

Opening Report of CRISPR/Cas9-based Screening Data Analysis

Y.Q. Yang

ABSTRACT

In the opening report, I did a brief academic research on sgRNA specific pooled library screening, and part of current algorithms including MAGeCK and BAGEL. Due to the difficulty of understanding these algorithm, I have problem finishing own-data analysis, which should be done in the work that follows.

Background

In the first week of starting this project, I think it necessary for understanding what CRISPR/Cas9-based genetic screening is, and what should be considered in analyzing the screening data. The idea of CRISPR/Cas9-based genetic screening was to use a pool of sgRNA-expressing lentivirus to generate a library of knockout cells that could be screened under both positive and negative selection.¹ In addition to transfection, Pooled screening can avoid experimental errors caused by high expression of sgRNA. However, the data generated by these screens pose several challenges to computational analysis. First, variance and statistical significance of comparisons between sample and control should be calculated under a extremely small sample size. Second, different sgRNAs target the same gene might have different specificities and knockout efficiencies, which should be taken into account in the algorithm. Third, the difference between read count distributions are significant, which calls for a robust normalization.²

Results

Detailed information about MAGeCK and BAGEL algorithms, which is concluded partially on my own opinion, is shown below.

Principles of MAGeCK Algorithm

Overview of MAGeCK Algorithm

A schematic of the MAGeCK Algorithm is presented as follow².

1. Read counts from different samples are median-normalized, which enables each sample to have the same median value.
2. A mean-variance model is established by following the **empirical** equation:

$$\hat{\sigma}^2 = \hat{\mu} + k\hat{\mu}^b \quad (1)$$

or

$$\log(\hat{\sigma}^2 - \hat{\mu}) = \log k + b \log \hat{\mu}, k \geq 0, b \geq 0 \quad (2)$$

In the above formula, $\hat{\sigma}$ represents sample variance, and $\hat{\mu}$ represents sample means. This approach aims to estimate the variance of the read counts within one condition in a small number of replicates.

3. The sample mean and variance obtained in the last step can be used as parameters of the negative binomial(NB)distribution, which is applied to rank sgRNA based on P-values calculated from the NB model. This model can be used in both positive and negative selection of each sgRNA.
4. Essential genes, which is targete by relatively huger amount of sgRNAs rank near the top of the sgRNA list generated in the last step, are identified using a modified robust ranking aggregation(RRA) algorithm.

Algorithm Characteristics

Negative Binomial Algorithm This algorithm particularly uses a negative binomial(NB) model to test whether each sgRNA abundance is significantly different between treatments and control based on the P-value calculated from the model². For a set of read counts of sgRNA i with replicates in two condition A and B(for example, in CRISPR/Cas9-treated samples and in control samples), the P-value is calculated as follow²:

$$p = \begin{cases} \sum_{x > \mu_{iB}} NB(x|\mu_{iA}, \sigma_{iA}^2), \mu_{iB} > \mu_{iA} \\ \sum_{x < \mu_{iB}} NB(x|\mu_{iA}, \sigma_{iA}^2), \mu_{iB} < \mu_{iA} \end{cases} \quad (3)$$

Where $NB(x|\mu_{iA}, \sigma_{iA}^2)$ is the probability mass function(PMF) of a read count x from the NB distribution with mean μ_{iA} and σ_{iA}^2 . It is applied to test whether the sgRNA is positively selected($\mu_{iB} > \mu_{iA}$) or negatively selected($\mu_{iB} < \mu_{iA}$).

Considering that the sample size of sgRNA-specific pooled screening is relatively small and discrete, commonly used probability distribution model such as binomial or Poisson, which is derived from large-sample asymptotic theory, may not appropriately model the count variability in RNA-Seq data.³ Current RNA-Seq methods, including FPKM and TPM, which have been introduced in class, typically normalize data by scaling the number of reads in a given lane or library to a common value across all sequenced libraries in the experiment. However, library size scaling is too simple for many biological conditions, true biological differences in RNA composition between samples will be the main reason for normalization. Depending on the experimental situation, Negative Binomial may be appropriate for the additional variation observed from biological replicates⁴.

Robust Ranking Aggregation(RRA) Algorithm⁴.

Essential genes are ranked separately using this algorithm. Suppose M sgRNAs are included in the experiment, and $R = (r_1, r_2, \dots, r_n)$ is the vector of ranks of n sgRNAs targeting a gene i ($n \ll M, r_i \ll M$). Firstly, the ranks are normalized into percentiles $U = (u_1, u_2, \dots, u_n)$, where $u_i = r_i/M$ ($i = 1, 2, \dots, n$). The k th smallest value among u_1, u_2, \dots, u_n is fit to a beta distribution with the null hypotheses as uniform distribution between 0 and 1. The significance score of the gene, the p value, is defined as $\rho = \min(\rho_1, \rho_2, \dots, \rho_n)$, where ρ_k is the P-value, which is based on the beta distribution, of the gene k .

Due to the incomparability of different gene expression levels caused by quite a number of factors such as differences in measurement platforms and lab protocols, finding a meaningful combination of different data sources is often a non-trivial task.⁵ Consequently, it might be better to analyze data from different genes separately and then aggregate the resulting gene lists.

Future Plan

For discovering MAGECK Algorithm:

- Learn more about Beta distribution;

References

1. Wang, T., Wei, J. J., Sabatini, D. M. & Lander, E. S. Genetic screens in human cells using the crispr-cas9 system. *Science* **343**, 80–84 (2014).
2. Li, W. *et al.* Mageck enables robust identification of essential genes from genome-scale crispr/cas9 knockout screens. *Genome biology* **15**, 554 (2014).
3. Di, Y., Schafer, D. W., Cumbie, J. S. & Chang, J. H. The nbp negative binomial model for assessing differential gene expression from rna-seq. *Stat. Appl. Genet. Mol. Biol.* **10** (2011).
4. Robinson, M. D. & Oshlack, A. A scaling normalization method for differential expression analysis of rna-seq data. *Genome biology* **11**, R25 (2010).
5. Kolde, R., Laur, S., Adler, P. & Vilo, J. Robust rank aggregation for gene list integration and meta-analysis. *Bioinformatics* **28**, 573–580, DOI: [10.1093/bioinformatics/btr709](https://doi.org/10.1093/bioinformatics/btr709) (2012). [/oup/backfile/content_public/journal/bioinformatics/28/4/10.1093_bioinformatics_btr709/2/btr709.pdf](http://oup/backfile/content_public/journal/bioinformatics/28/4/10.1093_bioinformatics_btr709/2/btr709.pdf).

LaTeX formats citations and references automatically using the bibliography records in your .bib file, which you can edit via the project menu. Use the cite command for an inline citation, e.g.

For data citations of datasets uploaded to e.g. *figshare*, please use the `howpublished` option in the bib entry to specify the platform and the link, as in the `Hao:gidmaps:2014` example in the sample bibliography file.

Acknowledgements (not compulsory)

Acknowledgements should be brief, and should not include thanks to anonymous referees and editors, or effusive comments. Grant or contribution numbers may be acknowledged.

Author contributions statement

Must include all authors, identified by initials, for example: A.A. conceived the experiment(s), A.A. and B.A. conducted the experiment(s), C.A. and D.A. analysed the results. All authors reviewed the manuscript.

Additional information

To include, in this order: **Accession codes** (where applicable); **Competing interests** (mandatory statement).
The corresponding author is responsible for submitting a [competing interests statement](#) on behalf of all authors of the paper. This statement must be included in the submitted article file.



Figure 1. Legend (350 words max). Example legend text.

Condition	n	p
A	5	0.1
B	10	0.01

Table 1. Legend (350 words max). Example legend text.

Figures and tables can be referenced in LaTeX using the ref command, e.g. Figure 1 and Table 1.