

AI and Human Capital Accumulation: Aggregate and Distributional Implications*

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Abstract

This paper develops a model to analyze the effects of AI advancements on human capital investment and their impact on aggregate and distributional outcomes in the economy. We construct an incomplete markets economy with endogenous asset accumulation and general equilibrium, where households decide on human capital investment and labor supply. Anticipating near-term AI advancements that will alter skill premiums, we analyze the transition dynamics toward a new steady state. Our findings reveal that human capital responses to AI amplify its positive effects on aggregate output and consumption, mitigate the AI-induced rise in precautionary savings, and stabilize the adjustments in wages and asset returns. Furthermore, while AI-driven human capital adjustments increase inequalities in income, earnings, and consumption, they unexpectedly reduce wealth inequality.

Keywords: AI, Job Polarization, Human Capital, Inequality

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¹ **1 Introduction**

² The distinctive nature of AI advancements lies in their ability to perform cognitive,
³ non-routine tasks that previously required significant education and expertise, fun-
⁴ damentally differentiating its impact on the labor market and economy from that
⁵ of general automation. For example, AI tools in medical diagnostics now assist ra-
⁶ diologists in analyzing medical images, potentially reducing demand for entry-level
⁷ radiologists while simultaneously increasing the productivity of senior professionals.
⁸ More generally, AI could shift the premium associated with various skills levels, de-
⁹ valuing middle-level skills while increasing the demand for high-level expertise. In
¹⁰ anticipation of these changes, households are likely to adjust their human capital
¹¹ investments.

¹² According to the National Center for Education Statistic,¹ college enrollment in
¹³ the U.S. has been declining since 2010. The National Student Clearinghouse Re-
¹⁴ search Center reports that the undergraduate college enrollment decline has acceler-
¹⁵ ated since the pandemic began, resulting in a loss of almost 6% of total enrollment
¹⁶ between fall 2019 to fall 2023, while graduate enrollment has risen by about 5%.²
¹⁷ These shifts, regardless of their causes, highlight evolving patterns in human capital
¹⁸ investment.

¹⁹ This paper develops a model to study the effects of AI advancements on human
²⁰ capital investment and their subsequent impact on aggregate and distributional
²¹ outcomes of the economy. We posit an economy consisting of three sectors, requiring
²² low, middle and high levels of skill (human capital) with increasing sectoral labor
²³ productivity. Households can invest in their human capital to move up to more
²⁴ productive sectors. But if they do not invest, their human capital depreciates and,
²⁵ over time, they will move down to less productive sectors. We model human capital
²⁶ investment at two levels, a low level attainable on the job and a high level requiring
²⁷ full-time commitment, such as pursuing higher education. Households are subject
²⁸ to uninsurable idiosyncratic risk in terms of productivity shocks that affect both
²⁹ labor productivity and effectiveness in human capital investment.

³⁰ The interaction between human capital investment and labor supply presents a
³¹ tradeoff at the household level between current wage earning and future wage gains.
³² At aggregate level, the interaction implies that when individuals transition from
³³ the middle to the high sector, they may temporarily exit the workforce to upskill,
³⁴ reducing immediate labor supply but improving future labor productivity.

³⁵ We model AI advancements as increasing the productivity for the low and high
³⁶ sectors but not for the middle sector so that the skill premium of the middle sector
³⁷ decreases and the skill premium of the high sector increases. Allowing for human

¹https://nces.ed.gov/programs/digest/d22/tables/dt22_303.70.asp

²<https://public.tableau.com/app/profile/researchcenter/viz/CTEEFall2023dashboard/CTEEFall2023>

38 capital adjustments not only alters AI's economic implications quantitatively, it also
39 makes a qualitative difference.

40 If the skill distribution is fixed, AI will unambiguously improve the labor pro-
41 ductivity of the whole economy. However, allowing human capital to adjust enables
42 workers to upskill or downskill. The response of overall labor productivity could be
43 enhanced, or dampened, or even reverted depending on whether workers move to
44 more or less productive sectors.

45 Using a two-period model, we show how households' labor supply and human
46 capital investment are affected by their productivity shocks, asset holdings and
47 stocks of human capital. The effects of AI, in this partial equilibrium analysis, are
48 shown to discourage human capital investment for households in the low sector and
49 encourage human capital investment for households in the middle sector, thereby
50 increasing human capital inequality. In addition, AI worsens consumption inequality
51 for households with low levels of human capital and reduces consumption inequality
52 for those with high levels of human capital.

53 At the economy level, the effects of AI advancements depend on the sectoral
54 distribution of households and the general equilibrium effects via wage and capital
55 return responses. We quantify these effects using a fully-fledged dynamic quanti-
56 tative model that incorporates an infinite horizon, endogenous asset accumulation,
57 and general equilibrium. The model is calibrated to reflect key features of the U.S.
58 economy, capturing realistic household heterogeneity. The steady state distribution
59 of human capital without AI advancements pins down the sectoral distribution of
60 households. We then introduce fully anticipated AI advancements happening in the
61 near future and study the transition dynamics from the current state of the economy
62 to the eventual new steady state.

63 We find that aggregate human capital rises sharply even before AI introduction,
64 indicating that a substantial portion of workers, anticipating changes in skill pre-
65 mium, leave the labor force early to accumulate human capital. The economy also
66 experiences AI-induced job polarization, with a notable reallocation of workers from
67 the middle sector to either low or high sectors.

68 Building on these labor dynamics, our model examines how AI influences both
69 the aggregate and distributional outcomes of the economy, including output, con-
70 sumption, investment, employment, income inequality, consumption inequality, and
71 wealth inequality. Our focus is on how human capital adjustments reshape AI's
72 effects on each of these outcomes. Specifically, we examine two primary chan-
73 nels through which human capital adjustments operate: the redistribution channel,
74 which reallocates workers across skill sectors, and the general equilibrium channel,
75 which operates through wages and capital return changes.

76 Our findings reveal that human capital responses to AI amplify its positive effects
77 on aggregate output and consumption, mitigate the AI-induced rise in precautionary

78 savings, and stabilize the adjustments in wages and asset returns. Furthermore,
79 while AI-driven human capital adjustments increase inequalities in income, earnings,
80 and consumption, they unexpectedly reduce wealth inequality. We also show that
81 the redistribution channel is the dominant factor in the effects of human capital
82 adjustments, whereas the general equilibrium channel, via wage and capital return
83 changes, plays a comparatively minor role.

84 INTRODUCING PRECAUTIONARY SAVING MOTIVE IN THE WAGE PO-
85 LARIZATION INVESTIGATION Autor *et al.*, (2006)

86 This paper relates to the literature examining how technological advancements,
87 including AI, have significantly contributed to job polarization. Goos and Manning
88 (2007) show that since 1975, the United Kingdom has experienced job polarization,
89 with increasing employment shares in both high- and low-wage occupations. Autor
90 and Dorn (2013) expanded on this by providing a unified analysis of the growth of
91 low-skill service occupations, highlighting key factors that amplify polarization in
92 the U.S. labor market. Empirical evidence from Goos *et al.*, (2014) further confirms
93 pervasive job polarization across 16 advanced Western European economies. In the
94 U.S., Acemoglu and Restrepo (2020) show that robots can reduce employment and
95 wages, finding robust negative effects of automation on both in various commuting
96 zones.

97 The introduction of AI and robotics has had adverse effects on labor markets,
98 with significant implications for employment and labor force participation. Lerch
99 (2021) highlights that the increasing use of robots not only displaces workers but
100 also negatively impacts overall labor force participation rates. Similarly, Faber *et al.*,
101 (2022) demonstrate that the detrimental effects of robots on the labor market have
102 resulted in a decline in job opportunities, particularly in sectors where automation
103 is prevalent. These findings suggest that while technological advancements bring
104 productivity gains, they simultaneously reduce employment prospects and partici-
105 pation in the labor market, exacerbating economic challenges for certain groups of
106 workers.

107 The introduction of AI and robotics also influences human capital accumulation
108 as workers respond to technological disruption. Faced with the employment risks
109 brought about by automation, many exposed workers may invest in additional ed-
110 ucation as a form of self-insurance, rather than relying on increases in the college
111 wage premium (Atkin, 2016; Beaudry *et al.*, 2016). Empirical evidence supports this
112 response. Di Giacomo and Lerch (2023) find that for every additional robot adopted
113 in U.S. local labor markets between 1993 and 2007, four individuals enrolled in col-
114 lege, particularly in community colleges, indicating a rise in educational investments
115 triggered by automation. Similarly, Dauth *et al.*, (2021) show that within German
116 firms, robot adoption has led to an increase in the share of college-educated workers,
117 as firms prioritize higher-skilled employees over those with apprenticeships.

118 The response of human capital accumulation to technological disruption could
119 also go to the other extreme. A 2022 report by Higher Education Strategy Associates
120 finds that following decades of growth, dropping student enrollment has become a
121 major trend in higher education in the Global North.³ In the U.S., the public across
122 the political spectrum has increasingly lost confidence in the economic benefits of
123 a college degree. Pew Research Center reports that about half of Americans say
124 having a college degree is less important today than it was 20 years ago in a survey
125 conducted in 2023.⁴ A 2022 study from Public Agenda, a nonpartisan research
126 organization, shows that young Americans without college degrees are most skeptical
127 about the value of higher education.

128 The rise of AI and automation also plays a significant role in exacerbating gen-
129 eral inequality, particularly through its impact on education and wealth distribution.
130 Prettner and Strulik (2020) present a model showing that innovation-driven growth
131 leads to an increasing proportion of college graduates, which in turn drives higher
132 income and wealth inequality. As technology advances, workers with higher educa-
133 tional attainment benefit disproportionately, widening the gap between those with
134 and without advanced skills. Sachs and Kotlikoff (2012) also explore this dynamic,
135 providing a model within an overlapping generations framework that examines the
136 interaction between automation and education. They demonstrate how automation
137 can further entrench inequality by favoring workers with higher levels of educa-
138 tion, as those without adequate skills are more likely to be displaced or see their
139 wages stagnate. This interaction between technological change and educational at-
140 tainment not only amplifies economic inequality but also perpetuates disparities in
141 wealth across generations.

142 The rest of the paper is organized as follows. Section 2 describes the model
143 environment. Section 3 solves the household’s problem using a two-period version
144 of the model. Section 4 solves the fully-fledged quantitative model and calibrates it
145 to fit key features of the U.S. economy, including employment rate, human capital
146 investment, and household heterogeneity. Section 5 incorporates AI into the quanti-
147 tative model and examines its economic impact on both aggregate and distributional
148 outcomes. Section 6 analyzes how human capital adjustments change the economic
149 impact of AI advancements. Section 7 concludes.

150 2 Model Environment

151 Time is discrete and infinite. There is a continuum of households. Each household
152 is endowed with one unit of indivisible labor and faces idiosyncratic productivity

³<https://higheredstrategy.com/world-higher-education-institutions-students-and-funding/>

⁴<https://www.pewresearch.org/social-trends/2024/05/23/public-views-on-the-value-of-a-college-degree/>

¹⁵³ shock, z , that follows an AR(1) process in logs:

$$\ln z' = \rho_z \ln z + \varepsilon_z, \varepsilon_z \stackrel{\text{iid}}{\sim} N(0, \sigma_z^2) \quad (1)$$

¹⁵⁴ The asset market is incomplete following Aiyagari (1994), and the physical capital,
¹⁵⁵ a , is the only asset available to households to insure against this idiosyncratic risk.
¹⁵⁶ Households can also invest in human capital, h , which allows them to work in sectors
¹⁵⁷ with different human capital requirement.

¹⁵⁸ 2.1 Production Technology

¹⁵⁹ The production technology in the economy is a constant-returns-to-scale Cobb-
¹⁶⁰ Douglas production function:

$$F(K, L) = K^{1-\alpha} L^\alpha \quad (2)$$

¹⁶¹ K represents the total physical capital accumulated by households, while L denotes
¹⁶² the total effective labor supplied by households, aggregated across three sectors: low,
¹⁶³ middle, and high. The marginal products of capital and effective labor determine
¹⁶⁴ the economy-wide wage rate, w , and interest rate, r .

¹⁶⁵ These sectors differ in their technologies for converting labor into effective labor
¹⁶⁶ units and in the levels of human capital required for employment. The middle sector
¹⁶⁷ employs households with human capital above h_M and converts one unit of labor
¹⁶⁸ to one effective labor unit. The high sector, requiring human capital above h_H ,
¹⁶⁹ converts one unit of labor to $1 + \lambda$ effective units, while the low sector, with no
¹⁷⁰ human capital requirement, converts one unit into $1 - \lambda$ effective units. This implies
¹⁷¹ a sectoral labor productivity $x(h)$ that is a step function in human capital:

$$x(h) = \begin{cases} 1 - \lambda & \text{low sector if } h < h_M \\ 1 & \text{middle sector if } h_M < h < h_H \\ 1 + \lambda & \text{high sector if } h > h_H \end{cases} \quad (3)$$

¹⁷² A household i who decides to work thus contributes $z_i x(h_i)$ units of effective labor,
¹⁷³ where z_i is his idiosyncratic productivity. Denote $n_i \in \{0, 1\}$ as the indicator that
¹⁷⁴ takes one if the household works and zero if the household does not. The aggregate
¹⁷⁵ labor is

$$L = \int n_i z_i x(h_i) di, \quad (4)$$

¹⁷⁶ assuming perfect substitutability of effective labor across the three sectors.

¹⁷⁷ 2.2 Household's Problem

¹⁷⁸ Households derive utility from consumption, incur disutility from labor and effort of
¹⁷⁹ human capital investment. A household maximizes the expected lifetime utility by
¹⁸⁰ optimally choosing consumption, saving, labor supply and human capital investment
¹⁸¹ each period, based on his idiosyncratic productivity shock z_t :

$$\max_{\{c_t, a_{t+1}, n_t, e_t\}_{t=0}^{\infty}} E_0 \left[\sum_{t=0}^{\infty} \beta^t (\ln c_t - \chi_n n_t - \chi_e e_t) \right] \quad (5)$$

¹⁸² where c_t represents consumption, a_{t+1} represents saving, $n_t \in \{0, 1\}$ is labor supply,
¹⁸³ and e_t is the effort of human capital investment.

¹⁸⁴ If a household decides to work in period t , he will be employed into the appropriate
¹⁸⁵ sector according to his human capital h_t and receive labor income $w_t z_t x(h_t)$.
¹⁸⁶ The household's budget constraint is

$$c_t + a_{t+1} = n_t(w_t z_t x(h_t)) + (1 + r_t)a_t \quad (6)$$

$$c_t \geq 0 \text{ and } a_{t+1} \geq 0 \quad (7)$$

¹⁸⁷ We prohibit households from borrowing $a_{t+1} \geq 0$ to simplify analysis.⁵

¹⁸⁸ Human capital investment can take three levels of effort: $\{0, e_L, e_H\}$. A non-
¹⁸⁹ working household is free to choose any of the three effort levels but a working
¹⁹⁰ household cannot devote the highest level of effort e_H , reflecting a trade-off between
¹⁹¹ working and human capital investment. Hence:

$$e_t \in \{0, e_L, (1 - n_t)e_H\}. \quad (8)$$

¹⁹² Its contribution to next-period human capital is subject to the productivity shock:

$$h_{t+1} = z_t e_t + (1 - \delta)h_t \quad (9)$$

¹⁹³ where δ is human capital's depreciation rate.

¹⁹⁴ **3 Household Decisions in a Two-Period Model**

¹⁹⁵ In this section, we solve the household's problem with two periods to gain intuition.

¹⁹⁶ **Period-2 decisions** Households do not invest in human capital or physical capital
¹⁹⁷ in the last period. The only relevant decision is whether to work.

⁵According to Aiyagari (1994), a borrowing constraint is necessarily implied by present value budget balance and nonnegativity of consumption. Since the borrowing limit is not essential to our analysis, we set it to zero for simplicity.

198 The household works $n = 1$ if and only if $z \geq \bar{z}(h, a)$, with $\bar{z}(h, a)$ defined as

$$\ln(w\bar{z}(h, a)x(h) + (1 + r)a) - \chi_n = \ln((1 + r)a) \quad (10)$$

199 The household faces a trade-off between earning labor income and incurring the
200 disutility of working. Given the sector-specific productivity $x(h)$ specified in (3),
201 the threshold for idiosyncratic productivity, $\bar{z}(h, a)$, takes on three possible values:

$$\bar{z}(h, a) = \begin{cases} \bar{z}(a)\frac{1}{1-\lambda} & \text{if } h < h_M \\ \bar{z}(a) & \text{if } h_M \leq h < h_H \\ \bar{z}(a)\frac{1}{1+\lambda} & \text{if } h > h_H \end{cases} \quad (11)$$

$$\text{where } \bar{z}(a) := \frac{(\exp(\chi_n) - 1)(1 + r)a}{w} \quad (12)$$

202 Households with higher human capital is more likely to work, whereas households
203 with higher physical capital is less likely to work.

204 **Period-1 decisions** In addition to labor supply, period-1 decisions include saving
205 and human capital investment, both of which are forward-looking and affected by
206 the idiosyncratic risk associated with the productivity shock z' . Our model also
207 features a trade-off between human capital investment and labor supply as a working
208 household cannot devote the highest level of effort e_H in human capital investment.
209 Therefore, human capital investment grants households the possibility of a discrete
210 wage hike in the future but may entail a wage loss in the current period.

211 To see the implication of this trade-off and how it interacts with uninsured
212 idiosyncratic risk, we proceed in two steps. We first derive the period-1 decisions
213 without uncertainty by assuming that z' is known to the household at period 1 and
214 z' is such that the household will work in period 2. We then reintroduce uncertainty
215 in z' and compare the decision rules with the case without uncertainty.

216 3.1 Period-1 Labor Supply and Human Capital Investment

217 3.1.1 Consumption and saving without uncertainty

218 The additive separability of household's utility implies that labor supply n and
219 human capital investment e enters in consumption and saving choices only via the
220 intertemporal budget constraint:

$$c + \frac{c'}{1 + r'} = (1 + r)a + n(wzx(h)) + \frac{w'z'x(h')}{1 + r'} \\ \text{with } h' = ze + (1 - \delta)h.$$

²²¹ The log utility in consumption implies the optimality condition:

$$c' = \beta(1 + r')c. \quad (13)$$

²²² Combining it with the budget constraint, we obtain the optimal consumption as a
²²³ function of labor supply n and human capital investment e :

$$c(n, e) = \frac{1}{1 + \beta} \left[(1 + r)a + n(wzx(h)) + \frac{w'z'x(h' = ze + (1 - \delta)h)}{1 + r'} \right]. \quad (14)$$

²²⁴ 3.1.2 Labor supply and human capital investment

²²⁵ The optimal consumption rules in (14) and (13) allow us to express the household's
²²⁶ problem as the maximization of an objective function in labor supply n and human
²²⁷ capital investment e :⁶

$$\max_{n, e} (1 + \beta) \ln c(n, e) - \chi_n n - \chi_e e \quad (15)$$

²²⁸ This maximization depends critically on the household's current human capital and
²²⁹ achievable next-period human capital. Accordingly, we partition households into
²³⁰ five ranges of h : $[0, h_M]$, $[h_M, h_M(1 - \delta)^{-1}]$, $[h_M(1 - \delta)^{-1}, h_H]$, $[h_H, h_H(1 - \delta)^{-1}]$,
²³¹ and $[h_H(1 - \delta)^{-1}, h_{\max}]$.

²³² We now derive the decision rules for households $h \in [h_M, h_M(1 - \delta)^{-1}]$ in detail,
²³³ as the decision rules for the other four ranges are similar. For households with
²³⁴ $h < h_M(1 - \delta)^{-1}$, we define two cutoffs in z :

$$\underline{z}_M(h) := \frac{h_M - (1 - \delta)h}{e_H}; \bar{z}_M(h) := \frac{h_M - (1 - \delta)h}{e_L} \quad (16)$$

²³⁵ These cutoffs divide households into three groups based on their ability to be em-
²³⁶ ployed in the middle sector in the next period.

²³⁷ **Non-learners** are households with $z < \underline{z}_M(h)$. They cannot achieve $h' > h_M$
²³⁸ with either e_L or e_H level of human capital investment today. As a result, they will
²³⁹ choose not to invest in human capital, $e = 0$, and their future sectoral productivity
²⁴⁰ will be $x(h') = 1 - \lambda$. These non-learners work $n = 1$ if and only if $z \geq \bar{z}_{non}^L(a)$:

$$\bar{z}_{non}^L(a) = \frac{(\exp(\frac{\chi_n}{1+\beta}) - 1)[(1 + r)a + \frac{w'z'(1-\lambda)}{1+r'}]}{w} \quad (17)$$

²⁴¹ **Slow learners** are households with $z \in (\underline{z}_M(h), \bar{z}_M(h))$. These households can
²⁴² reach $h' > h_M$ in the next period only by investing $e = e_H$ today. Their choice
²⁴³ is restricted to $e = 0$ or $e = e_H$, since selecting $e = e_L$ incurs a cost without any

⁶This follows since $c' = \beta(1 + r')c$, so $\ln c' = \ln \beta + \ln(1 + r') + \ln c$.

244 future benefit. Slow learners must trade off between working and human capital
 245 investment: choosing $e = e_H$ requires not working today ($n = 0$), while opting to
 246 work means forgoing investment in human capital ($n = 1, e = 0$).⁷

247 Slow learners prefer $(n = 1, e = 0)$ to $(n = 0, e = e_H)$ if and only if $z \geq \bar{z}_{slow}^L(a)$:

$$\bar{z}_{slow}^L(a) = \frac{(\exp(\frac{\chi_n - \chi_e e_H}{1+\beta}) - 1)[(1+r)a + \frac{w' z'}{1+r'}] + \lambda \frac{w' z'}{1+r'}}{w} \quad (18)$$

248 **Fast learners** are households with $z > \bar{z}_M(h)$. They can achieve $h' > h_M$ in
 249 the next period if they invest $e = e_L$ today. In this case, there is no need to exert
 250 high effort e_H in human capital investment. The fast learners choose among three
 251 options: $(n = 1, e = 0)$, $(n = 1, e = e_L)$, and $(n = 0, e = e_L)$.⁸

252 The decision rule for fast learners are as follows:

$$n(z, h, a), e(z, h, a) = \begin{cases} n = 1, e = 0 & \text{if } z \geq \bar{z}_{fast}^L(a) \\ n = 1, e = e_L & \text{if } \underline{z}_{fast}^L(a) \leq z < \bar{z}_{fast}^L(a) \\ n = 0, e = e_L & \text{if } z < \underline{z}_{fast}^L(a) \end{cases} \quad (19)$$

253 where

$$\bar{z}_{fast}^L(a) = \frac{\left\{ \exp(\frac{\chi_e e_L}{1+\beta}) \lambda \left[\exp(\frac{\chi_e e_L}{1+\beta}) - 1 \right]^{-1} - 1 \right\} \frac{w' z'}{1+r'} - (1+r)a}{w} \quad (20)$$

254

$$\underline{z}_{fast}^L(a) = \frac{(\exp(\frac{\chi_n}{1+\beta}) - 1)[(1+r)a + \frac{w' z'}{1+r'}]}{w} \quad (21)$$

255 We set up our model so that $\bar{z}_{fast}^L(a) > \underline{z}_{fast}^L(a)$.⁹

256 **Decision rule diagram:** Figure 1 illustrates the decision rule (n, e) as a function
 257 of states (z, h, a) for households with $h_M \leq h < h_M \frac{1}{1-\delta}$. The human capital h
 258 changes along the horizontal line and the idiosyncratic productivity z changes along
 259 the vertical line. The two diagonal lines, $\bar{z}_M(h)$ and $\underline{z}_M(h)$ defined in (16), separate
 260 the state space into three areas: the unshaded area represents the non-learners,
 261 the lightly-shaded area represents the slow learners, and the darkly-shaded area
 262 represents the fast learners. The areas are divided by four dashed horizontal lines
 263 associated with cutoffs $\bar{z}_{non}^L(a)$, $\bar{z}_{slow}^L(a)$, $\underline{z}_{fast}^L(a)$, and $\bar{z}_{fast}^L(a)$ that are functions of

⁷The choice between $(n = 0, e = e_H)$ and $(n = 0, e = 0)$ does not depend on z . For e_H to be relevant, λ must be large enough so that $(n = 0, e = e_H)$ is preferred to $(n = 0, e = 0)$. See the Appendix for details on the lower bound for λ .

⁸Similar to the case of slow learners, the choice between $(n = 0, e = e_L)$ and $(n = 0, e = 0)$ does not depend on z . Moreover, since our model is set up so that $(n = 0, e = e_H)$ dominates $(n = 0, e = 0)$, it implies that $(n = 0, e = e_L)$ dominates $(n = 0, e = 0)$.

⁹Appendix A.2 provides the parameter restrictions such that the condition for $(n = 0, e = e_H)$ to dominate $(n = 0, e = 0)$ is sufficient for $\bar{z}_{fast}^L(a) > \underline{z}_{fast}^L(a)$.

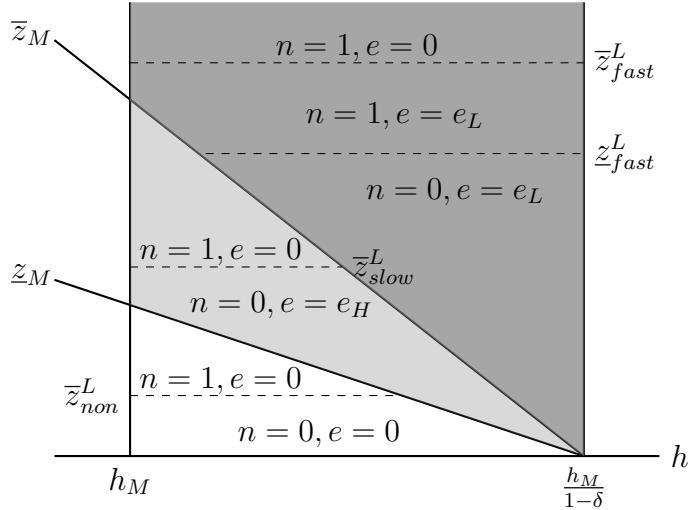


Figure 1: Decision Rule Diagram for $h_M \leq h < h_M(1 - \delta)^{-1}$

The human capital h changes along the horizontal line and the idiosyncratic productivity z changes along the vertical line. The two diagonal lines, $\bar{z}_M(h)$ and $\underline{z}_M(h)$, separate the state space into three areas: the unshaded area represents the non-learners, the lightly-shaded area represents the slow learners, and the darkly-shaded area represents the fast learners. The areas are divided by four dashed horizontal lines associated with cutoffs \bar{z}_{non}^L , \bar{z}_{slow}^L , \underline{z}_{fast}^L , and \bar{z}_{fast}^L that are functions of capital holding a .

²⁶⁴ capital holding a and defined in (17), (18), (21), and (20).

²⁶⁵ This decision rule diagram is representative for households in other four ranges
²⁶⁶ of human capital. Figure 2 illustrates the regions in which households make positive
²⁶⁷ human capital investments. Striped shading highlights where investment occurs,
²⁶⁸ with dark areas denoting fast learners and light areas representing slow learners.

²⁶⁹ For households with $h < h_M$, $\bar{z}_M(h)$ and $\underline{z}_M(h)$ continue to be the boundaries
²⁷⁰ that separate non-learners, slow learners and fast learners, but the four cutoffs are
²⁷¹ $\bar{z}_{non}^L \frac{1}{1-\lambda}$, $\bar{z}_{slow}^L \frac{1}{1-\lambda}$, $\underline{z}_{fast}^L \frac{1}{1-\lambda}$, and $\bar{z}_{fast}^L \frac{1}{1-\lambda}$.

²⁷² For households with $h_M \frac{1}{1-\delta} \leq h < h_H \frac{1}{1-\delta}$, the boundaries for state space division
²⁷³ change to $\bar{z}_H(h)$ and $\underline{z}_H(h)$:

$$\underline{z}_H(h) := \frac{h_H - (1 - \delta)h}{e_H}; \quad \bar{z}_H(h) := \frac{h_H - (1 - \delta)h}{e_L} \quad (22)$$

²⁷⁴ If $h_M \frac{1}{1-\delta} \leq h < h_H$, the four cutoffs that partition the decision regions for households
²⁷⁵ are denoted as $\bar{z}_{non}^M(a)$, $\bar{z}_{slow}^M(a)$, $\underline{z}_{fast}^M(a)$, and $\bar{z}_{fast}^M(a)$ (see Appendix A.1 for the
²⁷⁶ explicit formulae).¹⁰ If $h_H \leq h < h_H \frac{1}{1-\delta}$, the analogous cutoffs are given by $\bar{z}_{non}^M \frac{1}{1+\lambda}$,
²⁷⁷ $\bar{z}_{slow}^M \frac{1}{1+\lambda}$, $\underline{z}_{fast}^M \frac{1}{1+\lambda}$, and $\bar{z}_{fast}^M \frac{1}{1+\lambda}$.

²⁷⁸ Households with $h \geq h_H \frac{1}{1-\delta}$ are always non-learners, since their human capital
²⁷⁹ guarantees high-sector employment next period without further investment. For
²⁸⁰ them, only the cutoff $\bar{z}_{non}^H(a) \frac{1}{1+\lambda}$ matters.

¹⁰ Appendix A.2 provides parameter restrictions for $\bar{z}_{fast}^M(a) > \underline{z}_{fast}^M(a)$.

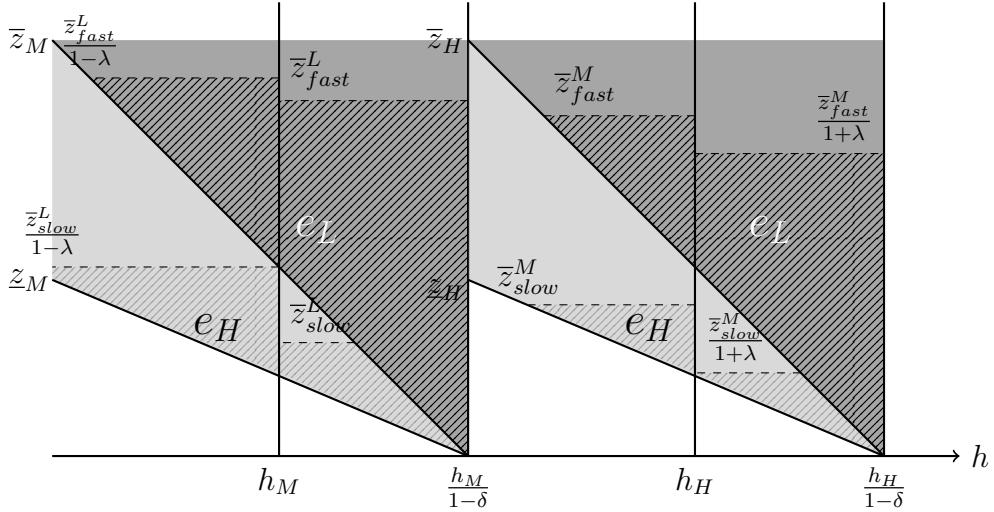


Figure 2: State Space for Human Capital Investment

The darkly-shaded striped areas indicate the state space for human capital investment equal to e_L by the fast learners. The lightly-shaded striped areas indicate the state space for human capital investment equal to e_H by the slow learners.

281 3.2 The Effects of Uninsured Idiosyncratic Risk

282 We now reintroduce the idiosyncratic risk to households in period 1 by assuming
 283 that z' follows a log-normal distribution with mean \bar{z}' and variance σ_z^2 .

284 Our previous analysis without uncertainty is a special case with $\sigma_z^2 = 0$. The
 285 effects of uninsured idiosyncratic risk can be thought as how households' decisions
 286 change when the distribution of z' undergoes a mean-preserving spread in the sense
 287 of second-order stochastic dominance.

288 From a consumption-saving perspective, the uncertain z' is associated with future
 289 labor income risk. It is well understood in the literature that idiosyncratic future
 290 income risk raises the expected marginal utility of future consumption for households
 291 with log utility and makes them save more. In our model, households can also supply
 292 more labor to mitigate the effect of idiosyncratic income risk on the marginal utility
 293 of consumption.

294 From the perspective of human capital investment, the uncertain z' is associated with risk in the return to human capital. Conditional on working, households'
 295 income increases with z' : $c' = (1 + r')a' + w'x(h')z'$. $\ln(c')$ is increasing and concave
 296 in z' , and a higher $x(h')$ increases the concavity.¹¹ Consider two levels of h' , $\bar{h}' > \underline{h}'$,

¹¹The marginal effect of z' on $\ln(c')$ is

$$\frac{\partial \ln(c')}{\partial z'} = \frac{w'x(h')}{(1 + r')a' + w'x(h')z'} > 0$$

The second derivative is

$$\frac{\partial^2 \ln(c')}{(\partial z')^2} = - \left[\frac{w'x(h')}{(1 + r')a' + w'x(h')z'} \right]^2 < 0$$

298 a mean-preserving spread of z' distribution reduces the expected utility at both
 299 levels of h' but the reduction is larger for the higher level \bar{h}' . Hence, the expected
 300 utility gain of moving from h' to \bar{h}' is smaller due to the idiosyncratic risk. Human
 301 capital investment is discouraged.

302 Taking into account endogenous labor supply reinforces the discouragement of
 303 human capital investment by the idiosyncratic risk. Recall from Section 3 that
 304 households with z' lower than a cutoff do not work. The endogenous labor supply
 305 therefore provides insurance against the lower tail risk of the idiosyncratic z' . More-
 306 over, the cutoff in z' is lower for those with higher human capital h' . This makes
 307 households with higher h' more exposed to the lower tail risk than those with lower
 308 h' , further reducing the gain of human capital investment.

309 **Proposition 1.** *The uninsured idiosyncratic risk in z' makes households in period
 310 1 save more, work more and invest less in human capital.*

311 3.3 Period-1 Saving and Human Capital Investment

312 In this section, we study the impact of endogenous human capital investment on
 313 households' saving decisions. Specifically, we compare optimal saving behavior in
 314 two scenarios: one in which households can choose to invest in human capital, and
 315 an alternative scenario in which human capital is exogenously fixed. To facilitate the
 316 comparison, we assume in this section that there is no human capital depreciation.¹²

317 When the optimal choice of human capital investment is zero, optimal saving is
 318 identical in both scenarios. When the optimal human capital investment is either e_L
 319 or e_H , we compare the household's optimal saving to the case where human capital
 320 investment is exogenously fixed at zero, i.e., $(n = 1, e = 0)$.¹³

321 To make the human capital relevant, we assume that $n' = 1$ in period 2. The
 322 additive separability of work and human capital investment effort from consumption
 323 allows us to consider the optimal saving conditional on a given choice of labor supply
 324 and human capital investment.

325 In particular, the household maximizes expected lifetime utility:

$$\max_{a'} : \ln(c) + \beta \mathbb{E}_{z'} [\ln(c')], \quad (23)$$

and is more negative if $x(h')$ is higher.

¹²If depreciation is allowed, the analysis proceeds similarly but involves more comparison pairs.

¹³Why not compare to $(n = 0, e = 0)$? Such a comparison is not meaningful when considering $(n = 1, e = e_L)$ because the two scenarios involve different state spaces. To see it, suppose conditions are such that $(n = 1, e = e_L)$ is optimal. If we were to fix $e = 0$ exogenously, the household's lifetime income would fall, and as a result the household would have a greater incentive to work. Thus, it is not possible for the household to deviate from choosing $n = 1$ when human capital is held fixed at $e = 0$. The comparison between $(n = 0, e = 0)$ and $(n = 0, e = e_L \text{ or } e_H)$ is similar to the comparison between $(n = 1, e = 0)$ to $(n = 1, e = e_L)$, since human capital investment does not affect period-1 labor income in either case.

³²⁶ subject to the budget constraints

$$c + a' = (1 + r)a + n(wzx(h)), \quad (24)$$

$$c' = (1 + r')a' + w'z'x(h'), \quad (25)$$

$$\text{with } h' = ze + (1 - \delta)h, e \in \{0, e_L, (1 - n)e_H\} \quad (26)$$

³²⁷ 3.3.1 Effect of on-job-training on saving

³²⁸ We now compare the optimal saving between $(n = 1, e = e_L)$ and $(n = 1, e = 0)$,
³²⁹ where e_L allows households to move to a higher sector in period 2 with higher
³³⁰ sectoral productivity $x(h')$.

³³¹ To simplify the notation while maintaining the key economic forces, we normalize
³³² $(1 + r) = (1 + r') = 1$, $w = w' = 1$, the period-1 productivity shock $z = 1$ and the
³³³ period-2 productivity shock z' to $\ln z' \sim \mathcal{N}(0, \sigma_z^2)$. The budget constraints become:

$$c + a' = a + x, \quad c' = a' + txz' \quad (27)$$

³³⁴ where $t \geq 1$ represents the effect of human capital investment on period-2 income:
³³⁵ $t > 1$ if $e = e_L$; $t = 1$ if $e = 0$.

³³⁶ The optimal saving is determined by the FOC:

$$\frac{1}{a + x - a'} = \beta \mathbb{E}_{z'} \left(\frac{1}{a' + txz'} \right) \quad (28)$$

³³⁷ Denoting the mean and variance of z' as μ and Σ , respectively:

$$\mu \equiv \mathbb{E}[z'] = e^{\sigma_z^2/2}, \quad \Sigma \equiv \text{Var}(z') = e^{\sigma_z^2}(e^{\sigma_z^2} - 1). \quad (29)$$

³³⁸ The second-order approximate solution to the FOC is:

$$a'^*(x, a; t) = \underbrace{\frac{\beta(a + x) - tx\mu}{1 + \beta}}_{\text{CE}} + \underbrace{\frac{t^2 x^2 \Sigma}{\beta(a + x + tx\mu)}}_{\text{Precautionary}} \quad (30)$$

³³⁹ The first term is the *certainty-equivalent* saving, which reflects the consumption
³⁴⁰ smoothing motive, increasing in the period-1 resources $a + x$ and decreasing in the
³⁴¹ period-2 expected labor income $tx\mu$. The second term is the *precautionary* saving,
³⁴² which is increasing in the variance of period-2 labor income $t^2 x^2 \Sigma$ and decreasing in
³⁴³ the expected total resources $a + x + tx\mu$.

³⁴⁴ The effect of on-job-training on saving can be decomposed into two components:

$$\frac{\partial a'^*}{\partial t}(x, a; t) = -\frac{x\mu}{1 + \beta} + \frac{x^2 \Sigma}{\beta} \frac{t[2(a + x) + tx\mu]}{(a + x + tx\mu)^2}. \quad (31)$$

³⁴⁵ The first term being negative captures the *crowd-out* effect on saving via consumption-

³⁴⁶ smoothing motive as on-job-training increases the expected period-2 labor income
³⁴⁷ $tx\mu$. The second positive term captures the *crowd-in* effect via precautionary saving
³⁴⁸ motive as on-job-training exposes households to larger future income risk.

³⁴⁹ To capture the overall impact of on-job-training on saving, we define:

$$\Delta_{\text{on-job}}(x, a; t) = a'^*(x, a; t) - a'^*(x, a; 1) = \int_1^t \frac{\partial a'^*}{\partial u}(x, a; u) du, \quad (32)$$

³⁵⁰ where $a'^*(x, a; t)$ is the optimal saving when households undertake on-job-training,
³⁵¹ and $a'^*(x, a; 1)$ is the optimal saving when human capital is kept exogenously fixed.

³⁵² Whether on-job-training increases or decreases saving ultimately depends on
³⁵³ the balance between the crowd-out effect (via higher expected future income) and
³⁵⁴ the precautionary crowd-in effect (via heightened future income risk). The next
³⁵⁵ proposition demonstrates that these effects can dominate differently depending on
³⁵⁶ skill, so that the overall impact of on-job-training on saving can differ between low-
³⁵⁷ and high-skilled households.

³⁵⁸ **Proposition 2.** *When the idiosyncratic shock is large enough, i.e., $\frac{\Sigma}{\mu} > \underline{\sigma}(t)$, on-
³⁵⁹ job-training crowds out saving for low-skilled households and crowds in saving for
³⁶⁰ high-skilled households: for $x < x^*(a, t)$, $e = e_L$ lowers saving $\Delta_{\text{on-job}}(x, a; t) < 0$;
³⁶¹ for $x > x^*(a, t)$, $e = e_L$ raises saving $\Delta_{\text{on-job}}(x, a; t) > 0$.*

³⁶² *Proof.* See Appendix B. □

³⁶³ 3.3.2 Effect of full-time training on saving

³⁶⁴ We next compare the optimal saving between $(n = 0, e = e_L \text{ or } e_H)$ and $(n =$
³⁶⁵ $1, e = 0)$. Note that full-time training requires the households to give up their labor
³⁶⁶ income in period 1, which is not the case for on-job-training. Following the same
³⁶⁷ normalization and notation as in the previous subsection, we can write the budget
³⁶⁸ constraints with full-time training and without training as:

$$e = e_H : c + a' = a, \quad c' = a' + txz' \quad (33)$$

$$e = 0 : c + a' = a + x, \quad c' = a' + xz' \quad (34)$$

³⁶⁹ where $t > 1$ captures the effect of full-time training on period-2 income.

³⁷⁰ The second-order approximate solution to the optimization problem is:

$$e = e_H : a'_{e_H}^*(x, a; t) = \underbrace{\frac{\beta a - tx\mu}{1 + \beta}}_{\text{CE}} + \underbrace{\frac{t^2 x^2 \Sigma}{\beta(a + tx\mu)}}_{\text{Precautionary}} \quad (35)$$

$$e = 0 : a'^*(x, a; 1) = \underbrace{\frac{\beta(a + x) - x\mu}{1 + \beta}}_{\text{CE}} + \underbrace{\frac{x^2 \Sigma}{\beta(a + x + x\mu)}}_{\text{Precautionary}} \quad (36)$$

³⁷¹ so that the total effect of full-time training on saving is:

$$\Delta_{\text{full-time}}(x, a; t) = a'_{e_H}^*(x, a; t) - a'^*(x, a; 1) \quad (37)$$

$$= \Delta_{\text{on-job}}(x, a; t) - x \frac{\beta}{1 + \beta} + \frac{t^2 x^2 \Sigma}{\beta} \frac{x}{(a + x + tx\mu)(a + tx\mu)} \quad (38)$$

³⁷² Compared to the effect of on-job-training, represented by $\Delta_{\text{on-job}}(x, a; t)$ defined in
³⁷³ (32), full-time training introduces two additional effects on saving. First, it further
³⁷⁴ reduces saving because households forgo their period-1 labor income, as reflected
³⁷⁵ in the second term. Second, it increases precautionary saving, since having lower
³⁷⁶ current resources leaves households less able to self-insure against idiosyncratic risk
³⁷⁷ in period 2, which is captured by the third term. Denote the net additional effect
³⁷⁸ of full-time training on saving as:

$$\Delta_H(x, a; t) \equiv x \left[-\frac{\beta}{1 + \beta} + \frac{\Sigma}{\beta} \frac{t^2 x^2}{(a + x + tx\mu)(a + tx\mu)} \right] \quad (39)$$

³⁷⁹ so that $\Delta_{\text{full-time}}(x, a; t) = \Delta_{\text{on-job}}(x, a; t) + \Delta_H(x, a; t)$. The next proposition shows
³⁸⁰ that the net additional effect is negative and stronger for higher skilled households.

³⁸¹ **Proposition 3.** *When the idiosyncratic shock is not too large, i.e., $\frac{\Sigma}{\mu} < \bar{\sigma}(t)$, full-
³⁸² time training crowds out more saving than on-job-training, $\Delta_H(x, a; t) < 0$. More-
³⁸³ over, the crowding-out effect is stronger for higher skilled households: $\Delta_H(x, a; t)$ is
³⁸⁴ decreasing in x .*

³⁸⁵ *Proof.* See Appendix B. □

³⁸⁶ 3.4 The Effects of an Anticipated Period-2 AI Shock

³⁸⁷ Suppose that an AI shock is anticipated to occur in period 2 and to increase the
³⁸⁸ labor productivity for the low sector and the high sector but not the middle sector.
³⁸⁹ The effect of AI shock on the sectoral productivity is captured by γ with $0 < \gamma < 1$:

$$x(h') = \begin{cases} 1 - \lambda + \gamma\lambda & \text{low sector if } h' < h_M \\ 1 & \text{middle sector if } h_M < h' < h_H \\ 1 + \lambda + \gamma\lambda & \text{high sector if } h' > h_H \end{cases} \quad (40)$$

³⁹⁰ In other words, the AI shock increases average labor productivity, reduces the earn-
³⁹¹ ings premium for the middle sector, and enlarges the earnings premium for the high
³⁹² sector relative to the middle sector.

³⁹³ 3.4.1 Effects on human capital investment

³⁹⁴ The AI shock lowers the incentive to work in the middle sector in period 2. Con-
³⁹⁵ sequently, households with $h < h_M/(1 - \delta)$ reduce their human capital investment,

396 while those with $h > h_M/(1 - \delta)$ increase it. More specifically, the upper bounds
 397 that determine whether households undertake positive human capital investment –
 398 denoted by \bar{z}_{slow}^L and \bar{z}_{fast}^L for $h < h_M/(1 - \delta)$, and \bar{z}_{slow}^M and \bar{z}_{fast}^M for $h > h_M/(1 - \delta)$
 399 – respond in opposite directions to the anticipated shock: the former decrease with
 400 γ and the latter increase. This relationship is formalized below.

401 **Proposition 4.** *An anticipated AI shock decreases human capital investment among*
 402 *households with $h < h_M/(1 - \delta)$, but increases it among those with $h > h_M/(1 - \delta)$.*
 403 *Specifically, \bar{z}_{slow}^L and \bar{z}_{fast}^L decrease with γ , while \bar{z}_{slow}^M and \bar{z}_{fast}^M increase with γ .*

404 *Proof.* See Appendix B. □

405 3.4.2 Effects on labor supply

406 **via income:** The AI shock raises period-2 labor income for households who will
 407 work in the low or high sector, leading to a positive income effect that reduces their
 408 labor supply in period 1.

409 **via full-time training:** Because full-time training and labor supply compete for
 410 time, the AI shock affects their tradeoff through its impact on human capital invest-
 411 ment incentives. For $h > h_M/(1 - \delta)$, where AI makes investing in additional skills
 412 more attractive, households are more likely to engage in full-time training and thus
 413 reduce period-1 labor supply. In contrast, for $h < h_M/(1 - \delta)$, where the AI shock
 414 lowers the payoff to investing in skills, households shift away from full-time training
 415 and supply more labor in the first period.

416 3.4.3 Effects on saving

417 The AI shock increases sectoral labor productivities for the low and high sectors in
 418 period 2, while leaving the middle sector's labor productivity unchanged. Its effect
 419 on saving can be analyzed as if we are varying the parameter t in the functions
 420 $\Delta_{on-job}(x, a; t)$, defined in (32), and $\Delta_H(x, a; t)$, defined in (39).

421 **Proposition 5.** $\Delta_{on-job}(x, a; t)$ is convex in t . $\Delta_H(x, a; t)$ is increasing in t .

- 422 • If $\Delta_{on-job}(x, a; t) > 0$ and $t > 1$, $\Delta_{on-job}(x, a; t') > \Delta_{on-job}(x, a; t)$ for $t' > t > 1$.
- 423 • If $\Delta_{on-job}(x, a; t) > 0$ and $t < 1$, $\Delta_{on-job}(x, a; t') < \Delta_{on-job}(x, a; t)$ for $1 > t' > t$.

424 *Proof.* See Appendix B. □

425 **Households who stay in the same sector** For middle-sector households, the
 426 AI shock leaves both their incomes and saving unchanged.

427 By contrast, low-sector and high-sector households experience an increase in
 428 period-2 labor income x' as a result of the AI shock. If they remain in the same

429 sector without needing additional human capital investment or on-the-job training,
430 their saving behavior in the absence of the AI shock can be compared to the scenario
431 with fixed human capital. Following the AI shock, however, their situation resembles
432 one with on-the-job training that enhances x' (i.e., $t > 1$). Thus, the effect of the
433 AI shock on saving is captured by the on-the-job training impact, $\Delta_{\text{on-job}}(x, a; t)$.

434 As shown in Proposition 2, $\Delta_{\text{on-job}}(x, a; t)$ has opposite signs for low-skill and
435 high-skill households. This implies that the AI shock *crowds out* saving among
436 low-sector households, while it *crowds in* saving for high-sector households.

437 For households who must undertake full-time training to remain in the high
438 sector, $\Delta_H(x, a; t)$ captures the additional effect of such training on saving. In this
439 case, a higher x' —brought about by the AI shock—corresponds to an increase in t ,
440 further boosting $\Delta_H(x, a; t)$ (Proposition 5). Consequently, the AI shock *crowds in*
441 saving for high-sector households in this scenario as well.

442 **Households who upskill** For low-sector households, saving behavior remains
443 unchanged, as the AI shock does not affect their future productivity after upskilling.

444 For the middle-sector households who upskill via on-job-training, the AI shock
445 boosts their future productivity gain from λ to $(1 + \gamma)\lambda$, which corresponds to a
446 higher t in $\Delta_{\text{on-job}}(x, a; t)$ with $t > 1$. According to Proposition 5, if the pre-shock
447 effect of on-the-job training on saving is positive, the AI shock will *raise* saving.
448 However, if this effect is negative, the overall impact of the AI shock on saving
449 becomes ambiguous.

450 For the middle-sector households who upskill via full-time training, there is an
451 *additional positive effect* of the AI shock on their saving, because a higher x' increases
452 $\Delta_H(x, a; t)$ (Proposition 5).

453 **Households who downskill** Downsampling, which reflects human capital depre-
454 ciation, does not require any new investment in skills. For high-sector households
455 who transition downward, the AI shock leaves their future productivity – and thus
456 their saving – unchanged.

457 For middle-sector households who downskill to the low sector, their saving differs
458 from the fixed human capital scenario by $\Delta_{\text{on-job}}(x, a; t)$ with $t < 1$. The AI shock
459 mitigates their future productivity loss by reducing it from λ to $(1 - \gamma)\lambda$, effectively
460 increasing t to a new value $t' < 1$. According to Proposition 5, if the pre-shock effect
461 $\Delta_{\text{on-job}}(x, a; t)$ is positive, the AI shock will *reduce* saving. If this effect is negative,
462 however, the overall impact of the AI shock on saving is ambiguous.

463 3.5 Limitations of the two-period model

464 Up to this point, our analysis has focused on how AI influences household-level
465 decisions regarding human capital investment, labor supply, and saving within the

466 framework of a two-period model. While this provides valuable insights into individual behavioral responses, understanding the broader, economy-wide implications
467 of AI requires moving to a more comprehensive setting – a quantitative model with
468 an infinite time horizon, endogenous asset accumulation, and general equilibrium
469 feedback.

471 **General equilibrium (GE) effects** When households adjust their investment in
472 human capital, labor supply, and savings in response to AI, these changes aggregate
473 up to affect the total supply of effective labor and capital in the economy. As these
474 aggregates shift, they exert downward or upward pressure on the wage rate and
475 the interest rate, feeding back into each household’s optimization problem. Thus,
476 general equilibrium effects capture the intricate loop by which individual decisions
477 shape, and are shaped by, the macroeconomic environment.

478 **Composition effects** Endogenizing human capital investment injects dynamism
479 into how households sort themselves among the three skill sectors. When an AI shock
480 occurs, individuals may choose to retrain, upskill, or even move to lower-skilled work,
481 reshaping the distribution of labor across sectors. This shifting composition changes
482 the relative size of each sector, with significant consequences for both aggregate
483 outcomes and the distributional effects of AI.

484 4 A Quantitative Model

485 We now solve the full dynamic model with infinite horizon, endogenous asset accumulation,
486 and general equilibrium. We calibrate the model to reflect key features of
487 the U.S. economy, capturing reasonable household heterogeneity.

488 4.1 Calibration

489 We calibrate the model to match the U.S. economy. For several preference parameters,
490 we adopt values commonly used in the literature. Other parameters are
491 calibrated to align with targeted moments. The model operates on an annual time
492 period. Table I summarizes the parameter values used in the benchmark model.

493 The time discount factor, β , is calibrated to match an annual interest rate of 4 percent.
494 We set χ_n to replicate an 80 percent employment rate. We calibrate χ_e to match the fact that around 30 percent of the population invests in human capital.
496 The borrowing limit, a , is set to 0.

497 We calibrate parameters regarding labor productivity process as follows. We
498 assume that x follows the AR(1) process in logs: $\log z' = \rho_z \log z + \epsilon_z$, where
499 $\epsilon_z \sim N(0, \sigma_z^2)$. The shock process is discretized using the Tauchen (1986) method,
500 resulting in a transition probability matrix with 9 grids. The persistence parameter

Table I: Parameters for the Calibration

Parameter	Value	Description	Target or Reference
β	0.91795	Time discount factor	Annual interest rate
ρ_z	0.94	Persistence of z shocks	See text
σ_z	0.287	Standard deviation of z shocks	Earnings Gini
\underline{a}	0	Borrowing limit	See text
χ_n	2.47	Disutility from working	Employment rate
χ_e	1.48	Disutility from HC effort	See text
\bar{n}	1/3	Hours worked	Average hours worked
e_H	1/3	High level of effort	Average hours worked
e_L	1/6	Low level of effort	See text
h_M	0.41	Human capital cutoff for M	See text
h_H	0.96	Human capital cutoff for H	See text
λ	0.2	Skill premium	Income Gini
α	0.36	Capital income share	Standard value
δ	0.1	Capital depreciation rate	Standard value

Table II: Key Moments

Moment	Data	Model
Employment rate	0.80	0.80
Human capital investment ratio	0.29	0.29
Gini coefficient for wealth	0.78	0.76
Gini coefficient for earnings	0.63	0.62
Gini coefficient for income	0.57	0.58

501 $\rho_z = 0.94$ is chosen based on estimates from the literature. The standard deviation
502 σ_z , is chosen to match the earnings Gini coefficient of 0.63.

503 We deviate from the two-period model by assuming that the labor supply is a
504 discrete choice between 0 and $\bar{n} = 1/3$. This change only rescales the two-period
505 model without altering the trade-off facing the households. But such rescaling facil-
506 itates the interpretation that households are deciding whether to allocate one-third
507 of their fixed time endowment to work. The high-level human capital accumulation
508 effort, e_H is assumed to equal \bar{n} . The low-level effort, e_L is set to half of e_H . The skill
509 premium across sectors, λ , is set at 0.2 to match the income Gini coefficient. Human
510 capital cutoffs, h_M and h_H , are set so that the population shares in low, middle, and
511 high sectors are, respectively, 20, 40, and 40 percent. This population distribution
512 roughly matches the fractions of U.S. workers in 2014 who are employed in routine
513 manual occupations (low sector), routine cognitive and non-routine manual (middle
514 sector), and non-routine cognitive (high sector) (Cortes *et al.*, 2017).

515 On the production side, we set the capital income share, α , to 0.36, and the
516 depreciation rate, δ , to 0.1.

517 *4.2 Key Moments: Data vs. Model*

518 In Table II, we present a comparison of key moments between the model and the
519 empirical data. The model does an excellent job of replicating the 80% employment
520 rate observed in the data. In this context, employment is defined as having positive
521 labor income in the given year, consistent with the common approach used in the
522 literature. According to OECD (1998), the share of the population investing in
523 human capital—those who are actively engaged in skill acquisition or education—is
524 approximately 30%, a figure well matched by the model’s predictions. This is an
525 important metric because it reflects the model’s capacity to capture the dynamics
526 of human capital formation, which plays a critical role in shaping long-run earnings
527 and income inequality. Additionally, the model accurately captures the distribution
528 of income and earnings, aligning closely with observed data. This suggests that the
529 model effectively incorporates the key mechanisms driving labor market outcomes
530 and the corresponding distributional aspects of earnings. Although the model does
531 not explicitly target the wealth Gini coefficient, it achieves a close match to the
532 data: the empirical wealth Gini is 0.78, while the model produces a value of 0.76.
533 This highlights the model’s ability to capture substantial wealth inequality in the
534 economy.

535 *4.3 Steady-state Distribution*

536 Table III presents the steady-state distribution of population, employment, and
537 assets across sectors. The population shares are calibrated to 20%, 40%, and
538 40% by adjusting the human capital thresholds that define sectors. The shares
539 of employment and assets are endogenously determined by households’ labor supply
540 and savings decisions. Notably, the high sector accounts for 46% of total employ-
541 ment—exceeding its population share—indicating that a disproportionate number
542 of households choose to work in that sector. Asset holdings are even more skewed:
543 the high sector holds 68% of total assets, while the low sector holds only 8%.

Table III: Distribution of Population, Employment and Assets

Sectors	Pop. Share (%)	Emp. Share (%)	Assets Share (%)
Low	20.76	18.58	8.07
Middle	38.87	35.35	23.92
High	40.35	46.07	68.01

Note: Human capital cutoffs, h_H and h_M , determine the population share across sectors. Employment share and assets share are implied by households labor supply decisions and saving decisions.

Figure 3: Steady-state Human Capital Distribution

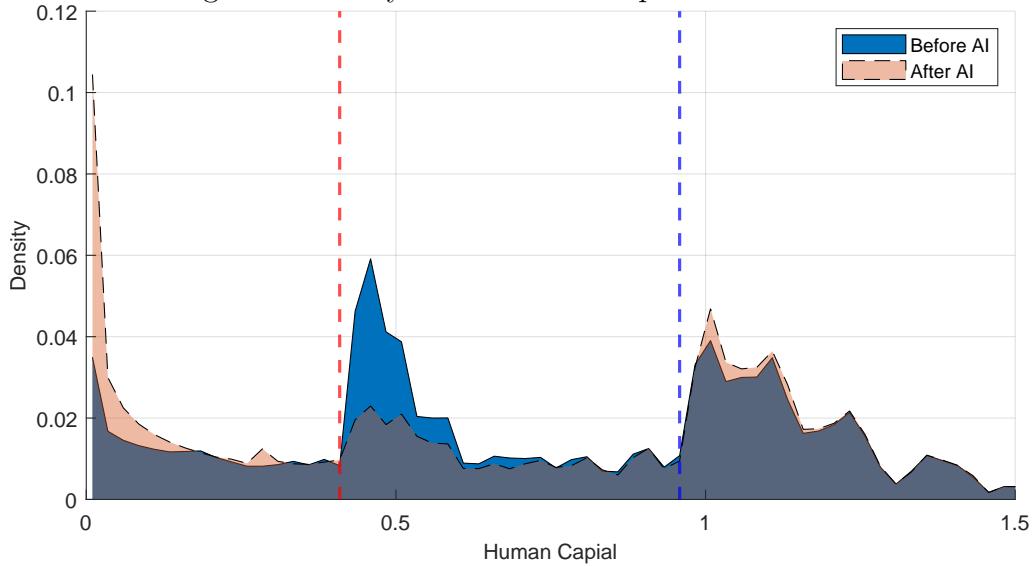


Figure 4: Steady-state Human Capital Investment

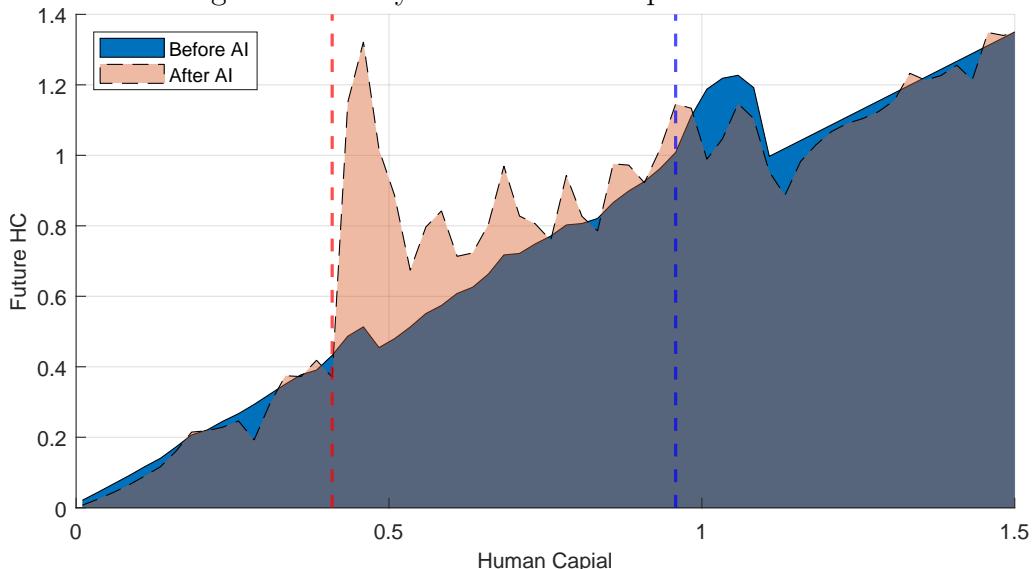
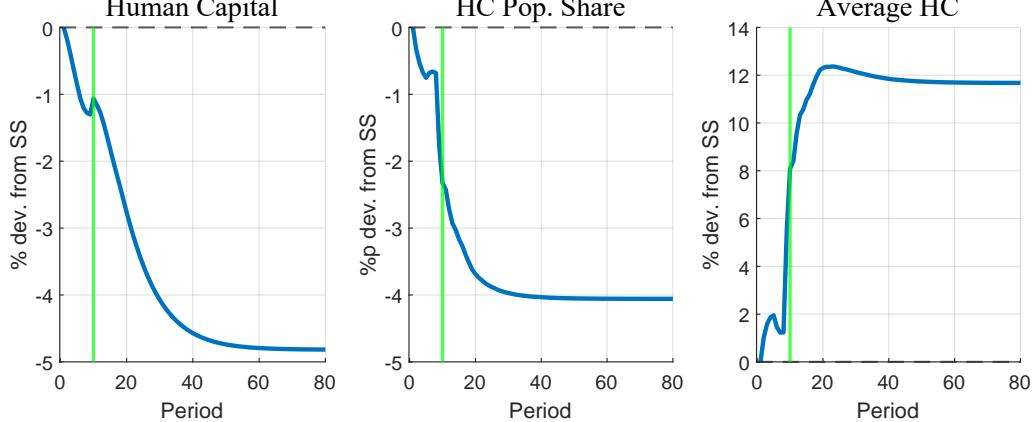


Figure 5: Transition Path for Human Capital Investment



544 5 AI's Impact on Human Capital Adjustments

545 We now introduce AI technology into the quantitative model, assuming that it will
546 be implemented in 10 years and that households have full information about its
547 arrival. We examine both the transition dynamics and the differences between the
548 initial and new steady states. This framework allows us to analyze how the economy
549 adjusts in anticipation of, and in response to, the adoption of AI.

550 The effect of AI on the sectorial productivity is modeled as in (40) with $\gamma = 0.3$.
551 That is, AI boosted the productivity of the low sector workers by 7.5% and the
552 productivity of the high sector workers by 5%, leaving the middle sector intact.
553 It captures the key idea that AI increases average labor productivity (Acemoglu
554 and Restrepo, 2019), but reduces the earning premium for the middle sector, and
555 enlarges the earning premium for the higher sector relative the middle sector.

556 5.1 Human Capital Adjustments

557 Given the employment distribution in the initial steady state, AI is projected to
558 increase the economy's labor productivity by 4% on average, assuming households
559 do not alter their decisions in response. However, changes in earning premiums
560 incentivize households to adjust their human capital investments.

561 **Steady-state human capital distribution:** Figure 3 illustrates how households
562 reallocate across sectors in the new steady state relative to the initial one. The x-axis
563 denotes the level of human capital, while the y-axis indicates the mass of households
564 at each human capital level. The red vertical line marks the cutoff between the low
565 and middle sectors, and the blue vertical line marks the cutoff between the middle
566 and high sectors.

567 The gray shaded area shows the overlap between the two steady-state distri-
568 butions. Within each sector, the distribution of households is skewed to the left,
569 reflecting the tendency for human capital investment to be concentrated among
570 those near the sectoral cutoffs. As shown in the decision rule diagram in Figure 2,
571 some households seek to upgrade their skills, while others aim to remain in more
572 skilled sectors. The blue shaded area highlights the mass of households who have
573 exited the middle sector following the AI shock. The pink areas represent the addi-
574 tional mass of households in the new steady-state distribution, concentrated at the
575 lower end of the low sector and the lower end of the high sector.

576 **Steady-state human capital investment:** This reallocation pattern reflects
577 shifts in human capital investment incentives driven by AI's impact on the skill
578 premium. Figure 4 plots human capital investment decisions in the initial and new
579 steady states across different human capital levels. Because both the productivity

580 shock (z) and current asset holdings (a) influence human capital investment, the
581 y-axis shows the weighted average of next-period human capital, where the weights
582 reflect the steady-state distribution of households by productivity shock and wealth
583 at each human capital level.

584 The changes in decision rules before and after the AI shock are highlighted in
585 the blue shaded area, where next-period human capital in the new steady state
586 is lower than in the initial steady state, and in the pink shaded area, where it is
587 higher. The most notable change is that the middle-sector households substantially
588 intensify their human capital investment, aiming to transition into high-sector roles.
589 In contrast, households in the low sector reduce their human capital investment,
590 causing those who might have moved up to the middle sector to remain in the low
591 sector or even drift further down to the very bottom of human capital distribution
592 as shown in Figure 3.

593 Somewhat surprisingly, most high-sector workers in the new steady state decrease
594 their human capital investment relative to the initial steady state. This is primarily
595 a composition effect: as more households move from the middle-sector to the high
596 sectors, the average asset holdings among high-sector households decline, making
597 intensive human capital investment less affordable [note that this is not supported
598 by the average asset in transition dynamics figure 9].

599 **Transition path** Figure 5 reports the transition dynamics of aggregate human
600 capital from the initial to the new steady state. The figure also displays its extensive
601 margin (the share of households making positive human capital investments) and
602 intensive margin (average human capital per household among those who invest).

603 As households reallocate from the middle sector to the low and high sectors, the
604 net effect is a gradual decline in aggregate human capital along the transition path.
605 This mirrors the steady-state change observed in Figure 3, where the increased mass
606 at the lower end of the low sector outweighs the increase in the high sector.

607 Additionally, human capital accumulation becomes increasingly concentrated
608 among a smaller share of the population. The proportion of households making
609 positive human capital investments steadily declines, ultimately stabilizing at a level
610 4% lower than in the initial steady state. Meanwhile, the average human capital
611 among those who invest rises, reaching a level 12% higher than the initial steady
612 state in the long run.¹⁴

613 5.2 Job Polarization

614 An important implication of human capital adjustments to the AI shock is job
615 polarization. Figure 6 illustrate the transition paths of population shares and em-

¹⁴The only exception to those patterns occurs at period 10 when the positive effects of AI on sectoral productivity are realized.

616 employment rates in each sector. Notably, the middle sector experiences a significant
617 decline, with its population share decreasing by approximately 13%. Additionally,
618 employment within this sector plummets to a level 16% lower than the initial steady
619 state. In contrast, both the low and high sectors see increases in their population
620 shares and employment rates. These dynamics indicate a reallocation of *workers*
621 from the middle sector to the low and high sectors following the introduction of AI.

622 **Voluntary job polarization** This worker reallocation aligns with the phenomenon
623 of “job polarization” (Goos *et al.*, 2014), where AI and automation technologies dis-
624 proportionately replace tasks commonly performed by middle-skilled workers. How-
625 ever, our model introduces a complementary mechanism to the conventional under-
626 standing of this reallocation. Specifically, households in our model voluntarily exit
627 the middle sector even before AI implementation by adjusting their human capital
628 investments – many middle-sector workers opt for non-employment to invest in skills
629 that will better position them for the post-AI labor market. To emphasize this key
630 difference, our model deliberately abstracts from any direct negative effect of AI on
631 middle-sector workers.

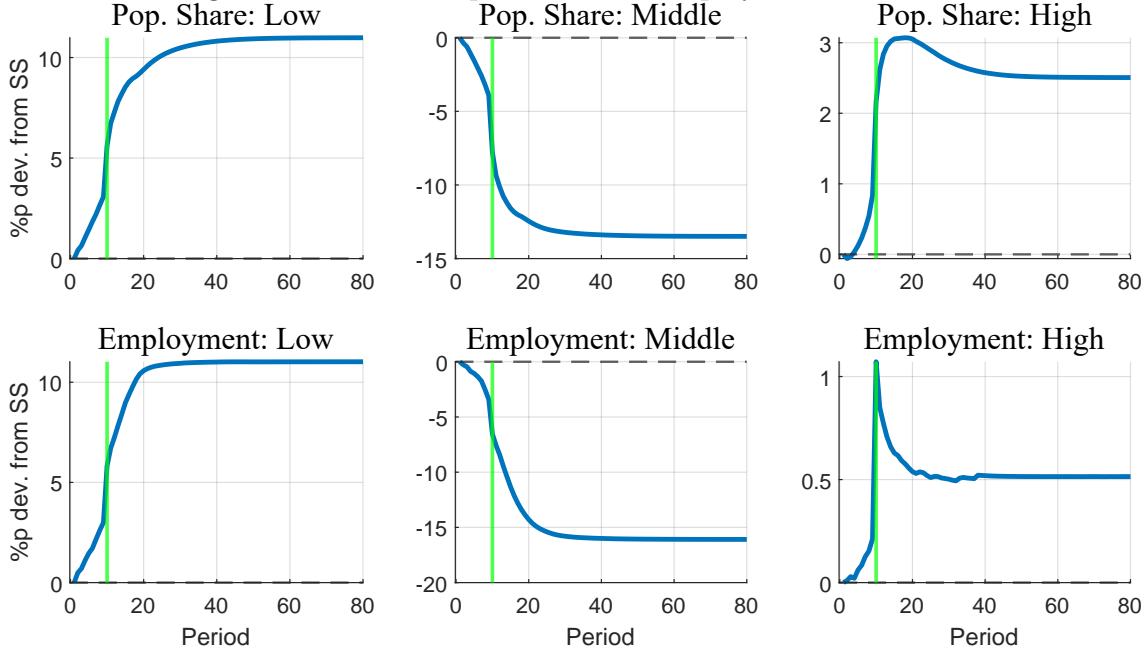
632 **Employment flows more towards the low sector** Another intriguing finding
633 in our model is the more pronounced employment effect in the low sector compared
634 to the high sector. In the new steady state, the employment rate in the low sector
635 increases by 12%, whereas in the high sector, it rises by only 0.5%. This asymmetry
636 in employment rate changes suggests an unbalanced reallocation of workers from the
637 middle sector, with a greater flow toward the low sector.

638 This disparity arises from two key factors. First, AI enhances the productivity of
639 low-sector workers by 7.5% and high-sector workers by 5%. However, this produc-
640 tivity differential alone does not fully account for the significant asymmetry. The
641 second factor is the variation in labor supply elasticity across sectors. Compared to
642 the high sector, the low sector exhibits higher labor supply elasticity, meaning that
643 the same change in labor earnings triggers larger labor supply responses. This is
644 because households in the low sector have lower consumption levels, making their
645 marginal utility of consumption more sensitive to changes in their budget. Con-
646 sequently, a greater proportion of households in the low sector are at the margin
647 between employment and non-employment (Chang and Kim, 2006).

648 6 The Aggregate and Distributional Effects of AI

649 The aggregate and distributional effects of AI are shaped by both its direct impact on
650 sectoral productivity and the endogenous response of human capital accumulation.
651 By altering sectoral productivity, AI changes labor earnings, which in turn influences
652 labor supply decisions and savings through income effects. Consequently, AI directly

Figure 6: Sectoral Population and Employment Transition



Note: The transition paths within each sector. The x-axis represents years, and the y-axis shows the percentage (or percentage point) deviation from the initial steady state. AI introduction is assumed to occur in period 10. “Pop. Share” denotes the population share within each sector. “Employment” is the percentage of households who are employed in each sector.

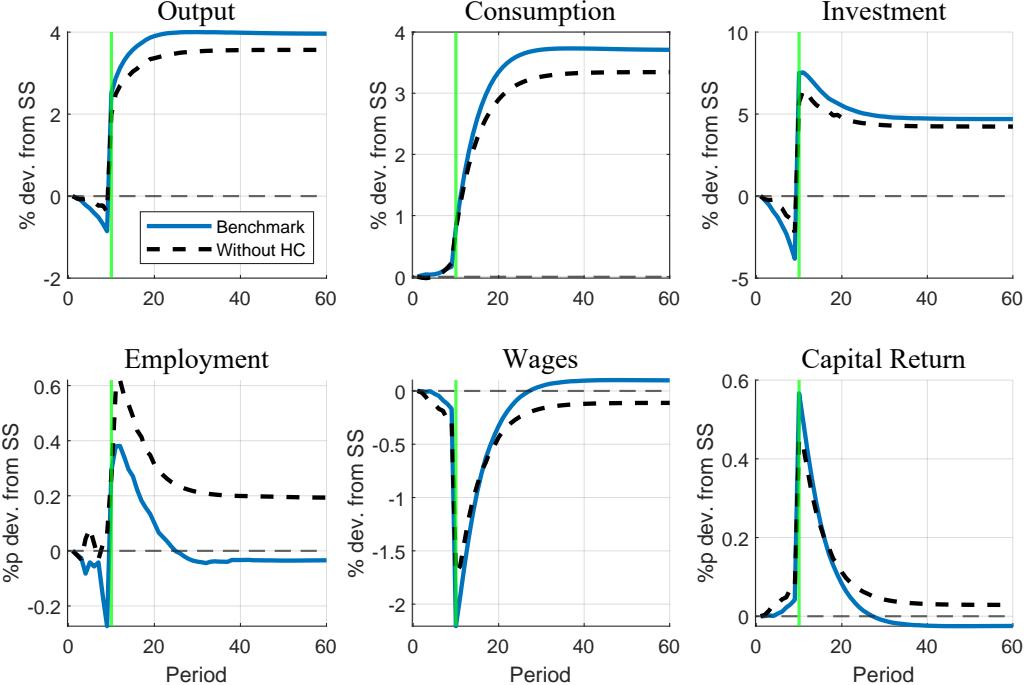
653 affects the supply of labor and capital, generating aggregate economic responses.
 654 Because AI’s productivity effects are heterogeneous across sectors, its impact is
 655 inherently distributional.

656 These sectoral differences also induce human capital adjustments, as households
 657 reallocate across sectors in response to changing incentives. This reallocation not
 658 only shifts the distribution of labor productivity and aggregate productivity, but
 659 also directly shapes distributional outcomes, as households’ relative positions in the
 660 income and asset distributions are altered by their movement across sectors.

661 In this section, we examine the importance of endogenous human capital ad-
 662 justment in shaping both the transitional and long-run effects of AI. To do so, we
 663 compare the benchmark economy – where households endogenously adjust their hu-
 664 man capital – with an alternative scenario in which households are held fixed at
 665 their initial steady-state human capital during the AI transition (“No HC model”).
 666 In both cases, households make endogenous decisions about consumption, savings,
 667 and labor supply.

668 By contrasting the transition dynamics across these two economies, we can disen-
 669 tangle the direct and indirect effects of AI. The transition path in the No-HC-model
 670 isolates the direct impact of AI on aggregate and distributional outcomes, as it ab-
 671 stracts from any human capital adjustments. The difference in outcomes between
 672 the benchmark and the No-HC-model then reveals the indirect effects of AI that
 673 operate through households’ adjustments in human capital. This decomposition al-
 674 lows us to assess the relative importance of human capital dynamics in driving both

Figure 7: Transition Path of Aggregate Variables: Benchmark vs. No HC Models.



Note: The transition paths of aggregate variables: benchmark vs. No HC models. The x-axis represents years, and the y-axis shows the percentage deviation from the initial steady state. AI introduction is assumed to occur in period 10. The No HC model is an economy in which workers maintain their initial steady-state level of human capital throughout the AI implementation until the new steady state is reached.

675 the aggregate and distributional consequences of AI.

676 6.1 Aggregate Implications

677 Figure 7 shows the transition paths of key macroeconomic variables—output, con-
678 sumption, investment, and employment—as well as factor prices, including the wage
679 rate and capital return. The blue solid lines depict results from the benchmark model
680 with endogenous human capital adjustment, while the black dashed lines represent
681 the No-HC model in which human capital is held fixed.

682 6.1.1 AI's direct impacts

683 The No-HC-model isolates the direct effects of AI. In the long run, the introduction
684 of AI leads to higher output, consumption, investment, and employment. However,
685 in anticipation of AI (prior to period 10), output and investment decline, while
686 consumption and employment remain stable.

687 Before the implementation of AI, sectoral productivity is unchanged; the only
688 difference is households' awareness of future increases in productivity in the low and
689 high sectors beginning in period 10. This anticipation raises households' expected
690 lifetime income, prompting them to save less and consume more ahead of the actual
691 productivity gains. As a result, aggregate capital stock falls, which lowers output and
692 reduces the marginal product of labor while raising the marginal product of capital.
693 Employment remains largely unchanged in this period, as sectoral productivity has

694 not yet shifted.

695 Following the AI shock, sectoral productivity in the low and high sectors rises,
696 boosting labor income, employment, and output in these sectors. Because produc-
697 tivity gains are labor-augmenting, the supply of efficient labor units rises sharply,
698 causing wages to decline and capital returns to increase. Employment and invest-
699 ment both adjust to dampen these factor price changes. In the new steady state, the
700 wage rate is slightly below its initial level, while the return to capital is marginally
701 higher.

702 6.1.2 AI's indirect impacts via endogenous human capital adjustments

703 The difference between the No-HC model and the benchmark model captures the
704 indirect effects of AI operating through endogenous human capital adjustments.
705 Among all macroeconomic variables, this indirect effect is most pronounced for em-
706 ployment.

707 In anticipation of AI, employment declines as some households temporarily exit
708 the labor market to invest in human capital and prepare for the post-AI economy.¹⁵
709 During this period, labor productivity remains unchanged, so the decline in em-
710 ployment directly translates to a reduction in output. Consistent with standard
711 consumption-smoothing behavior, this reduction is mainly absorbed by lower in-
712 vestment. Meanwhile, the drop in employment mitigates the direct effects of AI on
713 both wages and capital returns prior to the AI implementation.

714 After AI is introduced, employment rebounds as sectoral productivity increases.
715 However, continued human capital investment by middle-sector households keeps
716 employment lower than in the No-HC model, resulting in an almost neutral long-
717 run effect of AI on employment. Despite this, output, consumption, and investment
718 are all higher in the benchmark model because human capital adjustments reallocate
719 more labor to the low and high sectors, thereby better capturing the productivity
720 gains from AI.

721 This reallocation also reverses the steady-state comparison of factor prices: en-
722 dogenous human capital adjustment transforms the negative direct effect of AI on
723 the wage rate into a positive net effect, and the positive direct effect on capital
724 returns into a negative net effect.

725 6.2 Distributional Implications

726 The findings above underscore the importance of accounting for human capital ad-
727 justments when assessing the aggregate impact of AI, as households actively adapt
728 to a rapidly evolving labor market. When it comes to economic inequality, endoge-
729 nously adjusting human capital plays an even more significant role.

¹⁵Empirical studies, such as Lerch (2021) and Faber *et al.*, (2022), support the short-term adverse effects of AI adoption on labor markets.

730 Figure 8 shows the transition paths of Gini coefficients for earnings (labor in-
731 come), total income (capital and labor income), consumption, wealth (asset hold-
732 ings), and human capital. The black dashed lines represent results from the No-HC
733 model, capturing the direct impact of AI without human capital adjustment. In
734 contrast, the blue solid lines reflect the benchmark model, where human capital re-
735 sponds endogenously to both anticipated and realized changes in the skill premium
736 induced by AI.

737 **6.2.1 Income, earnings, and consumption inequalities**

738 The comparison of transition paths between the No-HC model and the benchmark
739 model reveals that endogenous human capital adjustments fundamentally alter the
740 impact of AI on income, earnings, and consumption inequalities.

741 **AI's direct impacts:** Without any human capital adjustments, AI's impact on
742 inequalities is primarily driven by productivity gains in the low and high sectors
743 – 7.5% and 5%, respectively. As a result, there is little direct impact on income
744 and earnings Gini coefficients in anticipation of AI before period 10. After AI is
745 implemented, both income and earnings inequality decline: higher labor productivity
746 raises earnings in the low sector, while wage declines in the middle sector compress
747 the distribution. Consumption inequality remains largely unchanged throughout
748 the transition.

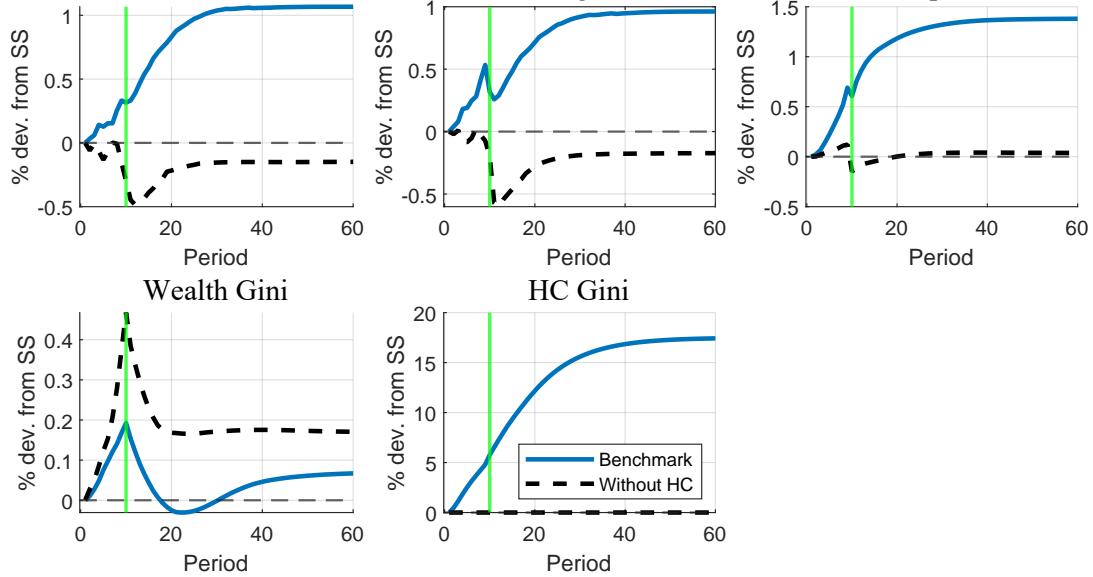
749 **Effects of AI-induced human capital adjustments:** Allowing human capital
750 to adjust endogenously, however, leads to pronounced job polarization, as shown in
751 Section 5.2. Households who would have qualified for middle-sector jobs now tran-
752 sition to either the low or high sector. Those moving to the low sector see reduced
753 labor earnings, while those shifting to the high sector enjoy increased earnings. This
754 polarization drives up earnings and income inequality, both before and after AI is
755 implemented. As income disparities widen, consumption inequality also increases.

756 **6.2.2 Wealth inequality**

757 In stark contrast to the effects on income and earnings inequality, allowing for en-
758 dogenous human capital adjustment actually mitigates the negative direct impact of
759 AI on wealth inequality. While AI's direct effect would otherwise widen disparities,
760 human capital responses help dampen the increase in wealth inequality, underscoring
761 the stabilizing role of human capital adjustments in the wealth distribution.

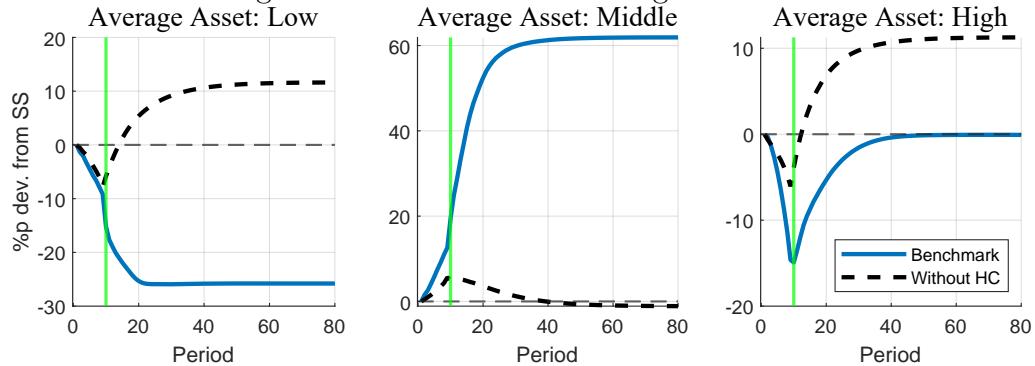
762 To disentangle the direct and indirect effects of AI on wealth inequality, Figure
763 9 presents the sectoral transition paths for asset holdings, while Figure 10 compares
764 steady-state asset investment decisions across different human capital levels.

Figure 8: Transition Path of Inequality Measures: Benchmark vs. No HC Models.



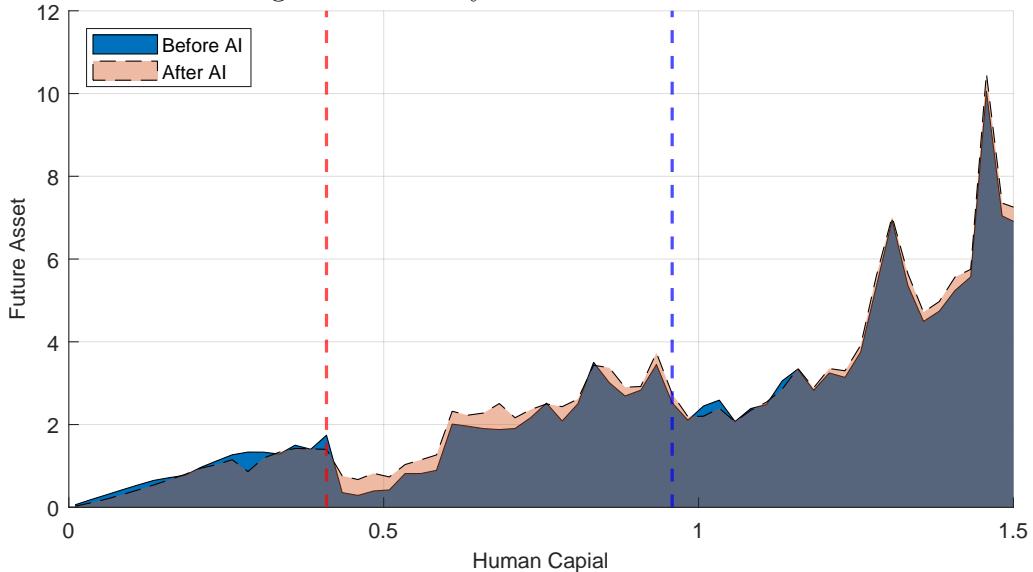
Note: The transition paths of inequality measures: benchmark vs. No HC models. The x-axis represents years, and the y-axis shows the percentage deviation from the initial steady state. AI introduction is assumed to occur in period 10. The No HC model is an economy in which workers maintain their initial steady-state level of human capital throughout the AI implementation until the new steady state is reached.

Figure 9: Sectoral Asset-holding Transition



Note: The transition paths of average capital within each sector. The x-axis represents years, and the y-axis shows the percentage deviation from the initial steady state. AI introduction is assumed to occur in period 10. "Average Capital" denotes the physical assets per household in each sector.

Figure 10: Steady-state Asset Investment



765 [Add a figure that compares the steady-state asset investment in the No-HC-
766 model (a counterpart of Figure 10).]

767 **AI's direct impacts:** We first focus on the black dashed lines in Figure 9. With-
768 out households reallocation across sectors, total assets and average asset holdings
769 follow similar patterns. In both the low and high sectors, households reduce their
770 savings in anticipation of AI, expecting higher lifetime labor income. After AI is
771 implemented at period 10, their savings increase alongside rising labor incomes.
772 In contrast, households in the middle sector, anticipating a negative income effect
773 from AI due to a lower wage rate, increase their savings prior to period 10. Once
774 AI is introduced and the wage rate recovers, middle-sector households reduce their
775 savings.

776 These shifts in sectoral saving patterns sharply increase wealth inequality before
777 period 10, as low-sector households – typically the least wealthy – reduce their asset
778 holdings. After AI is implemented and saving rates in the low sector recover, the
779 wealth Gini coefficient declines from its peak and stabilizes at a level about 0.2%
780 higher than its initial steady state.

781 **Effects of AI-induced human capital adjustments:** Average asset holding
782 isolates us from movements in the population share along the transition path.

783 1. Selection effect is dominant: From middle to low: low productivity and
784 middle-sector level wealth. Due to higher wealth level than the low-sector, the influx
785 should have increased the arrearage asset holding of the low sector, but because
786 they are low productivity households and they experience a reduction of sectoral
787 productivity. [But we still should have seen an increase in Average asset before
788 period 10???]

789 From middle to high: high productivity and middle-sector level wealth. Due
790 to lower wealth level than the high-sector, the influx of middle-sector households
791 reduces the average asset holding of the high sector. But since they are high-
792 productivity households, their saving rate increases.

793 2. Precautionary saving motive changes: For the low sector, the reduction of
794 skill premium in the benchmark model implies a reduction in idiosyncratic risk, so
795 households reduce saving. For the high sector, the opposite is true. In the No-HC-
796 model, changes in skill premium does not affect idiosyncratic risk since households
797 cannot change sector.

798 Allowing for endogenous human capital adjustment results in time-varying pop-
799 ulation shares across sectors along the transition path, which drives the divergence
800 between sectoral total and average asset holdings. In both the low and high sectors,
801 although the average household's asset holding declines substantially, the total as-
802 set holding in the low sector remains relatively stable, and in the high sector even
803 increases, due to the influx of households from the middle sector. Conversely, while

804 the average household in the middle sector saves more, the total asset holding in
805 the middle sector declines as its population share shrinks. These offsetting effects
806 between sectoral average asset holdings and shifting population shares help dampen
807 fluctuations in the wealth Gini coefficient along the transition path, compared to
808 the No-HC model (see Figure 8).

809 I cannot explain why the wealth gini in the benchmark model is lower than in
810 the No-HC-model, since from the total asset graphs, benchmark model has more
811 total assets in the higher sector in new steady state. So we have to turn to the
812 comparison of asset holding decision rule.

813 **Steady-state change in asset investment:** To explain the contrasting sectoral
814 changes in average asset holdings between the benchmark model and the No-HC-
815 model in the new steady state, Figure 10 shows how next-period asset holdings
816 change from the initial to the new steady state at each human capital level in the
817 benchmark model, while Figure XXX presents the corresponding results for the No-
818 HC-model. As in Figure 4, the y-axis displays the weighted average of next-period
819 asset holdings, with weights reflecting the steady-state distribution of households
820 by productivity shocks (z) and wealth (a) at each human capital level. Pink shaded
821 areas indicate an increase in next-period asset holdings, while blue shaded areas
822 indicate a decrease.

823 Note that in the benchmark model, the pink shaded areas are mostly located
824 in the middle sector. This is due to a “selection effect” since the households who
825 stays in the middle sector in the new steady after the AI shock are those with
826 higher productivity than those in the initial steady state. It is because those with
827 lower productivity would have already flow in the low sector. As productivity is
828 positively correlated with wealth, households remaining in the middle sector in the
829 new steady state tends to have more wealth, which boosts their saving. I cannot
830 explain why the high-sector average asset-holding remains unchanged in the new
831 steady state whereas the asset investment figure shows that the next-period asset
832 holding is reduced in the high sector.

833 Reduction in saving in the low sector, because of the influx of low-productivity
834 households from the middle sector? High sector, it is a mix so that average asset
835 holding remains the same as the initial steady state. in the benchmark, in the initial
836 steady state, the middle sector’s idiosyncratic productivity on average is lower than
837 the high sector households (that is the why they stay in the middle sector that has
838 requires lower human capital investment. Therefore, those moving to the high sector
839 has on average lower z and lower a . That explains why there is a reduction of asset
840 investment in the low end to high sector in the new steady state as the result of
841 more mover from the middle sector. Income effects are still present for the higher
842 end of high sector, which acts as a counterforce to the reduction of average asset
843 holding in the low end.

844 **7 Conclusion**

845 Recent studies on AI suggest that advancements are likely to reduce demand for
846 junior-level positions in high-skill industries while increasing the need for roles fo-
847 cused on advanced decision-making and AI oversight. We demonstrate how human
848 capital investments are expected to adapt in response to these shifts in skill demand,
849 highlighting the importance of accounting for these human capital responses when
850 assessing AI's economic impact.

851 Our work points to several promising directions for future research on the eco-
852 nomic impacts of AI. First, while general equilibrium effects—such as wage and
853 capital return adjustments—have a limited role in our model, further research could
854 examine how these effects might vary under different economic conditions or policy
855 environments. Second, if governments implement redistribution policies to address
856 AI-induced inequality, understanding how these policies influence human capital
857 accumulation, and thus their effectiveness, would be valuable. Finally, our model
858 assumes households have perfect foresight when making human capital investments.
859 Relaxing this assumption could reveal new insights into the economic trajectory of
860 AI advancements and offer important policy implications.

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911 **A Household Decision Rule Cutoffs**

912 *A.1 Additional cutoffs formulae for households*

$$\bar{z}_{non}^M(a) := \frac{(\exp(\frac{\chi_n}{1+\beta}) - 1)[(1+r)a + \frac{w'z'}{1+r'}]}{w} \quad (\text{A.1})$$

$$\bar{z}_{slow}^M(a) := \frac{(\exp(\frac{\chi_n - \chi_e e_H}{1+\beta}) - 1)[(1+r)a + \frac{w'z'(1+\lambda)}{1+r'}] + \lambda \frac{w'z'}{1+r'}}{w} \quad (\text{A.2})$$

$$\underline{z}_{fast}^M(a) := \frac{(\exp(\frac{\chi_n}{1+\beta}) - 1)[(1+r)a + \frac{w'z'(1+\lambda)}{1+r'}]}{w} \quad (\text{A.3})$$

$$\bar{z}_{fast}^M(a) := \frac{\left\{ \lambda \left[\exp(\frac{\chi_e e_L}{1+\beta}) - 1 \right]^{-1} - 1 \right\} \frac{w'z'}{1+r'} - (1+r)a}{w} \quad (\text{A.4})$$

$$\bar{z}_{non}^H(a) := \frac{(\exp(\frac{\chi_n}{1+\beta}) - 1)[(1+r)a + \frac{w'z'(1+\lambda)}{1+r'}]}{w} \quad (\text{A.5})$$

913 *A.2 Parameter restrictions for cutoffs ranking*

914 To guarantee that $(n = 0, e = e_H)$ dominates $(n = 0, e = 0)$, we need a lower bound
915 for λ . The slow learners prefer $(n = 0, e = e_H)$ if and only if

$$(1 + \beta) \ln c(n = 0, e = e_H) - \chi_e e_H \geq (1 + \beta) \ln c(n = 0, e = 0)$$

916 or equivalently:

$$\lambda \geq \underline{\lambda}_1 := \frac{(1+r)a + \frac{w'z'}{1+r'}}{\frac{w'z'}{1+r'}} \left(1 - \frac{1}{\exp(\frac{\chi_e e_H}{1+\beta})} \right) \text{ if } h < h_M \frac{1}{1-\delta} \quad (\text{A.6})$$

$$\lambda \geq \underline{\lambda}_3 := \frac{(1+r)a + \frac{w'z'}{1+r'}}{\frac{w'z'}{1+r'}} \left(\exp(\frac{\chi_e e_H}{1+\beta}) - 1 \right) \text{ if } h \geq h_M \frac{1}{1-\delta} \quad (\text{A.7})$$

917 To avoid $(n = 1, e = e_L)$ from being a dominated choice, we need another lower
918 bound for λ . To see it, recall that $(n = 1, e = 0)$ is better than $(n = 1, e = e_L)$
919 if $z > \bar{z}_{fast}$, and $(n = 1, e = e_L)$ is better than $(n = 0, e = e_L)$ if $z > \underline{z}_{fast}$.
920 $(n = 1, e = e_L)$ is therefore the best choice over the interval $(\underline{z}_{fast}, \bar{z}_{fast})$. For such an
921 interval to exist, it must be the case that when $z = \underline{z}_{fast}$, $z < \bar{z}_{fast}$. $z = \underline{z}_{fast}$ means
922 that the fast learners are indifferent between $(n = 1, e = e_L)$ and $(n = 0, e = e_L)$ so

923 that

$$(1+r)a + wzx(h) + \frac{w'z'}{1+r'} = \exp\left(\frac{\chi_n}{1+\beta}\right) \left[(1+r)a + \frac{w'z'}{1+r'} \right] \text{ if } h < h_M \frac{1}{1-\delta} \quad (\text{A.8})$$

$$(1+r)a + wzx(h) + \frac{w'z'(1+\lambda)}{1+r'} = \exp\left(\frac{\chi_n}{1+\beta}\right) \left[(1+r)a + \frac{w'z'(1+\lambda)}{1+r'} \right] \text{ if } h \geq h_M \frac{1}{1-\delta} \quad (\text{A.9})$$

924 For the fast learners to prefer $(n = 1, e = e_L)$ over $(n = 1, e = 0)$, we need

$$(1+\beta) \ln \frac{c(n=1, e=e_L)}{c(n=1, e=0)} \geq \chi_e e_L \quad (\text{A.10})$$

925 If $h < h_M \frac{1}{1-\delta}$, inequality (A.10) is:

$$(1+\beta) \ln \frac{(1+r)a + wzx(h) + \frac{w'z'}{1+r'}}{(1+r)a + wzx(h) + \frac{w'z'(1-\lambda)}{1+r'}} \geq \chi_e e_L$$

926 Evaluating the left-hand-side at $z = \underline{z}_{fast}$ yields:

$$\lambda \geq \underline{\lambda}_2 := \frac{(1+r)a + \frac{w'z'}{1+r'}}{\frac{w'z'}{1+r'}} \left(1 - \frac{1}{\exp(\frac{\chi_e e_L}{1+\beta})} \right) \exp\left(\frac{\chi_n}{1+\beta}\right) \quad (\text{A.11})$$

927 If $h > h_M \frac{1}{1-\delta}$, inequality (A.10) is:

$$(1+\beta) \ln \frac{(1+r)a + wzx(h) + \frac{w'z'(1+\lambda)}{1+r'}}{(1+r)a + wzx(h) + \frac{w'z'}{1+r'}} \geq \chi_e e_L$$

928 Evaluating the left-hand-side at $z = \underline{z}_{fast}$ yields:

$$\lambda \geq \underline{\lambda}_4 := \frac{(1+r)a + \frac{w'z'}{1+r'}}{\frac{w'z'}{1+r'}} \frac{\left(\exp\left(\frac{\chi_e e_L}{1+\beta}\right) - 1 \right) \exp\left(\frac{\chi_n}{1+\beta}\right)}{\exp\left(\frac{\chi_e e_L}{1+\beta}\right) + \exp\left(\frac{\chi_n}{1+\beta}\right) - \exp\left(\frac{\chi_e e_L + \chi_n}{1+\beta}\right)} \quad (\text{A.12})$$

929 We have that $\underline{\lambda}_1 > \underline{\lambda}_2$ and $\underline{\lambda}_3 > \underline{\lambda}_4$ if

$$\exp\left(\frac{\chi_e e_H}{1+\beta}\right) > \frac{\exp\left(\frac{\chi_e e_L}{1+\beta}\right)}{\exp\left(\frac{\chi_e e_L}{1+\beta}\right) + \exp\left(\frac{\chi_n}{1+\beta}\right) - \exp\left(\frac{\chi_e e_L + \chi_n}{1+\beta}\right)} \quad (\text{A.13})$$

930 Therefore, the inequality above implies that the conditions (A.6) and (A.7) are
931 sufficient for the conditions (A.11) and (A.12). Furthermore, $\underline{\lambda}_3 \geq \underline{\lambda}_1$ so that the
932 condition (A.7) is sufficient for the condition (A.6).

933 We can then conclude that the conditions (A.7) and (A.13) are sufficient for
934 1) the slower learners always prefers $(n = 0, e = e_H)$ over $(n = 0, e = 0)$, and 2)
935 $\bar{z}_{fast} > \underline{z}_{fast}$, i.e., there exists state space where $(n = 1, e = e_L)$ is optimal.

936 *A.3 Other cutoffs ranking for the two-period Model*

937 For the fast learners, their cutoffs rank as follows

$$\frac{\bar{z}_{fast}^L(a)}{1-\lambda} > \bar{z}_{fast}^L(a) > \bar{z}_{fast}^M(a) > \frac{\bar{z}_{fast}^M(a)}{1+\lambda} \quad (\text{A.14})$$

$$\frac{\underline{z}_{fast}^L(a)}{1-\lambda} > \underline{z}_{fast}^M(a) > \underline{z}_{fast}^L(a) > \frac{\underline{z}_{fast}^M(a)}{1+\lambda} \quad (\text{A.15})$$

938 For the slow learners, the rank of their cutoffs is

$$\frac{\bar{z}_{slow}^L(a)}{1-\lambda} > \bar{z}_{slow}^M(a) > \bar{z}_{slow}^L(a) > \frac{\bar{z}_{slow}^M(a)}{1+\lambda} \quad (\text{A.16})$$

939 For the non-learners, the rank of their cutoffs is

$$\frac{\bar{z}_{non}^L(a)}{1-\lambda} > \bar{z}_{non}^M(a) > \frac{\bar{z}_{non}^H(a)}{1+\lambda} > \frac{\bar{z}_{non}^M(a)}{1+\lambda} \quad (\text{A.17})$$

$$\bar{z}_{non}^M(a) > \bar{z}_{non}^L(a) \quad (\text{A.18})$$

940 **B Proof of Proposition**

941 *B.1 Proof of Proposition 2*

942 The derivative of saving with respect to t is

$$\frac{\partial a'^\star}{\partial t}(x, a; t) = -\frac{x\mu}{1+\beta} + \frac{x^2\Sigma}{\beta} \frac{t[2(x+a) + tx\mu]}{[(x+a) + tx\mu]^2}. \quad (\text{B.1})$$

943 The total effect of on-job-training on saving is

$$\Delta_{\text{on-job}}(x, a; t) = a'^\star(x, a; t) - a'^\star(x, a; 1) = \int_1^t \frac{\partial a'^\star}{\partial u}(x, a; u) du. \quad (\text{B.2})$$

944 Define

$$F(x, a; u) \equiv x \frac{u[2(x+a) + ux\mu]}{[(x+a) + ux\mu]^2}, \quad \bar{F}(x, a; t) \equiv \frac{1}{t-1} \int_1^t F(x, a; u) du.$$

945 Then equation (B.2) can be written as

$$\Delta_{\text{on-job}}(x, a; t) = x(t-1) \left[\frac{\Sigma}{\beta} \bar{F}(x, a; t) - \frac{\mu}{1+\beta} \right].$$

946 Differentiating $F(x, a; u)$ with respect to x gives

$$\frac{\partial F(x, a; u)}{\partial x} = \frac{2u a (a+x)}{(a+(1+u\mu)x)^3} > 0,$$

947 so $\bar{F}(x, a; t)$ is strictly increasing in x .

948 The sign of $\Delta_{\text{on-job}}(x, a; t)$ is governed by

$$S(x, a; t) \equiv \frac{\Sigma}{\beta} \bar{F}(x, a; t) - \frac{\mu}{1 + \beta}.$$

949 Because $\bar{F}(x, a; t)$ is strictly increasing, $S(x, a; t)$ increases monotonically with x .

950 For $x \rightarrow 0$, $F(x, a; u) \rightarrow 0$ and $\bar{F}(x, a; t) \rightarrow 0$ so that $S(x, a; t) \rightarrow -\frac{\mu}{1+\beta} < 0$,
951 implying $\Delta_{\text{on-job}}(x, a; t) < 0$ for small x .

952 For $x \rightarrow \infty$, $F(x, a; u) \rightarrow \frac{u(2+u\mu)}{(1+u\mu)^2}$ and $\bar{F}(x, a; t) \rightarrow \bar{F}_\infty(t) \equiv \frac{1}{t-1} \int_1^t \frac{u(2+u\mu)}{(1+u\mu)^2} du$. If

$$\frac{\Sigma}{\mu} > \underline{\sigma}(t) \equiv \frac{\beta}{1 + \beta} \frac{1}{\bar{F}_\infty(t)} \quad (\text{B.3})$$

953 then $S(x, a; t) > 0$ for sufficiently large x , and hence $\Delta_{\text{on-job}}(x, a; t) > 0$.

954 If idiosyncratic risk is large enough, i.e., condition (B.3) is satisfied, there exists
955 a unique threshold $x^*(t)$ at which the sign flips:

$$\Delta_{\text{on-job}}(x, a; t) < 0 \text{ for } x < x^*(a, t), \quad \Delta_{\text{on-job}}(x, a; t) > 0 \text{ for } x > x^*(a, t).$$

956 B.2 Proof of Proposition 3

957 Denote

$$G(x, a; t) \equiv \frac{t^2 x^2}{(a + x + tx\mu)(a + tx\mu)}$$

958 the net additional effect of full-time training on saving can be rewritten as

$$\Delta_H(x, a; t) \equiv x \left[-\frac{\beta}{1 + \beta} + \frac{\Sigma}{\beta} G(x, a; t) \right]$$

959 Differentiating $G(x, a; t)$ with respect to x gives

$$\frac{\partial G(x, a; t)}{\partial x} = \frac{t^2 x a (2tx\mu + 2a + x)}{(a + tx\mu)^2 (a + x + tx\mu)^2} > 0,$$

960 so $G(x, a; t)$ is strictly increasing in x .

961 The limits of $G(x, a; t)$ are:

$$G(x, a; t) \rightarrow 0 \quad (x \rightarrow 0),$$

962

$$G(x, a; t) \rightarrow G_\infty(t) \equiv \frac{t}{\mu(1 + t\mu)} \quad (x \rightarrow \infty),$$

963 Therefore, $G(x, a; t) < G_\infty(t)$ for any x .

964 If

$$\frac{\Sigma}{\beta} G_\infty(t) < \frac{\beta}{1 + \beta}, \text{ i.e. } \frac{\Sigma}{\mu} < \bar{\sigma}(t) \equiv \frac{\beta^2}{1 + \beta} \left(\frac{1}{t} + \mu \right). \quad (\text{B.4})$$

965 Then $\Delta_H(x, a; t) < x[-\frac{\beta}{1+\beta} + \frac{\Sigma}{\beta}G_\infty(t)] < 0$ for any x .

966 Furthermore, with some tedious algebra, we can show that for any x

$$G(x, a; t) + x \frac{\partial G(x, a; t)}{\partial x} < G_\infty(t)$$

967 Hence, the inequality (B.4) also implies that

$$\frac{\partial \Delta_H(x, a; t)}{\partial x} = \frac{\Sigma}{\beta}[G(x, a; t) + x \frac{\partial G(x, a; t)}{\partial x}] - \frac{\beta}{1+\beta} < \frac{\Sigma}{\beta}G_\infty(t) - \frac{\beta}{1+\beta} < 0. \quad (\text{B.5})$$

968 B.3 Proof of Proposition 4

969 The relevant upper bounds of z for positive human capital investment are functions
970 of γ (to the first order approximation):

$$\begin{aligned}\bar{z}_{slow}^L(a; \gamma) &= \bar{z}_{slow}^L(a; \gamma = 0) - \gamma \lambda \frac{w' z'}{w(1+r')} \\ \bar{z}_{fast}^L(a; \gamma) &= \bar{z}_{fast}^L(a; \gamma = 0) - \gamma \lambda \frac{w' z'}{w(1+r')} \frac{\exp(\frac{\chi_e e_L}{1+\beta})}{\exp(\frac{\chi_e e_L}{1+\beta}) - 1} \\ \bar{z}_{slow}^M(a; \gamma) &= \bar{z}_{slow}^M(a; \gamma = 0) + \gamma \lambda \frac{w' z'}{w(1+r')} \exp(\frac{\chi_n - \chi_e e_H}{1+\beta}) \\ \bar{z}_{fast}^M(a; \gamma) &= \bar{z}_{fast}^M(a; \gamma = 0) + \gamma \lambda \frac{w' z'}{w(1+r')} \frac{1}{\exp(\frac{\chi_e e_L}{1+\beta}) - 1}\end{aligned}$$

971 Therefore, an anticipated AI shock, $\gamma > 0$ makes those with $h < h_M \frac{1}{1-\delta}$ invest less
972 human capital and those with $h > h_M \frac{1}{1-\delta}$ invest more human capital.

973 B.4 Proof of Proposition 5

$$\Delta_{\text{on-job}}(x, a; t) = a'^*(x, a; t) - a'^*(x, a; 1) = \int_1^t \frac{\partial a'^*}{\partial u}(x, a; u) du.$$

974 differentiating with respect to t gives

$$\frac{d\Delta_{\text{on-job}}(x, a; t)}{dt} = \frac{\partial a'^*}{\partial t}(x, a; t)$$

975 Since

$$\frac{\partial^2 a'^*(x, a; t)}{\partial t^2} = \frac{\partial}{\partial t} \left(-\frac{x\mu}{1+\beta} + \frac{x^2\Sigma}{\beta} \frac{t[2(x+a) + tx\mu]}{[(x+a) + tx\mu]^2} \right) = \frac{2x^2\Sigma(a+x)^2}{\beta(a+x+tx\mu)^3} > 0. \quad (\text{B.6})$$

976 The slope $\frac{\partial a'^*}{\partial t}(x, a; t)$ is strictly increasing in t . Hence $\Delta_{\text{on-job}}(x, a; t)$ is convex in t .

$$\Delta_H(x, a; t) = x \left[-\frac{\beta}{1+\beta} + \frac{\Sigma}{\beta}G(x, a; t) \right] \text{ with } G(x, a; t) = \frac{t^2 x^2}{(a+x+tx\mu)(a+tx\mu)}$$

⁹⁷⁷ Differentiating $G(x, a; t)$ with respect to t gives

$$\frac{\partial G(x, a; t)}{\partial t} = \frac{tx^2(2a^2 + 2atx\mu + 2ax + \mu tx^2)}{(a + tx\mu)^2(a + x + tx\mu)^2} > 0,$$

⁹⁷⁸ so $G(x, a; t)$ is strictly increasing in t , and so is $\Delta_H(x, a; t)$.

⁹⁷⁹ We now consider the comparison between $\Delta_{\text{on-job}}(x, a; t)$ and $\Delta_{\text{on-job}}(x, a; t')$ for $t' >$
⁹⁸⁰ t . Given x and a , define

$$f(t) \equiv \frac{\partial a'^*}{\partial t}(x, a; t).$$

⁹⁸¹ so $f'(t) > 0$, i.e. $f(t)$ is strictly increasing in t .

⁹⁸² **Case 1:** $1 < t < t'$

⁹⁸³ Suppose $\Delta_{\text{on-job}}(x, a; t) > 0$. Then

$$\Delta_{\text{on-job}}(x, a; t) = \int_1^t f(u) du > 0.$$

⁹⁸⁴ Since f is increasing,

$$f(u) \leq f(t) \quad \text{for all } u \in [1, t],$$

⁹⁸⁵ which implies

$$\Delta_{\text{on-job}}(x, a; t) = \int_1^t f(u) du \leq (t - 1) f(t).$$

⁹⁸⁶ Because $t > 1$, the inequality $\Delta_{\text{on-job}}(x, a; t) > 0$ forces $f(t) > 0$.

⁹⁸⁷ Now for any $t' > t$,

$$f(u) \geq f(t) > 0 \quad \text{for all } u \in [t, t'],$$

⁹⁸⁸ and therefore

$$\Delta_{\text{on-job}}(x, a; t') - \Delta_{\text{on-job}}(x, a; t) = \int_t^{t'} f(u) du > 0.$$

⁹⁸⁹ We then have that:

$$1 < t < t', \Delta_{\text{on-job}}(x, a; t) > 0 \implies \Delta_{\text{on-job}}(x, a; t') > \Delta_{\text{on-job}}(x, a; t) \quad (\text{B.7})$$

⁹⁹⁰ That is, once $\Delta_{\text{on-job}}(x, a; t)$ becomes positive for $t > 1$, it is strictly increasing in t
⁹⁹¹ thereafter.

⁹⁹² **Case 2:** $t < t' < 1$

⁹⁹³ For $t < 1$,

$$\Delta_{\text{on-job}}(x, a; t) = \int_1^t f(u) du = - \int_t^1 f(u) du.$$

994 Suppose $\Delta_{\text{on-job}}(x, a; t) > 0$. Then

$$-\int_t^1 f(u) du > 0 \implies \int_t^1 f(u) du < 0.$$

995 Since f is increasing

$$f(u) \geq f(t) \quad \text{for all } u \in [t, 1],$$

996 which implies

$$\int_t^1 f(u) du \geq (1-t) f(t).$$

997 Because $t < 1$, the inequality $\Delta_{\text{on-job}}(x, a; t) > 0$ forces $f(t) < 0$.

998 Consider

$$\Delta_{\text{on-job}}(x, a; t') - \Delta_{\text{on-job}}(x, a; t) = \int_t^{t'} f(u) du$$

999 If $f(u) < 0$ for all $u \in [t, t']$, then $\int_t^{t'} f(u) du < 0$.

1000 If there exists some $t_s \in [t, t']$ such that $f(t_s) = 0$, so $f(u) < 0$ for $u < t_s$ and
1001 $f(u) > 0$ for $u > t_s$. Then $f(u) > 0$ for $u \in [t', 1]$. Hence,

$$\int_{t'}^1 f(u) du > 0$$

1002 This implies that

$$\Delta_{\text{on-job}}(x, a; t') = - \int_{t'}^1 f(u) du < 0$$

1003 Together with the inequality $\Delta_{\text{on-job}}(x, a; t) > 0$, we have that

$$\Delta_{\text{on-job}}(x, a; t') < \Delta_{\text{on-job}}(x, a; t)$$

1004 We then have that

$$t < t' < 1, \Delta_{\text{on-job}}(x, a; t) > 0 \implies \Delta_{\text{on-job}}(x, a; t') < \Delta_{\text{on-job}}(x, a; t). \quad (\text{B.8})$$

1005 Thus, for $t < 1$, whenever $\Delta_{\text{on-job}}(x, a; t) > 0$, increasing t toward 0 makes $\Delta_{\text{on-job}}$
1006 strictly decrease.

1007 C Computational Procedure for the Quantitative Model

1008 C.1 Steady-state Equilibrium

1009 In the steady-state, the measure of households, $\mu(a, h, x)$, and the factor prices are
1010 time-invariant. We find a time-invariant distribution μ . We compute the house-
1011 holds' value functions and the decisions rules, and the time-invariant measure of the
1012 households. We take the following steps:

1013 1. We choose the number of grid for the risk-free asset, a , human capital, h , and

1014 the idiosyncratic labor productivity, x . We set $N_a = 151$, $N_h = 151$, and
 1015 $N_x = 9$ where N denotes the number of grid for each variable. To better
 1016 incorporate the saving decisions of households near the borrowing constraint,
 1017 we assign more points to the lower range of the asset and human capital.

- 1018 2. Productivity x is equally distributed on the range $[-3\sigma_x/\sqrt{1-\rho_x^2}]$. As shown
 1019 in the paper, we construct the transition probability matrix $\pi(x'|x)$ of the
 1020 idiosyncratic labor productivity.
- 1021 3. Given the values of parameters, we find the value functions for each state
 1022 (a, h, x) . We also obtain the decision rules: savings $a'(a, h, x)$, and $h'(a, h, x)$.
 1023 The computation steps are as follow:
- 1024 4. After obtaining the value functions and the decision rules, we compute the
 1025 time-invariant distribution $\mu(a, h, x)$.
- 1026 5. If the variables of interest are close to the targeted values, we have found the
 1027 steady-state. If not, we choose the new parameters and redo the above steps.

1028 C.2 Transition Dynamics

1029 We incorporate the transition path from the status quo to the new steady state. We
 1030 describe the steps below.

- 1031 1. We obtain the initial steady state and the new steady state.
- 1032 2. We assume that the economy arrives at the new steady state at time T . We
 1033 set the T to 100. The unit of time is a year.
- 1034 3. We initialize the capital-labor ratio $\{K_t/L_t\}_{t=2}^{T-1}$ and obtain the associated
 1035 factor prices $\{r_t, w_t\}_{t=2}^{T-1}$.
- 1036 4. As we know the value functions at time T , we can obtain the value functions
 1037 and the decision rules in the transition path from $t = T - 1$ to 1.
- 1038 5. We compute the measures $\{\mu_t\}_{t=2}^T$ with the measures at the initial steady state
 1039 and the decision rules in the transition path.
- 1040 6. We obtain the aggregate variables in the transition path with the decision rules
 1041 and the distribution measures.
- 1042 7. We compare the assumed paths of capital and the effective labor with the
 1043 updated ones. If the absolute difference between them in each period is close
 1044 enough, we obtain the converged transition path. Otherwise, we assume new
 1045 capital-labor ratio and go back to 3.

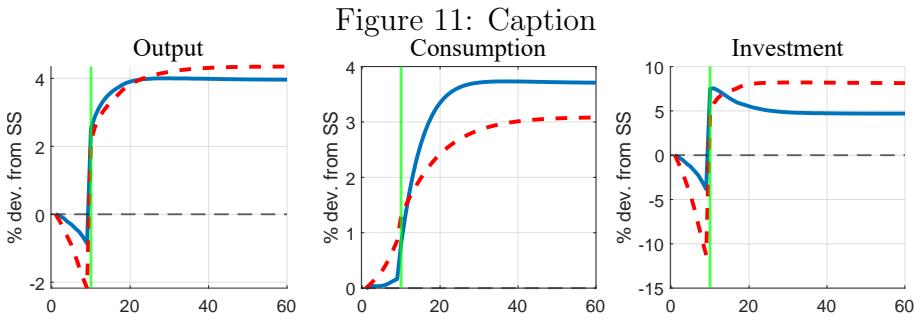


Figure 11: Caption
Consumption

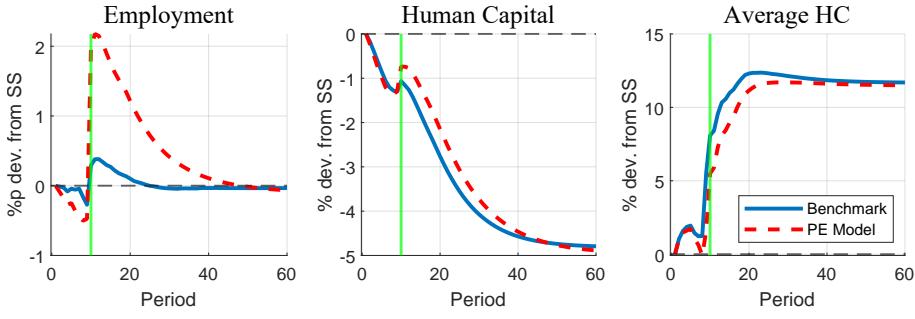


Figure 11: Caption

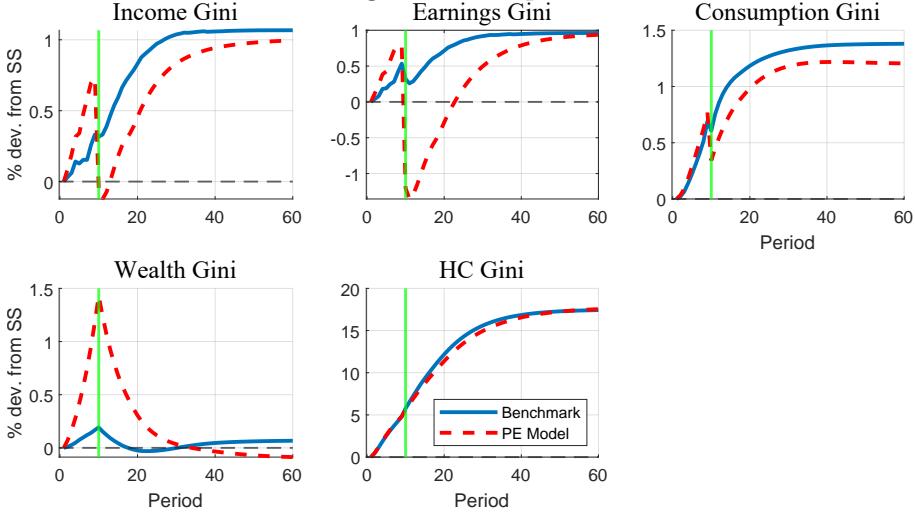
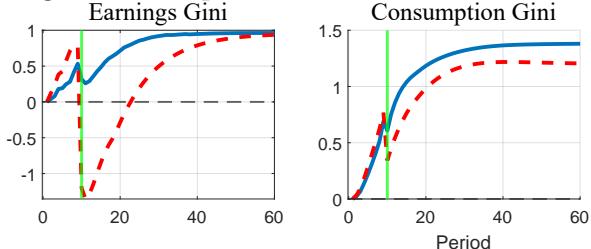


Figure 12: Caption



1046 D Investigating the GE channel of AI's impact

1047 **Redistribution versus general equilibrium effects:** The effects of human cap-
1048 ital adjustments on AI's aggregate impacts operate through two primary channels:
1049 the *redistribution channel*, which reallocates households across skill sectors, and the
1050 *general equilibrium (GE) channel*, which operates through changes in wages and
1051 capital returns. We now assess the relative importance of these channels in shaping
1052 economic outcomes.

1053 Figure ?? compares the transition dynamics between scenarios with and without
1054 human capital adjustments, while holding wages and capital returns fixed at their
1055 initial steady-state levels to eliminate GE effects. We refer to the former as the
1056 "PE Model" and the latter as the "No-HC PE Model." The difference between the
1057 solid blue line and the dashed red line isolates the effect of redistribution channel.

1058 Comparing this difference to the gap between the benchmark model and the No
1059 HC model in Figure 7 enables us to evaluate the importance of the redistribution
1060 channel relative to the GE channel. Two key observations emerge.

1061 First, the *redistribution channel* alone accounts for all the *qualitative effects* of
1062 human capital adjustments on AI's aggregate impacts. Redistribution of human
1063 capital increases consumption, even before AI implementation, as more households
1064 shift to the high sector. It also reduces investment by mitigating precautionary
1065 savings and lowers employment as middle-sector workers leave the labor market
1066 to invest in human capital. In the long run, redistribution amplifies AI's positive
1067 impact on output by reallocating more workers to sectors that benefit most from AI
1068 advancements.

1069 Second, the *GE channel* primarily affects the *quantitative magnitude* of human
1070 capital adjustments' impact on AI's aggregate outcomes. When the GE channel is
1071 included, the differences in output, consumption, and employment between models
1072 with and without human capital adjustments are smaller compared to when the
1073 GE channel is excluded. In contrast, and somewhat unexpectedly, the difference in
1074 investment is larger when the GE channel is included. This indicates that allowing
1075 capital returns to adjust amplifies the impact of human capital accumulation on
1076 how household savings respond to AI.

1077 When the *GE channel* is active (Figure ??), AI reduces the wealth Gini, but
1078 the *redistribution channel* moderates this effect. However, when the *GE channel*
1079 is disabled (Figure ??), AI increases wealth inequality in the long run without the
1080 *redistribution channel* from human capital adjustment. In contrast, with the *redis-
1081 tribution channel* active, AI reduces wealth inequality.

1082 These observations lead to two key conclusions:

1083 First, the *redistribution channel* alone introduces a qualitative shift in AI's long-
1084 run impact on the wealth Gini (as shown in Figure ??).

1085 Second, the *GE channel*, when combined with human capital adjustment, qual-
1086 itatively alters the effect of anticipating AI on the wealth Gini (as shown by com-
1087 paring the blue lines in Figures ?? and ??).

1088 **Policy implications:** The impact of human capital adjustments on AI's distribu-
1089 tional outcomes, along with the roles of the *redistribution channel* and *GE channel*,
1090 provides valuable insights for policy discussions on how to address the challenges
1091 posed by AI shocks.

1092 In particular, government interventions aimed at stabilizing wages in response
1093 to AI-induced economic shocks may unintentionally worsen wealth inequality. Our
1094 analysis indicates that if wages are prevented from adjusting to reflect productiv-
1095 ity differences, this distorts households' incentives to adjust their human capital
1096 and precautionary savings—both of which play a critical role in mitigating wealth
1097 inequality.