0

Type something...

01) Training Neural Networks 1

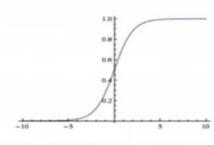
- 01_Activation Functions
- 4. Cinnald fundame
 - 2. tanh(x)
 - 3. ReLU = max(0, x)
 - 4. Leaky ReLU = max(0.01x, x)
 - 5. Exponential Linear Units(ELU)
 - 6. Maxout Neuron
- 02_Data Preprocess
- 03_Weight Initialization
 - 1. Xavier Initalization
- 2. He Initialization
- 04_Batch Normalization
- 05_Babysitting the learning process
- 06_Hyperparameter Optimization

01) Training Neural Networks

01_Activation Functions

1. Sigmoid functions

Activation Functions



Sigmoid

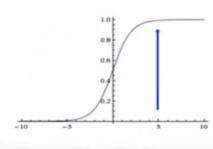
- $\sigma(x)=1/(1+e^{-x})$
- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems:

 Saturated neurons "kill" the gradients

- Sigmoid function은 지금은 잘 사용되지 않는 함수이다.
- 1. 그 이유는 gradient vanish 문제가 있기 때문이다.
- x값이 꽤 크거나 꽤 작으면 local gradient가 0에 가깝게 된다.

Activation Functions



Sigmoid

$$\sigma(x) = 1/(1+e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems:

- Saturated neurons "kill" the gradients
- 2 Sigmoid outputs are not zero

centered

- 2. 두번째 문제는 output이 0이 중심이지 않아 수렴하는데 오래 걸린다.
- 만약 x가 양수라면 w에 대한 gradient가 모두 al./df 의 부호가 같아지기 때문에 모두 양수이거나 모두 음수이다.

Consider what happens when the input to a neuron is always positive...

$$f\left(\sum_i w_i x_i + b
ight)$$

allowed gradient update directions

zig zag path gradient update directions hypothetical

optimal w vector

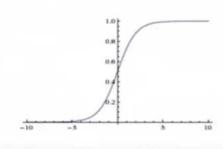
What can we say about the gradients on w?

Always all positive or all negative :(

(this is also why you want zero-mean data!)

zero-centered가 아니기 때문에 부호가 하나로 정해져서 수렴 속도가 느려지게 된다.

Activation Functions



Sigmoid

- $\sigma(x) = 1/(1 + e^{-x})$
- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

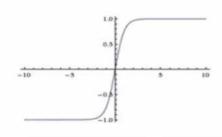
3 problems:

- Saturated neurons "kill" the gradients
- Sigmoid outputs are not zerocentered
- 3. exp() is a bit compute expensive

3. 마지막 문제는 exp() 연산이 매우 비싼 연산이라는 점이다.

2. tanh(x)

Activation Functions



- Squashes numbers to range [-1,1]
- zero centered (nice)
- still kills gradients when saturated :(

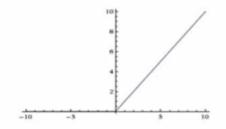
tanh(x)

[LeCun et al., 1991]

sigmoid의 문제점을 해결하기 위해 zero-centered된 함수를 만들었다.

3. ReLU = max(0, x)

Activation Functions

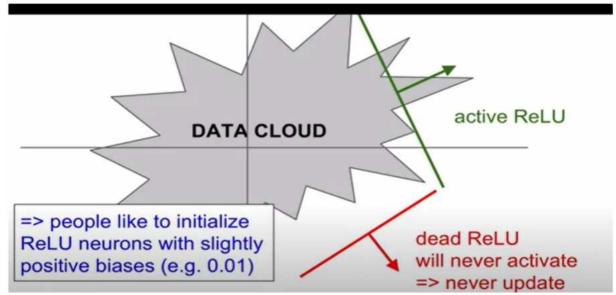


- Computes f(x) = max(0,x)
- Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)

ReLU (Rectified Linear Unit)

[Krizhevsky et al., 2012]

- 연산이 매우 효율적이고 수렴 속도가 빠르다.
- 현재 기본적인 activation function으로 사용되고 있다.



- 음수인 부분은 gradient가 0이기 때문에 update가 되지 않는 문제를 가지고 있다.
- learning_rate가 너무 큰 경우에도 발생한다.
- 그래서 사람들이 약간 작은 양수로 초기화 하는 것을 좋아한다.

4. Leaky ReLU = max(0.01x, x)

Activation Functions [Mass et al., 2013] [He et al., 2015] Does not saturate Computationally efficient Converges much faster than sigmoid/tanh in practice! (e.g. 6x) will not "die".

 $f(x) = \max(0.01x, x)$

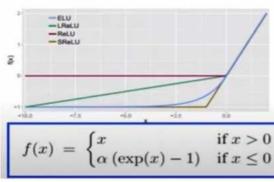
- 기울기가 죽지도 않는 좋은 함수로 보인다.
- 하지만 무조건 ReLU보다 낫다고는 말할 수 없다.

5. Exponential Linear Units(ELU)

Activation Functions

[Clevert et al., 2015]

Exponential Linear Units (ELU)



- All benefits of ReLU
- Does not die
- Closer to zero mean outputs
- Computation requires exp()
- ReLU의 장점을 가지면서 zero mean을 가지지만 exp 연산이 비싸다는 단점이 있다
- 6. Maxout Neuron

Maxout "Neuron"

[Goodfellow et al., 2013]

- Does not have the basic form of dot product -> nonlinearity
- Generalizes ReLU and Leaky ReLU
- Linear Regime! Does not saturate! Does not die!

$$\max(w_1^Tx+b_1,w_2^Tx+b_2)$$

Problem: doubles the number of parameters/neuron :(

• ReLu와 Leaky ReLu를 일반화한 함수라고 볼 수 있지만 parameter와 neuron이 2배로 든다는 단점이 있다.

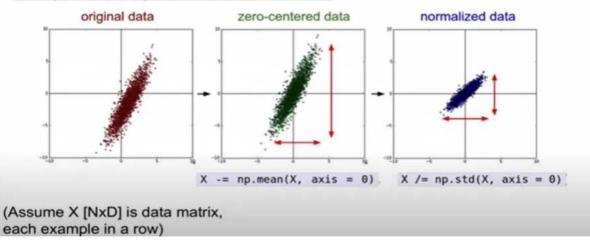
TLDR: In practice:

- Use ReLU. Be careful with your learning rates
- Try out Leaky ReLU / Maxout / ELU
- Try out tanh but don't expect much
- Don't use sigmoid

- 따라서 일반적으로는 ReLU를 사용하지만 Leaky ReLU/Maxout/ELU를 시도해 볼 수 있다.
- 하지만 sigmoid는 사용하지 마라.

02_Data Preprocess

Step 1: Preprocess the data



- · zero-centered + normalized
- 이미지에서는 값이 [0~255] 사이의 값을 가지기 때문에 굳이 normalized를 하지 않는다.

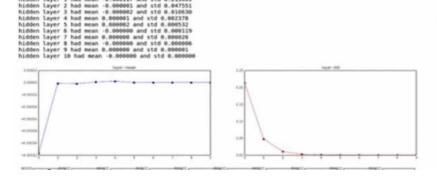
TLDR: In practice for Images: center only

e.g. consider CIFAR-10 example with [32,32,3] images

- Subtract the mean image (e.g. AlexNet) (mean image = [32,32,3] array)
- Subtract per-channel mean (e.g. VGGNet) (mean along each channel = 3 numbers)

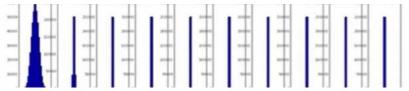
Not common to normalize variance, to do PCA or whitening

03_Weight Initialization



All activations become zero!

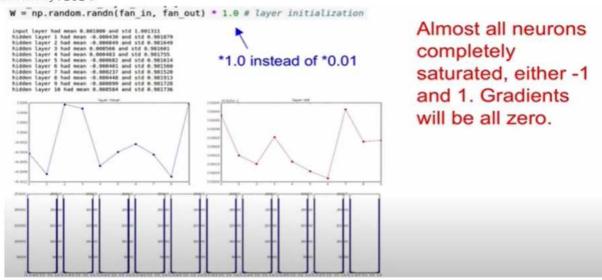
Q: think about the backward pass. What do the gradients look like?



dWI = X * dW2

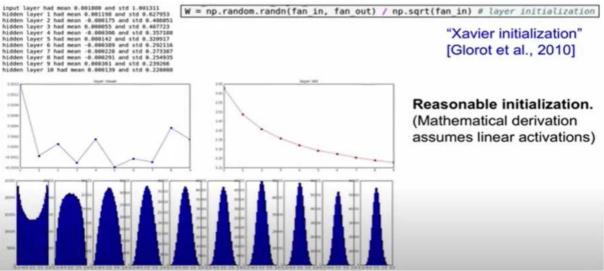
Hint: think about backward pass for a W*X gate.

- 랜덤으로 값을 초기화 한 후 학습을 시켜보니 activation이 0으로 가는 문제가 발생한다.
- 그 결과 gradient vanishing이 발생한다.

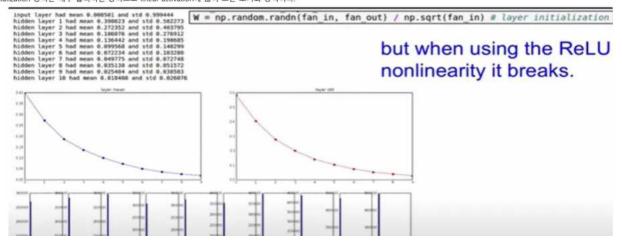


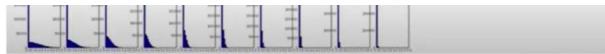
• 1로 초기화 하게 되면 값이 튀어서 -1 또는 1로 포화된다.

1. Xavier Initalization



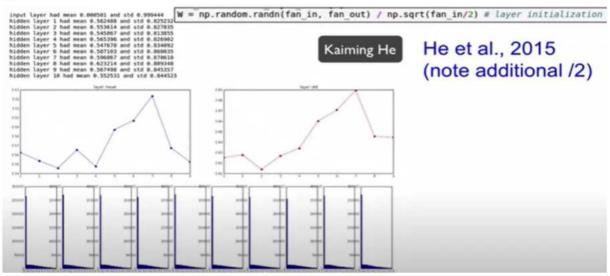
Xavier initialization 방식은 매우 합리적인 방식으로 linear activation에 많이 쓰는 초기화 방식이다.





• 하지만 ReLU같은 nonlinearity 함수에는 잘 적용되지 못했다.

2. He Initialization



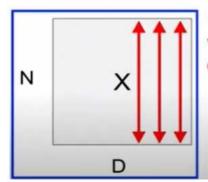
• ReLU에는 He initialization을 적용하면 잘 동작하는 것을 확인할 수 있다.

04_Batch Normalization

Batch Normalization

[loffe and Szegedy, 2015]

"you want unit gaussian activations? just make them so."



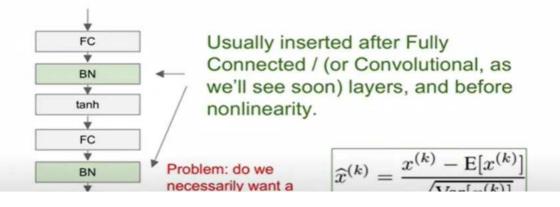
 compute the empirical mean and variance independently for each dimension.

2. Normalize

$$\widehat{x}^{(k)} = \frac{x^{(k)} - E[x^{(k)}]}{\sqrt{\text{Var}[x^{(k)}]}}$$

Batch Normalization

[loffe and Szegedy, 2015]



FC - BN - activation 순서로 적용한다.

Batch Normalization

Input: Values of x over a mini-batch: $\mathcal{B} = \{x_{1...m}\}$;
Parameters to be learned: γ , β Output: $\{y_i = \mathrm{BN}_{\gamma,\beta}(x_i)\}$ $\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^m x_i \qquad // \text{mini-batch mean}$ $\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2 \qquad // \text{mini-batch variance}$ $\widehat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}} \qquad // \text{normalize}$ $y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv \mathrm{BN}_{\gamma,\beta}(x_i) \qquad // \text{scale and shift}$

[loffe and Szegedy, 2015]

- Improves gradient flow through the network
- Allows higher learning rates
- Reduces the strong dependent on initialization
- Acts as a form of regularization in a funny way, and slightly reduces the need for dropout, maybe

• 자세한 과정은 과제를 참고하도록 하자.

Batch Normalization

Input: Values of x over a mini-batch: $\mathcal{B} = \{x_{1...m}\}$; Parameters to be learned: γ , β Output: $\{y_i = \mathrm{BN}_{\gamma,\beta}(x_i)\}$ $\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^m x_i \qquad // \text{mini-batch mean}$ $\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2 \qquad // \text{mini-batch variance}$ $\widehat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}} \qquad // \text{normalize}$ $y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv \mathrm{BN}_{\gamma,\beta}(x_i) \qquad // \text{scale and shift}$

[loffe and Szegedy, 2015]

Note: at test time BatchNorm layer functions differently:

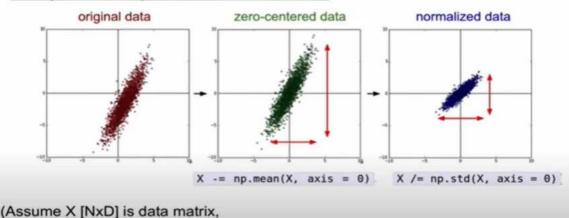
The mean/std are not computed based on the batch. Instead, a single fixed empirical mean of activations during training is used.

(e.g. can be estimated during training with running averages)

each example in a row)

05_Babysitting the learning process

Step 1: Preprocess the data

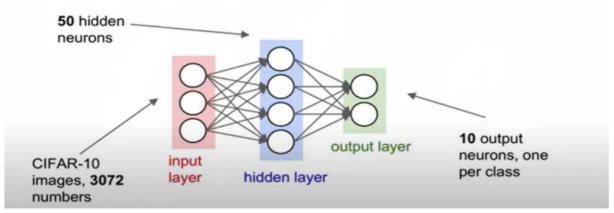


1. zero centered

[•] test를 할 때는 미리 mean과 variance를 저장해둔 것을 활용한다.

Step 2: Choose the architecture:

say we start with one hidden layer of 50 neurons:



2. Choose the architecture

Lets try to train now...

Tip: Make sure that you can overfit very small portion of the training data

Very small loss, train accuracy 1.00, nice!

- 작은 데이터를 취한 후에 학습을 시키면 무조건 overfitting이 나와야 한다.
- 이것이 모델이 잘 동작한다는 의미이다.

Lets try to train now...

I like to start with small regularization and find learning rate that makes the loss go down.

loss not going down: learning rate too low

Loss barely changing: Learning rate is probably too low

• Learning_rate가 너무 작으면 loss가 줄어들지 않는다.

Lets try to train now...

I like to start with small

makes the loss go down.

```
regularization and find 
| home/karpathy/cs231n/code/cs231n/classifiers/neural_net.py:50: RuntimeMarning: divide by zero en countered in log data loss = -np. sum(np. log(probs[range(N), y])) / N | home/karpathy/cs231n/code/cs231n/classifiers/neural_net.py:48: RuntimeMarning: invalid value encountered in subtract probs = np.exp(scores - np.max(scores, axis=1, keepdims=True))
                                                                                                                                                 Finished epoch 1 / 10: cost nan, train: 0.091000, val 0.087000, lr 1.000000e+06 Finished epoch 2 / 10: cost nan, train: 0.095000, val 0.087000, lr 1.000000e+06 Finished epoch 3 / 10: cost nan, train: 0.100000, val 0.087000, lr 1.000000e+06
```

loss not going down: learning rate too low loss exploding: learning rate too high

cost: NaN almost always means high learning rate...

• Learning_rate가 너무 크면 loss가 exploding 해버린다

06_Hyperparameter Optimization

Cross-validation strategy

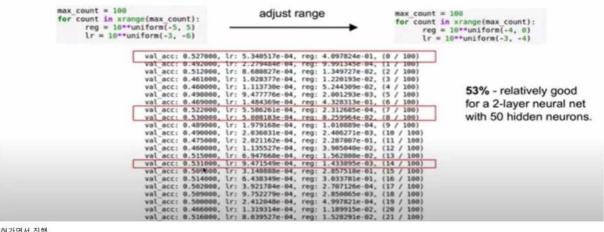
I like to do coarse -> fine cross-validation in stages

First stage: only a few epochs to get rough idea of what params work Second stage: longer running time, finer search ... (repeat as necessary)

Tip for detecting explosions in the solver: If the cost is ever > 3 * original cost, break out early

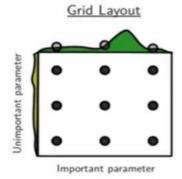
epoch을 작게 한 후 나중에 세부적으로 조정한다.

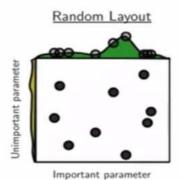
Now run finer search...



- 값을 점점 좁혀가면서 진행.
- boundary에 가까운 값이 최적이라면 범위를 다시 넓혀서 진행.

Random Search vs. Grid Search

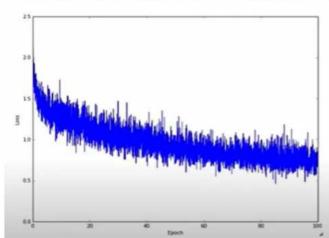


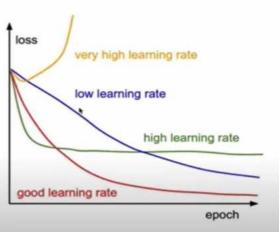


Random Search for Hyper-Parameter Optimization Bergstra and Bengio, 2012

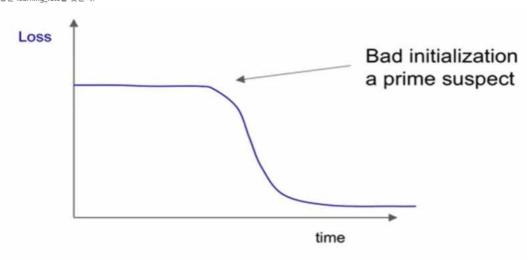
- grid 등간격으로 진행하면 우리가 찾고 싶은 최적의 parameter를 찾지 못할 수도 있다.
- 결국 최적화를 하기 위해서는 random하게 접근해야 한다.

Monitor and visualize the loss curve





• Loss curve를 통해서 좋은 learning_rate를 찾는다.



• Loss가 정체되는 것은 initialization이 잘못된 것을 의미한다.