```
Part I.a
The mean vector is:
                           21.686573
[ 97.69496
               3.8018749
                                        40.259743
                                                    20.341219
                                                                 40.420425
  22.267612
               39.2425
                           20.855335
                                        39.026905
                                                     19.592106
                                                                 50.949284
                                                     22.029108
   7.9109387
              54.60908
                           20.267107
                                        35.3882
                                                                 42.936165
                                                     79.75042
  19.485828
               41.552402
                            7.4116645 755.5226
                                                                  4.0397515
  38.330833
               3.7607067
                           24.988033 ]
The total variance is:
12504.28821890043
Part I.b
The inner form covariance matrix is:
[[ 1.05108330e+04
                                                     3.50970650e+01
                   1.60503891e+02
                                     9.12960911e+00
                                                     1.21090260e+01
   2.69952335e+01 -2.52280788e+01
                                     1.74939156e+01
                    7.55081463e+00
   8.43628025e+00
                                     3.73679137e+00
                                                      6.43250513e+00
   7.34506912e+01 -2.65625061e+02
                                     5.58117390e+00 -2.91737137e+01
   7.93596697e+00 -5.03670807e+01
                                     2.06760049e+00
                                                    -2.19027596e+01
   5.40530777e+01 -2.64632320e+01
                                   -2.32634918e+02
                                                      2.18936367e+01
   2.78560966e-01
                    6.60231781e+00
                                   -1.65634727e+011
 [ 1.60503891e+02
                    6.29766846e+01
                                   -2.99866378e-01
                                                      3.37784672e+00
  -9.78320688e-02
                    1.64662969e+00
                                   -1.55046415e+00
                                                      3.38748097e+00
  -1.43611670e-01
                    3.95963907e+00
                                   -1.15267682e+00
                                                     1.01116180e+01
  -3.81949949e+00
                    3.80073509e+01
                                   -2.26626086e+00
                                                      1.42326140e+00
  -1.10925972e+00
                    5.35448372e-01
                                   -2.51957726e+00
                                                    -2.88788438e-01
  -3.14045858e+00
                  -6.21034920e-01
                                     8.10511208e+00
                                                     1.17257810e+00
   1.87549388e+00
                                     5.99487349e-02]
                  -1.20906377e+00
 [ 9.12960911e+00
                                     2.57931495e+00
                                                     1.04811037e+00
                  -2.99866378e-01
                                                    -1.49226204e-01
   2.94722939e+00
                  -1.63981076e-02
                                     2.87512565e+00
   2.87730074e+00
                    6.82297647e-01
                                     2.62248707e+00
                                                    -2.14178219e-01
                                     2.84204984e+00
                                                     1.11029840e+00
   6.40429354e+00 -3.07682915e+01
   2.59309030e+00
                  -5.40439524e-02
                                     2.73335624e+00
                                                      4.78411704e-01
   5.83128166e+00
                  -1.78933370e+00
                                   -8.26768684e+00
                                                    -3.45058769e-01
  -1.44357896e+00
                    3.84864759e+00
                                   -1.44414812e-011
 [ 3.50970650e+01
                    3.37784672e+00
                                     1.04811037e+00
                                                      1.58340168e+01
   2.35463190e+00
                    1.29154320e+01
                                     2.02141047e+00
                                                      1.09387999e+01
   8.63116086e-01
                    1.52077875e+01
                                     1.51053643e+00
                                                      1.08868361e+01
   7.66139412e+00
                    3.03829308e+01
                                     1.79646537e-01
                                                      1.63027782e+01
  -2.33925492e-01
                    1.53042154e+01
                                     9.24035847e-01
                                                     1.26206970e+01
   7.21010590e+00
                   -8.65499878e+00
                                     1.62537193e+01
                                                      1.99883866e+00
                    1.06672554e+01
                                   -4.03386019e-02]
  -9.88266528e-01
 [ 2.69952335e+01
                                                      2.35463190e+00
                  -9.78320688e-02
                                     2.94722939e+00
   4.80888987e+00
                   -1.47799337e+00
                                                      8.67102206e-01
                                     3.23443627e+00
   3.41387653e+00
                    2.20445919e+00
                                     2.91462946e+00
                                                      5.85513890e-01
   1.07000732e+01
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                    7.85148382e-01
                                     2.98450327e+00
                                                     1.43242753e+00
                                                     2.82171249e-01
   9.23796272e+00
                  -2.15851164e+00
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                                   -3.52457136e-01]
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                    5.35894012e+00
 [-2.52280788e+01
                    1.64662969e+00
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                                                      1.29154320e+01
  -1.47799337e+00
                    1.65625305e+01
                                     1.12108064e+00
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                    1.27459326e+01
                                     8.28830481e-01
                                                     9.18897152e+00
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                    1.06888628e+00
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  -1.80307376e+00
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   6.54120088e-01
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                                   2.89051950e-01
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                                    3.38566041e+00 -2.51752257e+00
                                                    2.89051950e-01
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                                    4.01606989e+00
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   5.23015404e+00
                  3.25401735e+00
                                    7.15831089e+00
                                                     4.92847157e+00
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                                  -4.54942665e+01
                                                    2.51462817e+00
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  -6.38283396e+00 -1.51688118e+01 -1.52566314e+00 -1.00598497e+01
  -2.35712028e+00 -8.72031689e+00 -2.33782887e+00 -5.64395666e+00
  -5.63596153e+00
                  5.47489548e+01 -1.01451960e+01 -4.26271963e+00
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 [-2.32634918e+02
                   3.54698906e+01 -8.42102623e+00
                                                    1.72732697e+01
  -1.65108986e+01
  -1.18289261e+01
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  -5.16465187e+01
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  -8.75699043e+00
                   3.79379730e+01 -9.57178879e+00
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                   3.19434547e+00
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  -9.30089831e-01
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                                  -8.77806127e-01
                   2.59155846e+00
                                                    2.42848229e+00
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                                  -6.44496393e+00
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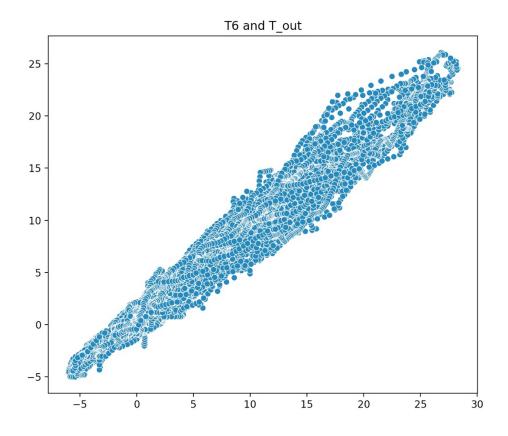
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                  3.36742252e-02
  7.92254567e-01
                                   6.99417174e-01
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 -1.43248826e-01
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  4.03147899e-02 -2.44097605e-01
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[-1.52282283e-01
 -5.05290806e-01
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-5.69119036e-01
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-3.00437659e-01
                  4.87354457e-01 -3.18848312e-01
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-5.74196756e-01 -9.20164734e-02
                                   1.00000000e+00 -1.76458403e-01
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 8.31249058e-02
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[ 8.71220604e-02
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 -2.18876123e-01
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 1.92936122e-01 -2.35032350e-01 -1.76458403e-01 7.51578715e-03 1.25972256e-01 -1.13418326e-02]
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                                    1.00000000e+00]
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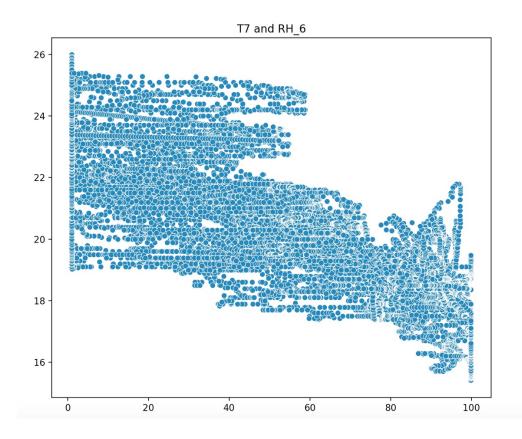
- i) The most correlated attributes are T6 and $T_{\rm out}$. Coefficient = 0.974787.
- ii) The most anti-correlated attributes are T7 and RH_6 . Coefficient = -0.753973.
- iii) The least correlated attributes are rv1 and Tdewpoint. Coefficient = 0.003943.

Plots are on pages that follow

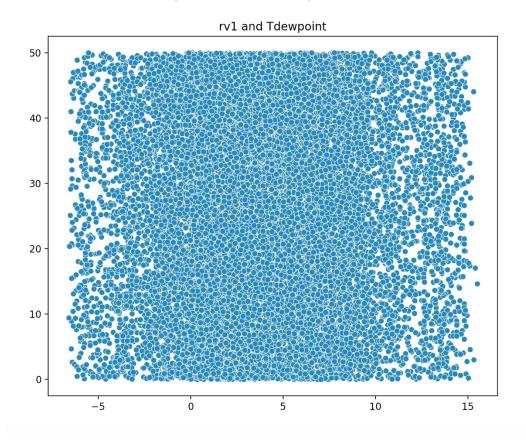
Part I.c i) The most correlated attribute pair: T6 and T_out

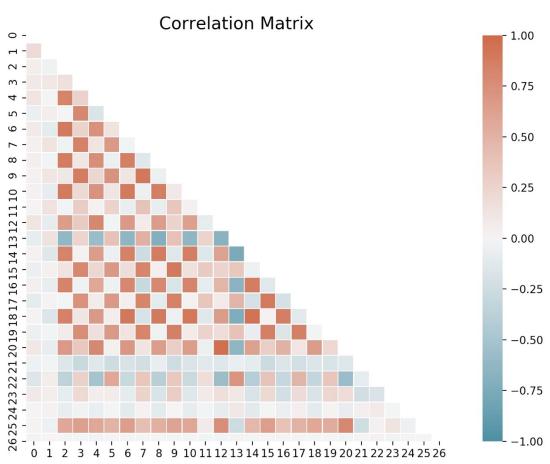


ii) The most anti-correlated attribute pair: T7 and RH_6



iii) The least correlated attribute pair: rv1 and Tdewpoint:





```
Part II.
The two eigenvectors are:
u1 = [9.99105099e-01 1.51964502e-02 9.79220626e-04 3.21871599e-03]
   2.72345362e-03 -2.61580986e-03 1.80060053e-03 9.66570422e-04
 9.62773783e-04 5.26607587e-04 4.80647649e-04 3.54839554e-04 7.48133475e-03 -2.87908902e-02 7.04873626e-04 -2.99052340e-03 8.93430013e-04 -5.09538148e-03 3.54461308e-04 -2.27319517e-03 5.56200613e-03 -2.46519855e-03 -2.35761110e-02 2.07670827e-03 -1.25283520e-04 7.34311442e-04 -1.63076345e-03]
u2 = [0.03580635 \quad 0.0414222 \quad -0.02793342 \quad 0.0330171 \quad -0.03727893]
05281056
                   0.05052722 - 0.04071391
                                                  0.05276296 -0.03235492
 -0.03574589
                                                                                    0.07589703
 0.07860035
                                                                                  0.00525308
  0.04205823 -0.02721032 0.006184351
The projected data points are:
                     35.347003091
[-38.3934171]
```

Process finished with exit code 0

[174.53005232 -53.11792166] [324.41603571 -47.57419798] [334.34081837 -46.71549429]]

35.063898811

33.79221355]

Plots is on pages that follow

[-38.40129011]

[-48.38569989]

