

[Tutorial 2.2]

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Question 1: voltage gated channel

```
%setting up the parameters
EL = -70; %leaky = -70mV
Rm = 5; % resistance = 5ohms
Cm = 2; % membrane capacitance = 5nF
Vth = -50; % threshold -50mV
Vreset = -65; % reset voltage -65mV
Vpeak = 50; %voltage peak = -50mV

%setting up time
dt = 0.0001; %0.1ms step size
tvec = 0:dt:2; % setting up the tvector 2seconds
tau_ref = 25; % tau reference 2.5*1ms= 2.5ms

%setting up voltage vector
vvec1 = zeros(size(tvec)); %voltage size same as tvec
vvec1(1) = EL; %initialize first element as leaky
```

setting up Euler's method

```
for range = 100:100:600 %setting up applied current constants
    pos = 1; %pos of iapp vec
    countvec1 = zeros(6);% define the spike vector
    iapp1 = zeros(6); %current vector
    vvec1avg = zeros(6);% the vm average vector
```

```

        vvec1avg(pos) = 0; % initialize = 0
        iapp1(pos) = range; % first element as the first applied current range
        refrac = 1 + tau_ref;
        countvec1(pos) = 0; % spike array counts
        vvec1add = 0; % define an sum vector for membrane potential
    for i = 2:length(tvec)
        if (refrac > tau_ref) %if time > refractory period, start firing
            %dVm/dt = ((E1 - Vm) /Rm + Iapp)/Cm.
            dVm_over_dt = ((EL-vvec1(i-1)) / Rm + iapp1(pos))/Cm;
            % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
            vvec1(i) = vvec1(i-1) + dVm_over_dt * dt;
        else %or it's just gonna stay at reset, while time increases
            refrac = refrac+1;
            vvec1(i) = Vreset;
        end
        if (vvec1(i) > Vth)% if vvec element is higher than V threshold
            vvec1(i-1) = Vpeak; %force the element to peak;
            vvec1(i) = Vreset;
            countvec1(pos)= countvec1(pos)+1; %spike count +1
            refrac = 0; % resset refractory period.
        end
        vvec1add = vvec1(i-1)+vvec1(i);
    end
    vvec1avg(pos) = vvec1add / length(tvec); % get the average
    pos = pos + 1;
    vvec1add = 0; % reset the sum to 0 to start another 'for' loop.
end

```

setting up Euler's method (membrane potential)

```

for range = 220:380:600 %setting up applied current constants
    pos = 1; %pos of iapp vec
    iapp = zeros(2); %current vector
    iapp(pos) = range; % first element as the first applied current range
    refrac = 1 + tau_ref; %refractory time initialization

    for i = 2:length(tvec)
        if (refrac > tau_ref) % if time achieves tau, start firing
            %dVm/dt = ((E1 - Vm) /Rm + Iapp)/Cm.
            dVm_over_dt = ((EL-vvec1(i-1)) / Rm + iapp(pos))/Cm;
            % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
            vvec1(i) = vvec1(i-1) + dVm_over_dt * dt;
        else%or it's just gonna stay at reset, while time increases
            refrac = refrac+1;
            vvec1(i) = Vreset;
        end
        if (vvec1(i) > Vth)% if vvec element is higher than V threshold
            vvec1(i-1) = Vpeak; %force the element to peak;
            vvec1(i) = Vreset;
            refrac = 0; %reset the refractory period
        end
    end
    pos = pos + 1; % move on to the next position array

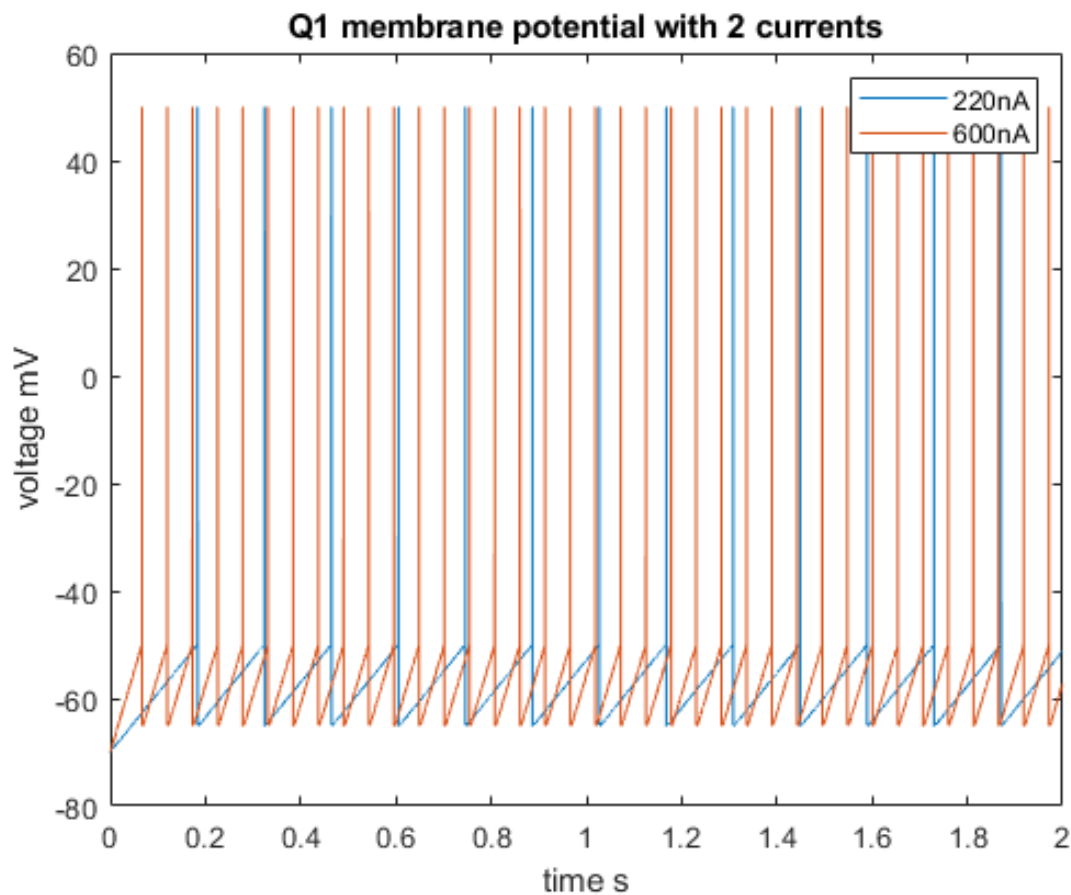
figure(1)

```

```

plot(tvec,vvec1)
hold on
title('Q1 membrane potential with 2 currents')
xlabel('time s')
ylabel('voltage mV')
end
legend({'220nA','600nA'})

```



Q2 Threshold Increase

```

%implement the new voltage threshold vector.
Vthvec = zeros(size(tvec)); %Vth is a variable
Vth0 = -50;%initial condition is -50mV
Vthvec(1) = Vth0; %initial condition is -50mV
Vthmax = 200; % max condition is 200mV
vvec2 = zeros(size(tvec));
vvec2(1) = EL;
%new parameters
tau_vth = 1;%refractory time const = 1ms

```

setting up Euler's method

```

for range = 100:100:600 %setting up applied current constants
    pos = 1; %pos of iapp vec
    countvec2 = zeros(6);% define the spike vector
    iapp2 = zeros(6); %current vector
    iapp2(pos) = range; % first element as the first applied current range
    vvec2avg = zeros(6);% the vm average vector

```

```

        vvec2avg(pos) = 0; % initialize = 0
        vvec2add = 0;
        countvec2(pos) = 0; % spike array counts
    for i = 2:length(tvec)
        %Euler's for V threshold
        %dVth/dt = (Vth0 - Vth)/tau_vth
        dVth_over_dt = (Vth0-Vthvec(i-1))/tau_vth;
        % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
        Vthvec(i) = Vthvec(i-1) + dVth_over_dt * dt;
        %dVm/dt = ((EL - Vm) /Rm + Iapp)/Cm.
        dVm_over_dt = ((EL-vvec2(i-1)) / Rm + iapp2(pos))/Cm;
        % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
        vvec2(i) = vvec2(i-1) + dVm_over_dt * dt;

        if (vvec2(i) > Vthvec(i))% if vvec element is higher than V threshold
            vvec2(i) = Vreset;
            Vth0 = Vthmax;
            countvec2(pos) = countvec2(pos) + 1;
        end
        vvec2add = vvec2(i-1)+vvec2(i);
    end
    vvec2avg(pos) = vvec2add/length(tvec);
    pos = pos + 1; % move on to the next position array
    vvec2add = 0;
end

```

setting up Euler's method (membrane potential)

```

for range = 220:380:600 %setting up applied current constants
    pos = 1; %pos of iapp vec
    iapp = zeros(2); %current vector
    iapp(pos) = range; % first element as the first applied current range
for i = 2:length(tvec)
    %Euler's for V threshold
    %dVth/dt = (Vth0 - Vth)/tau_vth
    dVth_over_dt = (Vth0-Vthvec(i-1))/tau_vth;
    % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
    Vthvec(i) = Vthvec(i-1) + dVth_over_dt * dt;
    %dVm/dt = ((EL - Vm) /Rm + Iapp)/Cm.
    dVm_over_dt = ((EL-vvec2(i-1)) / Rm + iapp(pos))/Cm;
    % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
    vvec2(i) = vvec2(i-1) + dVm_over_dt * dt;

    if (vvec2(i) > Vthvec(i))% if vvec element is higher than V threshold
        vvec2(i) = Vreset;
        Vth0 = Vthmax;
    end
end
pos = pos + 1; % move on to the next position array

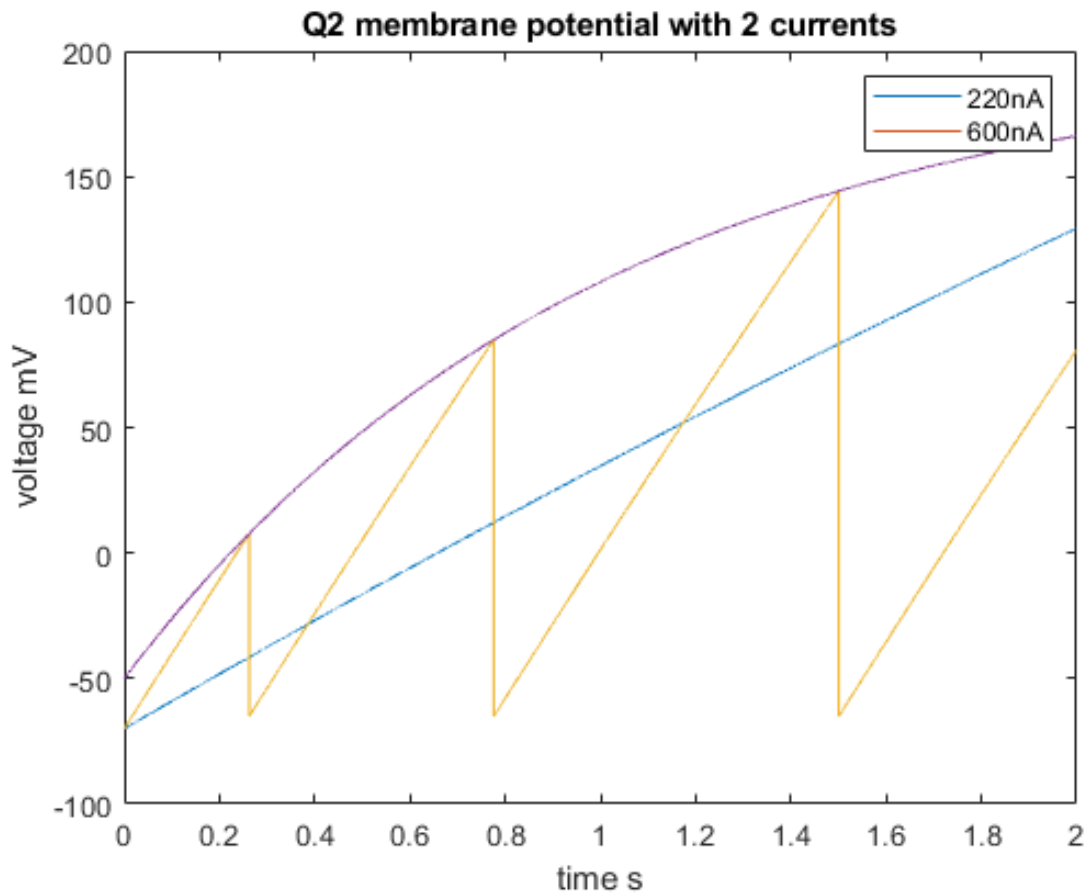
figure(2)
plot(tvec,vvec2)
hold on
plot(tvec,Vthvec)
title('Q2 membrane potential with 2 currents')

```

```

xlabel('time s')
ylabel('voltage mV')
end
legend({'220nA', '600nA'})

```



Q3 Refractory Conductance with Threshold Increase

```

% declare additional parameters
EK = -80; %Epotassium = -80mV
tau_gref = 0.2; %tau conductance refractory 0.2ms
%declare refractory conductance vectors
Gvec = zeros(size(tvec)); % declare Gvec
Gvec(1) = 0; %initialize first value to 0;
deltag = 2; %delta g = 2uS
vvec3 = zeros(size(tvec));
vvec3(1) = EL;

```

setting up Euler's method

```

countvec3 = zeros(6); % define the spike vector
iapp3 = zeros(6); %current vector
for range = 100:100:600 %setting up applied current constants
    pos = 1; %pos of iapp vec
    iapp3(pos) = range; % first element as the first applied current range
    countvec3(pos) = 0; % spike array counts
    vvec3avg = zeros(6);
    vvec3avg(pos) = 0;
    vvec3add = 0;

```

```

for i = 2:length(tvec)
    %Euler's for Gthreshold
    %dGref(t)/dt = -Gref(t)/tau_gref
    dGref_over_dt = -Gvec(i-1)/tau_gref;
    % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
    Gvec(i) = Gvec(i-1) + dGref_over_dt *dt;
    %Euler's for V threshold
    %dVth/dt = (Vth0 - Vth)/tau_vth
    dVth_over_dt = (Vth0-Vthvec(i-1))/tau_vth;
    % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
    Vthvec(i) = Vthvec(i-1) + dVth_over_dt * dt;
    %dVm/dt = ((EL - Vm) /Rm + Gref*(EK-Vm) Iapp)/Cm.
    dVm_over_dt = ((EL-vvec3(i-1)) / Rm + Gvec(i-1)*(EK-vvec3(i-1)) +iapp3(pos))/Cm;
    % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
    vvec3(i) = vvec3(i-1) + dVm_over_dt * dt;
    if (vvec3(i) > Vthvec(i))% if vvec element is higher than V threshold
        Gvec(i) = Gvec(i-1) + 2;
        Vth0 = Vthmax;
        countvec3(pos) = countvec3(pos) + 1;
    end
    vvec3add = vvec3(i-1)+vvec3(i);
end
vvec3avg(pos) = vvec3add / length(tvec);
pos = pos + 1; % move on to the next position array
vvec3add = 0;
end

```

setting up Euler's method (membrane potential)

```

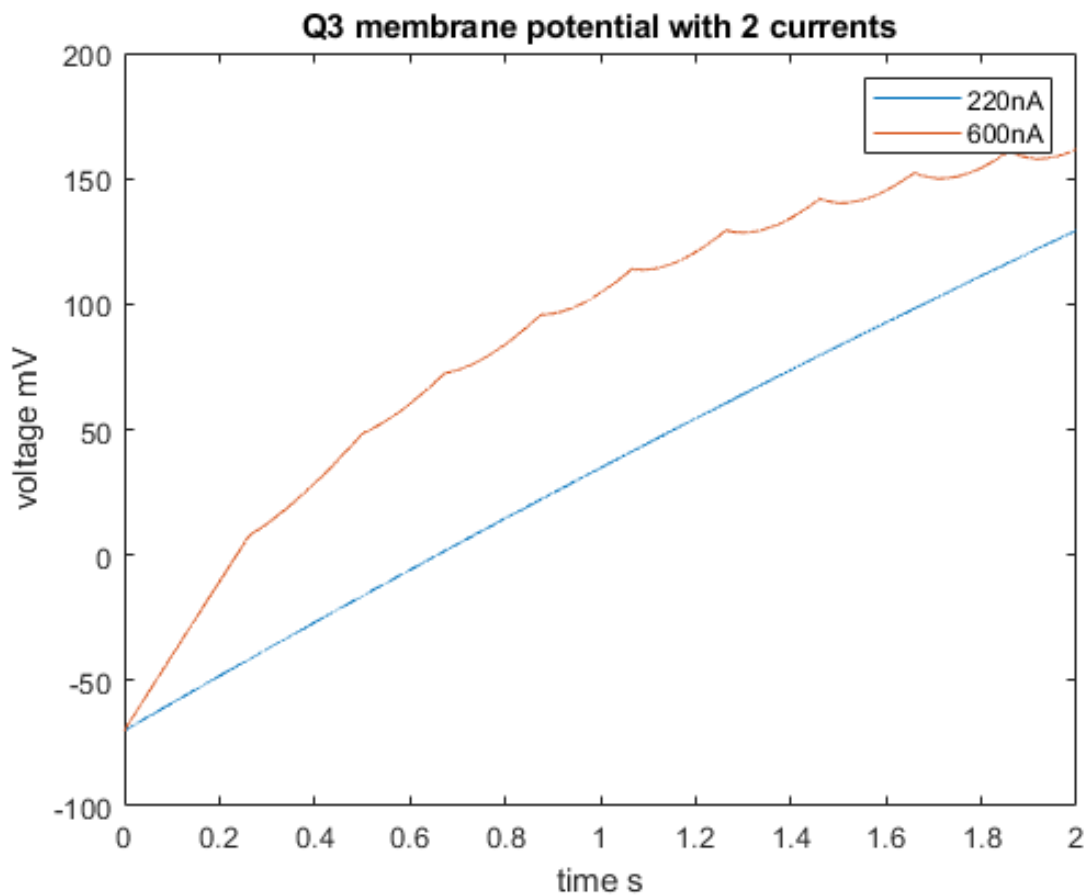
for range = 220:380:600 %setting up applied current constants
    pos = 1; %pos of iapp vec
    iapp = zeros(2); %current vector
    iapp(pos) = range; % first element as the first applied current range
for i = 2:length(tvec)
    %Euler's for Gthreshold
    %dGref(t)/dt = -Gref(t)/tau_gref
    dGref_over_dt = -Gvec(i-1)/tau_gref;
    % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
    Gvec(i) = Gvec(i-1) + dGref_over_dt *dt;
    %Euler's for V threshold
    %dVth/dt = (Vth0 - Vth)/tau_vth
    dVth_over_dt = (Vth0-Vthvec(i-1))/tau_vth;
    % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
    Vthvec(i) = Vthvec(i-1) + dVth_over_dt * dt;
    %dVm/dt = ((EL - Vm) /Rm + Gref*(EK-Vm) Iapp)/Cm.
    dVm_over_dt = ((EL-vvec3(i-1)) / Rm + Gvec(i-1)*(EK-vvec3(i-1)) +iapp(pos))/Cm;
    % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
    vvec3(i) = vvec3(i-1) + dVm_over_dt * dt;
    if (vvec3(i) > Vthvec(i))% if vvec element is higher than V threshold
        Gvec(i) = Gvec(i) + 2;
        Vth0 = Vthmax;
    end
end
pos = pos + 1; % move on to the next position array
figure(3)

```

```

plot(tvec,vvec3)
hold on
title('Q3 membrane potential with 2 currents')
xlabel('time s')
ylabel('voltage mV')
end
legend({'220nA','600nA'})

```



Drawing Requirements

```

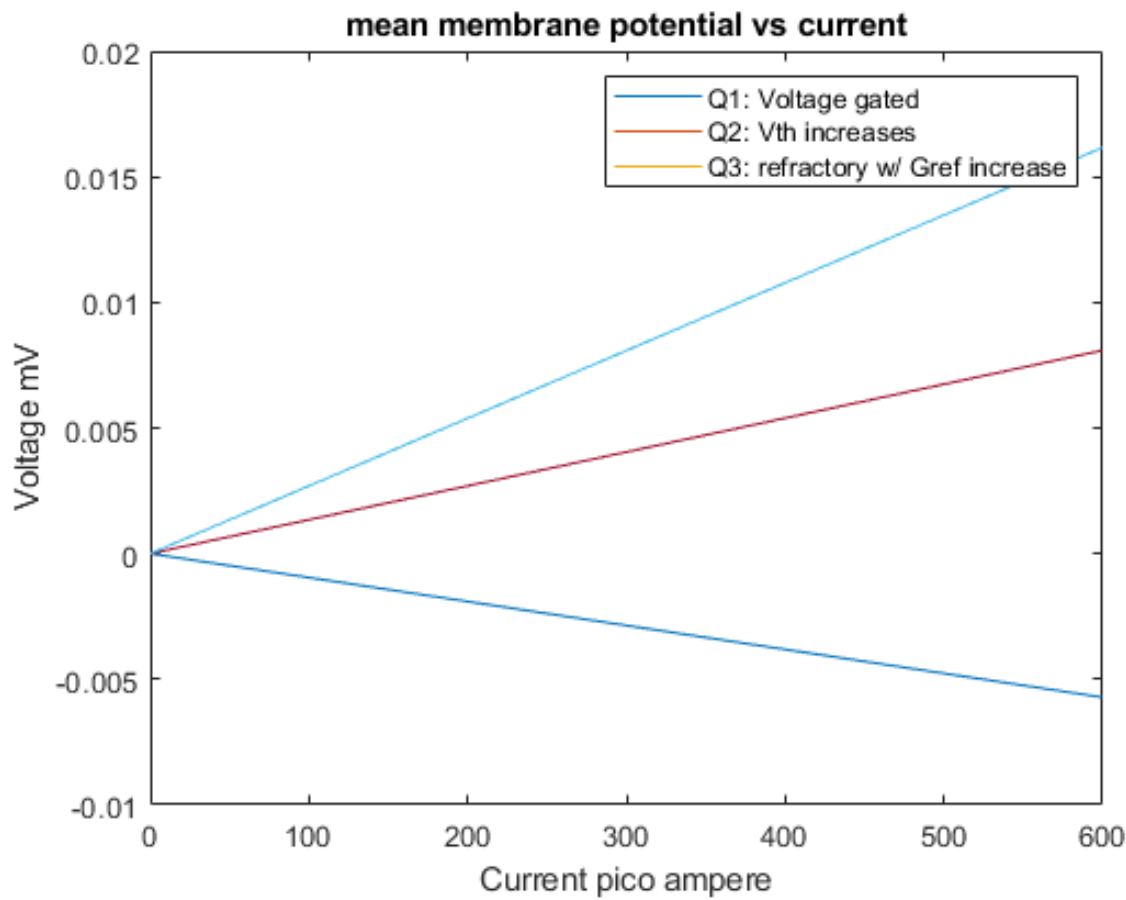
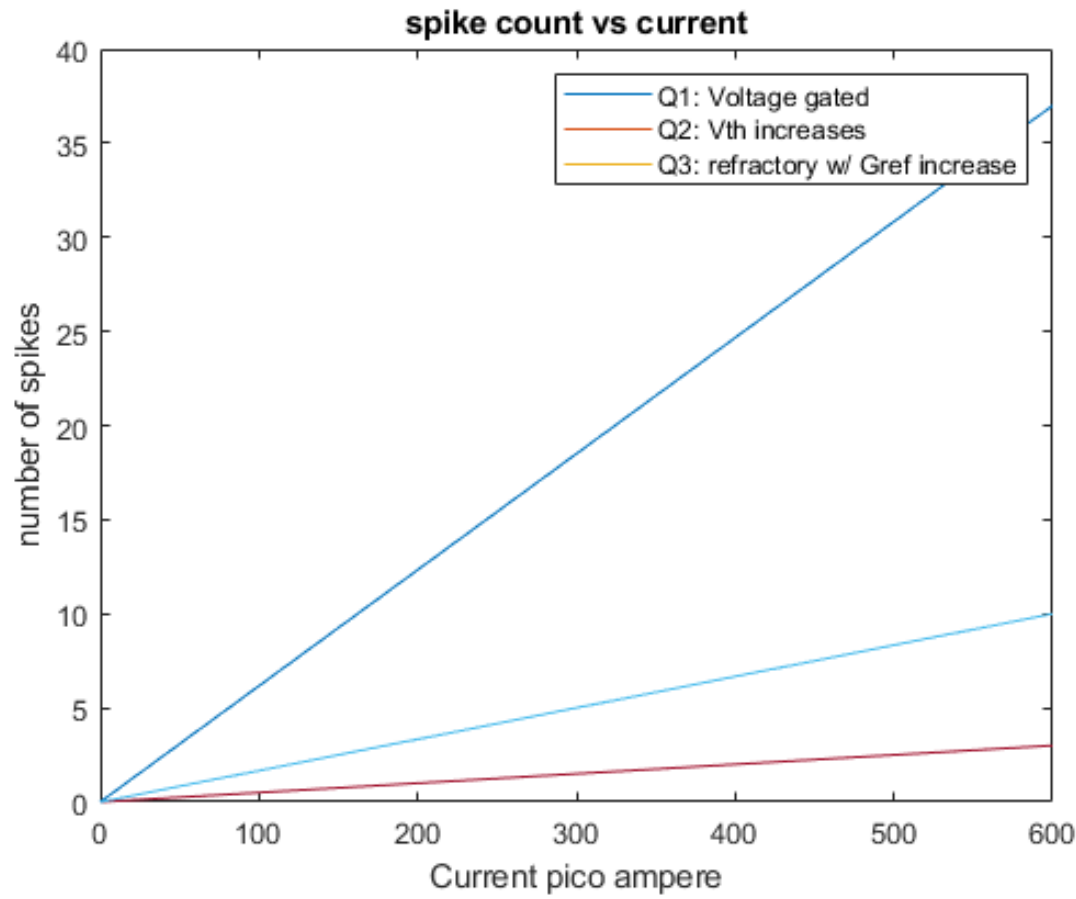
% number of spikes vs applied current
figure(4)
plot(iapp1, countvec1)
hold on
plot(iapp2, countvec2)
hold on
plot(iapp3, countvec3)
title('spike count vs current')
xlabel('Current pico ampere')
ylabel('number of spikes')
legend({'Q1: Voltage gated','Q2: Vth increases','Q3: refractory w/ Gref increase'})

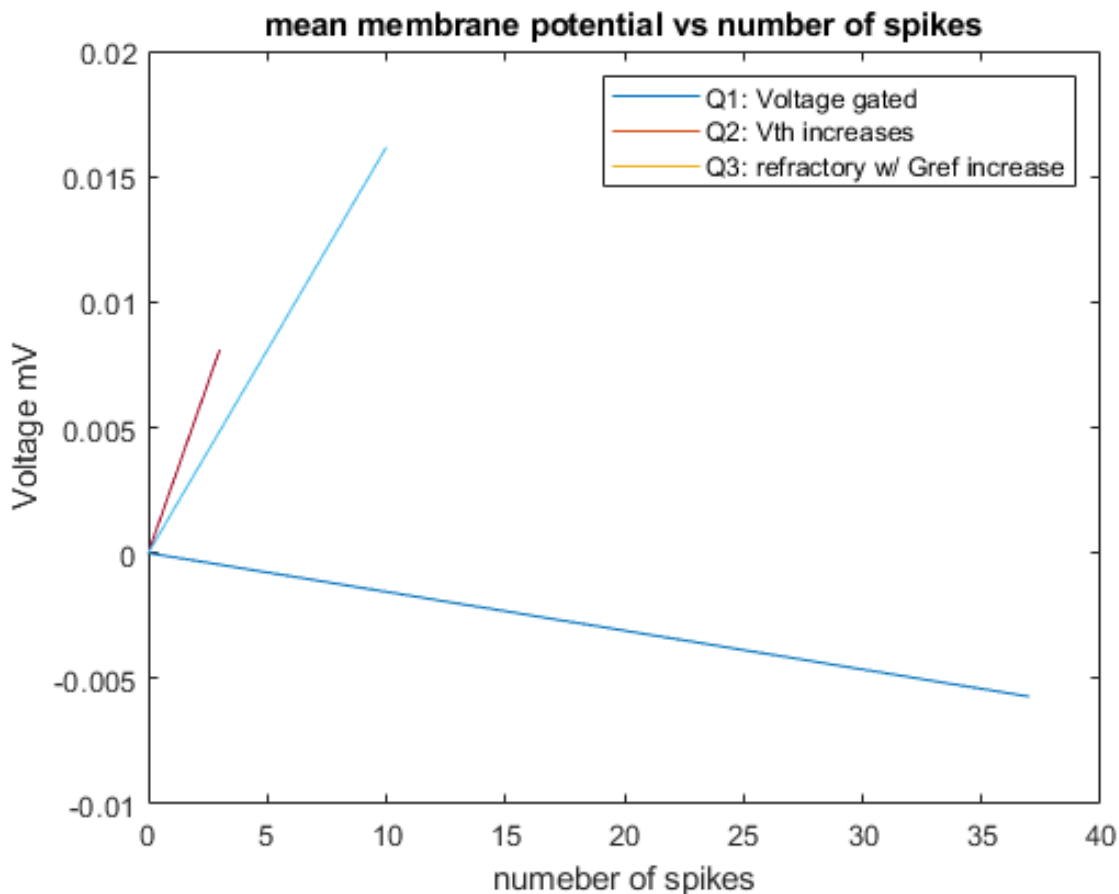
%mean membrane potential vs applied current.
figure(5)
plot(iapp1, vvec1avg)
hold on
plot(iapp2, vvec2avg)
hold on
plot(iapp3, vvec3avg)

```

```
title('mean membrane potential vs current')
xlabel('Current pico ampere')
ylabel('Voltage mV')
legend({'Q1: Voltage gated','Q2: Vth increases','Q3: refractory w/ Gref increase'})

% mean membrane vs spikes fired
figure (6)
plot(countvec1, vvec1avg)
hold on
plot(countvec2, vvec2avg)
hold on
plot(countvec3, vvec3avg)
title('mean membrane potential vs number of spikes')
xlabel('numeber of spikes')
ylabel('Voltage mV')
legend({'Q1: Voltage gated','Q2: Vth increases','Q3: refractory w/ Gref increase'})
```





Explanation

%there are obvious differences in both three methods of computation. On figure 4 where spike vs current, we can see that voltage gated has a higher slope than the other two, which means that the the larger applied current is, the voltage gated one is more prone to increases the number of spike by a whole margin. Therefore, the drawback of having a lot of action potentials is to have a more negative mean membrane potential as opposed to applied current, as can be seen by figure 5. The only negative slope is the voltage gated one. The other two still maintains a positive slope because they don't fire as much action potentials. As for figure 6, since we have different amounts of spikes, the line is, accordingly, in different length where voltage gated is the longest, and the shortest line has the highest slope. All of them are linear.

[Tutorial 2.3]

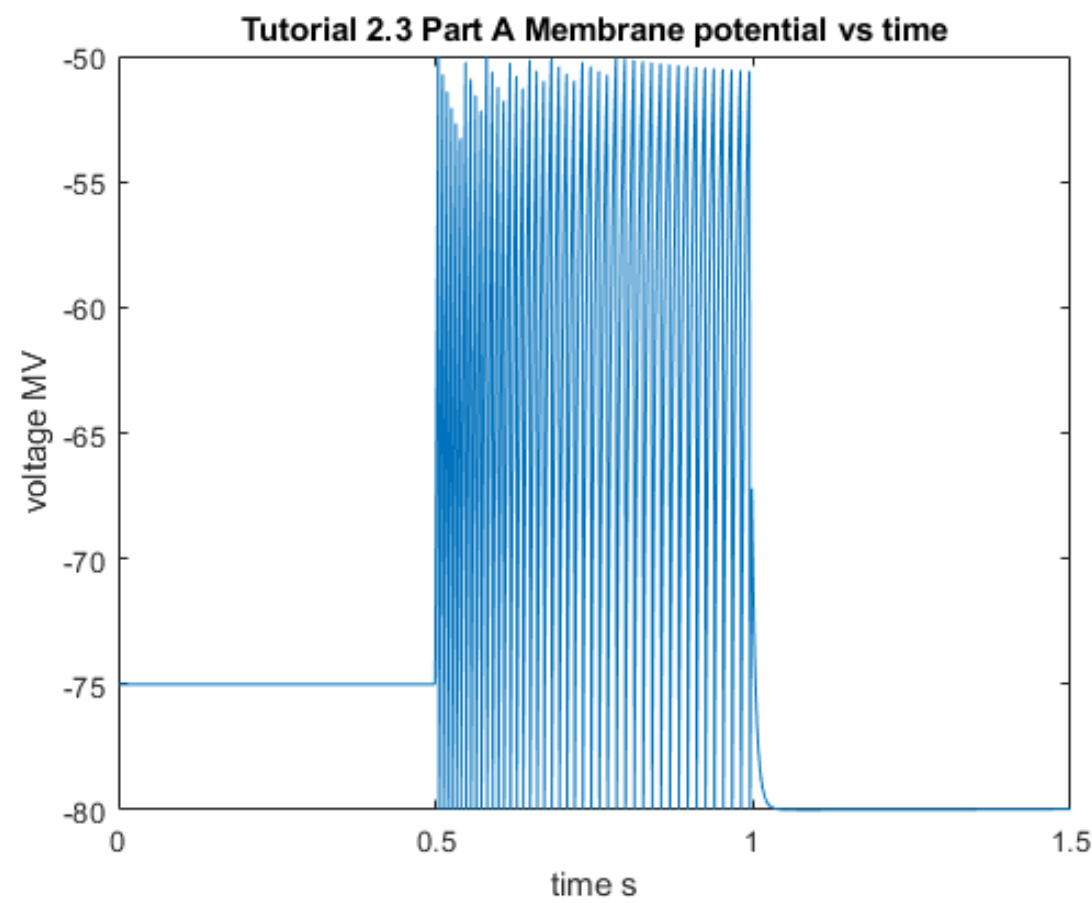
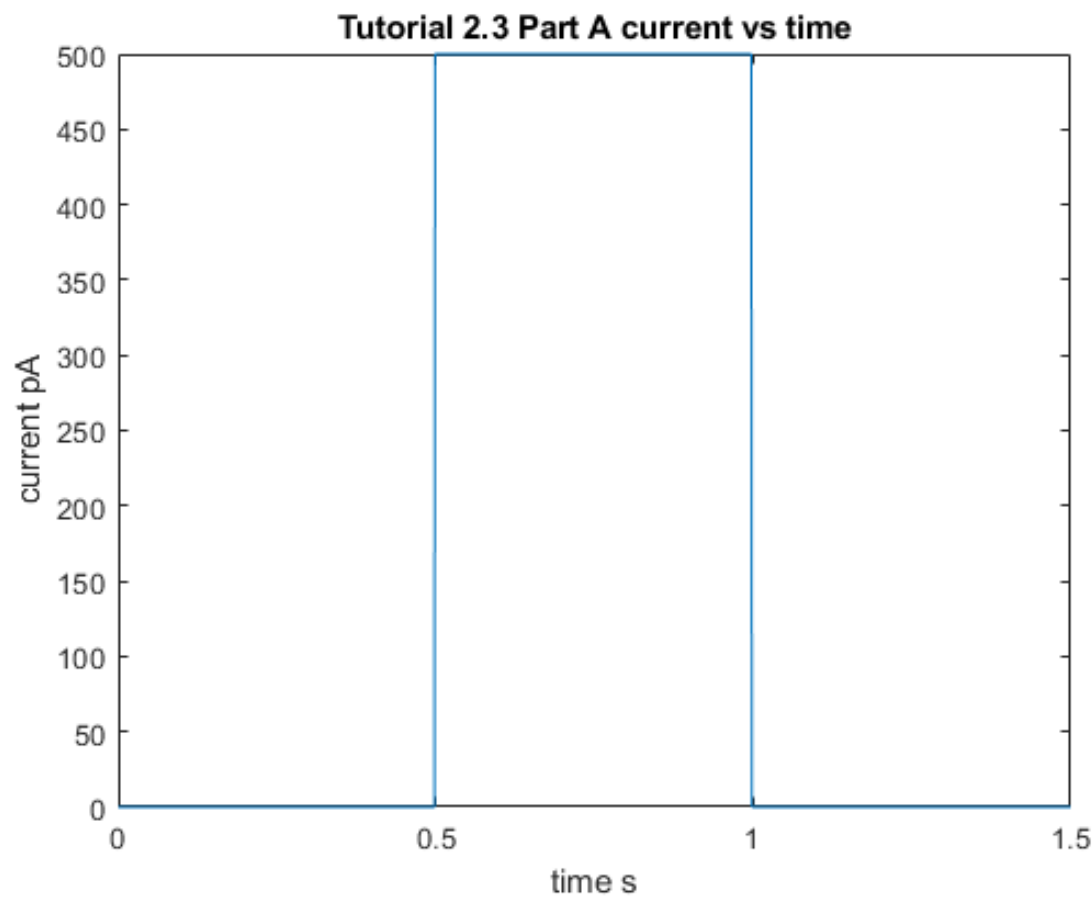
```
%Setting up parameters. (everything 10^3 for clarity)
EL = -75; %Leaky = -75mV
Vth = -50; % Threshold = -50mV
Vreset = -80; %the reset is 80mV
Rm = 100; % resistance is 100Mohms
Cm = 0.1; % Capacitance is 0.1pF
Ek = -80; %Equilibrium potassium = -80mV
deltaG = 1; % deltaGSRA = 1nS
tau = 0.2; % tau = 200ms
```

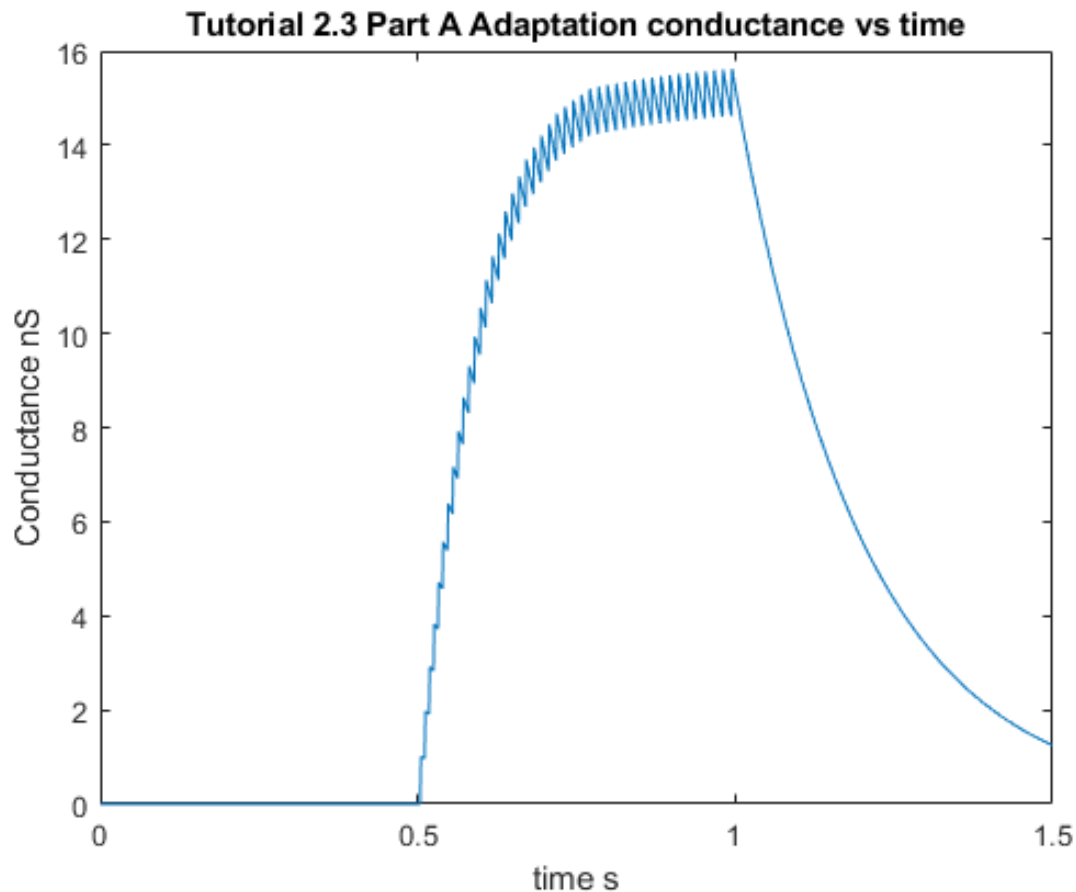
Part a

```
%setting up time vec
dt = 0.001; % step size = 0.1ms
tvec = 0:dt:1.5; % until 1.5s
%setting up Voltage vector
vvec = zeros(size(tvec));
vvec(1) = EL; %initialize the first term
%setting up conductance vector
gvec = zeros(size(tvec));
gvec(1) = 0; % initialize the first term
%Setting up Euler's method
iapp = zeros(size(tvec)); % have a variable iapp.
for i = 2:length(tvec)
    if (i > 500 && i < 1000)
        iapp(i-1) = 500;%500pA for applied curve
    else
        iapp(i-1) = 0;
    end
    %dG/dt = -G/tau
    dG_over_dt = -gvec(i-1)/tau;
    gvec(i) = gvec(i-1) + dG_over_dt * dt;
    %dV/dt = ((EL - V) /Rm + G(EK-V)+Iapp)/Cm.
    dV_over_dt = ((EL-vvec(i-1)) / Rm + gvec(i-1)*(EK-vvec(i-1))+iapp(i-1))/Cm;
    % Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
    vvec(i) = vvec(i-1) + dV_over_dt * dt;
    if (vvec(i) > Vth)% if vvec element is higher than V threshold
        vvec(i) = Vreset; %force the element to reset to Vreset
        gvec(i) = gvec(i-1) + deltaG;
    end
end
figure (7)
plot(tvec,iapp)
title('Tutorial 2.3 Part A current vs time')
xlabel('time s')
ylabel('current pA')

figure (8)
plot(tvec,vvec)
title('Tutorial 2.3 Part A Membrane potential vs time')
xlabel('time s')
ylabel('voltage MV')

figure (9)
plot(tvec,gvec)
title('Tutorial 2.3 Part A Adaptation conductance vs time')
xlabel('time s')
ylabel('Conductance nS')
```





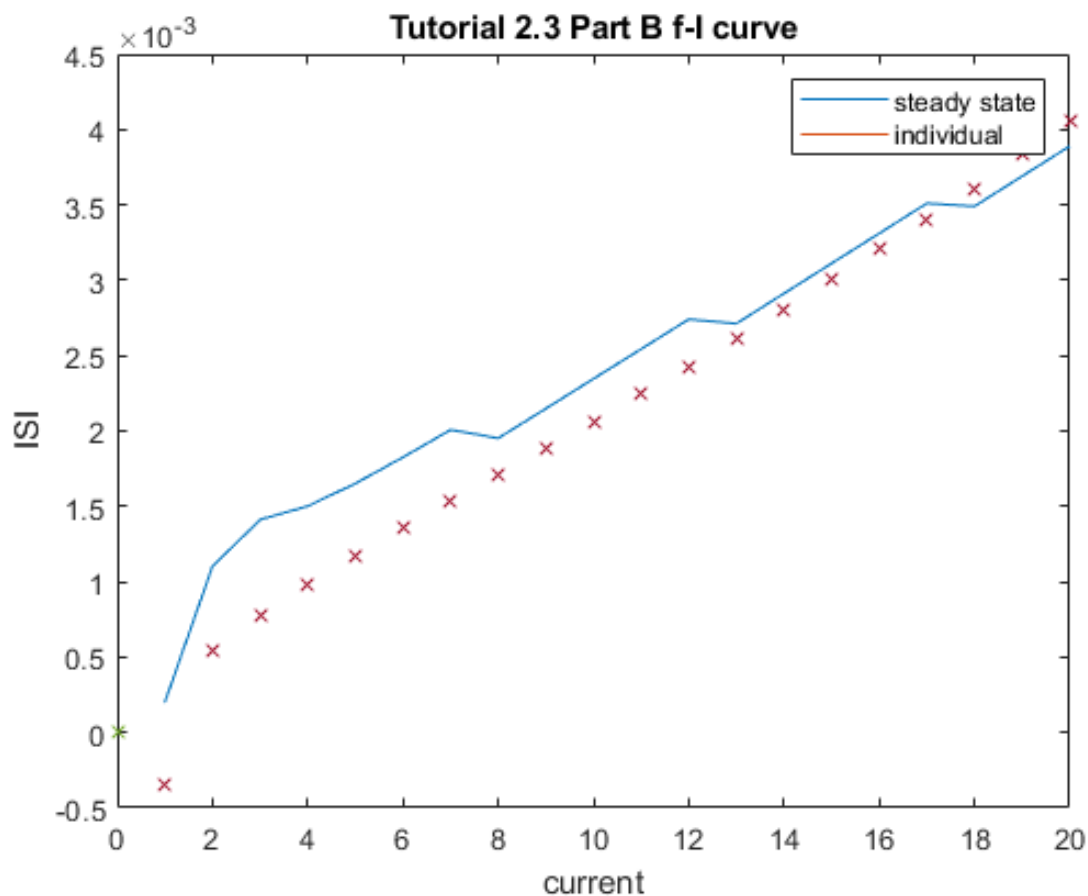
Part B

```
%time changes
tvec2 = 0:dt:5; % until 5s
%setting up Voltage vector
vvec4 = zeros(size(tvec2));
vvec4(1) = EL; %initialize the first term
%setting up conductance vector
gvec2 = zeros(size(tvec2));
gvec2(1) = 0; % initialize the first term
%Setting up Euler's method
inv_isi_time1 = zeros(20);
inv_isi_steady = zeros(20);
pos = 1;
iapp = 0;
irange = zeros(20);
for range = 1:1:20
    iapp = range;
    t1 = 0;
    t2 = 0;
    k = 0;
    j1 = 0;
    j2 = 0;
for i = 2:length(tvec2)
    %dG/dt = -G/tau
    t1 = t1 + 1;
    t2 = t2+1;
    dG_over_dt = -gvec2(i-1)/tau;
    gvec2(i) = gvec2(i-1) + dG_over_dt * dt;
    %dV/dt = ((EL - V) /Rm + G(EK-V)+Iapp)/Cm.
```

```

dV_over_dt = ((EL-vvec4(i-1)) / Rm + gvec2(i-1)*(EK-vvec4(i-1))+iapp)/Cm;
% Vmi = Vmi-1 + dt*f(ti-1,vmi-1)
vvec4(i) = vvec4(i-1) + dV_over_dt * dt;
if (vvec4(i) > Vth)% if vvec element is higher than V threshold
    vvec4(i) = Vreset; %force the element to reset to Vreset
    gvec2(i) = gvec2(i-1) + deltaG;
    k = k+1;
    if k == 1
        j1 = t1;
    elseif k == 2
        j2 = t2;
    end
end
end
inv_isi_time1(pos) = 1 / (j2-j1);
inv_isi_steady(pos) = 1 / ((length(tvec2)-j2)/ k);
irange(pos) = range;
hold on
pos = pos+1;
end
figure (10)
plot(irange,inv_isi_steady)
hold on
plot(irange,inv_isi_time1,('x'))
legend('steady state','individual')
xlabel('current')
ylabel('ISI')
title('Tutorial 2.3 Part B f-I curve')

```



comment:

the initial firing frequency is less than the steady state frequency, yet when applied current is increasing to a greater degree the initial firing frequency becomes larger.

Pod Times

We met on Thursday from 7 to 9PM to work and clear up setting parameters

```
% I helped by sharing my codes and graphs to them and clearing up the  
% values of parameters because of margin of error.  
  
% I had questions on the theoretical curves and what the graphs should  
% actually look like to confirm if my plot is correct.
```

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