Exploring Diffraction Monitor in Tidy3D

Diffraction Monitor Documentation

```
# this uses scienceplots to make plots look better
plt.style.use(['science', 'notebook', 'grid'])
```

Stuff

```
# Import the necessary packages
import matplotlib.pyplot as plt
import numpy as np
import tidy3d as td
import tidy3d.web as web
import scienceplots

# Set logging level to ERROR to reduce output verbosity
td.config.logging_level = "ERROR"
```

```
# 0 Define a FreqRange object with desired wavelengths
fr = td.FreqRange.from_wvl_interval(wvl_min=1.1, wvl_max=1.6)
N = 301 # num_points
freq0 = fr.freq0
lda0 = td.C_0 / fr.freq0
```

```
# 1 Computational Domain Size
h = 0.220  # Height of cylinder
spc = 2
Lz = spc + h + h + spc

Px = Py = P = 0.666  # periodicity
sim_size = [Px, Py, Lz]
```

```
# 2 Grid Resolution
dl = P / 128
horizontal_grid = td.UniformGrid(dl=dl)
vertical_grid = td.AutoGrid(min_steps_per_wvl=32)
grid_spec=td.GridSpec(
    grid_x=horizontal_grid,
    grid_y=horizontal_grid,
    grid_z=vertical_grid,
)
```

```
r = 0.242 # radius of the cylinder
n_Si = 3.5
Si = td.Medium(permittivity=n_Si**2, name='Si')
cylinder = td.Structure(
    geometry=td.Cylinder(center=[0, 0, h / 2], radius=r, length=h, axis=2), medium=S
)
```

```
# Background medium for the first simulation
n_glass = 1.4
n_{Si02} = 1.45
glass = td.Medium(permittivity=n_glass**2, name='glass')
SiO2 = td.Medium(permittivity=n_SiO2**2, name='oxide')
substrate = td.Structure(
    geometry=td.Box(
        center=(0, 0, -Lz/2),
        size=(td.inf,td.inf,2 * (spc+h))
    ),
    medium=SiO2,
    name='substrate'
)
glass = td.Structure(
    geometry=td.Box(
        center=(0, 0, Lz/2),
        size=(td.inf,td.inf,2 * (spc+h))
    ),
    medium=glass,
    name='superstrate'
)
# Background medium for the second simulation
# Polymer
n_polymer = 1.66
polymer = td.Structure(
    geometry=td.Box(
        center=(0,0,0),
        size=(td.inf,td.inf,td.inf)
    medium=td.Medium(permittivity=n_polymer**2, name='polymer'),
    name='polymer'
)
source = td.PlaneWave(
    source_time=fr.to_gaussian_pulse(),
    size=(td.inf, td.inf, 0),
    center=(0, 0, Lz/2 - spc + 0.5 * lda0),
    direction="-",
    pol_angle=0
)
monitor = td.DiffractionMonitor(
    center=(0, 0, -Lz/2 + spc - 0.5 * lda0),
    size=(td.inf,td.inf,0),
    freqs=fr.freqs(N),
    name='diffraction_monitor',
    normal_dir='-', # away from structure
)
```

```
bandwidth = fr.fmax - fr.fmin
run_time = 200 / bandwidth

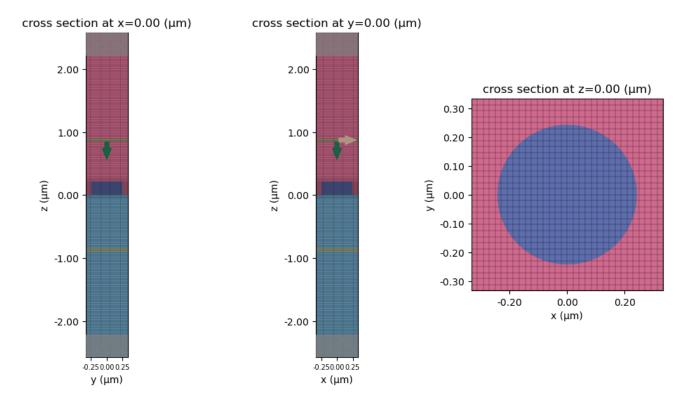
bc = td.BoundarySpec(
    x=td.Boundary.periodic(),
    y=td.Boundary.periodic(),
    z=td.Boundary.pml()
)
```

```
def simulation_helper(background, monitors, run_time):
   Create normalization and actual tidy3d simulations, visualize geometry,
   and return both as a dictionary.
   Parameters
    -----
   background: list of td.Structure
        Background structures (without the cylinder).
   monitors : list of td.Monitor
        Monitors for the normalization run.
   run_time : float
        Run time for the normalization simulation.
   Returns
    -----
   dict
        {"norm": Simulation without cylinder,
         "actual": Simulation with cylinder}
   Notes
    ----
   Saves cross-sectional plots of the actual simulation (x=0, y=0, z=0)
   with grid overlay for verification.
   sim_empty=td.Simulation(
        size=sim_size,
        grid_spec=grid_spec,
        structures=background,
        sources=[source],
        monitors=monitors,
        run_time=run_time,
        boundary_spec=bc
    )
   background.append(cylinder)
   sim_actual = td.Simulation(
        size=sim_size,
        grid_spec=grid_spec,
        structures=background,
        sources=[source],
        monitors=monitors,
        run_time=run_time,
        boundary_spec=bc
```

```
)
# Always visualize simulation before running
fig, (ax1, ax2, ax3) = plt.subplots(1, 3, figsize=(12, 6))
ax1.tick_params(axis='x', labelsize=7)
ax2.tick_params(axis='x', labelsize=7)
sim_actual.plot(x=0, ax=ax1)
sim_actual.plot_grid(x=0, ax=ax1)
sim_actual.plot(y=0, ax=ax2)
sim_actual.plot_grid(y=0, ax=ax2)
sim_actual.plot(z=0, ax=ax3)
sim_actual.plot_grid(z=0, ax=ax3)
plt.savefig(f'huygens_structure_{background[0].name}.png', dpi=300)
plt.show()
sims = {
    "norm": sim_empty,
    "actual": sim_actual,
}
return sims
```

Simulation

```
sims = simulation_helper(
   background=[substrate, glass],
   monitors=[monitor],
   run_time=run_time
)
```



```
batch = web.Batch(simulations=sims, verbose=True)
batch_data = batch.run(path_dir="data/huygens_diffraction")
```

20:41:03 EDT Started working on Batch containing 2 tasks.

20:41:05 EDT Maximum FlexCredit cost: 0.050 for the whole batch.

Use 'Batch.real_cost()' to get the billed FlexCredit cost after the Batch has completed.

20:41:16 EDT Batch complete.

```
dD = batch_data["actual"]["diffraction_monitor"]
norm_data = batch_data["norm"]["diffraction_monitor"]
# diffraction_data.help()
```

dD.monitor

```
DiffractionMonitor(attrs={}, type='DiffractionMonitor', center=(0.0, 0.0,
-0.8718518518518521), size=(inf, inf, 0.0), name='diffraction_monitor',
interval_space=(1, 1, 1), colocate=False, freqs=(187370286250000.0,
187654180623106.06, 187938074996212.12, 188221969369318.2, 188505863742424.25,
188789758115530.3, 189073652488636.38, 189357546861742.44, 189641441234848.47,
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197874378054924.25, 198158272428030.3, 198442166801136.34, 198726061174242.4,
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203552265517045.44, 203836159890151.5, 204120054263257.56, 204403948636363.62,
204687843009469.7, 204971737382575.75, 205255631755681.8, 205539526128787.88,
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206958997994318.16, 207242892367424.22, 207526786740530.28, 207810681113636.34,
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238755167782196.94, 239039062155303.0, 239322956528409.06, 239606850901515.12,
239890745274621.2, 240174639647727.25, 240458534020833.3, 240742428393939.38,
241026322767045.44, 241310217140151.5, 241594111513257.53, 241878005886363.6,
242161900259469.66, 242445794632575.72, 242729689005681.78, 243013583378787.84,
243297477751893.9, 243581372124999.97, 243865266498106.03, 244149160871212.1,
244433055244318.16, 244716949617424.2, 245000843990530.25, 245284738363636.3,
245568632736742.38, 245852527109848.44, 246136421482954.5, 246420315856060.56,
246704210229166.62, 246988104602272.7, 247271998975378.75, 247555893348484.8,
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260331140138257.53, 260615034511363.6, 260898928884469.66, 261182823257575.7,
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269415760077651.47, 269699654450757.5, 269983548823863.56, 270267443196969.62,
270551337570075.7, 270835231943181.75, 271119126316287.8, 271403020689393.88,
271686915062499.94, 271970809435606.0, 272254703808712.06, 272538598181818.12),
apodization=ApodizationSpec(attrs={}, start=None, end=None, width=None,
type='ApodizationSpec'), normal_dir='-')
```

dD.Er

```
xarray.DiffractionDataArray
                               (orders_x: 1, orders_y: 1, f: 301)
```

```
array([[[-0.-0.j, -0.-0.j, -0.-0.j, -0.-0.j, -0.-0.j, -0.-0.j, -0.-0.j,
                -0.-0.j, -0.-0.j, -0.-0.j, -0.+0.j, -0.+0.j, -0.+0.j, -0.+0.j,
                -0.+0.j, -0.+0.j, -0.+0.j, -0.+0.j, -0.+0.j, -0.+0.j, -0.+0.j,
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```

▼ Coordinates:

```
orders x
                    (orders_x)
                               int64 0
  orders y
                    (orders_y)
                               int64 0
  f
                    (F)
                               float64 1.874e+14 1.877e+14 ... 2.725e+14
▶ Indexes: (3)
```

▼ Attributes:

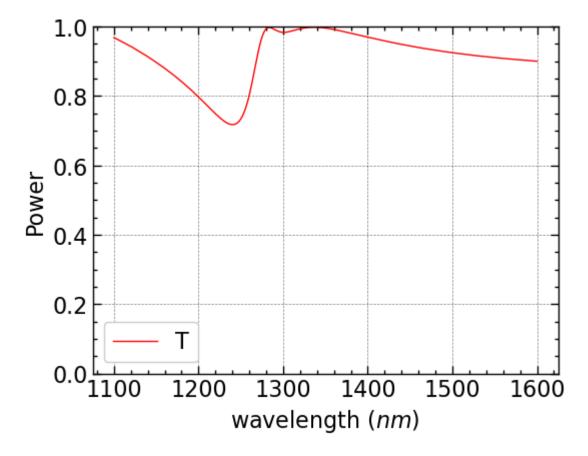
long_name: diffraction amplitude

```
print(dD.medium)
```

oxide

```
power = np.array(dD.power[0][0])
```

```
# plot transmission, compare to paper results, look similar
fig, ax = plt.subplots(1, 1, figsize=(6, 4.5))
plt.plot(td.C_0 / fr.freqs(N) * 1000, power / norm_power, "r", lw=1, label="T")
plt.xlabel(r"wavelength ($nm$)")
plt.ylabel("Power")
plt.ylim(0, 1)
plt.legend()
plt.show()
```



```
amps = np.array(dD.amps[0][0][:,0])
print(amps.shape)
```

(301,)

```
import pandas as pd
print(pd.DataFrame(amps[0][0]).head())
```

```
Θ
0 -7.477880e-09-8.372133e-
                                                10j
                                                     0.400083+0.860127j
1 -7.466276e-09-2.064935e-
                                                09j
                                                     0.385044+0.867238j
2 -7.082986e-09-3.138136e-
                                                     0.369848+0.874091j
                                                09j
3 -6.485964e-09-3.902346e-
                                                     0.354497+0.880677j
                                                09j
4 -5.897012e-09-4.333861e-
                                                     0.339016+0.886985j
                                                09j
```

Phase

```
phase = np.unwrap(np.angle(amps))

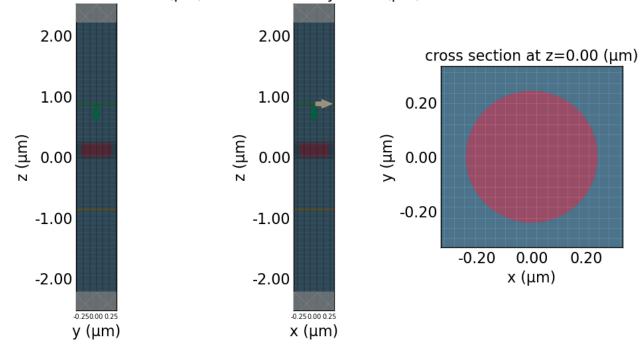
new_amps = batch_data["actual"]["diffraction_monitor"].amps

monitor = td.DiffractionMonitor(
    center=(0, 0, -Lz/2 + spc - (td.C_0 / fr.freq0)),
    size=(td.inf,td.inf,0),
```

```
size=(td.inf,td.inf,0),
freqs=fr.freqs(N),
name='diffraction_monitor',
normal_dir='-', # away from structure
)
```

```
sims = simulation_helper(
   background=[polymer],
   monitors=[monitor],
   run_time=700 / (fr.fmax - fr.fmin)
)
```

cross section at x=0.00 (μ m) cross section at y=0.00 (μ m)

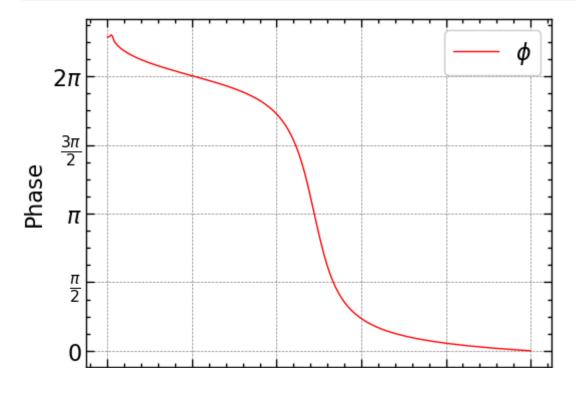


```
batch = web.Batch(simulations=sims, verbose=True)
batch_data = batch.run(path_dir="data/huygens_pol")
```

22:18:45 EDT Batch complete.

```
first_order = batch_data["actual"]["diffraction_monitor"].amps[1][1]
norm_amps = batch_data["norm"]["diffraction_monitor"].amps[1][1]
phase_p2 = np.unwrap(np.angle(first_order[:, 1]))
phase_p2 = phase_p2 - phase_p2[0]
norm_phase_p2 = np.unwrap(np.angle(norm_amps[:, 1]))
norm_phase_p2 = norm_phase_p2 - norm_phase_p2[0]

phase = phase_p2 - norm_phase_p2
```



1100 1200 1300 1400 1500 1600 wavelength (*nm*)