YANIS TAZI HOMEWORK. 2 DEEP LEARNING SYSTEMS

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Question 1)

Co-adaptation is when neurons depend highly on each other. This is a very important matters because one affected neuron (receiving bad input for example) will affect all the neurons that depend on this one and this is the kind of issue leading to overfitting for example.

Internal covariate shift refers to the change in the distribution of network activations due to change in network parameters during training. To reduce this, we can use normalization at each layer so that we achieve fix distribution of inputs for every layer. One of the most common technque is to use Batch normalization.

Internal covariate shift often leads to slow training and can create non convergence

Question 2)

Train LeNet 5:

```
In [56]: import tensorflow as tf
from sklearn.preprocessing import StandardScaler
from tensorflow.keras.models import Sequential
from tensorflow.keras import models, layers
import tensorflow.keras as keras
from tensorflow.keras.layers import BatchNormalization, LayerNormalizati
on
import tensorflow as tf
from tensorflow.keras.layers import Dropout
import matplotlib.pyplot as plt
if tf.test.gpu_device_name():
    print('Default GPU Device: {}'.format(tf.test.gpu_device_name()))
else:
    print("Please install GPU version of TF")
```

Please install GPU version of TF

Model 1: Standard normalization for input layer and batch normalization for hidden layers

a) Data with standard normalization

```
In [2]: # Load dataset as train and test sets
        (x_train, y_train), (x_test, y_test) = tf.keras.datasets.mnist.load_data
        ()
        # Set numeric type to float32 from uint8
        x_train = x_train.astype('float32')
        x_test = x_test.astype('float32')
        # Normalize value to [0, 1]
        x_train /= 255
        x_test /= 255
        # Standard normalization
        mean_train = x_train.mean()
        std_train = x_train.std()
        x_train -= mean_train
        x_train /= std_train
        x_test -= mean_train
        x test /= std train
        # Transform lables to one-hot encoding
        y_train = tf.keras.utils.to_categorical(y_train, 10)
        y_test = tf.keras.utils.to_categorical(y_test, 10)
        # Reshape the dataset into 4D array
        x train = x train.reshape(x train.shape[0], 28,28,1)
        x_test = x_test.reshape(x_test.shape[0], 28,28,1)
        x train std input = x train
        x test std input = x test
```

```
In [3]: tf.random.set seed(17)
        #Instantiate an empty model
        model = Sequential()
        # C1 Convolutional Layer
        model.add(layers.Conv2D(6, kernel size=(5, 5), strides=(1, 1), activatio
        n='tanh', input shape=(28,28,1), padding='same'))
        model.add(BatchNormalization())
        # S2 Pooling Layer
        model.add(layers.AveragePooling2D(pool_size=(2, 2), strides=(1, 1), padd
        ing='valid'))
        model.add(BatchNormalization())
        # C3 Convolutional Layer
        model.add(layers.Conv2D(16, kernel size=(5, 5), strides=(1, 1), activati
        on='tanh', padding='valid'))
        model.add(BatchNormalization())
        # S4 Pooling Layer
        model.add(layers.AveragePooling2D(pool size=(2, 2), strides=(2, 2), padd
        ing='valid'))
        model.add(BatchNormalization())
        # C5 Fully Connected Convolutional Layer
        model.add(layers.Conv2D(120, kernel_size=(5, 5), strides=(1, 1), activat
        ion='tanh', padding='valid'))
        model.add(BatchNormalization())
        #Flatten the CNN output so that we can connect it with fully connected 1
        ayers
        model.add(layers.Flatten())
        # FC6 Fully Connected Layer
        model.add(layers.Dense(84, activation='tanh'))
        model.add(BatchNormalization())
        #Output Layer with softmax activation
        model.add(layers.Dense(10, activation='softmax'))
        # Compile the model
        model.compile(loss=keras.losses.categorical crossentropy, optimizer='SG
        D', metrics=['accuracy'])
```

While the original paper talks about applying batch norm just before the activation function, it has been found in practice that applying batch norm after the activation yields better results.

Therefore, I apply it after activation for the hidden layers

In [4]: model.summary()

Model: "sequential"

Layer (type)	Output	Shape	Param #
conv2d (Conv2D)	(None,	28, 28, 6)	156
batch_normalization (BatchNo	(None,	28, 28, 6)	24
average_pooling2d (AveragePo	(None,	27, 27, 6)	0
batch_normalization_1 (Batch	(None,	27, 27, 6)	24
conv2d_1 (Conv2D)	(None,	23, 23, 16)	2416
batch_normalization_2 (Batch	(None,	23, 23, 16)	64
average_pooling2d_1 (Average	(None,	11, 11, 16)	0
batch_normalization_3 (Batch	(None,	11, 11, 16)	64
conv2d_2 (Conv2D)	(None,	7, 7, 120)	48120
batch_normalization_4 (Batch	(None,	7, 7, 120)	480
flatten (Flatten)	(None,	5880)	0
dense (Dense)	(None,	84)	494004
batch_normalization_5 (Batch	(None,	84)	336
dense_1 (Dense)	(None,	10)	850

Total params: 546,538 Trainable params: 546,042 Non-trainable params: 496

In [5]: hist = model.fit(x=x_train_std_input,y=y_train, epochs=20, batch_size=12
8, validation_data=(x_test_std_input, y_test), verbose=1)

```
Epoch 1/20
- accuracy: 0.9425 - val loss: 0.0996 - val accuracy: 0.9736
Epoch 2/20
469/469 [============== ] - 6s 13ms/step - loss: 0.0860
- accuracy: 0.9778 - val_loss: 0.0716 - val_accuracy: 0.9795
Epoch 3/20
- accuracy: 0.9839 - val_loss: 0.0545 - val_accuracy: 0.9848
Epoch 4/20
469/469 [============= ] - 6s 12ms/step - loss: 0.0514
- accuracy: 0.9867 - val_loss: 0.0542 - val_accuracy: 0.9838
Epoch 5/20
469/469 [============= ] - 6s 12ms/step - loss: 0.0436
- accuracy: 0.9889 - val_loss: 0.0437 - val_accuracy: 0.9871
Epoch 6/20
469/469 [============== ] - 6s 12ms/step - loss: 0.0375
- accuracy: 0.9908 - val loss: 0.0445 - val accuracy: 0.9865
- accuracy: 0.9919 - val_loss: 0.0407 - val_accuracy: 0.9885
Epoch 8/20
- accuracy: 0.9929 - val_loss: 0.0359 - val_accuracy: 0.9891
Epoch 9/20
469/469 [============= ] - 6s 12ms/step - loss: 0.0265
- accuracy: 0.9938 - val loss: 0.0359 - val accuracy: 0.9889
Epoch 10/20
469/469 [============= ] - 6s 12ms/step - loss: 0.0238
- accuracy: 0.9945 - val loss: 0.0329 - val accuracy: 0.9901
Epoch 11/20
- accuracy: 0.9952 - val loss: 0.0340 - val accuracy: 0.9898
Epoch 12/20
- accuracy: 0.9959 - val loss: 0.0306 - val accuracy: 0.9911
469/469 [============= ] - 6s 12ms/step - loss: 0.0184
- accuracy: 0.9962 - val loss: 0.0303 - val accuracy: 0.9908
Epoch 14/20
469/469 [============== ] - 6s 12ms/step - loss: 0.0171
- accuracy: 0.9966 - val loss: 0.0314 - val accuracy: 0.9901
Epoch 15/20
- accuracy: 0.9968 - val loss: 0.0288 - val accuracy: 0.9909
Epoch 16/20
469/469 [============= ] - 6s 12ms/step - loss: 0.0149
- accuracy: 0.9973 - val loss: 0.0317 - val accuracy: 0.9907
Epoch 17/20
469/469 [=============== ] - 6s 12ms/step - loss: 0.0139
- accuracy: 0.9976 - val loss: 0.0294 - val accuracy: 0.9913
Epoch 18/20
469/469 [=============== ] - 6s 12ms/step - loss: 0.0131
- accuracy: 0.9978 - val loss: 0.0300 - val accuracy: 0.9909
Epoch 19/20
- accuracy: 0.9979 - val loss: 0.0275 - val accuracy: 0.9917
```

```
In [49]:
    for i in [1,3,5,7,9,12]:
       print(model.layers[i].name)
       print()
       print('Gamma :
                    '+ str(model.layers[i].get_weights()[0].toli
     st()))
       print()
       print('Beta :
                   '+ str(model.layers[i].get_weights()[1].tolis
     t()))
       print ()
       ############# ')
       print ()
```

batch_normalization

Gamma: [1.0001033544540405, 1.0001364946365356, 1.00005304813 385, 1.0000249147415161, 1.0000289678573608, 1.000061273574829]

Beta: [-3.193265651901811e-09, -3.1261129240789387e-09, 1.074 4865441836282e-08, -1.8673049773099137e-09, -2.641025842464728e-09, -6. 1343565782578935e-09]

batch normalization 1

Gamma: [1.080140471458435, 1.1022557020187378, 1.047233939170 8374, 1.026122808456421, 1.024849772453308, 1.055171012878418]

Beta: [-0.07621415704488754, -0.02155950292944908, 0.22738882 899284363, -0.011400452814996243, 0.10398653149604797, -0.0037515745498 239994]

batch normalization 2

Gamma: [1.0000356435775757, 1.0000033378601074, 1.00000834465 02686, 1.0000169277191162, 1.0000183582305908, 1.0000218152999878, 1.00 0011682510376, 1.0000137090682983, 1.0000096559524536, 1.00000619888305 66, 1.0000522136688232, 1.0000017881393433, 1.0000300407409668, 1.00001 31130218506, 1.0000200271606445, 1.0000075101852417]

Beta: [-2.463348858228187e-09, 2.005402288673963e-09, 1.62071 37021329032e-10, 1.5322434432363252e-09, -1.3839591694875253e-09, -3.12 52422871830277e-09, -3.3732927562368786e-10, -3.91772919661193e-10, 4.1 625791702415427e-10, 1.1608524558281985e-10, 1.0016080187469356e-09, -1.153854012336808e-09, 1.8028366577382826e-09, 2.276902222320132e-09, 3.3491312501077175e-10, -4.598384728549121e-10]

batch normalization 3

Gamma: [1.0338406562805176, 1.006487250328064, 1.014200329780 5786, 1.017224907875061, 1.0104438066482544, 1.0181764364242554, 1.0087 862014770508, 1.0160397291183472, 1.005645751953125, 1.007005929946899 4, 1.047123670578003, 0.9986793994903564, 1.0332375764846802, 1.0144470 930099487, 1.0219016075134277, 1.0124233961105347]

Beta: [-0.002855873666703701, 0.001166807720437646, -0.004663

 $181956857443, \ 0.004320188425481319, \ -0.009904230013489723, \ -0.011273208074271679, \ 0.007533228490501642, \ -0.013439025729894638, \ -0.005260499194264412, \ 0.008676453493535519, \ -0.0031983396038413048, \ 0.003110519843176073, \ 0.012730601243674755, \ 0.0038798220921307802, \ -0.008165532723069191, \ 0.0025515514425933361$

batch normalization 4

[1.0056623220443726, 1.0002540349960327, 1.00180220603 Gamma: 94287, 1.0066707134246826, 1.0092597007751465, 1.0071388483047485, 1.00 72309970855713, 0.9957995414733887, 1.0101786851882935, 1.0164235830307 007, 1.0066404342651367, 1.0052077770233154, 1.0055514574050903, 1.0036 792755126953, 1.0043503046035767, 1.0096917152404785, 1.00645089149475 1, 1.0025393962860107, 1.0074964761734009, 1.0047550201416016, 1.000993 013381958, 0.9988912343978882, 1.0064479112625122, 0.9974077939987183, 1.0029772520065308, 1.0045174360275269, 1.0033620595932007, 1.007863759 9945068, 1.0041853189468384, 1.002315878868103, 1.0109084844589233, 1.0 090458393096924, 1.0084309577941895, 1.0023661851882935, 1.006669163703 9185, 1.0024234056472778, 1.003269076347351, 1.005169153213501, 1.00593 3165550232, 0.9983053803443909, 1.0032063722610474, 0.9978740215301514, 1.0113455057144165, 1.008239507675171, 1.0073041915893555, 1.0022174119 94934, 1.002747654914856, 0.9994053840637207, 0.9990352392196655, 1.003 086805343628, 0.9998452067375183, 1.0092865228652954, 0.998435318470001 2, 1.0023771524429321, 1.0014634132385254, 1.0023584365844727, 1.008378 7441253662, 1.013611912727356, 0.9999356269836426, 1.0093258619308472, 1.0075217485427856, 1.0061134099960327, 1.0038620233535767, 1.015642166 1376953, 1.0063326358795166, 1.0024514198303223, 1.0096383094787598, 1. 0029706954956055, 1.0026702880859375, 1.0199156999588013, 1.00515305995 94116, 1.0050839185714722, 1.0054091215133667, 1.0023939609527588, 0.99 96649026870728, 1.013514518737793, 1.0103176832199097, 1.01385784149169 92, 0.9989141225814819, 1.0042575597763062, 0.9978541135787964, 1.00949 82385635376, 0.9994216561317444, 1.0033928155899048, 1.001430630683899, 1.0026663541793823, 1.0066559314727783, 1.0063748359680176, 1.002204418 182373, 1.007834792137146, 0.9986542463302612, 1.001767873764038, 1.004 9982070922852, 1.0009055137634277, 1.0031565427780151, 1.00262212753295 9, 1.002833366394043, 1.0056177377700806, 1.0114803314208984, 0.9991413 950920105, 0.9986771941184998, 1.005359172821045, 1.0078128576278687, 1.0053293704986572, 1.001425862312317, 1.0197887420654297, 1.0087956190 109253, 1.0069087743759155, 1.0082004070281982, 1.008539080619812, 1.01 63979530334473, 1.0013022422790527, 0.9979588985443115, 1.0011752843856 812, 1.0037761926651, 1.0104435682296753, 0.9994767904281616, 0.9976818 561553955, 1.0070868730545044, 1.0001554489135742]

Beta: [0.001124291098676622, 0.0005901519907638431, -0.002198457717895508, 0.00010894873412325978, -0.0019466871162876487, -0.0005352898151613772, -0.0033958384301513433, -0.0010184940183535218, -0.003453400218859315, 0.0015058420831337571, -0.0014921720139682293, 0.001248329528607428, -0.0004696552350651473, 2.4880162527551875e-05, 0.003014389891177416, -0.0017457314534112811, -0.0007751599187031388, 0.0025623925030231476, -0.0015817326493561268, 0.002309000352397561, -0.001256747404113412, 0.0020975738298147917, 0.0020140092819929123, -0.0005003346013836563, 0.0015787516022101045, -0.00043038136209361255, -0.00155605922

91876674, 0.0005733513389714062, -0.0025358612183481455, 5.677256194758 229e-05, 0.004662738647311926, -0.00040494761196896434, -0.000196141860 21499336, -0.0009334749775007367, 0.0007417193264700472, 0.001036077970 6388712, -0.0031069170217961073, -0.0001801229373086244, -0.00023045636771712452, 0.0010385994100943208, 0.0006547464872710407, -0.00150509621 $0166812, \quad -0.0013453575083985925, \quad -0.0017636660486459732, \quad -0.00174194399$ 73309636, 0.002555257175117731, 0.0019506033277139068, -0.0007243838626 891375, -0.0023608196061104536, 0.0013325171312317252, -0.0002909032336 9018734, -5.2844512538285926e-05, -0.001144959358498454, 0.001336176646 873355, 0.0013341348385438323, 0.0018369388999417424, 0.000185029493877 6642, -0.002749239094555378, -0.0012618439504876733, 0.0018150972900912 $166, -0.0007615818758495152, \ 0.00012803601566702127, \ -0.002366545610129$ 8332, 0.00011361933866282925, -0.0007389850215986371, 0.000483945943415 16495, -0.0003616343019530177, -0.0005119805573485792, -0.0002927032182 9244494, -0.00016640231478959322, 0.0020666508935391903, 0.000586774316 6163564, -0.0008726856322027743, -0.0005122057627886534, -0.001182940904982388, -0.0011479889508336782, -0.0019359468715265393, 0.002917088801 $0412455, \quad -0.0020914669148623943, \quad 0.0008942880085669458, \quad -0.001271036569$ $9604154, -0.0011192521778866649, -9.706370474305004 \\ e-05, -0.00089256936$ 91708148, -0.001172817312180996, -0.0008061046828515828, 0.002108468441 2926435, 0.0013441269984468818, 0.0020949963945895433, 0.00089947861852 $12433, \ -0.0008241339819505811, \ 0.00014087320596445352, \ 0.00083104439545$ 42279, -2.537005093472544e-05, 0.0010218500392511487, 0.001176875084638 5956, -0.0028767904732376337, -0.0002652867406141013, 4.538970097200945 $\mathtt{e-05}, \ -0.00208503776229918, \ -0.0010540963849052787, \ -0.0013663598801940$ $68, \quad -0.0014983313158154488, \quad -0.002451713662594557, \quad -0.00058318435912951$ 83, 0.0027133007533848286, -0.0011870344169437885, 0.002734000794589519 5, 0.0021771600004285574, -0.0011616094270721078, 0.000269299314823001 6, -0.004542726557701826, 0.0011777520412579179, 0.0014645763440057635,9.493681136518717e-05, -0.002649039961397648, 0.0027524407487362623, -0.00275244074873626230.0003103430208284408, -0.0007679365808144212, 0.0005505988374352455]

batch normalization 5

Gamma: [1.0615262985229492, 1.039718508720398, 1.038655996322 6318, 1.0391103029251099, 1.020777702331543, 1.0288842916488647, 1.0355 119705200195, 1.0326181650161743, 1.0356547832489014, 1.03204476833343 5, 1.0745348930358887, 1.0581867694854736, 1.054201602935791, 1.0620614 290237427, 1.0565823316574097, 1.0438120365142822, 1.0563002824783325, 1.03714919090271, 1.0537210702896118, 1.0315293073654175, 1.03064179420 4712, 1.0392262935638428, 1.037245273590088, 1.0563414096832275, 1.0364 030599594116, 1.050891637802124, 1.062117099761963, 1.0535331964492798, 1.0555459260940552, 1.0582879781723022, 1.0416603088378906, 1.025170207 0236206, 1.0372323989868164, 1.0637003183364868, 1.0374497175216675, 1. 0296249389648438, 1.0574452877044678, 1.0502383708953857, 1.06677579879 76074, 1.0457359552383423, 1.057141900062561, 1.0459693670272827, 1.056 2243461608887, 1.0574266910552979, 1.0156569480895996, 1.05148971080780 03, 1.0520153045654297, 1.0462865829467773, 1.0244661569595337, 1.03965 43741226196, 1.049127459526062, 1.0304591655731201, 1.0449737310409546, 1.034093976020813, 1.0514894723892212, 1.0646445751190186, 1.0314774513 24463, 1.0358623266220093, 1.0460479259490967, 1.0569781064987183, 1.06 28811120986938, 1.0610231161117554, 1.0231566429138184, 1.0534456968307

495, 1.0600019693374634, 1.0535024404525757, 1.043460488319397, 1.02035 20059585571, 1.0438870191574097, 1.0487699508666992, 1.021136164665222 2, 1.0495728254318237, 1.0329267978668213, 1.0658795833587646, 1.036788 7020111084, 1.065355896949768, 1.0290696620941162, 1.028918743133545, 1.0448110103607178, 1.044732689857483, 1.0588737726211548, 1.0495487451 553345, 1.041137933731079, 1.0506408214569092]

[-0.0006841294816695154, 7.09985542926006e-05, -0.00735]7184309512377, 0.009201510809361935, 0.0005656683933921158, -0.00413913 931697607, 0.0047630551271140575, 0.007424724753946066, -0.002051409101 $113677, \ 0.0039805080741643906, \ -0.0006112591945566237, \ -0.0052905264310$ 53877, -0.0018889709608629346, -0.004128921311348677, -0.00392347527667 8801, -0.00962114054709673, -8.10254059615545e-05, 0.0021121702156960964, 0.003959633409976959, -0.0020060292445123196, 0.010553175583481789, 0.009844976477324963, -0.007894470356404781, -0.00780536700040102, 0.007520067505538464, 0.01277607399970293, -0.005623600445687771, -0.014072 90156930685, -0.0021203721407800913, -0.013125053606927395, -0.00855076 6855478287, -0.006940011400729418, 0.003943008370697498, 0.0024210987612605095, -0.0057405284605920315, 0.0026334745343774557, 0.0031888689845 8004, -0.0005172445089556277, 0.005010656546801329, -0.0028656867798417 807, 0.004122504033148289, -0.0031393086537718773, 0.000797886052168905 7, -0.00093594950158149, -0.0023288445081561804, -0.007952450774610043,-0.0017311711562797427, 0.0003689189616125077, 0.004880804568529129, 0.0048808045685291290558559335768223, 0.006316308863461018, -0.005518085788935423, 0.008858 502842485905, 0.0036259950138628483, -0.0023634417448192835, 0.00163141 26551151276, 0.007857171818614006, 0.0055394042283296585, 0.00921817030 7576656, -0.010433212853968143, 0.004861378576606512, 0.003201061626896 262, 0.006094268523156643, -0.006958217825740576, -0.00235053035430610 2, 0.007631663233041763, 0.0004118015931453556, -0.0002614204131532460 5, -0.0048215556889772415, 0.011411644518375397, 0.00257382751442492, -0.00251532974652946, -0.013403575867414474, 0.007119462359696627, 0.0055313087068498135, -0.010606273077428341, -0.0036545847542583942, -0.004 8754620365798471

Question 3:

a) Data without standard normalization

```
In [7]: # Load dataset as train and test sets
    (x_train, y_train), (x_test, y_test) = tf.keras.datasets.mnist.load_data
    ()

# Set numeric type to float32 from uint8
    x_train = x_train.astype('float32')
    x_test = x_test.astype('float32')

# Normalize value to [0, 1]
    x_train /= 255
    x_test /= 255

# Transform lables to one-hot encoding
    y_train = tf.keras.utils.to_categorical(y_train, 10)
    y_test = tf.keras.utils.to_categorical(y_test, 10)

# Reshape the dataset into 4D array
    x_train = x_train.reshape(x_train.shape[0], 28,28,1)
    x_test = x_test.reshape(x_test.shape[0], 28,28,1)
```

Model 2: Batch normalization for input and hidden layers

```
In [8]: tf.random.set seed(17)
        #Instantiate an empty model
        model batch = Sequential()
        # C1 Convolutional Layer
        model batch.add(BatchNormalization(input shape=(28,28,1)))
        model_batch.add(layers.Conv2D(6, kernel_size=(5, 5), strides=(1, 1), act
        ivation='tanh', input_shape=(28,28,1), padding='same'))
        model batch.add(BatchNormalization())
        # S2 Pooling Layer
        model batch.add(layers.AveragePooling2D(pool_size=(2, 2), strides=(1, 1
        ), padding='valid'))
        model batch.add(BatchNormalization())
        # C3 Convolutional Layer
        model batch.add(layers.Conv2D(16, kernel size=(5, 5), strides=(1, 1), ac
        tivation='tanh', padding='valid'))
        model batch.add(BatchNormalization())
        # S4 Pooling Layer
        model batch.add(layers.AveragePooling2D(pool size=(2, 2), strides=(2, 2
        ), padding='valid'))
        model batch.add(BatchNormalization())
        # C5 Fully Connected Convolutional Layer
        model_batch.add(layers.Conv2D(120, kernel_size=(5, 5), strides=(1, 1), a
        ctivation='tanh', padding='valid'))
        model batch.add(BatchNormalization())
        \# Flatten the CNN output so that we can connect it with fully connected 1
        ayers
        model batch.add(layers.Flatten())
        # FC6 Fully Connected Layer
        model batch.add(layers.Dense(84, activation='tanh'))
        model batch.add(BatchNormalization())
        #Output Layer with softmax activation
        model batch.add(layers.Dense(10, activation='softmax'))
        # Compile the model
        model batch.compile(loss=keras.losses.categorical crossentropy, optimize
        r='SGD', metrics=['accuracy'])
```

In [9]: | model_batch.summary()

Model: "sequential_1"

Layer (type)	Output	Shape	Param #
batch_normalization_6 (Batch	(None,	28, 28, 1)	4
conv2d_3 (Conv2D)	(None,	28, 28, 6)	156
batch_normalization_7 (Batch	(None,	28, 28, 6)	24
average_pooling2d_2 (Average	(None,	27, 27, 6)	0
batch_normalization_8 (Batch	(None,	27, 27, 6)	24
conv2d_4 (Conv2D)	(None,	23, 23, 16)	2416
batch_normalization_9 (Batch	(None,	23, 23, 16)	64
average_pooling2d_3 (Average	(None,	11, 11, 16)	0
batch_normalization_10 (Batc	(None,	11, 11, 16)	64
conv2d_5 (Conv2D)	(None,	7, 7, 120)	48120
batch_normalization_11 (Batc	(None,	7, 7, 120)	480
flatten_1 (Flatten)	(None,	5880)	0
dense_2 (Dense)	(None,	84)	494004
batch_normalization_12 (Batc	(None,	84)	336
dense_3 (Dense)	(None,	10)	850

Trainable params: 546,044 Non-trainable params: 498

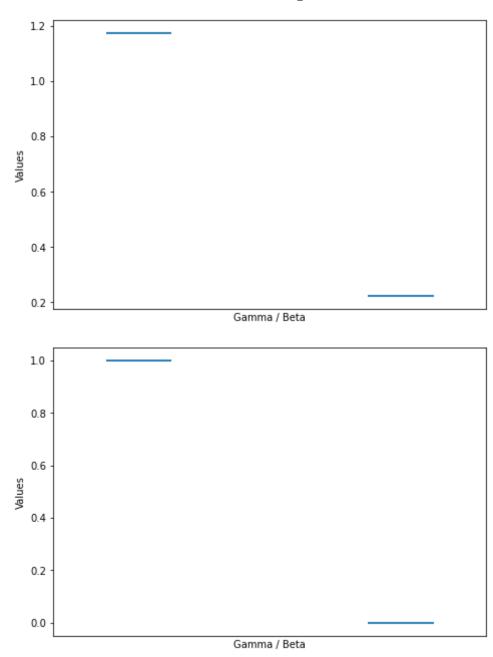
```
Epoch 1/20
469/469 [============== ] - 7s 15ms/step - loss: 0.2065
- accuracy: 0.9428 - val loss: 0.0993 - val accuracy: 0.9731
Epoch 2/20
469/469 [============== ] - 6s 13ms/step - loss: 0.0848
- accuracy: 0.9782 - val_loss: 0.0704 - val_accuracy: 0.9804
Epoch 3/20
- accuracy: 0.9840 - val_loss: 0.0541 - val_accuracy: 0.9849
Epoch 4/20
469/469 [============= ] - 6s 13ms/step - loss: 0.0507
- accuracy: 0.9867 - val_loss: 0.0535 - val_accuracy: 0.9850
Epoch 5/20
469/469 [============= ] - 6s 13ms/step - loss: 0.0431
- accuracy: 0.9890 - val_loss: 0.0434 - val_accuracy: 0.9871
Epoch 6/20
- accuracy: 0.9909 - val loss: 0.0435 - val accuracy: 0.9868
Epoch 7/20
- accuracy: 0.9920 - val_loss: 0.0402 - val_accuracy: 0.9886
Epoch 8/20
- accuracy: 0.9929 - val_loss: 0.0360 - val_accuracy: 0.9887
Epoch 9/20
469/469 [============== ] - 6s 13ms/step - loss: 0.0262
- accuracy: 0.9941 - val loss: 0.0357 - val accuracy: 0.9888
Epoch 10/20
469/469 [============= ] - 6s 13ms/step - loss: 0.0235
- accuracy: 0.9947 - val loss: 0.0328 - val accuracy: 0.9901
Epoch 11/20
- accuracy: 0.9952 - val loss: 0.0341 - val accuracy: 0.9895
Epoch 12/20
- accuracy: 0.9958 - val loss: 0.0307 - val accuracy: 0.9912
469/469 [============= ] - 6s 13ms/step - loss: 0.0182
- accuracy: 0.9963 - val loss: 0.0301 - val accuracy: 0.9910
Epoch 14/20
469/469 [============= ] - 6s 13ms/step - loss: 0.0169
- accuracy: 0.9967 - val loss: 0.0313 - val accuracy: 0.9901
Epoch 15/20
- accuracy: 0.9970 - val loss: 0.0285 - val accuracy: 0.9915
Epoch 16/20
469/469 [============= ] - 6s 13ms/step - loss: 0.0148
- accuracy: 0.9972 - val loss: 0.0317 - val accuracy: 0.9901
Epoch 17/20
- accuracy: 0.9976 - val loss: 0.0291 - val accuracy: 0.9913
Epoch 18/20
469/469 [============== ] - 6s 13ms/step - loss: 0.0130
- accuracy: 0.9978 - val loss: 0.0300 - val accuracy: 0.9911
Epoch 19/20
- accuracy: 0.9979 - val loss: 0.0272 - val accuracy: 0.9916
```

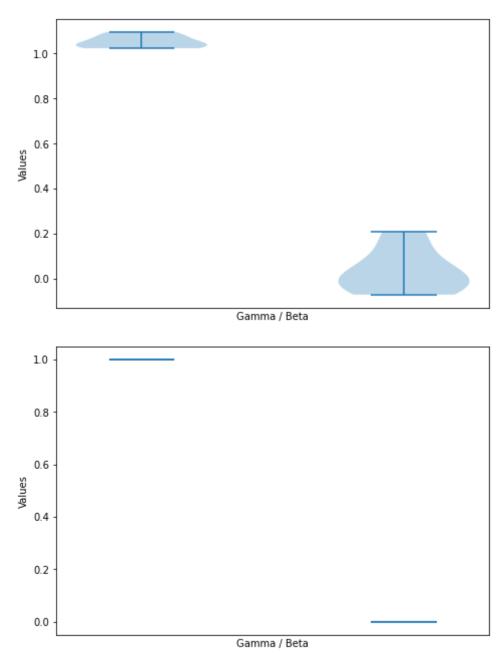
```
In [66]:
    for i in [0,2,4,6,8,10,13]:
        data_to_plot = [model_batch.layers[i].get_weights()[0].tolist(), mod
        el_batch.layers[i].get_weights()[1].tolist()]

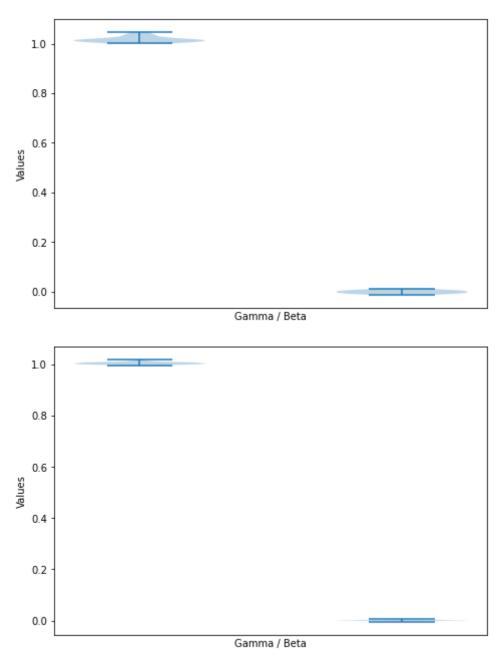
# Create a figure instance
        fig = plt.figure()

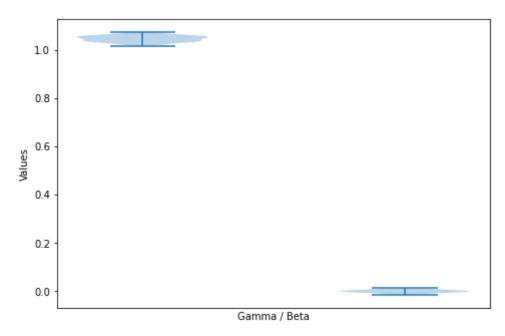
# Create an axes instance
        ax = fig.add_axes([0,0,1,1])

# Create the boxplot
        bp = ax.violinplot(data_to_plot)
        ax.axes.get_xaxis().set_ticks([])
        plt.xlabel("Gamma / Beta")
        plt.ylabel("Values")
        plt.show()
```









```
for i in [0,2,4,6,8,10,13]:
In [61]:
       print(model batch.layers[i].name)
       print()
       print('Gamma :
                    '+ str(model_batch.layers[i].get_weights()[0
     ].tolist()))
       print()
       print('Beta :
                    '+ str(model_batch.layers[i].get_weights()[1]
     .tolist()))
       print ()
       ############# ')
       print ()
```

batch normalization 6

Gamma: [1.1744343042373657]

Beta: [0.22457078099250793]

batch_normalization_7

Gamma: [1.0000983476638794, 1.0001249313354492, 1.00004518032 07397, 1.000023365020752, 1.0000228881835938, 1.0000643730163574]

Beta: [-7.3766730501745315e-09, -4.5491428402044676e-09, 1.07 02621427993719e-10, 4.27229318589184e-09, -4.696779853929911e-09, -1.12 79193135038668e-09]

batch normalization 8

Gamma: [1.0776439905166626, 1.0955561399459839, 1.04287016391 75415, 1.0234375, 1.0232908725738525, 1.0513699054718018]

Beta: [-0.07066694647073746, -0.01616567187011242, 0.20733587 443828583, -0.008760466240346432, 0.0963069275021553, -0.00071161740925 163031

batch normalization 9

Gamma: [1.0000356435775757, 1.0000054836273193, 1.00000786781 31104, 1.0000122785568237, 1.0000206232070923, 1.0000176429748535, 1.00 00079870224, 1.0000152587890625, 1.0000146627426147, 1.000005841255188, 1.000051498413086, 1.000001072883606, 1.0000293254852295, 1.00001811981 20117, 1.0000125169754028, 1.0000038146972656]

Beta: [-5.601688002343508e-10, -3.754273281142417e-11, 7.4549 38333317784e-10, 1.3708636448228617e-09, -3.3621125883342984e-09, -2.12 63983907005013e-09, -5.515064793737423e-11, 8.792996886164417e-10, 1.79 04006055502464e-09, -2.0890402741002845e-09, -1.368022362058241e-09, 2. 1246681497499864e-11, 1.4884056209751861e-09, 7.725603490271737e-10, 3. 6389211643950148e-09, 1.5337006109561457e-09]

################

batch normalization 10

Gamma: [1.0341215133666992, 1.0039653778076172, 1.01289129257 20215, 1.0154327154159546, 1.013261079788208, 1.0165857076644897, 1.009 5893144607544, 1.0178035497665405, 1.007718801498413, 1.006762385368347 2, 1.047182559967041, 1.0002268552780151, 1.0327712297439575, 1.0152435 302734375, 1.020142674446106, 1.010878086090088]

Beta: [-0.0045372662134468555, 0.0005203681066632271, -0.003558523254469037, 0.004170415457338095, -0.009523607790470123, -0.01109848078340292, 0.006995310075581074, -0.01202782429754734, -0.005124170798808336, 0.008881361223757267, -0.0030007953755557537, 0.002937089651823044, 0.012201976031064987, 0.0034679649397730827, -0.006961768958717585, 0.0014267554506659508]

batch normalization 11

Gamma: [1.0052587985992432, 1.000139832496643, 1.001922845840 454, 1.006265640258789, 1.008581280708313, 1.0073052644729614, 1.007601 3803482056, 0.9958900213241577, 1.0108489990234375, 1.0162434577941895, 1.0070840120315552, 1.005264163017273, 1.0054093599319458, 1.0031290054 32129, 1.004520058631897, 1.009005069732666, 1.0070281028747559, 1.0021 543502807617, 1.007168173789978, 1.0047032833099365, 1.000771999359130 9, 0.9994423389434814, 1.0065604448318481, 0.9974638819694519, 1.002911 8061065674, 1.0043927431106567, 1.0034414529800415, 1.0074909925460815, 1.0040936470031738, 1.0027133226394653, 1.0112006664276123, 1.008933067 3217773, 1.00880765914917, 1.0024033784866333, 1.0062967538833618, 1.00 24409294128418, 1.003140926361084, 1.0053129196166992, 1.00642943382263 18, 0.9981534481048584, 1.0038822889328003, 0.9976579546928406, 1.01090 71731567383, 1.0082029104232788, 1.0073271989822388, 1.001951098442077 6, 1.0029511451721191, 0.9991244673728943, 0.9989830255508423, 1.003076 195716858, 1.0000693798065186, 1.0088599920272827, 0.9984415769577026, 1.0024769306182861, 1.0010745525360107, 1.001888632774353, 1.0082155466 079712, 1.013014793395996, 0.9997944831848145, 1.0093351602554321, 1.00 7354736328125, 1.0060356855392456, 1.0035005807876587, 1.01493799686431 88, 1.006460428237915, 1.002143383026123, 1.0090845823287964, 1.0028389 692306519, 1.0026636123657227, 1.0194510221481323, 1.0047345161437988, 1.0056579113006592, 1.005800485610962, 1.0022318363189697, 0.9996469020 843506, 1.0135589838027954, 1.0101220607757568, 1.0128202438354492, 0.9 995080232620239, 1.0044492483139038, 0.9978495836257935, 1.009016275405 8838, 0.9997790455818176, 1.0031810998916626, 1.0014065504074097, 1.002 4688243865967, 1.0062905550003052, 1.0067492723464966, 1.00246882438659 67, 1.0076700448989868, 0.9985764026641846, 1.0017824172973633, 1.00503 14664840698, 1.000797986984253, 1.0034449100494385, 1.0026159286499023, 1.0024282932281494, 1.0055179595947266, 1.011406660079956, 0.9994918704 032898, 0.9990472197532654, 1.0051100254058838, 1.0086188316345215, 1.0 054848194122314, 1.0013679265975952, 1.0197211503982544, 1.009021401405 3345, 1.0065478086471558, 1.0085139274597168, 1.0084258317947388, 1.015 3049230575562, 1.0012198686599731, 0.9983121156692505, 1.00108599662780 76, 1.0039886236190796, 1.0109390020370483, 0.9997484087944031, 0.99752

71821022034, 1.007455825805664, 1.00033164024353031

[0.0010533033637329936, 0.0007036763709038496, -0.00208]5362793877721, 9.090618550544605e-05, -0.001968103228136897, -0.0004403 $733473736793, \quad -0.003414415754377842, \quad -0.0010265377350151539, \quad -0.0035364$ 669747650623, 0.0014711128314957023, -0.0014315377920866013, 0.00132564 24572318792, -0.00043726712465286255, 1.2391078030304925e-07, 0.0031030 38063272834, -0.0017474110936746001, -0.0007057064212858677, 0.00266171 27005010843, -0.0015560751780867577, 0.002399908611550927, -0.001198221 $8129560351,\ 0.002085247077047825,\ 0.0018445991445332766,\ -0.00062133074$ 97091591, 0.0015760164242237806, -0.0005756649188697338, -0.00162180466 5774107, 0.0006325808935798705, -0.002656911965459585, 0.00015462891315 110028, 0.004566132090985775, -0.00044837422319687903, -0.0002062796411 337331, -0.0009527691872790456, 0.0006716742063872516, 0.00099207530729 47264, -0.003129907650873065, -0.00023055952624417841, -0.0002612094976 939261, 0.0010294950334355235, 0.0006142333149909973, -0.00167404580861 33003, -0.0014964313013479114, -0.0017876705387607217, -0.0016702774446 $457624,\ 0.002510586753487587,\ 0.0019314270466566086,\ -0.000778038694988$ 9362, -0.0024118837900459766, 0.0012879582354798913, -0.000365159328794 10684, 0.0001681772992014885, -0.0010840485338121653, 0.001256949966773 3908, 0.001248324173502624, 0.0018012933433055878, 0.000135124937514774 5, -0.0028093259315937757, -0.0012254540342837572, 0.001892545027658343 3, -0.0006966259679757059, 0.00011096659727627411, -0.00233471300452947 $6,\ 6.523869524244219 \\ e-05,\ -0.0006349883042275906,\ 0.000562687346246093$ 5, -0.0002250545658171177, -0.00048457770026288927, -0.0003365697921253 741, -0.00018297780479770154, 0.0019598889630287886, 0.0005735055310651 66, -0.0007671168423257768, -0.00064840231789276, -0.001130310934968292 7, -0.0010996715864166617, -0.0020463543478399515, 0.002863544505089521 4, -0.0020908762235194445, 0.0008373147575184703, -0.001286128303036093 7, -0.0011515046935528517, -0.0002559356507845223, -0.00089419342111796 $14, \ -0.001217835582792759, \ -0.0006358709651976824, \ 0.00202113110572099$ 7, 0.001275059417821467, 0.002213583793491125, 0.0009163131471723318, -0.0007526439148932695, 2.388357461313717e-05, 0.0007840882171876729, -0.0001455596648156643, 0.001123476424254477, 0.0012963585322722793, -0.00129635853227227930029234394896775484, -0.00032991435728035867, 9.385023440700024e-05, -0.0021514880936592817, -0.001039752154611051, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.0013921601930633187, -0.00139216019306331870.001326416851952672, -0.0024970988743007183, -0.0004410594410728663, 0.0027187583036720753, -0.0012052664533257484, 0.0027848673053085804,0.002017634455114603, -0.0011310462141409516, 0.0004675565578509122, -0.004531759303063154, 0.0012351487530395389, 0.0014310673577710986, -4. 221291237627156e-05, -0.0027097766287624836, 0.0027845948934555054, -0. 00028952330467291176, -0.0007827087538316846, 0.0005921937408857048]

batch normalization 12

Gamma: [1.0612136125564575, 1.0398560762405396, 1.03955388069 15283, 1.0386760234832764, 1.020702838897705, 1.028437614440918, 1.0354 441404342651, 1.0325572490692139, 1.0350160598754883, 1.031826496124267 6, 1.0736597776412964, 1.0579160451889038, 1.0536558628082275, 1.062543 8690185547, 1.0552042722702026, 1.043561339378357, 1.0550681352615356, 1.0371156930923462, 1.0531249046325684, 1.0316314697265625, 1.030505061 1495972, 1.0384547710418701, 1.036906361579895, 1.0566296577453613, 1.0

364665985107422, 1.0501279830932617, 1.061496376991272, 1.0529338121414 185, 1.055050015449524, 1.057979702949524, 1.0413564443588257, 1.025724 8878479004, 1.0366038084030151, 1.063535213470459, 1.0369486808776855, 1.0294815301895142, 1.0567388534545898, 1.0504050254821777, 1.066788673 400879, 1.0452245473861694, 1.0561500787734985, 1.046491265296936, 1.05 67829608917236, 1.0565285682678223, 1.0154483318328857, 1.0512311458587 646, 1.05126953125, 1.0461827516555786, 1.0238131284713745, 1.039643287 6586914, 1.04896879196167, 1.0306458473205566, 1.0446697473526, 1.03395 676612854, 1.0511891841888428, 1.0643560886383057, 1.031791090965271, 1.0357686281204224, 1.0453524589538574, 1.0564340353012085, 1.062582373 6190796, 1.060795545578003, 1.024033784866333, 1.052892804145813, 1.059 4714879989624, 1.0530486106872559, 1.0443867444992065, 1.02026724815368 65, 1.0437109470367432, 1.0490092039108276, 1.0210005044937134, 1.04907 41729736328, 1.0338023900985718, 1.065394639968872, 1.0365632772445679, 1.0652766227722168, 1.0288386344909668, 1.0286762714385986, 1.044765353 2028198, 1.0443572998046875, 1.0587347745895386, 1.0487102270126343, 1. 0407977104187012, 1.05098474025726321

Beta: [-0.0008692556293681264, 0.0004808119556400925, -0.0072]137764655053616, 0.009035460650920868, 0.0006586991949006915, -0.004097 374621778727, 0.0046732197515666485, 0.007280650082975626, -0.001932174 4330227375, 0.003851494286209345, 2.85836558759911e-05, -0.005384916905 31373, -0.0017548587638884783, -0.004126016516238451, -0.00391753762960 434, -0.009419938549399376, 0.0001730532676447183, 0.002150830347090959 5, 0.003596246475353837, -0.002177702495828271, 0.010159330442547798, 0.009885822422802448, -0.007434303406625986, -0.007985561154782772, 0.0072942329570651054, 0.012714598327875137, -0.005438168533146381, -0.013 720403425395489, -0.0019007171504199505, -0.012599308975040913, -0.0081 23181760311127, -0.006509695202112198, 0.003702538087964058, 0.00215646 81082963943, -0.005515757016837597, 0.0023110629990696907, 0.0031397666 316479445, -0.000557487946934998, 0.00464083906263113, -0.0029092032928 01976, 0.0039813644252717495, -0.003198189428076148, 0.0007314523099921 644, -0.0008894737111404538, -0.0023849380668252707, -0.007846469059586 525, -0.00178744294680655, 0.000701487879268825, 0.0046749962493777275, 0.0022615070920437574, 0.00046671839663758874, -0.0012962330365553498, -0.011212168261408806, 0.010269800201058388, -0.0014958319952711463, 0.010269800201058388 $002203281968832016,\ 0.00637700455263257,\ -0.005733649246394634,\ 0.00880$ 1814168691635, 0.003929481841623783, -0.002303466899320483, 0.001259794 8079928756, 0.007495399098843336, 0.0052605909295380116, 0.008851370774 2095, -0.009923121891915798, 0.004494238644838333, 0.00320960395038127 9, 0.005816757213324308, -0.0069657862186431885, -0.002194028347730636 6, 0.007474885787814856, 0.00040936964796856046, -0.000433505076216533 8, -0.004530641250312328, 0.011161871254444122, 0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.002604279201477766, -0.0026042792014776, -0.0026042792014776, -0.0026042792014776, -0.0026042792014776, -0.0026042792014776, -0.0026042792014776, -0.0026042792014776, -0.0026042792014776, -0.00260427920147776, -0.00260427920147776, -0.0026042792014776, -0.0026042792014776, -0.0026042792014776, -0.002604279201476, -0.002604279201476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260476, -0.00260400.00278839492239058, -0.012905885465443134, 0.007219281978905201, 0.005192923359572887, -0.010496263392269611, -0.0037754857912659645, -0.0044 822362251579761

The performances have been similar.

Question4:

a) Data without standard normalization

```
In [12]: # Load dataset as train and test sets
    (x_train, y_train), (x_test, y_test) = tf.keras.datasets.mnist.load_data
    ()

# Set numeric type to float32 from uint8
    x_train = x_train.astype('float32')
    x_test = x_test.astype('float32')

# Normalize value to [0, 1]
    x_train /= 255
    x_test /= 255

# Transform lables to one-hot encoding
    y_train = tf.keras.utils.to_categorical(y_train, 10)
    y_test = tf.keras.utils.to_categorical(y_test, 10)

# Reshape the dataset into 4D array
    x_train = x_train.reshape(x_train.shape[0], 28,28,1)
    x_test = x_test.reshape(x_test.shape[0], 28,28,1)
```

Model 3: Dropout and no batch normalization

(dropout not applied on pooling layers)

```
In [14]: #Instantiate an empty model
         model dropout = Sequential()
         # C1 Convolutional Layer
         model_dropout.add(Dropout(0.2, input_shape=(28,28,1)))
         model_dropout.add(layers.Conv2D(6, kernel_size=(5, 5), strides=(1, 1), a
         ctivation='tanh', input_shape=(28,28,1), padding='same'))
         # S2 Pooling Layer
         model dropout.add(layers.AveragePooling2D(pool size=(2, 2), strides=(1,
         1), padding='valid'))
         # C3 Convolutional Layer
         model dropout.add(Dropout(0.5))
         model dropout.add(layers.Conv2D(16, kernel size=(5, 5), strides=(1, 1),
         activation='tanh', padding='valid'))
         # S4 Pooling Layer
         model dropout.add(layers.AveragePooling2D(pool size=(2, 2), strides=(2,
         2), padding='valid'))
         # C5 Fully Connected Convolutional Layer
         model dropout.add(Dropout(0.5))
         model_dropout.add(layers.Conv2D(120, kernel_size=(5, 5), strides=(1, 1),
         activation='tanh', padding='valid'))
         \# Flatten the CNN output so that we can connect it with fully connected 1
         ayers
         model dropout.add(layers.Flatten())
         # FC6 Fully Connected Layer
         model dropout.add(Dropout(0.5))
         model dropout.add(layers.Dense(84, activation='tanh'))
         #Output Layer with softmax activation
         model dropout.add(Dropout(0.5))
         model dropout.add(layers.Dense(10, activation='softmax'))
         # Compile the model
         model dropout.compile(loss=keras.losses.categorical crossentropy, optimi
         zer='SGD', metrics=['accuracy'])
```

In [15]: model_dropout.summary()

Model: "sequential_3"

Layer (type)	Output Shape	Param #
dropout_5 (Dropout)	(None, 28, 28, 1)	0
conv2d_9 (Conv2D)	(None, 28, 28, 6)	156
average_pooling2d_6 (Avera	age (None, 27, 27, 6)	0
dropout_6 (Dropout)	(None, 27, 27, 6)	0
conv2d_10 (Conv2D)	(None, 23, 23, 16)	2416
average_pooling2d_7 (Avera	age (None, 11, 11, 16)	0
dropout_7 (Dropout)	(None, 11, 11, 16)	0
conv2d_11 (Conv2D)	(None, 7, 7, 120)	48120
flatten_3 (Flatten)	(None, 5880)	0
dropout_8 (Dropout)	(None, 5880)	0
dense_6 (Dense)	(None, 84)	494004
dropout_9 (Dropout)	(None, 84)	0
dense_7 (Dense)	(None, 10)	850

Total params: 545,546 Trainable params: 545,546 Non-trainable params: 0

In [16]: hist_dropout = model_dropout.fit(x=x_train,y=y_train, epochs=20, batch_s
ize=128, validation_data=(x_test, y_test), verbose=1)

```
Epoch 1/20
- accuracy: 0.6741 - val loss: 0.3821 - val accuracy: 0.8858
Epoch 2/20
469/469 [============== ] - 5s 11ms/step - loss: 0.5666
- accuracy: 0.8236 - val_loss: 0.3058 - val_accuracy: 0.9061
Epoch 3/20
- accuracy: 0.8433 - val_loss: 0.2700 - val_accuracy: 0.9205
Epoch 4/20
- accuracy: 0.8571 - val_loss: 0.2478 - val_accuracy: 0.9299
Epoch 5/20
469/469 [============= ] - 5s 11ms/step - loss: 0.4338
- accuracy: 0.8677 - val_loss: 0.2283 - val_accuracy: 0.9333
Epoch 6/20
469/469 [============== ] - 5s 12ms/step - loss: 0.4050
- accuracy: 0.8755 - val loss: 0.2157 - val accuracy: 0.9369
Epoch 7/20
- accuracy: 0.8819 - val_loss: 0.2026 - val_accuracy: 0.9407
Epoch 8/20
- accuracy: 0.8870 - val_loss: 0.1925 - val_accuracy: 0.9429
Epoch 9/20
469/469 [============== ] - 5s 11ms/step - loss: 0.3556
- accuracy: 0.8914 - val loss: 0.1830 - val accuracy: 0.9453
Epoch 10/20
469/469 [============= ] - 5s 11ms/step - loss: 0.3442
- accuracy: 0.8954 - val loss: 0.1723 - val accuracy: 0.9483
Epoch 11/20
- accuracy: 0.8979 - val loss: 0.1676 - val accuracy: 0.9492
Epoch 12/20
469/469 [============== ] - 5s 11ms/step - loss: 0.3213
- accuracy: 0.9029 - val loss: 0.1581 - val accuracy: 0.9507
469/469 [============= ] - 5s 11ms/step - loss: 0.3091
- accuracy: 0.9066 - val loss: 0.1519 - val accuracy: 0.9543
Epoch 14/20
469/469 [============= ] - 5s 11ms/step - loss: 0.3021
- accuracy: 0.9086 - val loss: 0.1465 - val accuracy: 0.9555
Epoch 15/20
- accuracy: 0.9119 - val loss: 0.1423 - val accuracy: 0.9554
Epoch 16/20
469/469 [============= ] - 5s 11ms/step - loss: 0.2850
- accuracy: 0.9159 - val loss: 0.1342 - val accuracy: 0.9581
Epoch 17/20
469/469 [=============== ] - 5s 11ms/step - loss: 0.2776
- accuracy: 0.9159 - val loss: 0.1291 - val accuracy: 0.9603
Epoch 18/20
469/469 [=============== ] - 5s 11ms/step - loss: 0.2658
- accuracy: 0.9186 - val loss: 0.1247 - val accuracy: 0.9611
Epoch 19/20
- accuracy: 0.9216 - val_loss: 0.1224 - val accuracy: 0.9617
```

Test accuracy has significantly dropped! (0.9641 for dropout only vs 0.9920 for batch norm only)

Question 5:

a) Data without standard normalization

```
In [18]: # Load dataset as train and test sets
    (x_train, y_train), (x_test, y_test) = tf.keras.datasets.mnist.load_data
    ()

# Set numeric type to float32 from uint8
    x_train = x_train.astype('float32')
    x_test = x_test.astype('float32')

# Normalize value to [0, 1]
    x_train /= 255
    x_test /= 255

# Transform lables to one-hot encoding
    y_train = tf.keras.utils.to_categorical(y_train, 10)
    y_test = tf.keras.utils.to_categorical(y_test, 10)

# Reshape the dataset into 4D array
    x_train = x_train.reshape(x_train.shape[0], 28,28,1)
    x_test = x_test.reshape(x_test.shape[0], 28,28,1)
```

Model 4: Dropout and batch normalization

```
In [19]: from tensorflow.keras.layers import Dropout
         #Instantiate an empty model
         model dropout batch = Sequential()
         # C1 Convolutional Layer
         model dropout batch.add(BatchNormalization(input shape=(28,28,1)))
         model dropout batch.add(Dropout(0.2, input shape=(28,28,1)))
         model dropout batch.add(layers.Conv2D(6, kernel size=(5, 5), strides=(1,
         1), activation='tanh', input shape=(28,28,1), padding='same'))
         model dropout batch.add(BatchNormalization())
         # S2 Pooling Layer
         model dropout batch.add(layers.AveragePooling2D(pool size=(2, 2), stride
         s=(1, 1), padding='valid'))
         model dropout batch.add(BatchNormalization())
         # C3 Convolutional Layer
         model dropout batch.add(Dropout(0.5))
         model_dropout_batch.add(layers.Conv2D(16, kernel_size=(5, 5), strides=(1
         , 1), activation='tanh', padding='valid'))
         model dropout batch.add(BatchNormalization())
         # S4 Pooling Layer
         model dropout batch.add(layers.AveragePooling2D(pool size=(2, 2), stride
         s=(2, 2), padding='valid'))
         model dropout batch.add(BatchNormalization())
         # C5 Fully Connected Convolutional Layer
         model dropout batch.add(Dropout(0.5))
         model dropout batch.add(layers.Conv2D(120, kernel size=(5, 5), strides=(
         1, 1), activation='tanh', padding='valid'))
         model dropout batch.add(BatchNormalization())
         #Flatten the CNN output so that we can connect it with fully connected 1
         ayers
         model dropout batch.add(layers.Flatten())
         # FC6 Fully Connected Layer
         model dropout batch.add(Dropout(0.5))
         model dropout batch.add(layers.Dense(84, activation='tanh'))
         model dropout batch.add(BatchNormalization())
         #Output Layer with softmax activation
         model dropout batch.add(Dropout(0.5))
         model dropout batch.add(layers.Dense(10, activation='softmax'))
         # Compile the model
         model dropout batch.compile(loss=keras.losses.categorical crossentropy,
         optimizer='SGD', metrics=['accuracy'])
```

In [20]: model_dropout_batch.summary()

Model: "sequential_4"

Layer (type)	Output	Shape	Param #
batch_normalization_13 (Batc	(None,	28, 28, 1)	4
dropout_10 (Dropout)	(None,	28, 28, 1)	0
conv2d_12 (Conv2D)	(None,	28, 28, 6)	156
batch_normalization_14 (Batc	(None,	28, 28, 6)	24
average_pooling2d_8 (Average	(None,	27, 27, 6)	0
batch_normalization_15 (Batc	(None,	27, 27, 6)	24
dropout_11 (Dropout)	(None,	27, 27, 6)	0
conv2d_13 (Conv2D)	(None,	23, 23, 16)	2416
batch_normalization_16 (Batc	(None,	23, 23, 16)	64
average_pooling2d_9 (Average	(None,	11, 11, 16)	0
batch_normalization_17 (Batc	(None,	11, 11, 16)	64
dropout_12 (Dropout)	(None,	11, 11, 16)	0
conv2d_14 (Conv2D)	(None,	7, 7, 120)	48120
batch_normalization_18 (Batc	(None,	7, 7, 120)	480
flatten_4 (Flatten)	(None,	5880)	0
dropout_13 (Dropout)	(None,	5880)	0
dense_8 (Dense)	(None,	84)	494004
batch_normalization_19 (Batc	(None,	84)	336
dropout_14 (Dropout)	(None,	84)	0
dense_9 (Dense)	(None,	10)	850

Total params: 546,542 Trainable params: 546,044 Non-trainable params: 498

In [22]: hist_dropout_batch = model_dropout_batch.fit(x=x_train,y=y_train, epochs
=50, batch_size=128, validation_data=(x_test, y_test), verbose=1)

```
Epoch 1/50
469/469 [============== ] - 7s 14ms/step - loss: 0.1473
- accuracy: 0.9561 - val loss: 0.0587 - val accuracy: 0.9812
Epoch 2/50
469/469 [============== ] - 7s 14ms/step - loss: 0.1435
- accuracy: 0.9575 - val_loss: 0.0568 - val_accuracy: 0.9817
Epoch 3/50
- accuracy: 0.9586 - val_loss: 0.0554 - val_accuracy: 0.9827
Epoch 4/50
469/469 [============ ] - 7s 14ms/step - loss: 0.1397
- accuracy: 0.9583 - val_loss: 0.0540 - val_accuracy: 0.9824
Epoch 5/50
469/469 [============= ] - 7s 14ms/step - loss: 0.1377
- accuracy: 0.9592 - val_loss: 0.0525 - val_accuracy: 0.9831
Epoch 6/50
469/469 [=============== ] - 7s 14ms/step - loss: 0.1375
- accuracy: 0.9588 - val loss: 0.0529 - val accuracy: 0.9823
Epoch 7/50
- accuracy: 0.9596 - val_loss: 0.0527 - val_accuracy: 0.9832
Epoch 8/50
- accuracy: 0.9597 - val_loss: 0.0500 - val_accuracy: 0.9835
Epoch 9/50
469/469 [============== ] - 7s 14ms/step - loss: 0.1310
- accuracy: 0.9604 - val loss: 0.0508 - val accuracy: 0.9846
Epoch 10/50
469/469 [============= ] - 7s 14ms/step - loss: 0.1266
- accuracy: 0.9628 - val loss: 0.0523 - val accuracy: 0.9833
Epoch 11/50
- accuracy: 0.9632 - val loss: 0.0501 - val accuracy: 0.9849
Epoch 12/50
469/469 [============= ] - 7s 14ms/step - loss: 0.1237
- accuracy: 0.9632 - val loss: 0.0474 - val accuracy: 0.9845
469/469 [============= ] - 7s 14ms/step - loss: 0.1240
- accuracy: 0.9635 - val loss: 0.0490 - val accuracy: 0.9846
Epoch 14/50
469/469 [============= ] - 7s 14ms/step - loss: 0.1250
- accuracy: 0.9624 - val loss: 0.0481 - val accuracy: 0.9847
Epoch 15/50
- accuracy: 0.9633 - val loss: 0.0448 - val accuracy: 0.9852
Epoch 16/50
469/469 [============= ] - 7s 14ms/step - loss: 0.1189
- accuracy: 0.9650 - val loss: 0.0463 - val accuracy: 0.9848
Epoch 17/50
469/469 [============== ] - 7s 14ms/step - loss: 0.1179
- accuracy: 0.9652 - val loss: 0.0449 - val accuracy: 0.9856
Epoch 18/50
469/469 [============== ] - 7s 14ms/step - loss: 0.1189
- accuracy: 0.9639 - val loss: 0.0453 - val accuracy: 0.9847
Epoch 19/50
- accuracy: 0.9659 - val_loss: 0.0451 - val accuracy: 0.9850
```

```
Epoch 20/50
469/469 [============= ] - 7s 14ms/step - loss: 0.1152
- accuracy: 0.9649 - val_loss: 0.0462 - val_accuracy: 0.9853
Epoch 21/50
- accuracy: 0.9657 - val loss: 0.0436 - val accuracy: 0.9853
Epoch 22/50
- accuracy: 0.9663 - val_loss: 0.0433 - val_accuracy: 0.9858
Epoch 23/50
469/469 [============== ] - 7s 14ms/step - loss: 0.1141
- accuracy: 0.9657 - val_loss: 0.0432 - val_accuracy: 0.9855
Epoch 24/50
469/469 [============= ] - 7s 14ms/step - loss: 0.1119
- accuracy: 0.9663 - val loss: 0.0440 - val accuracy: 0.9861
Epoch 25/50
469/469 [============== ] - 7s 14ms/step - loss: 0.1092
- accuracy: 0.9671 - val_loss: 0.0417 - val_accuracy: 0.9860
Epoch 26/50
- accuracy: 0.9671 - val_loss: 0.0423 - val_accuracy: 0.9862
Epoch 27/50
- accuracy: 0.9670 - val_loss: 0.0423 - val_accuracy: 0.9863
Epoch 28/50
- accuracy: 0.9680 - val_loss: 0.0404 - val_accuracy: 0.9871
Epoch 29/50
469/469 [============== ] - 7s 14ms/step - loss: 0.1067
- accuracy: 0.9680 - val loss: 0.0423 - val accuracy: 0.9863
Epoch 30/50
- accuracy: 0.9684 - val loss: 0.0399 - val accuracy: 0.9868
Epoch 31/50
- accuracy: 0.9680 - val loss: 0.0404 - val accuracy: 0.9868
Epoch 32/50
469/469 [============= ] - 7s 14ms/step - loss: 0.1061
- accuracy: 0.9677 - val loss: 0.0395 - val accuracy: 0.9868
Epoch 33/50
469/469 [============= ] - 7s 14ms/step - loss: 0.1042
- accuracy: 0.9682 - val loss: 0.0401 - val accuracy: 0.9864
Epoch 34/50
- accuracy: 0.9687 - val loss: 0.0390 - val accuracy: 0.9869
Epoch 35/50
469/469 [============= ] - 7s 14ms/step - loss: 0.1020
- accuracy: 0.9691 - val loss: 0.0397 - val accuracy: 0.9870
469/469 [=============] - 7s 14ms/step - loss: 0.1038
- accuracy: 0.9687 - val loss: 0.0397 - val accuracy: 0.9873
Epoch 37/50
469/469 [============== ] - 7s 14ms/step - loss: 0.1030
- accuracy: 0.9693 - val loss: 0.0394 - val accuracy: 0.9865
Epoch 38/50
469/469 [============== ] - 7s 14ms/step - loss: 0.1007
- accuracy: 0.9699 - val loss: 0.0408 - val accuracy: 0.9870
```

```
Epoch 39/50
     469/469 [============= ] - 7s 14ms/step - loss: 0.1017
     - accuracy: 0.9699 - val loss: 0.0375 - val accuracy: 0.9880
     Epoch 40/50
     - accuracy: 0.9703 - val loss: 0.0374 - val accuracy: 0.9883
     Epoch 41/50
     - accuracy: 0.9704 - val_loss: 0.0361 - val_accuracy: 0.9876
     Epoch 42/50
     469/469 [============= ] - 7s 14ms/step - loss: 0.0978
     - accuracy: 0.9704 - val_loss: 0.0370 - val_accuracy: 0.9873
     - accuracy: 0.9709 - val loss: 0.0376 - val accuracy: 0.9877
     Epoch 44/50
     469/469 [============== ] - 7s 14ms/step - loss: 0.0960
     - accuracy: 0.9711 - val loss: 0.0380 - val accuracy: 0.9873
     Epoch 45/50
     - accuracy: 0.9711 - val_loss: 0.0372 - val_accuracy: 0.9877
     Epoch 46/50
     - accuracy: 0.9712 - val_loss: 0.0363 - val_accuracy: 0.9880
     Epoch 47/50
     - accuracy: 0.9710 - val_loss: 0.0361 - val_accuracy: 0.9880
     Epoch 48/50
     - accuracy: 0.9711 - val loss: 0.0368 - val accuracy: 0.9881
     - accuracy: 0.9719 - val loss: 0.0371 - val accuracy: 0.9880
     Epoch 50/50
     - accuracy: 0.9717 - val loss: 0.0367 - val accuracy: 0.9883
In [ ]: model dropout batch.save('model4 dropout batch all.h5')
```

The performance compared to dropout only has significantly increased (0.9850 for dropout. + batch. norm vs 0.9641 for dropout only). (compared on 20 epochs)

The performance compared to batch norm only has been slightly reduced (0.9850 vs 0.9920). (compared on 20 epochs)

Conclusion:

Dropout seems to increase the training time but also avoid overfitting. Dropout is mostly a technique for regularization. It introduces noise into a neural network to force the neural network to learn to generalize well enough to deal with noise.

Batch normalization is mostly a technique for improving optimization and it happens that it also. introduce some noise and therefore help for regularization. As for large dataset like ours, optimization is more important than regularizationso batch normalization seems to be more important. A combination of both can also be applied.

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