

7.4.

$$\text{10. } \nabla \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t} = \sigma \vec{E} + \epsilon \frac{\partial \vec{E}}{\partial t} = \sigma \vec{E} - i\omega \epsilon \vec{E} = -i\omega \left( i\frac{\sigma}{\omega} + \epsilon \right) \vec{E}.$$

$$n = \sqrt{\frac{\epsilon_1}{\epsilon_0}} = \sqrt{\frac{i\sigma}{\omega} + \epsilon}$$

$$Ae^{i\varphi} = \frac{E_r}{E_i} = \frac{1-n}{1+n} = \frac{\sqrt{\epsilon_0} - \sqrt{i\frac{\sigma}{\omega} + \epsilon}}{\sqrt{\epsilon_0} + \sqrt{i\frac{\sigma}{\omega} + \epsilon}}$$

(b).

$$\frac{\sqrt{\epsilon_0} - \sqrt{i\frac{\sigma}{\omega} + \epsilon}}{\sqrt{\epsilon_0} + \sqrt{i\frac{\sigma}{\omega} + \epsilon}} \approx 1 - \frac{1+i}{\sqrt{2}} \frac{\sqrt{\frac{\sigma}{\omega}}}{\sqrt{\epsilon_0}} = \frac{-(1+i) + \sqrt{2\frac{\sigma}{\omega}}}{1+i + \sqrt{2\frac{\sigma}{\omega}}}$$

$$R = |A|^2 = \frac{\left(\sqrt{\frac{\sigma\omega\epsilon_0}{6}} - 1\right)^2 + 1}{\left(\sqrt{\frac{\sigma\omega\epsilon_0}{6}} + 1\right)^2 + 1} = \frac{\frac{\sigma\omega\epsilon_0}{6} - 2\sqrt{\frac{\sigma\omega\epsilon_0}{6}} + 2}{\frac{\sigma\omega\epsilon_0}{6} + 2\sqrt{\frac{\sigma\omega\epsilon_0}{6}} + 2} \approx 1 - 2\sqrt{\frac{\sigma\omega\epsilon_0}{6}}$$

$$\approx 1 - 2\frac{\omega}{c} \delta. \quad \delta = \sqrt{\frac{2c^2\epsilon_0}{\omega\sigma}} = \sqrt{\frac{2}{\mu_0\omega\sigma}}$$

