

$$1. \mu = IA, \quad I = q \frac{\Omega}{2\pi} = \frac{q^2 B}{2\pi m}, \quad A = \pi r^2 = \pi \frac{m^2 v_{\perp}^2}{q^2 B^2}. \quad (r = \frac{mv_{\perp}}{qB})$$

$$= \frac{W_{\perp}}{B}, \quad W_{\perp} = \frac{1}{2} m v_{\perp}^2 \text{ 横向动能. } ①$$

$$dW_{\perp} = qE \cdot dr_{\perp}, \quad dr_{\perp} = v_{\perp} dt.$$

$$\text{回旋一周: } \Delta W_{\perp} = \int_0^{2\pi/\Omega} qE \cdot v_{\perp} dt$$

$$\text{由于磁场缓慢, 所以 } \Delta W_{\perp} \approx q \oint_L E \cdot dl = q \iint_S (\nabla \times E) \cdot dS = -q \iint_S \frac{\partial B}{\partial t} \cdot dS.$$

$$\rightarrow \Delta W_{\perp} = q \cdot \pi r^2 \frac{dB}{dt}.$$

$$\frac{dW_{\perp}}{dt} \approx \frac{\Delta W_{\perp}}{T}, \quad T = \frac{2\pi r}{v_{\perp}} = \frac{2\pi m}{qB}.$$

$$\approx \frac{m v_{\perp}^2}{2B} \frac{dB}{dt} = \mu \frac{dB}{dt}. \quad ②$$

$$\text{由 ① 式: } dW_{\perp} = B \frac{d\mu}{dt} + \mu \frac{dB}{dt}. \quad ③$$

$$\text{由 ②, ③ 式: } \frac{d\mu}{dt} = 0.$$