well why the wealth gini in the benchmark model is lower
791 than in the No-HC-model, please help to improve this part.

7 Conclusion

793 Recent studies on AI suggest that advancements are likely to reduce demand for
794 junior-level positions in high-skill industries while increasing the need for roles fo-
795 cused on advanced decision-making and AI oversight. We demonstrate how human
796 capital investments are expected to adapt in response to these shifts in skill demand,
797 highlighting the importance of accounting for these human capital responses when
798 assessing AI's economic impact.

799 Our work points to several promising directions for future research on the eco-
800 nomic impacts of AI. First, while general equilibrium effects—such as wage and
801 capital return adjustments—have a limited role in our model, further research could
802 examine how these effects might vary under different economic conditions or policy
803 environments. Second, if governments implement redistribution policies to address
804 AI-induced inequality, understanding how these policies influence human capital
805 accumulation, and thus their effectiveness, would be valuable. Finally, our model
806 assumes households have perfect foresight when making human capital investments.
807 Relaxing this assumption could reveal new insights into the economic trajectory of
808 AI advancements and offer important policy implications.

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870 A Household Decision Rule Cutoffs

871 A.1 Additional cutoffs formulae for households

$$\bar{z}_{non}^M(a) := \frac{(\exp(\frac{\chi_n}{1+\beta}) - 1)[(1+r)a + \frac{w'z'}{1+r'}]}{w} \quad (\text{A.1})$$

$$\bar{z}_{slow}^M(a) := \frac{(\exp(\frac{\chi_n - \chi_e e_H}{1+\beta}) - 1)[(1+r)a + \frac{w'z'(1+\lambda)}{1+r'}] + \lambda \frac{w'z'}{1+r'}}{w} \quad (\text{A.2})$$

$$\underline{z}_{fast}^M(a) := \frac{(\exp(\frac{\chi_n}{1+\beta}) - 1)[(1+r)a + \frac{w'z'(1+\lambda)}{1+r'}]}{w} \quad (\text{A.3})$$

$$\bar{z}_{fast}^M(a) := \frac{\left\{ \lambda \left[\exp(\frac{\chi_e e_L}{1+\beta}) - 1 \right]^{-1} - 1 \right\} \frac{w'z'}{1+r'} - (1+r)a}{w} \quad (\text{A.4})$$

$$\bar{z}_{non}^H(a) := \frac{(\exp(\frac{\chi_n}{1+\beta}) - 1)[(1+r)a + \frac{w'z'(1+\lambda)}{1+r'}]}{w} \quad (\text{A.5})$$

872 A.2 Parameter restrictions for cutoffs ranking

- 873 To guarantee that $(n = 0, e = e_H)$ dominates $(n = 0, e = 0)$, we need a lower bound
 874 for λ . The slow learners prefer $(n = 0, e = e_H)$ if and only if

$$(1 + \beta) \ln c(n = 0, e = e_H) - \chi_e e_H \geq (1 + \beta) \ln c(n = 0, e = 0)$$

875 or equivalently:

$$\lambda \geq \underline{\lambda}_1 := \frac{(1+r)a + \frac{w'z'}{1+r'}}{\frac{w'z'}{1+r'}} \left(1 - \frac{1}{\exp(\frac{\chi_e e_H}{1+\beta})} \right) \text{ if } h < h_M \frac{1}{1-\delta} \quad (\text{A.6})$$

$$\lambda \geq \underline{\lambda}_3 := \frac{(1+r)a + \frac{w'z'}{1+r'}}{\frac{w'z'}{1+r'}} \left(\exp(\frac{\chi_e e_H}{1+\beta}) - 1 \right) \text{ if } h \geq h_M \frac{1}{1-\delta} \quad (\text{A.7})$$

876 To avoid $(n = 1, e = e_L)$ from being a dominated choice, we need another lower
 877 bound for λ . To see it, recall that $(n = 1, e = 0)$ is better than $(n = 1, e = e_L)$
 878 if $z > \bar{z}_{fast}$, and $(n = 1, e = e_L)$ is better than $(n = 0, e = e_L)$ if $z > \underline{z}_{fast}$.
 879 $(n = 1, e = e_L)$ is therefore the best choice over the interval $(\underline{z}_{fast}, \bar{z}_{fast})$. For such an
 880 interval to exist, it must be the case that when $z = \underline{z}_{fast}$, $z < \bar{z}_{fast}$. $z = \underline{z}_{fast}$ means
 881 that the fast learners are indifferent between $(n = 1, e = e_L)$ and $(n = 0, e = e_L)$ so
 882 that

$$(1+r)a + wzx(h) + \frac{w'z'}{1+r'} = \exp(\frac{\chi_n}{1+\beta}) \left[(1+r)a + \frac{w'z'}{1+r'} \right] \text{ if } h < h_M \frac{1}{1-\delta} \quad (\text{A.8})$$

$$(1+r)a + wzx(h) + \frac{w'z'(1+\lambda)}{1+r'} = \exp(\frac{\chi_n}{1+\beta}) \left[(1+r)a + \frac{w'z'(1+\lambda)}{1+r'} \right] \text{ if } h \geq h_M \frac{1}{1-\delta} \quad (\text{A.9})$$

883 For the fast learners to prefer $(n = 1, e = e_L)$ over $(n = 1, e = 0)$, we need

$$(1+\beta) \ln \frac{c(n=1, e=e_L)}{c(n=1, e=0)} \geq \chi_e e_L \quad (\text{A.10})$$

884 If $h < h_M \frac{1}{1-\delta}$, inequality (A.10) is:

$$(1+\beta) \ln \frac{(1+r)a + wzx(h) + \frac{w'z'}{1+r'}}{(1+r)a + wzx(h) + \frac{w'z'(1-\lambda)}{1+r'}} \geq \chi_e e_L$$

885 Evaluating the left-hand-side at $z = \underline{z}_{fast}$ yields:

$$\lambda \geq \underline{\lambda}_2 := \frac{(1+r)a + \frac{w'z'}{1+r'}}{\frac{w'z'}{1+r'}} \left(1 - \frac{1}{\exp(\frac{\chi_e e_L}{1+\beta})} \right) \exp(\frac{\chi_n}{1+\beta}) \quad (\text{A.11})$$

886 If $h > h_M \frac{1}{1-\delta}$, inequality (A.10) is:

$$(1+\beta) \ln \frac{(1+r)a + wzx(h) + \frac{w'z'(1+\lambda)}{1+r'}}{(1+r)a + wzx(h) + \frac{w'z'}{1+r'}} \geq \chi_e e_L$$

887 Evaluating the left-hand-side at $z = \underline{z}_{fast}$ yields:

$$\lambda \geq \underline{\lambda}_4 := \frac{(1+r)a + \frac{w'z'}{1+r'}}{\frac{w'z'}{1+r'}} \frac{\left(\exp\left(\frac{\chi_e e_L}{1+\beta}\right) - 1\right) \exp\left(\frac{\chi_n}{1+\beta}\right)}{\exp\left(\frac{\chi_e e_L}{1+\beta}\right) + \exp\left(\frac{\chi_n}{1+\beta}\right) - \exp\left(\frac{\chi_e e_L + \chi_n}{1+\beta}\right)} \quad (\text{A.12})$$

888 We have that $\underline{\lambda}_1 > \underline{\lambda}_2$ and $\underline{\lambda}_3 > \underline{\lambda}_4$ if

$$\exp\left(\frac{\chi_e e_H}{1+\beta}\right) > \frac{\exp\left(\frac{\chi_e e_L}{1+\beta}\right)}{\exp\left(\frac{\chi_e e_L}{1+\beta}\right) + \exp\left(\frac{\chi_n}{1+\beta}\right) - \exp\left(\frac{\chi_e e_L + \chi_n}{1+\beta}\right)} \quad (\text{A.13})$$

889 Therefore, the inequality above implies that the conditions (A.6) and (A.7) are
890 sufficient for the conditions (A.11) and (A.12). Furthermore, $\lambda_3 \geq \lambda_1$ so that the
891 condition (A.7) is sufficient for the condition (A.6).

892 We can then conclude that the conditions (A.7) and (A.13) are sufficient for
893 1) the slower learners always prefers $(n = 0, e = e_H)$ over $(n = 0, e = 0)$, and 2)
894 $\bar{z}_{fast} > \underline{z}_{fast}$, i.e., there exists state space where $(n = 1, e = e_L)$ is optimal.

895 A.3 Other cutoffs ranking for the two-period Model

896 For the fast learners, their cutoffs rank as follows

$$\frac{\bar{z}_{fast}^L(a)}{1-\lambda} > \bar{z}_{fast}^L(a) > \bar{z}_{fast}^M(a) > \frac{\bar{z}_{fast}^M(a)}{1+\lambda} \quad (\text{A.14})$$

$$\frac{\underline{z}_{fast}^L(a)}{1-\lambda} > \underline{z}_{fast}^M(a) > \underline{z}_{fast}^L(a) > \frac{\underline{z}_{fast}^M(a)}{1+\lambda} \quad (\text{A.15})$$

897 For the slow learners, the rank of their cutoffs is

$$\frac{\bar{z}_{slow}^L(a)}{1-\lambda} > \bar{z}_{slow}^M(a) > \bar{z}_{slow}^L(a) > \frac{\bar{z}_{slow}^M(a)}{1+\lambda} \quad (\text{A.16})$$

898 For the non-learners, the rank of their cutoffs is

$$\frac{\bar{z}_{non}^L(a)}{1-\lambda} > \bar{z}_{non}^M(a) > \frac{\bar{z}_{non}^H(a)}{1+\lambda} > \frac{\bar{z}_{non}^M(a)}{1+\lambda} \quad (\text{A.17})$$

$$\bar{z}_{non}^M(a) > \bar{z}_{non}^L(a) \quad (\text{A.18})$$

899 B Proof of Proposition

900 B.1 Proof of Proposition 2

901 The derivative of saving with respect to t is

$$\frac{\partial a'^*}{\partial t}(x, a; t) = -\frac{x\mu}{1+\beta} + \frac{x^2\Sigma}{\beta} \frac{t[2(x+a) + tx\mu]}{[(x+a) + tx\mu]^2}. \quad (\text{B.1})$$

902 The total effect of on-job-training on saving is

$$\Delta_{\text{on-job}}(x, a; t) = a'^*(x, a; t) - a'^*(x, a; 1) = \int_1^t \frac{\partial a'^*}{\partial u}(x, a; u) du. \quad (\text{B.2})$$

903 Define

$$F(x, a; u) \equiv x \frac{u[2(x + a) + ux\mu]}{[(x + a) + ux\mu]^2}, \quad \bar{F}(x, a; t) \equiv \frac{1}{t-1} \int_1^t F(x, a; u) du.$$

904 Then equation (B.2) can be written as

$$\Delta_{\text{on-job}}(x, a; t) = x(t-1) \left[\frac{\Sigma}{\beta} \bar{F}(x, a; t) - \frac{\mu}{1+\beta} \right].$$

905 Differentiating $F(x, a; u)$ with respect to x gives

$$\frac{\partial F(x, a; u)}{\partial x} = \frac{2u a (a + x)}{(a + (1 + u\mu)x)^3} > 0,$$

906 so $\bar{F}(x, a; t)$ is strictly increasing in x .

907 The sign of $\Delta_{\text{on-job}}(x, a; t)$ is governed by

$$S(x, a; t) \equiv \frac{\Sigma}{\beta} \bar{F}(x, a; t) - \frac{\mu}{1+\beta}.$$

908 Because $\bar{F}(x, a; t)$ is strictly increasing, $S(x, a; t)$ increases monotonically with x .

909 For $x \rightarrow 0$, $F(x, a; u) \rightarrow 0$ and $\bar{F}(x, a; t) \rightarrow 0$ so that $S(x, a; t) \rightarrow -\frac{\mu}{1+\beta} < 0$,
910 implying $\Delta_{\text{on-job}}(x, a; t) < 0$ for small x .

911 For $x \rightarrow \infty$, $F(x, a; u) \rightarrow \frac{u(2+u\mu)}{(1+u\mu)^2}$ and $\bar{F}(x, a; t) \rightarrow \bar{F}_\infty(t) \equiv \frac{1}{t-1} \int_1^t \frac{u(2+u\mu)}{(1+u\mu)^2} du$. If

$$\frac{\Sigma}{\mu} > \underline{\sigma}(t) \equiv \frac{\beta}{1+\beta} \frac{1}{\bar{F}_\infty(t)} \quad (\text{B.3})$$

912 then $S(x, a; t) > 0$ for sufficiently large x , and hence $\Delta_{\text{on-job}}(x, a; t) > 0$.

913 If idiosyncratic risk is large enough, i.e., condition (B.3) is satisfied, there exists
914 a unique threshold $x^*(t)$ at which the sign flips:

$$\Delta_{\text{on-job}}(x, a; t) < 0 \text{ for } x < x^*(a, t), \quad \Delta_{\text{on-job}}(x, a; t) > 0 \text{ for } x > x^*(a, t).$$

915 B.2 Proof of Proposition 3

916 Denote

$$G(x, a; t) \equiv \frac{t^2 x^2}{(a + x + tx\mu)(a + tx\mu)}$$

⁹¹⁷ the net additional effect of full-time training on saving can be rewritten as

$$\Delta_H(x, a; t) \equiv x \left[-\frac{\beta}{1+\beta} + \frac{\Sigma}{\beta} G(x, a; t) \right]$$

⁹¹⁸ Differentiating $G(x, a; t)$ with respect to x gives

$$\frac{\partial G(x, a; t)}{\partial x} = \frac{t^2 x a (2tx\mu + 2a + x)}{(a + tx\mu)^2 (a + x + tx\mu)^2} > 0,$$

⁹¹⁹ so $G(x, a; t)$ is strictly increasing in x .

⁹²⁰ The limits of $G(x, a; t)$ are:

$$G(x, a; t) \rightarrow 0 \quad (x \rightarrow 0),$$

⁹²¹

$$G(x, a; t) \rightarrow G_\infty(t) \equiv \frac{t}{\mu(1+t\mu)} \quad (x \rightarrow \infty),$$

⁹²² Therefore, $G(x, a; t) < G_\infty(t)$ for any x .

⁹²³ If

$$\frac{\Sigma}{\beta} G_\infty(t) < \frac{\beta}{1+\beta}, \text{ i.e. } \frac{\Sigma}{\mu} < \bar{\sigma}(t) \equiv \frac{\beta^2}{1+\beta} \left(\frac{1}{t} + \mu \right). \quad (\text{B.4})$$

⁹²⁴ Then $\Delta_H(x, a; t) < x[-\frac{\beta}{1+\beta} + \frac{\Sigma}{\beta} G_\infty(t)] < 0$ for any x .

⁹²⁵ Furthermore, with some tedious algebra, we can show that for any x

$$G(x, a; t) + x \frac{\partial G(x, a; t)}{\partial x} < G_\infty(t)$$

⁹²⁶ Hence, the inequality (B.4) also implies that

$$\frac{\partial \Delta_H(x, a; t)}{\partial x} = \frac{\Sigma}{\beta} [G(x, a; t) + x \frac{\partial G(x, a; t)}{\partial x}] - \frac{\beta}{1+\beta} < \frac{\Sigma}{\beta} G_\infty(t) - \frac{\beta}{1+\beta} < 0. \quad (\text{B.5})$$

⁹²⁷ B.3 Proof of Proposition 4

⁹²⁸ The relevant upper bounds of z for positive human capital investment are functions
⁹²⁹ of γ (to the first order approximation):

$$\begin{aligned} \bar{z}_{slow}^L(a; \gamma) &= \bar{z}_{slow}^L(a; \gamma = 0) - \gamma \lambda \frac{w' z'}{w(1+r')} \\ \bar{z}_{fast}^L(a; \gamma) &= \bar{z}_{fast}^L(a; \gamma = 0) - \gamma \lambda \frac{w' z'}{w(1+r')} \frac{\exp(\frac{\chi_e e_L}{1+\beta})}{\exp(\frac{\chi_e e_L}{1+\beta}) - 1} \\ \bar{z}_{slow}^M(a; \gamma) &= \bar{z}_{slow}^M(a; \gamma = 0) + \gamma \lambda \frac{w' z'}{w(1+r')} \exp\left(\frac{\chi_n - \chi_e e_H}{1+\beta}\right) \\ \bar{z}_{fast}^M(a; \gamma) &= \bar{z}_{fast}^M(a; \gamma = 0) + \gamma \lambda \frac{w' z'}{w(1+r')} \frac{1}{\exp(\frac{\chi_e e_L}{1+\beta}) - 1} \end{aligned}$$

930 Therefore, an anticipated AI shock, $\gamma > 0$ makes those with $h < h_M \frac{1}{1-\delta}$ invest less
931 human capital and those with $h > h_M \frac{1}{1-\delta}$ invest more human capital.

932 *B.4 Proof of Proposition 5*

$$\Delta_{\text{on-job}}(x, a; t) = a'^*(x, a; t) - a'^*(x, a; 1) = \int_1^t \frac{\partial a'^*}{\partial u}(x, a; u) du.$$

933 differentiating with respect to t gives

$$\frac{d\Delta_{\text{on-job}}(x, a; t)}{dt} = \frac{\partial a'^*}{\partial t}(x, a; t)$$

934 Since

$$\frac{\partial^2 a'^*(x, a; t)}{\partial t^2} = \frac{\partial}{\partial t} \left(-\frac{x\mu}{1+\beta} + \frac{x^2\Sigma}{\beta} \frac{t[2(x+a)+tx\mu]}{[(x+a)+tx\mu]^2} \right) = \frac{2x^2\Sigma(a+x)^2}{\beta(a+x+tx\mu)^3} > 0. \quad (\text{B.6})$$

935 The slope $\frac{\partial a'^*}{\partial t}(x, a; t)$ is strictly increasing in t . Hence $\Delta_{\text{on-job}}(x, a; t)$ is convex in t .

$$\Delta_H(x, a; t) = x \left[-\frac{\beta}{1+\beta} + \frac{\Sigma}{\beta} G(x, a; t) \right] \text{ with } G(x, a; t) = \frac{t^2 x^2}{(a+x+tx\mu)(a+tx\mu)}$$

936 Differentiating $G(x, a; t)$ with respect to t gives

$$\frac{\partial G(x, a; t)}{\partial t} = \frac{tx^2(2a^2 + 2atx\mu + 2ax + \mu tx^2)}{(a+tx\mu)^2(a+x+tx\mu)^2} > 0,$$

937 so $G(x, a; t)$ is strictly increasing in t , and so is $\Delta_H(x, a; t)$.

938 We now consider the comparison between $\Delta_{\text{on-job}}(x, a; t)$ and $\Delta_{\text{on-job}}(x, a; t')$ for $t' >$
939 t . Given x and a , define

$$f(t) \equiv \frac{\partial a'^*}{\partial t}(x, a; t).$$

940 so $f'(t) > 0$, i.e. $f(t)$ is strictly increasing in t .

941 **Case 1:** $1 < t < t'$

942 Suppose $\Delta_{\text{on-job}}(x, a; t) > 0$. Then

$$\Delta_{\text{on-job}}(x, a; t) = \int_1^t f(u) du > 0.$$

943 Since f is increasing,

$$f(u) \leq f(t) \quad \text{for all } u \in [1, t],$$

944 which implies

$$\Delta_{\text{on-job}}(x, a; t) = \int_1^t f(u) du \leq (t-1) f(t).$$

945 Because $t > 1$, the inequality $\Delta_{\text{on-job}}(x, a; t) > 0$ forces $f(t) > 0$.

946 Now for any $t' > t$,

$$f(u) \geq f(t) > 0 \quad \text{for all } u \in [t, t'],$$

947 and therefore

$$\Delta_{\text{on-job}}(x, a; t') - \Delta_{\text{on-job}}(x, a; t) = \int_t^{t'} f(u) du > 0.$$

948 We then have that:

$$1 < t < t', \Delta_{\text{on-job}}(x, a; t) > 0 \implies \Delta_{\text{on-job}}(x, a; t') > \Delta_{\text{on-job}}(x, a; t) \quad (\text{B.7})$$

949 That is, once $\Delta_{\text{on-job}}(x, a; t)$ becomes positive for $t > 1$, it is strictly increasing in t
950 thereafter.

951 **Case 2:** $t < t' < 1$

952 For $t < 1$,

$$\Delta_{\text{on-job}}(x, a; t) = \int_1^t f(u) du = - \int_t^1 f(u) du.$$

953 Suppose $\Delta_{\text{on-job}}(x, a; t) > 0$. Then

$$-\int_t^1 f(u) du > 0 \implies \int_t^1 f(u) du < 0.$$

954 Since f is increasing

$$f(u) \geq f(t) \quad \text{for all } u \in [t, 1],$$

955 which implies

$$\int_t^1 f(u) du \geq (1-t) f(t).$$

956 Because $t < 1$, the inequality $\Delta_{\text{on-job}}(x, a; t) > 0$ forces $f(t) < 0$.

957 Consider

$$\Delta_{\text{on-job}}(x, a; t') - \Delta_{\text{on-job}}(x, a; t) = \int_t^{t'} f(u) du$$

958 If $f(u) < 0$ for all $u \in [t, t']$, then $\int_t^{t'} f(u) du < 0$.

959 If there exists some $t_s \in [t, t']$ such that $f(t_s) = 0$, so $f(u) < 0$ for $u < t_s$ and
960 $f(u) > 0$ for $u > t_s$. Then $f(u) > 0$ for $u \in [t', 1]$. Hence,

$$\int_{t'}^1 f(u) du > 0$$

961 This implies that

$$\Delta_{\text{on-job}}(x, a; t') = - \int_{t'}^1 f(u) du < 0$$

962 Together with the inequality $\Delta_{\text{on-job}}(x, a; t) > 0$, we have that

$$\Delta_{\text{on-job}}(x, a; t') < \Delta_{\text{on-job}}(x, a; t)$$

963 We then have that

$$t < t' < 1, \Delta_{\text{on-job}}(x, a; t) > 0 \implies \Delta_{\text{on-job}}(x, a; t') < \Delta_{\text{on-job}}(x, a; t). \quad (\text{B.8})$$

964 Thus, for $t < 1$, whenever $\Delta_{\text{on-job}}(x, a; t) > 0$, increasing t toward 0 makes $\Delta_{\text{on-job}}$
965 strictly decrease.

966 C Computational Procedure for the Quantitative Model

967 C.1 Steady-state Equilibrium

968 In the steady-state, the measure of households, $\mu(a, h, x)$, and the factor prices are
969 time-invariant. We find a time-invariant distribution μ . We compute the house-
970 holds' value functions and the decisions rules, and the time-invariant measure of the
971 households. We take the following steps:

- 972 1. We choose the number of grid for the risk-free asset, a , human capital, h , and
973 the idiosyncratic labor productivity, x . We set $N_a = 151$, $N_h = 151$, and
974 $N_x = 9$ where N denotes the number of grid for each variable. To better
975 incorporate the saving decisions of households near the borrowing constraint,
976 we assign more points to the lower range of the asset and human capital.
- 977 2. Productivity x is equally distributed on the range $[-3\sigma_x/\sqrt{1-\rho_x^2}, \sqrt{1-\rho_x^2}]$. As shown
978 in the paper, we construct the transition probability matrix $\pi(x'|x)$ of the
979 idiosyncratic labor productivity.
- 980 3. Given the values of parameters, we find the value functions for each state
981 (a, h, x) . We also obtain the decision rules: savings $a'(a, h, x)$, and $h'(a, h, x)$.
982 The computation steps are as follow:
- 983 4. After obtaining the value functions and the decision rules, we compute the
984 time-invariant distribution $\mu(a, h, x)$.
- 985 5. If the variables of interest are close to the targeted values, we have found the
986 steady-state. If not, we choose the new parameters and redo the above steps.

987 *C.2 Transition Dynamics*

988 We incorporate the transition path from the status quo to the new steady state. We
989 describe the steps below.

- 990 1. We obtain the initial steady state and the new steady state.
- 991 2. We assume that the economy arrives at the new steady state at time T . We
992 set the T to 100. The unit of time is a year.
- 993 3. We initialize the capital-labor ratio $\{K_t/L_t\}_{t=2}^{T-1}$ and obtain the associated
994 factor prices $\{r_t, w_t\}_{t=2}^{T-1}$.
- 995 4. As we know the value functions at time T , we can obtain the value functions
996 and the decision rules in the transition path from $t = T - 1$ to 1.
- 997 5. We compute the measures $\{\mu_t\}_{t=2}^T$ with the measures at the initial steady state
998 and the decision rules in the transition path.
- 999 6. We obtain the aggregate variables in the transition path with the decision rules
1000 and the distribution measures.
- 1001 7. We compare the assumed paths of capital and the effective labor with the
1002 updated ones. If the absolute difference between them in each period is close
1003 enough, we obtain the converged transition path. Otherwise, we assume new
1004 capital-labor ratio and go back to 3.

1005 **D Investigating the GE channel of AI's impact**

1006 **Redistribution versus general equilibrium effects:** The effects of human cap-
1007 ital adjustments on AI's aggregate impacts operate through two primary channels:
1008 the *redistribution channel*, which reallocates households across skill sectors, and the
1009 *general equilibrium (GE) channel*, which operates through changes in wages and
1010 capital returns. We now assess the relative importance of these channels in shaping
1011 economic outcomes.

1012 Figure ?? compares the transition dynamics between scenarios with and without
1013 human capital adjustments, while holding wages and capital returns fixed at their
1014 initial steady-state levels to eliminate GE effects. We refer to the former as the
1015 "PE Model" and the latter as the "No-HC PE Model." The difference between the
1016 solid blue line and the dashed red line isolates the effect of redistribution channel.
1017 Comparing this difference to the gap between the benchmark model and the No
1018 HC model in Figure 6 enables us to evaluate the importance of the redistribution
1019 channel relative to the GE channel. Two key observations emerge.

1020 First, the *redistribution channel* alone accounts for all the *qualitative effects* of
1021 human capital adjustments on AI's aggregate impacts. Redistribution of human

Figure 8: Caption
Consumption

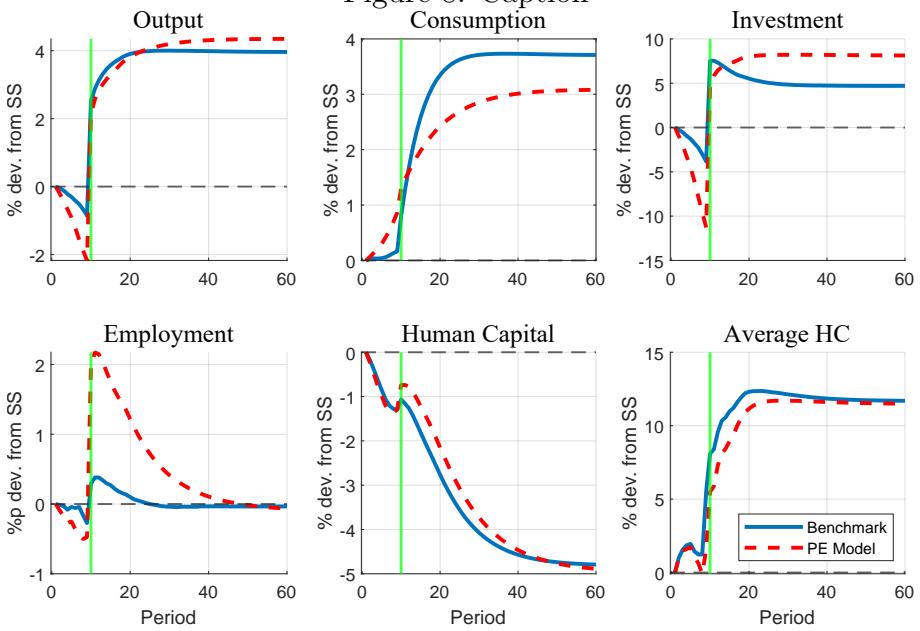
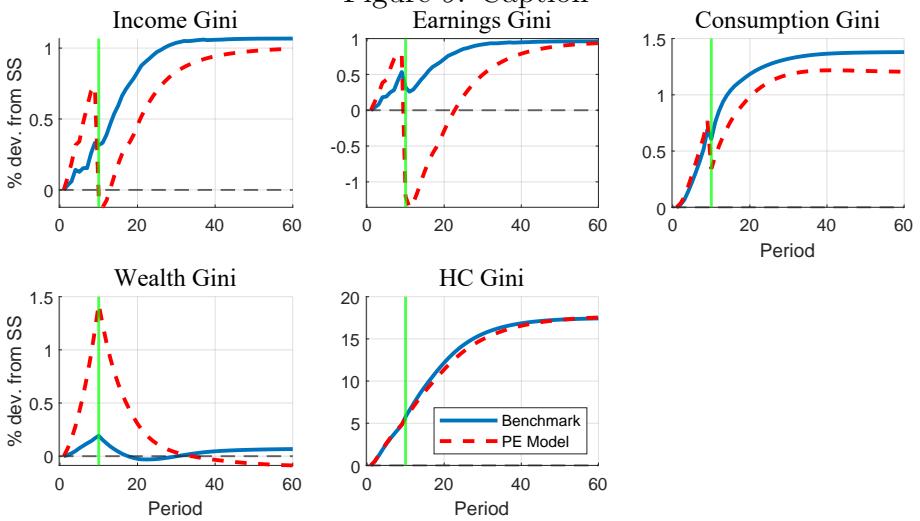


Figure 9: Caption
Earnings Gini



1022 capital increases consumption, even before AI implementation, as more households
1023 shift to the high sector. It also reduces investment by mitigating precautionary
1024 savings and lowers employment as middle-sector workers leave the labor market
1025 to invest in human capital. In the long run, redistribution amplifies AI's positive
1026 impact on output by reallocating more workers to sectors that benefit most from AI
1027 advancements.

1028 Second, the *GE channel* primarily affects the *quantitative magnitude* of human
1029 capital adjustments' impact on AI's aggregate outcomes. When the GE channel is
1030 included, the differences in output, consumption, and employment between models
1031 with and without human capital adjustments are smaller compared to when the
1032 GE channel is excluded. In contrast, and somewhat unexpectedly, the difference in
1033 investment is larger when the GE channel is included. This indicates that allowing
1034 capital returns to adjust amplifies the impact of human capital accumulation on
1035 how household savings respond to AI.

1036 When the *GE channel* is active (Figure ??), AI reduces the wealth Gini, but
1037 the *redistribution channel* moderates this effect. However, when the *GE channel*
1038 is disabled (Figure ??), AI increases wealth inequality in the long run without the
1039 *redistribution channel* from human capital adjustment. In contrast, with the *redis-*
1040 *tribution channel* active, AI reduces wealth inequality.

1041 These observations lead to two key conclusions:

1042 First, the *redistribution channel* alone introduces a qualitative shift in AI's long-
1043 run impact on the wealth Gini (as shown in Figure ??).

1044 Second, the *GE channel*, when combined with human capital adjustment, qual-
1045 itatively alters the effect of anticipating AI on the wealth Gini (as shown by com-
1046 paring the blue lines in Figures ?? and ??).

1047 **Policy implications:** The impact of human capital adjustments on AI's distribu-
1048 tional outcomes, along with the roles of the *redistribution channel* and *GE channel*,
1049 provides valuable insights for policy discussions on how to address the challenges
1050 posed by AI shocks.

1051 In particular, government interventions aimed at stabilizing wages in response
1052 to AI-induced economic shocks may unintentionally worsen wealth inequality. Our
1053 analysis indicates that if wages are prevented from adjusting to reflect productiv-
1054 ity differences, this distorts households' incentives to adjust their human capital
1055 and precautionary savings—both of which play a critical role in mitigating wealth
1056 inequality.