

# REACTION MECHANISMS AND RATE CONSTANTS OF ELEMENTARY STEPS IN METHANE-OXYGEN FLAMES

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The concentrations of all stable and unstable species have been measured in the reaction zone of lean and stoichiometric methane-oxygen flames burning at 40 torr.

The rate constant of Reaction [1],  $\text{CH}_4 + \text{OH} \rightarrow \text{CH}_3 + \text{H}_2\text{O}$ , was found to be  $k_1 = 3 \times 10^{13} \times \exp(-6000/RT)$  mole<sup>-1</sup> cm<sup>3</sup> sec<sup>-1</sup>. In stoichiometric flames, half of the fuel is consumed via Reaction [1'],  $\text{CH}_4 + \text{H} \rightarrow \text{CH}_3 + \text{H}_2$ , and at  $T = 1600^\circ\text{K}$ ,  $k_1'$  is reported to be  $3.2 \times 10^{12}$ . It is shown conclusively that the great majority of the methyl radicals is removed by Reaction [2],  $\text{CH}_3 + \text{O} \rightarrow \text{CH}_2\text{O} + \text{H}$ , with  $k_2 = 1.3 \times 10^{14} \exp(-2000/RT)$ . The rate-determining step is a reaction resulting in an increase of the number of particles, Reaction [13]:  $\text{CH}_2\text{O} + \text{M} \rightarrow \text{CO} + \text{H}_2 + \text{M}$ ; the value  $k_{13} = 2.1 \times 10^{16} \exp(-35,000/RT)$  was derived. Another part of the formaldehyde disappears via Reaction [3]:  $\text{CH}_2\text{O} + \text{OH} \rightarrow \text{CHO} + \text{H}_2\text{O}$ ; the rate constant is  $k_3 \approx 2.3 \times 10^{13}$  in the range  $T = 1400^\circ\text{--}1800^\circ\text{K}$ . Most of the CHO radicals react with  $\text{O}_2$ :  $\text{CHO} + \text{O}_2 \rightarrow \text{HO}_2 + \text{CO}$ ;  $k_4 \approx 3 \times 10^{13}$  at  $T = 1600^\circ\text{K}$ . In lean flames,  $\text{HO}_2$  is removed mainly by reactions involving OH and O:  $\text{HO}_2 + \text{OH}(\text{O}) \rightarrow \text{O}_2 + \text{H}_2\text{O}(\text{OH})$ ; and  $k_5 \approx 5 \times 10^{13}$  at  $T = 1600^\circ\text{K}$ . Carbon dioxide is formed by Reaction [6]:  $\text{CO} + \text{OH} \rightarrow \text{CO}_2 + \text{H}$ ; the rate constant was found to be  $k_6 = 2.8 \times 10^{11}$  at  $T = 1750^\circ\text{K}$ , and the activation energy  $E_6 = 5.5 \pm 2$  kcal/mole in the range  $T = 1500^\circ\text{--}1900^\circ\text{K}$ .

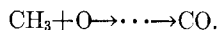
In the burned gas of lean flames, the radical "pool" decays by Reaction [11]:  $\text{H} + \text{O}_2 + \text{M} \rightarrow \text{HO}_2 + \text{M}$ , the rate constant (for  $\text{M} = \text{O}_2$ ) being  $k_{11} = 2.5 \times 10^{15}$  at  $T = 1900^\circ\text{K}$ .

## Introduction

The reaction mechanism of methane-oxygen flames is not yet fully understood.

Most important of all, no satisfactory rate-determining step has been proposed as yet, as is evident from the work of Bradley *et al.*,<sup>1</sup> who found none of the accepted reaction mechanisms in agreement with the experimental values and the pressure dependence of the burning velocity.

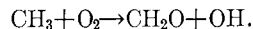
Another unresolved problem is the fate of the methyl radical. According to Fenimore,<sup>2</sup>  $\text{CH}_3$  is destroyed by an O atom:



Fristrom,<sup>3</sup> as well as other authors, favors a

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reaction with  $\text{O}_2$ :



Other obscure points are: (i) the source of  $\text{H}_2$ , the production of which cannot be explained solely by removal of H by H atoms; (ii) the fate of the CHO radical; (iii) the role of  $\text{HO}_2$  in the reaction mechanism; and (iv) the growth and decay of the concentrations of the main reactive species, OH, O, and H.

Finally, no sufficiently precise data are available for the rate constants of many of the elementary reactions.

In order to settle these questions unambiguously, we measured the concentrations of all species, unstable as well as stable, throughout the reaction zone of a few low-pressure methane-oxygen flames.

### Experimental

The need for supersonic molecular-beam sampling, and subsequent mass-spectrometric analysis, is evident if a single technique is to be used for measuring all species. A few groups of workers have applied this technique in the past.<sup>4-6</sup>

The apparatus consists of three differentially pumped stages, the first one being equipped with a conical, thin-walled, deactivated quartz sampling probe, 25 mm high, with an apex angle of 40° and a 0.1-mm-diam orifice. The core of the supersonic gas jet emerging from this sampling orifice is allowed to enter the second stage through a 1.5×3 mm skimmer orifice in the tip of a brass cone, located 20 mm downstream of the sampling orifice. The molecular beam is modulated mechanically at 32 Hz, and passes through a 0.8×8-mm collimating slit into the third stage, where it traverses the modified ion source of an Edwards E 60 mass spectrometer. The output of the ion multiplier is fed to a PAR 121 lock-in amplifier.

The dimensions of the beam-forming elements (sampling probe and skimmer) were chosen as stated above, after a detailed study of their influence on the intensity and quality of the molecular beam. The following brief outline of the problem clearly shows the necessity for a compromise solution.

The angle of the sampling cone should be small to minimize the disturbance of the flame. However, this leads to appreciable reflection of jet molecules from the inner probe walls, and to a low conductance in the probe-skimmer region, both detrimental to the beam intensity. Moreover, a "secondary" beam might be formed, due to effusion of background gas or randomized jet molecules through the skimmer orifice. To minimize these effects, the sampling orifice should be made small—even though the ratio of wall collisions to gas-phase collisions is adversely affected and the theoretical final Mach Number is lowered<sup>7</sup>—and the "nozzle"-to-skimmer distance should be made much larger than usual to ensure a sufficiently high conductance.

The final beam intensity obtained with the stated beam-formation-element geometry is rather low, but the beam composition is really representative of the sample composition, except for a well-known mass discrimination effect,<sup>8</sup> and the flame disturbance is minimal, as was confirmed by several tests.

The over-all sensitivity of the apparatus depends, for all species in a nearly identical way, on the pressure, the temperature, and the mean molecular weight of the sampled gas. Therefore, relative values of the mole fractions of stable

species could be determined accurately by direct calibration.

The flame radicals and atoms were, for obvious reasons, measured at ionizing-electron energies a few electron volts above the respective ionization potentials. The accurate calibration of O, H, and OH was made possible by the fact that the four H<sub>2</sub>/O<sub>2</sub>-system reactions were found to be equilibrated to within a few percent in the burned gas of a lean-CH<sub>4</sub>/O<sub>2</sub> flame.

A calibration factor for CH<sub>3</sub> could be determined in a fuel-rich C<sub>2</sub>H<sub>6</sub>/H<sub>2</sub>/O<sub>2</sub> flame at the point where the rate of formation of CH<sub>4</sub>, mainly via CH<sub>3</sub>+H<sub>2</sub>→CH<sub>4</sub>+H, is equal to its rate of destruction, mainly by the reverse reaction.

For the other unstable species, use was made of reasonable estimates of ionization cross sections (error less than a factor of 2).

The temperature profile was determined, using a 0.1-mm-thick BeO-Y<sub>2</sub>O<sub>3</sub> coated<sup>9</sup> Pt-Pt/10% Rh thermocouple. Radiation losses were compensated for by heating the thermocouple with an AC supply; exact compensation is attained when both the electrical-power input and the junction temperature are the same as in a vacuum.

The area expansion ratios were measured only

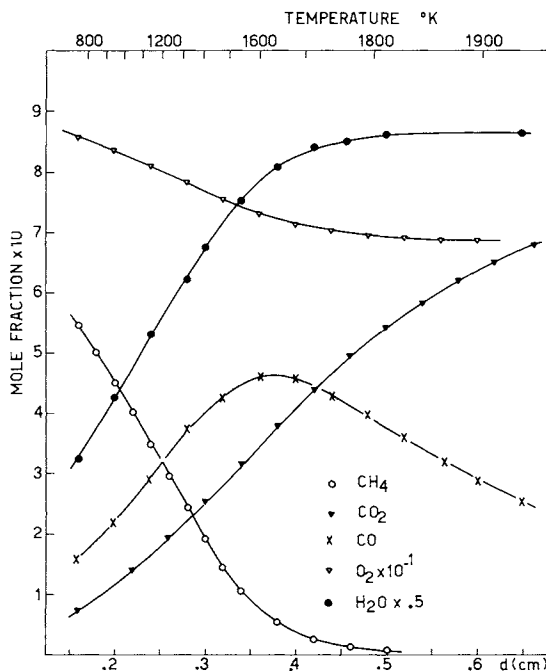


FIG. 1. Temperature and mole fractions of CH<sub>4</sub>, O<sub>2</sub>, CO, CO<sub>2</sub>, and H<sub>2</sub>O versus distance from burner in lean methane-oxygen flame (9.5% CH<sub>4</sub>-90.5% O<sub>2</sub>);  $v_0 = 67$  cm/sec;  $p = 40$  torr.

in the nonignited mixtures. The novel technique used here is based on the measurement of the heat transfer between the flowing gas and a wire normal to the flow direction. The heat exchange is proportional to the Nusselt Number,<sup>10</sup> which was experimentally found to be proportional to  $Re^{0.25}$ , whereas the Reynolds Number  $Re$ , itself, is inversely proportional to the area expansion ratio  $A$ .

The water-cooled flat-flame burner, with a diameter of 5 cm, was of the perforated disk type (2500 holes of 0.7 mm diam). All flames investigated burned at 40 torr.

### Results

Detailed composition traverses were obtained for a lean- $CH_4/O_2$  flame (9.5%  $CH_4$ , 90.5%  $O_2$ ), burning at 40 torr. The fresh-gas-stream velocity was 67 cm/sec. The distance scale was corrected each time for the slight shift of the flame away from the burner when the probe penetrates into the flame. The results are partially shown in Figs. 1, 2, and 3. For the sake of clarity, only every second or third experimental point is given. The mole fractions of OH, H, O, CO,  $H_2$ , and  $CO_2$ , from  $z=1.0$ –4.5 cm, were also deter-

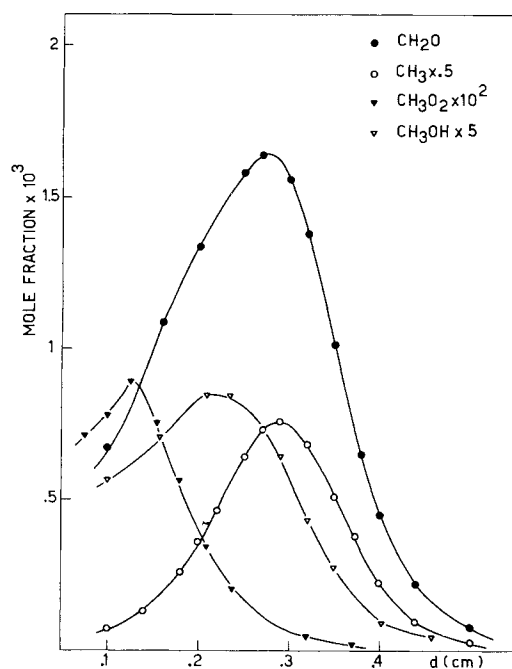


FIG. 2. Mole fractions of  $CH_2O$ ,  $CH_3$ ,  $CH_3O_2$ , and  $CH_3OH$  versus distance from burner. Same flame as in Fig. 1.

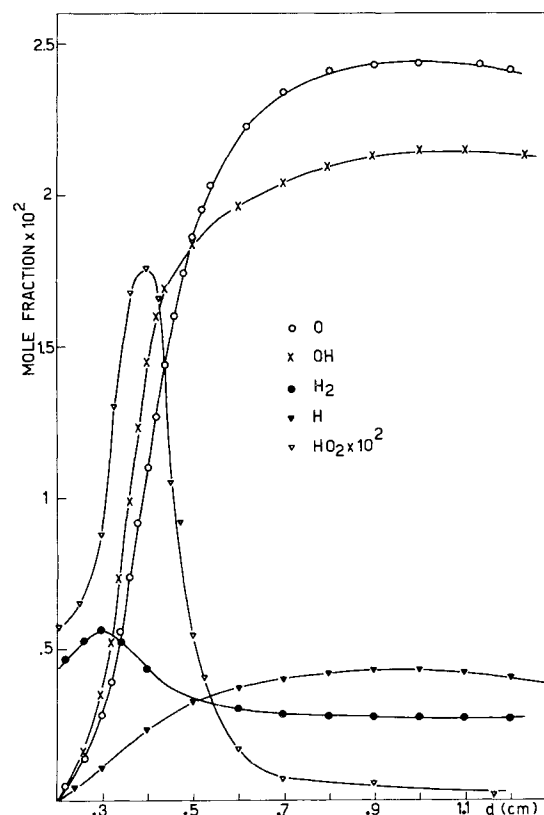


FIG. 3. Mole fractions of O, OH,  $H_2$ , H, and  $HO_2$  versus distance from burner. Same flame as in Fig. 1. The  $HO_2$  profile should be shifted 0.05 cm to the left.

mined. Small amounts of  $C_2H_6$ ,  $C_2H_4$ , CHO ( $X_{max} \approx 10^{-6}$ ), and  $CH_2$  ( $X_{max} \approx 5 \times 10^{-6}$ ) were also detected. The temperature is indicated in Fig. 1. The area expansion ratio is  $A = 1 + 0.19z$ , with  $z$  being the distance from the burner.

The mole fluxes per unit inlet area,  $F_i$ , were computed using

$$F_i = AN_i(v + V_i), \quad (1)$$

where  $N_i$  is the concentration (mole  $cm^{-3}$ ) of species  $i$ ,  $V_i$  its local diffusion velocity<sup>11</sup> (taking thermal diffusion into account), and  $v$  the local mass-average velocity. The mole fluxes per unit inlet area of  $CH_4$ , OH, O, and H are shown in Fig. 4. The maximum deviation of the derived total carbon-atom flux from the initial value is 8%. For the other elements, the maximum deviation is only a few percent.

The net chemical reaction rate  $K_i$  of all

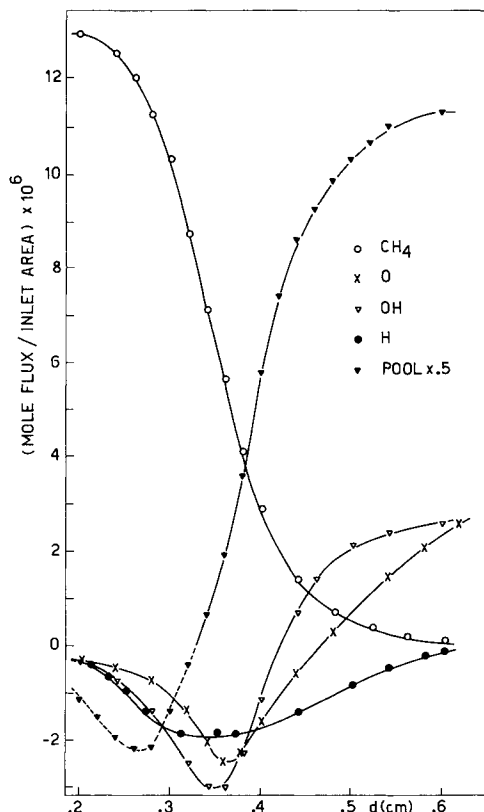


FIG. 4. Mole fluxes per unit inlet area (mole  $\text{cm}^{-2} \text{sec}^{-1}$ ) of  $\text{CH}_4$ , O, OH, and H versus distance from burner. The "pool-flux" profile,  $F_p = 3F_H + 2F_{\text{CO}} + 2F_{\text{H}_2} + 2F_{\text{O}} + F_{\text{OH}} + F_{\text{CH}_3}$ , is also shown. Same flame as in Fig. 1.

species was calculated, using

$$K_i = (1/A) (dF_i/dz). \quad (2)$$

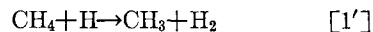
In the lean flame, the  $\text{CH}_4$ -disappearance rate peaks at  $z = 0.34 \text{ cm}$ :  $(-K_{\text{CH}_4})_{\text{max}} = 8.4 \times 10^{-5} \text{ mole cm}^{-3} \text{sec}^{-1}$ .

Some measurements were also made on a stoichiometric  $\text{CH}_4/\text{O}_2/\text{Ar}$  flame (9.5%  $\text{CH}_4$ ) burning at 42 torr, with an initial stream velocity  $v_0 = 67 \text{ cm/sec}$ . In this flame, the ratio  $K_{\text{CH}_4}/X_{\text{CH}_4}$  in the exponential decay zone is identical to that same ratio in the lean flame. The final temperature is about 2000°K. At the point where  $-K_{\text{CH}_4}$  peaks, the ratios of the mole fractions in the stoichiometric flame to those in the lean flame are 2.3 for  $\text{CH}_3$ , 0.13 for  $\text{O}_2$ , 0.36 for O, 0.58 for OH, 3.9 for H, 6.3 for  $\text{H}_2$ , 0.7 for  $\text{CH}_2\text{O}$ , and about 4 for CHO.

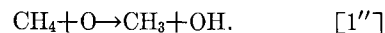
## Discussion and Conclusions

### $\text{CH}_4$

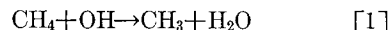
In the lean flame, H removal from  $\text{CH}_4$  by H:



can be neglected. Allowance was made, however, for



Its rate was calculated using the known rate constant<sup>12</sup> and subtracted from the observed  $(-K_{\text{CH}_4})$  value, whence the rate constant of the most important process



could be derived at each point. The resulting plot of  $\log k_1$  versus  $1/T$  is shown in Fig. 5:  $k_1 = 3 \times 10^{13} \exp(-6000/RT) \text{ mole}^{-1} \text{ cm}^3 \text{sec}^{-1}$ , in the range  $1100^\circ\text{K} < T < 1900^\circ\text{K}$ . Combination

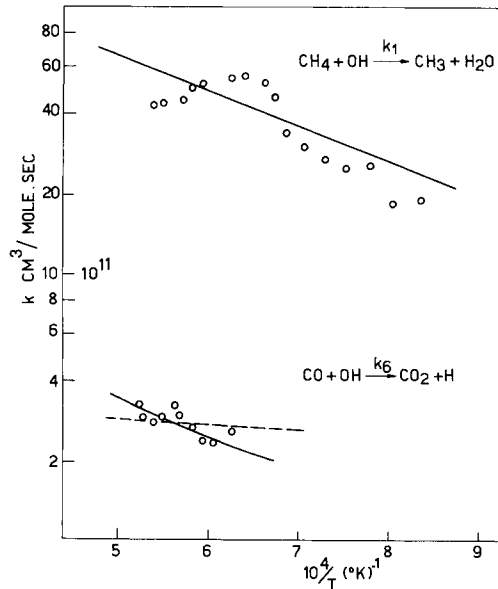


FIG. 5. Experimental values of the rate constants of Reactions [1] and [6] (lean-flame data).

(a)  $\text{CH}_4 + \text{OH} \rightarrow \text{CH}_3 + \text{H}_2\text{O}$ :

$$k_1 = 3 \times 10^{13} \exp(-6000/RT) \text{ mole}^{-1} \text{ cm}^3 \text{sec}^{-1}.$$

(b)  $\text{CO} + \text{OH} \rightarrow \text{CO}_2 + \text{H}$ :

$$--- k_6 = 3.5 \times 10^{11} \exp(-800/RT)$$

(in combination with result at 300°K of Ref. 19);

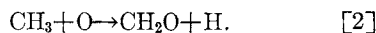
— Dryer's analytical expression (Ref. 20).

of our data with Westenberg's result<sup>13</sup> at 300°K yields:  $k_1 = 2.2 \times 10^{13} \exp(-5000/RT)$ .

In the stoichiometric flame, the rate of destruction of  $\text{CH}_4$  by H is about equal to that by OH. At  $T = 1600^\circ\text{K}$ , the rate constant of Reaction [1'] was found to be  $k_1' = 3.2 (\pm 0.6) \times 10^{12}$ , in excellent agreement with Walker's expression<sup>14</sup>:  $k_1' = 1.26 \times 10^{14} \exp(-11,900/RT)$ .

$\text{CH}_3$

Our results allow us to conclude definitively that  $\text{CH}_3$  is mainly removed by O atoms, in lean flames as well as in stoichiometric flames

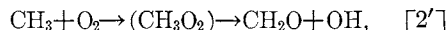


The conclusive proof follows from the  $\text{X}_{\text{CH}_3}$ ,  $\text{X}_{\text{O}}$  and  $\text{X}_{\text{O}_2}$  values in the lean and stoichiometric flames. At the point where  $K_{\text{CH}_3}$  vanishes,  $-K_{\text{CH}_4} = k_2[\text{CH}_3][\text{Z}]$ , with Z being either O or  $\text{O}_2$ ;  $\text{X}_{\text{CH}_3}$  is 2.3 times larger in the stoichiometric flame than in the lean one,  $\text{X}_{\text{O}}$  is 2.8 times smaller, and  $\text{X}_{\text{O}_2}$  is 7.8 times smaller, whereas the  $K_{\text{CH}_4}$  values and the temperatures are about equal. Clearly, only the product  $[\text{CH}_3][\text{O}]$  correlates with  $-K_{\text{CH}_4}$  and, hence, with the  $\text{CH}_3$ -removal rate.

Furthermore, one has in lean flames, at each point:

$$k_2/k_1 = \frac{\{[\text{OH}] + (k_1''/k_1)[\text{O}]\}[\text{CH}_4]}{[\text{CH}_3][\text{Z}]} - \frac{K_{\text{CH}_3}}{k_1[\text{CH}_3][\text{Z}]} \quad (3)$$

Supposing  $\text{Z} = \text{O}_2$ ,



the  $k_2'/k_1$  values could not be fitted to an  $\exp(-\Delta E/RT)$  type function, as is shown in Fig. 6, and a much-too-large frequency factor would be required for  $k_2'$  (exceeding  $10^{15} \text{ mole}^{-1} \text{ cm}^3 \text{ sec}^{-1}$ ). Only when  $[\text{O}]$  is still very small could an appreciable fraction of  $\text{CH}_3$  perhaps react with  $\text{O}_2$ , explaining in this way the presence of some  $\text{CH}_3\text{O}_2$  in the earlier stages of the flame (see Fig. 2). With  $\text{Z} = \text{atomic oxygen}$ , however, the  $k_2/k_1$  values were found to fit perfectly to an  $\exp(-\Delta E/RT)$  type function (see Fig. 6), with  $k_2 = 1.3 \times 10^{14} \exp(-2000/RT)$ . This expression also agrees well with the low-temperature result of Niki *et al.*,<sup>15</sup> and with Clark's value<sup>16</sup> at 1500°K. The kinetic coefficient of [2] appears to be about 20 times larger than that of  $\text{CH}_3 + \text{OH} \rightarrow \dots$ .<sup>17</sup>

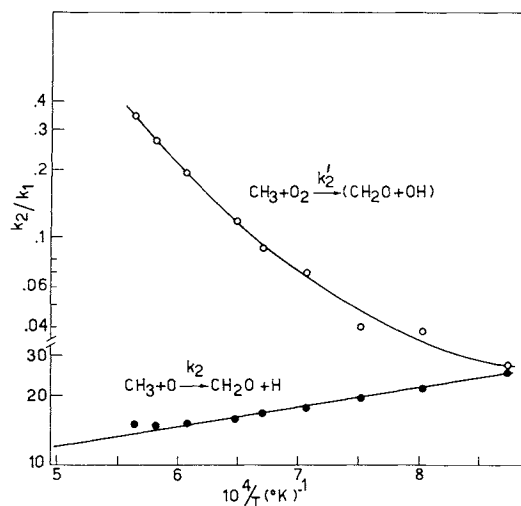
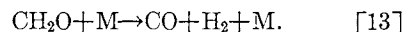


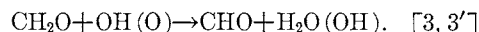
FIG. 6.  $\log k_2/k_1$  and  $\log k_2'/k_1$  versus  $1/T$  (see text);  $k_2/k_1 = 4.4 \exp(4000/RT)$ .

$\text{CH}_2\text{O}$ ,  $\text{CHO}$ , and  $\text{HO}_2$

As shown below, an appreciable fraction (40% in the lean flame) of the formaldehyde disappears by thermal decomposition:

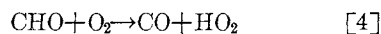


Our results indicate also that, in lean flames, the remainder reacts predominantly with OH, and a smaller part reacting with O



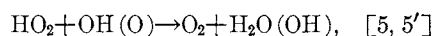
The rate constant of [3] was found to be about  $2.5 \times 10^{13}$  at  $T = 1600^\circ\text{K}$ , with an activation energy near 1 kcal/mole. The kinetic coefficient of [3'] is therefore about  $10^{13}$ .

The CHO mole fraction ( $\approx 10^{-5}$  in the lean flame and  $5 \times 10^{-5}$  in the stoichiometric flame) remains so low that only  $\text{O}_2$  can be considered as the reaction partner,



with  $k_4 \approx 3 \times 10^{13}$  at  $1400^\circ\text{K} < T < 1800^\circ\text{K}$ .

The hydroperoxyl radical reacts in the lean flame, mainly with O and OH,



with measured rate constants  $k_5 \approx 5 \times 10^{13}$  (assumed identical for OH and O) at  $T = 1400^\circ\text{K}$ .

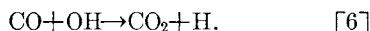
1800°K. The rate constant of



has been estimated<sup>18</sup> to be  $7 \times 10^{13}$ .

#### CO and CO<sub>2</sub>

Our results demonstrate that, except perhaps for a few percent, all CO<sub>2</sub> is formed via



The rate constant was evaluated taking the reverse reaction into account. In the range  $T = 1600^\circ\text{--}1900^\circ\text{K}$ , as shown in Fig. 5,  $k_6 = 2.8 (\pm 0.5) \times 10^{11}$ . Combination with Greiner's result<sup>19</sup> at 300°K yields  $k_6 = 3.5 \times 10^{11} \exp(-800/RT)$ . However, our results fit better to Dryer's "variable activation energy" expression,<sup>20</sup> predicting an  $E$  value of about 5.5 kcal/mole in the range  $T = 1600^\circ\text{--}1900^\circ\text{K}$  (see Fig. 5).

The fact that the experimental  $k_6$  values in the postcombustion zone remain constant up to a point where the reaction is only some 30% from complete equilibrium, demonstrates the precision of the mole fraction data for OH and H.

#### H<sub>2</sub>/O<sub>2</sub>-System Reactions

Using, directly, the mass-spectrometer output currents, it was found that, in the constant  $T$  region ( $T = 1900^\circ\text{K}$ ,  $z = 1.2\text{--}3.2$  cm) of the lean-CH<sub>4</sub>/O<sub>2</sub> flame, the ratios

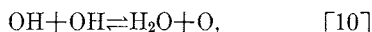
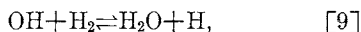
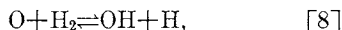
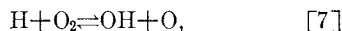
$$(i_{\text{O}} \cdot i_{\text{OH}}) / (i_{\text{H}} \cdot i_{\text{O}_2}),$$

$$(i_{\text{OH}} \cdot i_{\text{H}}) / (i_{\text{O}} \cdot i_{\text{H}_2}),$$

and

$$(i_{\text{H}} \cdot i_{\text{H}_2\text{O}}) / (i_{\text{OH}} \cdot i_{\text{H}_2}),$$

remained constant to within 5%. The individual O, H, and OH currents, however, decreased appreciably. It was concluded, therefore, that the four reactions



were fully balanced in the specified region. This fact enabled us to compute precise calibration factors for H, O, and OH.

The same reactions were also very nearly

balanced in the burned gas of the stoichiometric flame.

In the lean-flame reaction zone, Reaction [7] is never less than 50% balanced. Using the known rate constant<sup>21</sup> and the equilibrium constant, the net O<sub>2</sub>-removal rate computed by [7] is about 70% of the measured O<sub>2</sub>-disappearance rate in the region where [7] is less than 90% balanced (up to  $z = 0.4$  cm). It should be noted that, at 90% equilibrium, a 10°K error in  $T$  leads to a 30% error in the computed rate.

The other H<sub>2</sub>/O<sub>2</sub>-system reactions are also quite fast, in particular [9] and [10].

In order to check the mechanism of the degradation of CH<sub>4</sub> to CO, the flame reactions were divided into two groups, the first one comprising the CH<sub>4</sub>→CO conversion reactions, and the second group the Reactions [6]–[10].

The basic idea is that the amount of H<sub>2</sub>O, H<sub>2</sub>, OH, O, and H produced (or destroyed) by the first group of reactions can be evaluated indirectly by subtracting the rates of formation or removal of these species by the second group from the net observed reaction rates.

The net rates of [8], [9], and [10] were computed, using the known rate constants<sup>21–24</sup> and the equilibrium constants, whereas the net rates of [6] and [7] were derived from the observed CO<sub>2</sub> and O<sub>2</sub> mole flux gradients. Thus, it was found that the CH<sub>4</sub>→CO degradation reactions result in the formation of 1.4 H<sub>2</sub>O, 0.75 H, and 0.5 H<sub>2</sub> particles and the destruction of 0.65 OH and 1.7 O particles per CH<sub>4</sub> molecule consumed in the lean flame.

These "over-all stoichiometric coefficients" correspond to the mechanism comprising the Reactions [1]–[5], such that, in the lean flame, (i) CH<sub>4</sub> reacts 75% with OH, 15% with O, and 10% with H (based on known or derived rate constants); (ii) CH<sub>3</sub> is destroyed by O atoms; (iii) CH<sub>2</sub>O disappears 40% by thermal decomposition (see below), 40% by reaction with OH, and 20% by O attack (based on total OH and O reaction rates); (iv) CHO reacts with O<sub>2</sub>; (v) HO<sub>2</sub> is destroyed 45% by OH, 40% by O (rate constants assumed equal), and 15% by H (rate constant known<sup>18</sup>).

It should be noted that the net O, OH, and H reaction rates are initially negative, and that they vanish at the point where the CH<sub>4</sub> removal rate peaks (see  $F_{\text{OH}}$ ,  $F_{\text{H}}$  and  $F_{\text{O}}$  in Fig. 4).

#### Radical and Atom Decay

The "pool" concept<sup>25,26</sup> was used to investigate radical and atom decay in the burned gas region. However, since that concept was found to be useful also in connection with the highly im-

portant question of the formation of atoms and radicals (see below), a concise new derivation of the "pool laws" and of their implications will first be given here.

The "pool laws" are simply linear combinations of the element conservation laws and of the expression for the conservation of the total number of chemical bonds in a system, the latter being valid only if solely binary reactions of the type  $A+B \rightarrow C+D$  occur. If  $\bar{F}(C_xH_yO_z)_i$  is the mole flux of the  $i$ th species, containing  $b_i$  chemical bonds (whether single or multiple), any linear combination of the four conservation equations,

$$F_p = p_i \sum_i x_i \bar{F}(C_xH_yO_z)_i + q_i \sum_i y_i \bar{F}_i + r_i \sum_i z_i \bar{F}_i + s_i \sum_i b_i \bar{F}_i, \quad (4)$$

can be written as a weighted sum of mole fluxes, or as a species pool flux,

$$F_p = \sum_i [(px_i + qy_i + rz_i + sb_i) \bar{F}(C_xH_yO_z)_i], \quad (5)$$

each species having a weight factor

$$m_i = px_i + qy_i + rz_i + sb_i. \quad (6)$$

A pool flux that is of particular interest is one with  $m_i = 0$  for all major products. For a lean flame, where the  $m_i$  values of  $O_2$ ,  $CO_2$ , and  $H_2O$  should be zero, it is easily found, using Eq. (6), that the relevant pool is a linear combination, Eq. (4), with coefficients  $p=4$ ,  $q=3$ ,  $r=2$ , and  $s=-4$ , one of these being chosen arbitrarily:

$$m_i = 4x_i + 3y_i + 2z_i - 4b_i. \quad (7)$$

Therefore, in the burned gas of a lean- $CH_4/O_2$  flame, using Eq. (7), one has

$$F_p = 3F_H + 2F_{CO} + 2F_{H_2} + 2F_O + F_{OH}. \quad (8)$$

Obviously,  $F_p$  should remain rigorously constant unless reactions occur with a change in the number of chemical bonds or, what amounts to the same in the absence of cyclic compounds, with a change in the number of particles. In that case, the chemical rate of change of the pool,  $K_p = (1/A)(dF_p/dz)$ , is equal to  $-4$  (the value of the coefficient  $s$ ) times the net rate of formation of chemical bonds, or four times the net production rate of particles.

In the lean-flame burned gas, the pool decay

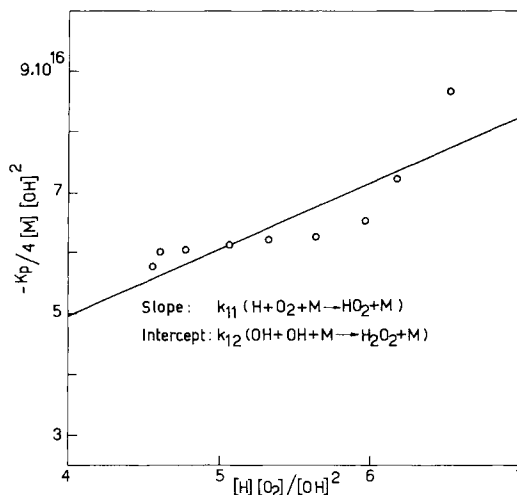
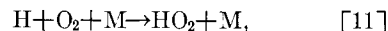
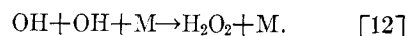


FIG. 7. Rate constants of  $H+O_2+M \rightarrow HO_2+M$ :  $k_{11} = 1.12 \times 10^{16} \text{ mole}^{-2} \text{ cm}^6 \text{ sec}^{-1}$ ; and of  $OH+OH+M \rightarrow H_2O_2+M$ :  $k_{12} \approx 0.5 \times 10^{16}$ ;  $K_p = (1/A) \times (dF_p/dz)$  (lean-flame data in the region  $d = 1.2-4.5 \text{ cm}$ );  $T = 1900^\circ\text{K}$ ; burned gas composition:  $X_{O_2} = 0.69$ ,  $X_{H_2O} = 0.18$ ,  $X_{CO_2} = 0.093$ .

is consistent with the recombination process



and, to a lesser extent, with



In Fig. 7,  $-K_p/(4[M][OH]^2)$  is plotted versus  $[H][O_2]/[OH]^2$ , the slope of the resulting straight line being equal to the rate constant of [11]:  $k_{11} = 1.12 \times 10^{16} \text{ mole}^{-2} \text{ cm}^6 \text{ sec}^{-1}$ , and the ordinate intercept to  $k_{12} \approx 0.5 \times 10^{16}$ . Using the known relative efficiencies<sup>21</sup> of  $O_2$ ,  $H_2O$ , and  $CO_2$  as the third body, it follows that  $k_{11}(M=O_2) = 2.5 \times 10^{15}$  at  $T = 1900^\circ\text{K}$ .

#### The Rate-Determining Step

In the reaction zone of a lean- $CH_4/O_2$  flame, the pool flux given by Eq. (5), using the  $m_i$  values of Eq. (7), is equal to

$$F_p = 3F_H + 2F_O + F_{OH} + 2F_{H_2} + 2F_{CO} + F_{CH_4}. \quad (9)$$

The  $m_i$  values of  $CH_4$ ,  $O_2$ ,  $CH_2O$ ,  $H_2O$ , and  $CO_2$  are indeed zero, and the species with  $X < 10^{-4}$  were neglected. Equation (9) shows that if the active species necessary for flame propagation,

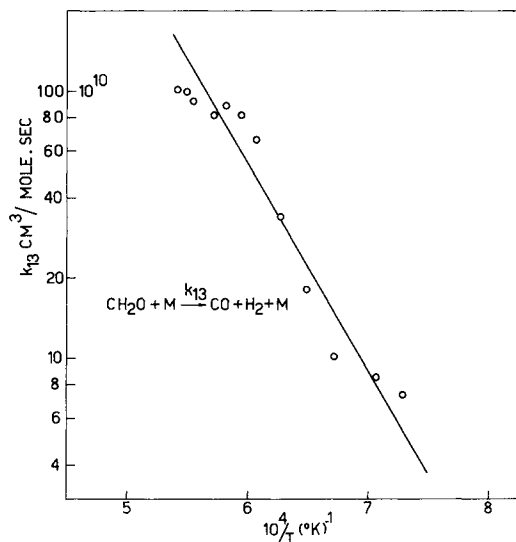
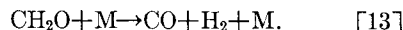


FIG. 8. Log  $k_{13}$  versus  $1/T$ ;  
 $k_{13} = (dF_p/dz)/(4A[\text{CH}_2\text{O}][\text{M}]$  (lean-flame data);  
 $k_{13} \approx 2.1 \times 10^{16} \exp(-35,000/RT) \text{ mole}^{-1} \text{ cm}^3 \text{ sec}^{-1}$ .

OH, O, and H, are to be present in the flame at all, the value of  $F_p$  must be positive. Since its value is zero in the fresh gases of a  $\text{CH}_4/\text{O}_2$  flame, OH, O, and H cannot have formed, and a flame cannot exist, unless a reaction occurs that decreases the number of chemical bonds (see above). Such a reaction can be either a thermal decomposition process or an  $A+B \rightarrow C+D+E$  type reaction.

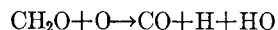
A body of evidence has been gathered that, in  $\text{CH}_4/\text{O}_2$  flames, this process—the real rate-determining step, as can be shown<sup>29</sup>—is the reaction



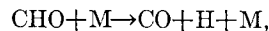
Its rate being equal to  $K_p/4 = (1/4A)(dF_p/dz)$ , it could be found from the pool flux (see Fig. 4) that 40% of the fuel is oxidized in the lean flame, according to a scheme comprising the decomposition process. The rate constant of [13] was also determined from the  $F_p$  gradient:  $k_{13} \approx 2.1 \times 10^{16} \exp(-35,000/RT)$  (see Fig. 8), with a possible error of 5 kcal/mole in the activation energy.

One of the arguments for Reaction [13] is that it explains quantitatively the formation via the  $\text{CH}_4 \rightarrow \text{CO}$  conversion reactions of about 0.5  $\text{H}_2$  molecules per  $\text{CH}_4$  molecule consumed (see above). Another argument is that the derived activation energy is in good agreement with the

over-all “activation energy” of lean- $\text{CH}_4/\text{O}_2$  flames (about 40 kcal/mole). On that basis also, a low-activation-energy reaction such as

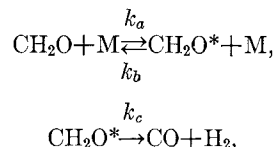


must be rejected as the rate-determining step. The same applies to



with an activation energy<sup>27</sup> of only 15 kcal/mole. Moreover, using the known rate constant<sup>27,28</sup> of that reaction, it is found that the CHO mole fraction required to account for the observed rate of increase of the pool flux is about twenty times the measured value in the lean flame, and about five times the actual value in the stoichiometric flame. Reaction [13], on the other hand, is consistent with the experimental pool flux increase in both these flames.

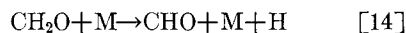
Accepting a Lindemann-Hinshelwood mechanism for Reaction [13],



it might be argued that the pressure at which the transition to first-order kinetics occurs is quite low ( $P_{1/2} < 1 \text{ atm}$ ), since  $k_c$  is probably small. First-order kinetics for Reaction [13] would explain the observed<sup>1</sup> pressure dependence of the burning velocity of  $\text{CH}_4/\text{O}_2$  flames ( $\sim p^{-1/2}$ ).

It appears then that the rate-determining decomposition process in  $\text{CH}_4/\text{O}_2$  flames is probably Reaction [13] (pseudomonomolecular or bimolecular); however, no direct proof could be found as yet.

The rate constant  $k_{13}$  reported here is some 3 orders-of-magnitude larger than the values given by Gay *et al.*,<sup>30</sup> and by Schecker and Jost,<sup>31</sup> for the kinetic coefficient of the decomposition of formaldehyde. Moreover, these authors consider



to be the major decomposition path. In shock-tube studies,  $\text{CH}_2\text{O} + \text{M} \rightarrow \text{CO} + \text{H}_2 + \text{M}$  cannot contribute significantly to the removal of  $\text{CH}_2\text{O}$ —even if it were somewhat faster than Reaction [14]—since the major part of the  $\text{CH}_2\text{O}$  is con-



sumed by H atoms in a chain mechanism initiated by Reaction [14].

The much larger rate of decomposition in flames may be due to the fact that  $\text{CH}_2\text{O}$  is formed here (together with an H atom) by a highly exothermic process (Reaction [2] with  $\Delta H = -67$  kcal/mole), while at the same time its average lifetime in the flame is only  $5 \times 10^{-6}$  sec, during which it undergoes only some 700 collisions. It might be argued, therefore, that the  $\text{CH}_2\text{O}$  in the flame front is vibrationally quite "hot," resulting in an appreciable decrease of the activation energy and, hence, a much larger rate of decomposition. Moreover, the results of Refs. 30 and 31 were obtained with Ne or Ar as diluents, whereas in the flames investigated here the "third body" is mainly  $\text{O}_2$ ,  $\text{H}_2\text{O}$ , and  $\text{CO}_2$ . Many instances are known where such species are an order-of-magnitude more effective than Ne or Ar.

To conclude, it can be shown<sup>29</sup> that a decomposition-type reaction is a *conditio sine qua non* for all hydrocarbon-oxygen flames, except for those burning hydrogen or acetylene, which are therefore both very fast flames.

#### Acknowledgments

The authors are greatly indebted to the late Professor A. Van Tiggelen for his stimulating interest and encouragement at the inception of this work. We express our thanks to Dr. P. J. Van Tiggelen for his valuable support and to Dr. C. Vinckier for his useful comments. One of us (J.P.) is grateful to the "Nationaal Fonds voor Wetenschappelijk Onderzoek." Financial support was received from the "Fonds voor Kollektief Fundamenteel Onderzoek—Fonds de la Recherche Fondamentale et Collective."

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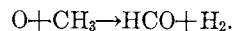
## COMMENTS

A. R. Hall, *Ministry of Defence, Rocket Propulsion Est., Westcott, Aylesbury, Bucks, England.* The illustration of your apparatus indicated the use of a supersonic, rather than an effusive, molecular beam for sampling the flame gases. Gordon J. Williams (in work to be reported elsewhere) has noted that the well-known mass-discrimination effects with such a beam depend on the composition, pressure, and temperature of the source gas, and on the distance between sample orifice and skimmer. How have you corrected for the effect in obtaining your concentration profiles, especially for the lower-molecular-weight constituents?

*Authors' Reply.* We have observed that, in our system, at source Knudsen Numbers of about 0.02 to 0.08, mass discrimination is adequately described (to within 5%) by the expression  $X_b/X_0 = M/\bar{M}$ , where  $X_b$  and  $X_0$  are the respective mole fractions in the beam and in the sample,  $M$  the molecular weight of the considered species, and  $\bar{M}$  the mean molecular weight of the mixture. No attempt was made yet to check this expression at higher or lower Knudsen Numbers, and the investigated molecular-weight range was rather limited (16 to 44). However, as both the pressure and the nozzle-skimmer distance were kept constant in our experiments, and since the effect of the composition on the mass discrimination was known (i.e., the mean molecular weight), we had to be concerned only with possible changes in the mass discrimination with temperature, which does vary considerably in the flame. Fortunately, there were no such changes, since, upon adding traces of argon and helium to the lean methane flame, it was found that the ratio of the beam signals of these species was the same behind the flame front (1900°K) as in the fresh gases (300°K). A slight discrepancy of about 5% could be ascribed entirely to radial thermal diffusion of helium toward the central, hotter parts of the flame. In our opinion, it is primarily due to the low jet density in front of the skimmer and to the absence of jet-skimmer interactions, that only the simple and easily understood type of mass discrimination occurs in our system.

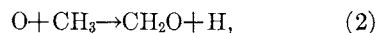
K. D. Bayes, *Dept. of Chemistry, University of California, Los Angeles, Cal.* In the room-temperature reaction of oxygen atoms with methane, we have observed directly the HCO radical (I. T. N. Jones & K. D. Bayes: *J. Am.*

*Chem. Soc.*, in press). The kinetic behavior of the HCO requires that it be formed in the reaction

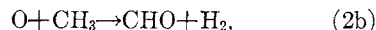


This is not necessarily the major reaction path, but it is significant. Would the inclusion of this source of HCO, and especially H<sub>2</sub>, alter your interpretation?

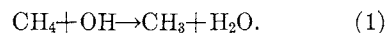
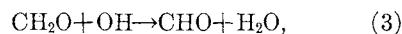
*Authors' Reply.* Our arguments for accepting



and not



as the major reaction path, are based on the following: the assumption that the sole product is CH<sub>2</sub>O leads to a reasonable value for the ratio  $k_3/k_1$ ,



At  $T = 1600^\circ\text{K}$ , we find  $k_3/k_1 = 6 \pm 2$  (assuming also that 40% of the CH<sub>2</sub>O disappears by thermal decomposition, and that  $k_3$  is at least as large as  $k_3'$ ).<sup>1</sup> This result is entirely consistent with the value  $k_3/k_1 = 33 \pm 3$  at  $T = 800^\circ\text{K}$ , as reported by Blundell *et al.*,<sup>2</sup> and with a ( $E_1 - E_3$ ) value of about 5 kcal/mole as found by us (an upper limit of  $E_3 \approx 2$  kcal/mole can also be inferred from the work of Herron *et al.*<sup>1</sup>).

However, the derived value of  $k_3/k_1$  would remain almost unchanged if it were assumed that Reaction (2b) accounts for 40% of the total CH<sub>3</sub> removal, and if, at the same time, thermal decomposition of CH<sub>2</sub>O (40% of its removal rate) were dropped entirely from the reaction scheme. It would be very tempting indeed to adopt this alternative—especially since it still explains, quantitatively, the observed H<sub>2</sub> production—if it were not for the difficulty of finding another decomposition reaction (within the pool concept) that fits the experimental results.

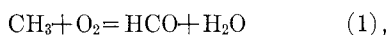
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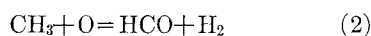
2. Blundell, R. V., Cook, W. G. A., Hoare, D. E., and Milne, G. S.: *Tenth Symposium (International) on Combustion*, p. 445, The Combustion Institute, 1965.

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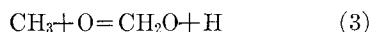
Dennis M. Zallen, *Purdue University, W. Lafayette, Ind.* There seems to be considerable disagreement with respect to the formaldehyde and formyl radical reactions being used in the methane-oxygen mechanisms. Skinner<sup>1</sup> completely deletes CH<sub>2</sub>O and HCO species, since relevant reactions occur in rapid succession and formaldehyde does nothing but decompose very rapidly. Bowman<sup>2</sup> also neglects CH<sub>2</sub>O, uses



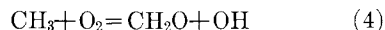
and neglects



during the induction period. Seery and Bowman<sup>3</sup> used



in addition to (1). Higgin and Williams<sup>4</sup> used



in place of (1), and Lifshitz<sup>5</sup> considers (4) to be one of the two predominant reactions controlling induction times. Asaba<sup>6</sup> considers the mechanism of oxidation of formaldehyde to explain the branching-chain type ignition and the activation energy. Would you please comment as to the importance of these species and the reactions necessary in methane-oxygen flames.

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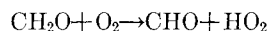
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*Authors' Reply.* As explained in our reply to Dr. Bayes' comment, our results strongly

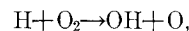
indicate that the larger part of the methyl radicals in the flame yield formaldehyde upon oxidation. Moreover, in the very lean to stoichiometric flames investigated by us, reaction between CH<sub>3</sub> and O<sub>2</sub> is negligible in the main reaction zone, as could be established beyond reasonable doubt. Indeed, in a series of four investigated flames, there was no correlation whatsoever between the [CH<sub>3</sub>][O<sub>2</sub>] product and the CH<sub>3</sub>-removal rate, whereas the latter was directly proportional (to within 15%) to the [CH<sub>3</sub>][O] product.

Most probably, however, matters are entirely different during induction periods of CH<sub>4</sub>/O<sub>2</sub> explosions, or during the exponential growth period behind shock waves: as long as [O<sub>2</sub>] is still very much larger (perhaps 1000 times) than [O], the reaction between CH<sub>3</sub> and O<sub>2</sub> must, of course, outrun that between CH<sub>3</sub> and O.

Although degenerate branching is probably important in low-temperature oxidation (and maybe also during ignition), it certainly is not in flames: due to the high activation energy of



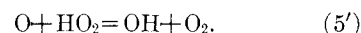
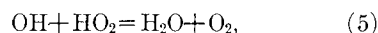
( $E \simeq 40$  kcal/mole), its rate is negligible compared to that of



which is indeed the fastest of all the reactions occurring in the flames investigated by us. This difference between low-temperature systems and flames is again the consequence of the strongly different concentrations of highly reactive species, such as H atoms.

↓

G. Dixon-Lewis, *Univ. of Leeds, England.* I am concerned about the high values quoted for the rate constants of the reactions:



Both of these are quoted as  $\simeq 5 \times 10^{13}$  at  $T = 1400^\circ - 1800^\circ \text{K}$ . Work on hydrogen-oxygen flames (This Symposium) suggests a *maximum* value of  $k_5 = 7 \times 10^{13}$  at around  $900^\circ \text{K}$ , assuming that  $k_{5'} = 0$ ; where another possible combination was  $k_5 = 4 \times 10^{12}$ , with  $k_{5'} = 3.3 \times 10^{13}$ ; activation energies were not high.

*Authors' Reply.* Assuming that  $k_{5'} = 0$ , the value of  $k_5$  required to account for the observed

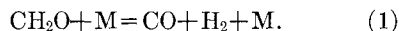
HO<sub>2</sub>-destruction rate in the lean flame would be about  $10^{14}$  at  $T=1600^\circ\text{K}$ . In my opinion, this upper limit agrees reasonably well with the analogous maximum value of  $7 \times 10^{13}$  at  $T=900^\circ\text{K}$ , reported by Dr. Dixon-Lewis.

It should be emphasized, however, that HO<sub>2</sub> is one of the few species (together with CHO, CH<sub>2</sub>, and CH<sub>3</sub>O<sub>2</sub>) for which concentrations had to be obtained from estimated ionization cross sections at ionizing electron energies a few eV above the threshold. When similar cross-section estimation methods were applied to O, OH, H, and CH<sub>3</sub>, concentrations were found that were, respectively, 1.5, 3, 1.1, and 2 times lower than the values obtained by calibration. The values of  $k_5$  and  $k_5'$  (and also of  $k_4$ ) reported here are, therefore, also expected to be in error by a factor of about 2.

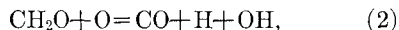
On the other hand, the results derived by Dr. Dixon-Lewis depend upon, among other things, the values of the rate constants of Reaction (5'') and upon those of reactions (7)-(9); not all of these are known as precisely as one might wish.

↓

*G. Dixon-Lewis.* I should like also to comment briefly, as well as to interject a word of caution, on two of the arguments advanced by the authors in connection with their proposed reaction:



First, the fact that the "over-all activation energy" of lean-CH<sub>4</sub>/O<sub>2</sub> flames is about 40 kcal mole<sup>-1</sup> leads them to the rejection of low-activation-energy reactions, such as



as steps determining the rate of growth of the radical pool. However, in the case of a rich-H<sub>2</sub>/O<sub>2</sub> supported flame, we have recently used a reaction mechanism having no step with activation energy greater than 16.5 kcal mole<sup>-1</sup>, in order to investigate the effect of a small change of initial temperature on the computed burning velocity.<sup>1</sup> The "over-all activation energy," obtained by plotting  $\log(S_{u,\text{calc}})^2$  against  $1/T_b$ , turned out to be around 50 kcal mole<sup>-1</sup>. Clearly, in the H<sub>2</sub>/O<sub>2</sub> case, an argument involving an over-all activation energy would have led to an incorrect conclusion, and it may be that such arguments are generally invalid.

The second point concerns the pressure dependence of burning velocity, for which global reaction-rate approaches, such as those of

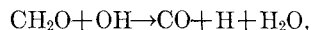
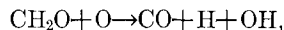
Zeldowich, Semenov, and Frank-Kamenetskii, predict  $S_u \propto p^{-1/2}$  for first order, and  $S_u$  independent of pressure for second-order kinetics. On the basis of these results, Peeters and Mahnen use the observed pressure dependence of CH<sub>4</sub>/O<sub>2</sub> burning velocities ( $\sim p^{-1/2}$ ) to argue that their radical pool-controlling step probably is first order, i.e., a pseudounimolecular decomposition. However, detailed computation on a single H<sub>2</sub>/O<sub>2</sub> flame<sup>2</sup> again does not support the conclusions of the global reaction approaches. Instead, it was found that, for a flame mechanism containing only a mixture of second- and third-order reactions,  $S_{u,\text{calc}} \propto p^{-1/4}$ , approximately. Extreme caution is therefore necessary in drawing conclusions about elementary reaction steps from these over-all flame properties.

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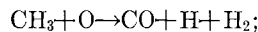
1. Day, M. J., Dixon-Lewis, G., and Thompson, K.: Proc. Roy. Soc. (London), In press.
2. Dixon-Lewis, G., Isles, G. L., and Walmsley, R.: Proc. Roy. Soc. (London), In press.

*Authors' Reply.* The computed results for the "over-all activation energy" of the rich H<sub>2</sub>/O<sub>2</sub> flame are indeed unexpected, and should weaken our confidence in arguments based on over-all flame properties. It is puzzling, however, that the measured "over-all activation energy" of hotter, near-stoichiometric H<sub>2</sub>/O<sub>2</sub>/N<sub>2</sub> flames is much lower (about 20 kcal/mole).<sup>1</sup>

Nevertheless, there remain other arguments against the importance of the reactions



and also



for their rates to match the observed pool-growth profile, activation energies of about 15 to 20 kcal/mole and preexponential factors of about  $10^{15}$  cm<sup>3</sup> mole<sup>-1</sup> sec<sup>-1</sup>, or larger, would be required.

The computed negative-pressure dependence of the H<sub>2</sub>/O<sub>2</sub> burning velocities ( $\sim p^{-1/4}$ ) is due to third-order chain-termination processes. In the 40-torr CH<sub>4</sub>/O<sub>2</sub> flames, however, the rate of the fastest termolecular recombination reactions is only 1% of that of the bimolecular branching and termination processes. It is justified, then, in my opinion, to neglect the third-order processes, also, in the reaction zone of CH<sub>4</sub> flames burning at 0.25 atm, where their rates can be estimated to be about 5% of the bimolecular

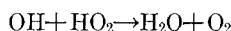
termination rates. It can be shown, using the complete set of differential equations describing a flame, that the eigenvalue for the burning velocity is rigorously independent of the pressure if all reactions are bimolecular. However, according to the most-recent measurements,<sup>2</sup> the  $p^{-1/2}$  pressure dependence of methane-air burning velocities persists even down to 0.25 atm, the lowest investigated pressure.

## REFERENCES

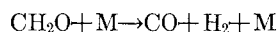
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2. Bradley, D. and Hundy, G-F.: *Thirteenth Symposium (International) on Combustion*, p. 575, The Combustion Institute, 1971.

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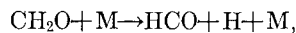
J. Troe, *Institut de Chimie-Physique de l'EPF-Lausanne, Avenue des Bains 31 1007 Lausanne, Switzerland*. From our investigation<sup>1</sup> of HO<sub>2</sub> profiles in the thermal dissociation of H<sub>2</sub>O<sub>2</sub> near 1400°K, we had to conclude that the rate constant of



is about  $10^{13.0 \pm 0.3} \text{ cm}^3 \text{ mole}^{-1} \text{ sec}^{-1}$ . With your high value of  $k_5 \simeq 10^{13.7} \text{ cm}^3 \text{ mole}^{-1} \text{ sec}^{-1}$ , we would have seen much smaller HO<sub>2</sub> concentrations than actually observed. Since your apparent rate constant for



differs considerably from the rate constant of the unimolecular dissociation,<sup>2</sup>



it rather corresponds to a complex dissociation path.

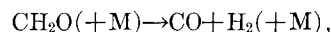
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1. J. Troe: *Ber. Bunsenges. Physik. Chem.* 73, 946 (1969).
2. H. G. Schecker and W. Jost: *Ber. Bunsenges. Physik. Chem.* 73, 521 (1969).

*Authors' Reply.* Our value of  $k(\text{OH} + \text{HO}_2)$  is estimated to be good within a factor of 2. Kaufman<sup>1</sup> estimates a value of  $k(\text{OH} + \text{HO}_2) \geq 6 \times 10^{12} \text{ cm}^3 \text{ mole}^{-1} \text{ sec}^{-1}$  at 300°K; combination with our

results at 1600°K yields a reasonable activation energy  $\leq 1.5 \text{ kcal/mole}$ .

It should be emphasized that we have not directly observed decomposition of CH<sub>2</sub>O. Rather, we ascribe the mole change observed in the flame to the specific process

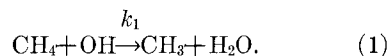


as this reaction appears to satisfy the experimental results. Possible reasons for our high value of the rate constant are given in the paper.

## REFERENCE

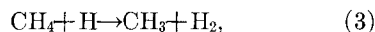
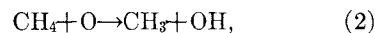
1. Kaufman, F.: *Ann. Geophys.* 20, 106 (1964).

F. L. Dryer, *Guggenheim Laboratories, Princeton University, Princeton, N.J.* Would the authors care to comment on the limits of error associated with their reported rate constant for the reaction



You have noted throughout the region of methane consumption, equal concentrations of oxygen atoms and hydroxyl radicals; furthermore, in the initial stages of reactions, the concentration of H atoms was not negligible compared to [O] or [OH].

If one accepts recent literature values for  $k_1$ ,<sup>1</sup>  $k_2$ ,<sup>2</sup> and  $k_3$ ,<sup>3</sup>



it is apparent that Reaction (1) should account for no more than 60%, and as little as 40% of your observed methane consumption rate, depending upon the position in the flame. If this is the case, your evaluation of (1) intrinsically contains errors associated with Reactions (2) and (3). Herron<sup>2</sup> has suggested that the evaluation of  $k_2$  is good to within a factor of 1.5 at your temperatures, while Kurylo and Timmons<sup>3</sup> suggest the value of  $k_3$  is determined to within a factor of 2.

Admittedly, linear extrapolation of Greiner's results from 500°K to ~1200°K on an Arrhenius plot must be met with some skepticism. However, it appears that no reasonable pre-exponential temperature dependence of  $k_1$  can reconcile your reported measurements of  $k_1$  with those of Greiner, especially when one considers that Reactions (2) and (3) must have some pre-exponential temperature dependence themselves.

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1. N. R. Greiner: J. Chem. Phys. *53*, 1070 (1970).
2. J. T. Herron: Intern. J. Chem. Kinetics *1*, 527 (1969).
3. M. J. Kurylo and R. B. Timmons: J. Chem. Phys. *50*, 5076 (1969).

*Authors' Reply.* Our value of  $k(\text{CH}_4 + \text{OH})$  depends primarily on the shape and position of the profiles of the methane disappearance rate and of the OH concentration. Combined systematic errors amount here to at most 25%. Taking the respective rate constants and their error limits from the sources quoted by Dr. Dryer, the combined rates of  $\text{CH}_4 + \text{O}$  and  $\text{CH}_4 + \text{H}$  are, on the average,  $20 \pm 10\%$  of the total observed  $\text{CH}_4$ -disappearance rate. In the worst case, therefore, our smoothed  $k(\text{CH}_4 + \text{OH})$  value might be too high or too low by a factor of 1.5. In fact, in our derivation, we have neglected the small ( $\pm 6\%$ ) contribution of  $\text{CH}_4 + \text{H}$ .

Even when the upper limits of the respective rate constants are used to evaluate the contributions of  $\text{CH}_4 + \text{O}$  and  $\text{CH}_4 + \text{H}$ , Greiner's value of  $k(\text{CH}_4 + \text{OH})$  is still too low, by a factor of 3.5, to account for the remainder (70%) of the observed  $\text{CH}_4$ -disappearance rate. In his paper, Greiner notes that the extrapolation above 500°K of his Arrhenius lines predicts  $k(\text{CH}_4 + \text{OH})$  and also  $k(\text{H}_2 + \text{OH})$  values that are a factor of 3 lower than the combustion data, and therefore further experimental work may be necessary.

It is worthwhile to point out that the recent data of Horne and Norrish<sup>1</sup> support our higher value of  $k(\text{CH}_4 + \text{OH})$ .

## REFERENCE

1. Horne, D. G. and Norrish, R. G. W.: Nature, *215*, 1373 (1967).

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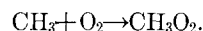
*J. E. Dove, Dept. of Chemistry, University of Toronto, Toronto, Ontario, Canada.* The authors' application of the "pool" concept of Kaskan and Schott is very interesting. When trying to elucidate the kinetic behavior of an over-all reaction whose mechanism is incompletely known, the

use of the pool concept may well be more immediately fruitful than, e.g., computer calculations based on large systems of rate equations.

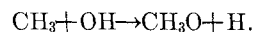
It should be borne in mind that, in the pool law, many species which could be present in this system, such as  $\text{HO}_2$ ,  $\text{CH}_3\text{O}$ , and  $\text{CH}_3\text{O}_2$ , have negative values of  $m$ . Formation of these species would allow the concentrations of other reactive species to increase without violating the pool law. Presumably, the concentrations of species with negative  $m$  are much too small to account directly for the observed apparent rapid increase in the pool. However, the formation and subsequent rapid decomposition of a species such as  $\text{CH}_3\text{O}_2$  might still be important in forming the pool.

*Authors' Reply.* The maximum sum of the observed mole fluxes of  $\text{HO}_2$  and  $\text{CH}_3\text{O}_2$  (both with  $m = -1$ ) is 2 to 3 orders of magnitude less than the value of the pool flux. Therefore, these species could indeed be neglected.

It should be emphasized that the total observed rate of decomposition is very large in the flame: on the average, about 40% of the  $\text{CH}_4$ -destruction rate. Therefore, only fast processes need be considered. It is highly unlikely that  $\text{CH}_3\text{O}_2$  is formed in a fast reaction; moreover, the small observed amount of  $\text{CH}_3\text{O}_2$  is most probably formed in a reaction that decreases the pool,



In this respect, matters might be different for  $\text{CH}_3\text{O}$ : one could indeed have



The rate constant of  $\text{CH}_3 + \text{OH}$ , however, as measured by Fenimore,<sup>1</sup> is about 6 times too low to account for the observed pool-flux growth, even when one assumes that  $\text{CH}_3\text{O}$  and H are the sole products and that all  $\text{CH}_3\text{O}$  decomposes (into  $\text{CH}_2\text{O} + \text{H}$ ).

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