微積 I 試験予想問題 解説

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(1)

$$\lim_{x \to 0} \frac{\sin 3x}{\sin 7x} = \frac{3}{7}$$

(2)

$$\lim_{x \to \frac{\pi}{2}} \frac{\cos x}{x - \frac{\pi}{2}}$$

 $t=x-rac{\pi}{2}$ とおくと , t o 0 だから ,

$$= \lim_{t \to 0} \frac{\cos(t + \frac{\pi}{2})}{t} = \lim_{t \to 0} \frac{-\sin t}{t}$$
$$= -1$$

(3)

$$\lim_{x \to 0} \frac{\sin(\sin^2 x)}{x^2} = \lim_{x \to 0} \left(\frac{\sin(\sin^2 x)}{\sin^2 x} \cdot \frac{\sin^2 x}{x^2} \right)$$
$$= 1$$

(4)

$$\lim_{x \to 0} \frac{2x \tan(3x^2)}{\sin(2x^3)} = \lim_{x \to 0} \left(\frac{2x}{\sin(2x^3)} \cdot \frac{\tan(3x^2)}{x^2} \cdot 3x^2 \right)$$
$$= \lim_{x \to 0} \left(\frac{6x^3}{\sin(2x^3)} \cdot \frac{\sin(3x^2)}{3x^2} \cdot \frac{1}{\cos(3x^2)} \right) = 3$$