

Description of project

Literature

- Pukthuanthong & Roll ("Global market integration: An alternative measure and its application," 2008) and Cotter, Gabriel and Roll ("Can Housing Risk Be Diversified? A Cautionary Tale from the Housing Boom and Bust," 2015) have suggested that real estate portfolios should be diversified based on a "cointegration factor".
- They argue that this is a more accurate measure than correlation due to the fact that correlation is backward-looking.
- Cotter, Gabriel and Roll define the integration factor for a US state as the R-squared value derived from regressing the real estate returns in each state against country level factors, which provides a measure of the level of integration between the state's returns and economic activity in the US overall.
- I apply Cotter et. al's methodology to Canadian provinces, using the following variables sourced from StatCan:

Dependent Variable:

- Housing Price Index for each province for residential property (indexed at 2017)
- 9 regression specifications are carried out for:

	Alberta
	British Columbia
	Saskatchewan
	Manitoba
	Quebec
	Ontario
	Newfoundland and L
abrador	
	Nova Scotia
	Atlantic Region
	New Brunswick
	Prince Edward Isla
nd	

Explanatory Variables:

- debt to disposable income ratio
- mortgage interest rates

- household consumption
- household expenditure
- % change in the S&P/TSX Composite in a given year

Visualization

- The R-squared factor for the p each regression level of integration is then plotted onto the Google Maps API as a choropleth map, using shapefiles for provincial boundaries sourced from StatCan.

1. Cleaning data for regression

```
In [66]: 1 # import libraries
2 import pandas as pd
3 import numpy as np
4 import matplotlib.pyplot as plt
5 import seaborn as sns
6 import qeds
7 from sklearn import linear_model
8
9 import geopandas as gpd
10 from shapely.geometry import Point
11
12 import gmaps
13 import gmaps.datasets
14 import requests
15 import json
16 import random
17 import pygeoj
18
19 import colourmap
20 from colourmap import rgb2hex
21
22 import math
```

```
In [67]: 1 # - 1. load and clean housing data
2
3 # - read housing price data in
4 housing_data = pd.read_csv("project_data/housing-index-by-census-met-
5 #housing_data.info()
6
7 # - get date, geography and value only
8 housing_data.tail()
9 housing_data_small = housing_data[["REF_DATE", "GEO", "New housing p
10 # housing_data_small
11
```

```

12 # - drop to keep house only
13 housing_data_small_1 = housing_data_small.loc[housing_data_small["Ne
14 housing_data_small_1
15
16 # - drop to keep 2010 - 2018 only
17 # housing_data_small_1[["REF_DATE"]]
18 housing_data_small_1["Year"] = "20" + housing_data_small_1["REF_DATE
19 # housing_data_small_1
20 housing_data_small_2 = housing_data_small_1.loc[pd.to_numeric(housin
21 # housing_data_small_2
22
23 # - merge index based on GEO
24 housing_data_small_3 = housing_data_small_2.set_index(["GEO", "Year"
25 # housing_data_small_3
26
27
28 # - get only certain provinces
29 housing_data_small_4 = housing_data_small_3.loc[["Alberta",
30                                                  "British Columbia",
31                                                  "Saskatchewan",
32                                                  "Manitoba",
33                                                  "Quebec",
34                                                  "Ontario",
35                                                  "Newfoundland and La
36                                                  "Nova Scotia",
37                                                  "Atlantic Region",
38                                                  "New Brunswick",
39                                                  "Prince Edward Islan
40
41                                     ]]
42
43 housing_data_small_4 = housing_data_small_4.reset_index()
44 # get date
45 housing_data_small_4["Month"] = housing_data_small_4["REF_DATE"].str
46 housing_data_small_4["Date-str"] = "1 " + housing_data_small_4["Montl
47 housing_data_small_4["Date"] = pd.to_datetime(housing_data_small_4["1
48
49 # - put date on horizontal
50 housing_data_small_5 = housing_data_small_4.pivot_table(
51     index="Date",
52     columns="GEO",
53     values="VALUE")
54
55 housing_data_small_5.to_csv("cleaned_data/housing_index.csv")
56
57 housing_index_data_clean = housing_data_small_5

```

/opt/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:18: S
ettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using `.loc[row_indexer,col_indexer] = value` instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
(https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy)

In [68]: 1 housing_index_data_clean.head()

Out[68]:

GEO	Alberta	Atlantic Region	British Columbia	Manitoba	New Brunswick	Newfoundland and Labrador	Nova Scotia	Ontario	Prince Edward Island
Date									
2010-01-01	92.7	93.6	94.5	80.2	97.3	92.9	90.6	75.7	101.2
2010-02-01	92.9	93.6	95.2	80.4	97.5	92.9	90.7	75.6	100.4
2010-03-01	93.3	93.6	96.2	80.9	97.5	92.9	90.8	76.1	99.8
2010-04-01	93.3	94.1	96.7	81.2	97.4	94.2	90.8	76.3	99.4
2010-05-01	93.7	94.4	97.0	81.5	97.9	94.5	90.9	76.9	99.8

```
In [69]: 1 # - 1a. load and clean data for factor group 1: Canadians' financial
2 income_data = pd.read_csv("project_data/household-financial-health-L
3 # income_data
4
5 # - only keep Canada level data
6 income_data_small = income_data.loc[income_data["GEO"] == "Canada"]
7
8 # - only keep financial health data
9 income_data_small_1 = income_data_small.loc[income_data_small["Charac
10
11 # - rename REF_DATE to year
12 income_data_small_1["Year"] = pd.to_numeric(income_data_small_1["REF
13
14 # - get year between 2010 and 2017
15 income_data_small_2 = income_data_small_1.loc[(income_data_small_1["
16
17 income_data_small_2["Year"] = income_data_small_2["Year"].apply(str)
18
19 # - set year as index
```

```

20 income_data_small_3 = income_data_small_2.pivot_table(
21     index = "Year",
22     columns = "Net worth indicators (wealth)",
23     values = "VALUE")
24
25 income_data_small_3 = income_data_small_3[["Debt to disposable income
26 income_data_small_3 = income_data_small_3.reset_index()
27
28 # - spread data to every year
29 income_data_small_3["Jan"] = "01 " + "Jan" + " " + income_data_small
30 income_data_small_3["Feb"] = "01 " + "Feb" + " " + income_data_small
31 income_data_small_3["Mar"] = "01 " + "Mar" + " " + income_data_small
32 income_data_small_3["Apr"] = "01 " + "Apr" + " " + income_data_small
33 income_data_small_3["May"] = "01 " + "May" + " " + income_data_small
34 income_data_small_3["Jun"] = "01 " + "Jun" + " " + income_data_small
35 income_data_small_3["Jul"] = "01 " + "Jul" + " " + income_data_small
36 income_data_small_3["Aug"] = "01 " + "Aug" + " " + income_data_small
37 income_data_small_3["Sep"] = "01 " + "Sep" + " " + income_data_small
38 income_data_small_3["Oct"] = "01 " + "Oct" + " " + income_data_small
39 income_data_small_3["Nov"] = "01 " + "Nov" + " " + income_data_small
40 income_data_small_3["Dec"] = "01 " + "Dec" + " " + income_data_small
41
42 # - melt
43 income_data_small_4 = income_data_small_3.melt(id_vars=["Year", "Debt
44 income_data_small_4["Date"] = pd.to_datetime(income_data_small_4["va
45
46 # get cols
47 income_data_small_5 = income_data_small_4[["Date",
48                                             "Debt to disposable income
49
50 # - save as df
51 income_data_small_5.to_csv("cleaned_data/canadians_financial_health_
52
53 financial_health_stats_clean = income_data_small_5

```

/opt/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:12: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
(https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy)

/opt/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:17: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using `.loc[row_indexer,col_indexer] = value` instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
(https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy)

In [70]: `1 financial_health_stats_clean.head()`

Out[70]:

	Date	Debt to disposable income ratio
0	2010-01-01	167.2
1	2011-01-01	169.7
2	2012-01-01	170.0
3	2013-01-01	169.9
4	2014-01-01	171.8

```
In [71]: 1 # - 1b. load and clean data for factor 2: mortgage interest rates
2 mortgage_data = pd.read_csv("project_data/canada-mortgage-lending-rates.csv")
3 mortgage_data
4
5 # - keep only 2010 to 2018 data
6 mortgage_data["Year"] = mortgage_data["REF_DATE"].str[:4]
7 mortgage_data_small = mortgage_data.loc[pd.to_numeric(mortgage_data["Year"]
8
9
10 # - get average mortgage rate for each year
11 mortgage_data_small_1 = mortgage_data_small[["REF_DATE",
12                                             "VALUE"]
13
14
15 mortgage_data_small_1["Date-str"] = mortgage_data_small_1["REF_DATE"]
16 mortgage_data_small_1["Date"] = pd.to_datetime(mortgage_data_small_1["Date-str"])
17
18 mortgage_data_small_1.rename(columns = {'VALUE': 'Mortgage Rate'}, inplace=True)
19
20 mortgage_data_small_2 = mortgage_data_small_1[["Date", "Mortgage Rate"]]
21
22 # - write to csv
23 mortgage_data_small_2.to_csv("cleaned_data/mortgage_rate_clean.csv")
24
25 mortgage_rate_clean = mortgage_data_small_2
```

/opt/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:15: S

```
/opt/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:16: SettingWithCopyWarning:
```

A value is trying to be set on a copy of a slice from a DataFrame.
Try using `.loc[row_indexer,col_indexer] = value` instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
(https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy)

```
/opt/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:16: SettingWithCopyWarning:
```

A value is trying to be set on a copy of a slice from a DataFrame.
Try using `.loc[row_indexer,col_indexer] = value` instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
(https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy)

```
/opt/anaconda3/lib/python3.7/site-packages/pandas/core/frame.py:4133: SettingWithCopyWarning:
```

A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
(https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy)

```
In [72]: 1 mortgage_rate_clean.head()
```

Out[72]:

	Date	Mortgage Rate
708	2010-01-01	4.80
709	2010-02-01	4.73
710	2010-03-01	4.71
711	2010-04-01	5.15
712	2010-05-01	5.30

```
In [73]: 1 # - 1c. get factor group 3: household consumption/expenditure
```

```

2 household_spending = pd.read_csv("project_data/expenditure-consumption")
3
4 # - keep national level data only
5 household_spending_small = household_spending.loc[household_spending["National level"] == "National level"]
6
7 # - keep 2010 to 2017 data only
8 household_spending_small_1 = household_spending_small.loc[pd.to_datetime(household_spending_small["Date"]) >= pd.to_datetime("2010-01-01") && pd.to_datetime(household_spending_small["Date"]) <= pd.to_datetime("2017-12-31")]
9
10 # - keep expenditure and consumption only
11 household_spending_small_2 = household_spending_small_1.set_index("Household", drop=True)
12 household_spending_small_3 = household_spending_small_2.loc[:, ["Total expenditure", "Total consumption"]]
13
14
15 # - reshape to set index and year
16 household_spending_small_3.rename(columns = {'REF_DATE': 'Year'}, inplace=True)
17
18 household_spending_small_3["Year"] = household_spending_small_3["Year"].str[:4]
19
20
21 household_spending_small_4 = household_spending_small_3.pivot_table(
22     index = "Year",
23     columns = "Household expenditures, summary-level categories",
24     values = "VALUE")
25
26 household_spending_small_4 = household_spending_small_4.reset_index()
27 # - spread to monthly
28 # - spread data to every year
29 household_spending_small_4["Jan"] = "01 " + "Jan" + " " + household_spending_small_4["Total expenditure"]
30 household_spending_small_4["Feb"] = "01 " + "Feb" + " " + household_spending_small_4["Total expenditure"]
31 household_spending_small_4["Mar"] = "01 " + "Mar" + " " + household_spending_small_4["Total expenditure"]
32 household_spending_small_4["Apr"] = "01 " + "Apr" + " " + household_spending_small_4["Total expenditure"]
33 household_spending_small_4["May"] = "01 " + "May" + " " + household_spending_small_4["Total expenditure"]
34 household_spending_small_4["Jun"] = "01 " + "Jun" + " " + household_spending_small_4["Total expenditure"]
35 household_spending_small_4["Jul"] = "01 " + "Jul" + " " + household_spending_small_4["Total expenditure"]
36 household_spending_small_4["Aug"] = "01 " + "Aug" + " " + household_spending_small_4["Total expenditure"]
37 household_spending_small_4["Sep"] = "01 " + "Sep" + " " + household_spending_small_4["Total expenditure"]
38 household_spending_small_4["Oct"] = "01 " + "Oct" + " " + household_spending_small_4["Total expenditure"]
39 household_spending_small_4["Nov"] = "01 " + "Nov" + " " + household_spending_small_4["Total expenditure"]
40 household_spending_small_4["Dec"] = "01 " + "Dec" + " " + household_spending_small_4["Total expenditure"]
41
42 # - melt
43
44 household_spending_small_4 = household_spending_small_4.melt(id_vars="Year", var_name="Month", value_name="Value")
45
46
47
48 household_spending_small_4["Date"] = pd.to_datetime(household_spending_small_4["Year"] + "-" + household_spending_small_4["Month"] + "-" + household_spending_small_4["Value"].str[:2])
49
50 household_spending_small_5 = household_spending_small_4[["Date", "Value"]]
51
52

```



```

53 # - write to dataframe
54 household_spending_small_5.to_csv("cleaned_data/consumption_expenditure")
55
56
57 household_spending_clean = household_spending_small_5

```

In [74]: 1 household_spending_clean.head()

Out[74]:

	Date	Total expenditure	Total current consumption
0	2010-01-01	72075.0	54013.0
1	2011-01-01	73646.0	55227.0
2	2012-01-01	75695.0	56330.0
3	2013-01-01	79098.0	58576.0
4	2014-01-01	80727.0	59055.0

```

In [75]: 1 # - 1d. get factor 4: tsx performance
2 tsx_data = pd.read_csv("project_data/tsx-monthly.csv")
3
4 # - keep only 2009 - 2019
5 tsx_data["Year"] = tsx_data["REF_DATE"].str[:4]
6 tsx_data_small = tsx_data.loc[pd.to_numeric(tsx_data["Year"]).between(
7
8 # - index by tse stats
9 tsx_data_small_1 = tsx_data_small.set_index("Toronto Stock Exchange :
10 tsx_data_small_2 = tsx_data_small_1.loc[["Standard and Poor's/Toronto
11
12 # - get time series data
13 tsx_data_small_3 = tsx_data_small_2.set_index("Year")
14 tsx_data_small_4 = tsx_data_small_3[["VALUE",
15                                     "REF_DATE"]]
16
17 # - get yearly change
18 tsx_data_small_4["Month"] = tsx_data_small_4["REF_DATE"].str[-2:]
19
20 tsx_data_small_4["Date"] = pd.to_datetime(tsx_data_small_4["REF_DATE"]
21 tsx_data_small_4 = tsx_data_small_4.reset_index()
22
23 tsx_data_small_5 = tsx_data_small_4[["Date",
24                                     "VALUE",
25                                     "Year"]]
26
27 tsx_data_small_6 = tsx_data_small_5.set_index(["Date", "Year"])
28
29 tsx_data_small_7 = tsx_data_small_6.pct_change()
30 tsx_data_small_7 = tsx_data_small_7.reset_index()

```

```

31
32 tsx_data_small_8 = tsx_data_small_7.loc[pd.to_numeric(tsx_data_small_
33
34 tsx_data_small_8["TSX Pct Change"] = tsx_data_small_8["VALUE"]*100
35 tsx_data_small_9 = tsx_data_small_8[["Date",
36                                     "TSX Pct Change"]]
37
38
39 # tsx_data_small_9.rename(columns = {'VALUE':'TSX pct change'}, inplace=
40
41 # - write to csv
42 tsx_data_small_9.to_csv("cleaned_data/tsx_change_clean.csv")
43
44 tsx_change_clean = tsx_data_small_9

```

/opt/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:18: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using `.loc[row_indexer,col_indexer] = value` instead

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/opt/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:20: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using `.loc[row_indexer,col_indexer] = value` instead

In [76]: 1 tsx_change_clean.head()

Out[76]:

	Date	TSX Pct Change
12	2010-01-01	-5.549071
13	2010-02-01	4.825176
14	2010-03-01	3.509140
15	2010-04-01	1.436899
16	2010-05-01	-3.666538

In [77]:

```
1  # - 2e. merge datasets into 1 df
2
3  # housing_index_data_clean
4  # mortgage_rate_clean
5  # tsx_change_clean
6  # household_spending_clean
7  # financial_health_stats_clean
8
9  # - merge housing index and mortgage rate
10 merge1 = pd.merge(mortgage_rate_clean, housing_index_data_clean, on = "Date")
11
12 # - merge in tsx change
13 merge2 = pd.merge(merge1, tsx_change_clean, on = "Date")
14
15 # - merge in household spending
16 merge3 = pd.merge(merge2, household_spending_clean, on = "Date")
17
18 # - merge in financial health stats
19 merge4 = pd.merge(merge3, financial_health_stats_clean, on = "Date")
20
21 regression_data = merge4.set_index("Date")
22
23 # - write to csv
24 regression_data.to_csv("cleaned_data/regression_data.csv")
```

In [78]: 1 regression_data

Out[78]:

	Mortgage Rate	Alberta	Atlantic Region	British Columbia	Manitoba	New Brunswick	Newfoundland and Labrador	Nova Scotia	Onta
Date									
2010-01-01	4.80	92.7	93.6	94.5	80.2	97.3	92.9	90.6	71
2010-02-01	4.73	92.9	93.6	95.2	80.4	97.5	92.9	90.7	71
2010-03-01	4.71	93.3	93.6	96.2	80.9	97.5	92.9	90.8	71
2010-04-01	5.15	93.3	94.1	96.7	81.2	97.4	94.2	90.8	71
2010-05-01	5.30	93.7	94.4	97.0	81.5	97.9	94.5	90.9	71
...
2017-08-01	3.82	100.1	99.9	107.8	103.6	100.5	98.6	100.9	101
2017-09-01	3.89	99.9	100.0	108.2	104.1	100.5	98.6	101.0	101
2017-10-01	3.98	100.0	100.0	108.7	104.2	100.5	98.6	101.4	101
2017-11-01	4.04	100.2	100.2	108.7	104.4	100.9	98.8	101.4	101
2017-12-01	4.07	100.0	100.3	108.7	104.5	101.1	98.8	101.3	101

96 rows × 16 columns

In [79]: 1 regression_data.info()

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 96 entries, 2010-01-01 to 2017-12-01
Data columns (total 16 columns):
#   Column                                Non-Null Count  Dtype
---  -
0   Mortgage Rate                        96 non-null     float64
1   Alberta                             96 non-null     float64
2   Atlantic Region                      96 non-null     float64
3   British Columbia                    96 non-null     float64
4   Manitoba                             96 non-null     float64
5   New Brunswick                       96 non-null     float64
6   Newfoundland and Labrador           96 non-null     float64
7   Nova Scotia                         96 non-null     float64
8   Ontario                             96 non-null     float64
9   Prince Edward Island                96 non-null     float64
10  Quebec                              96 non-null     float64
11  Saskatchewan                         96 non-null     float64
12  TSX Pct Change                      96 non-null     float64
13  Total expenditure                    96 non-null     float64
..  ..                                ..            ..
..  ..                                ..            ..
```

2. Data exploration

In [80]:

```
1 # - 2a. convert to date format
2 housing_data_small_plotting = housing_data_small_4.reset_index()
3 housing_data_small_plotting["Month"] = housing_data_small_plotting["Date"]
4 housing_data_small_plotting["Date-str"] = "1 " + housing_data_small_plotting["Date"]
5
6 housing_data_small_plotting["Date"] = pd.to_datetime(housing_data_small_plotting["Date-str"])
7
8 housing_data_small_plotting = housing_data_small_plotting[["Date",
9                                                             "VALUE",
10                                                            "GEO"]]
11 housing_data_small_plotting.head()
```

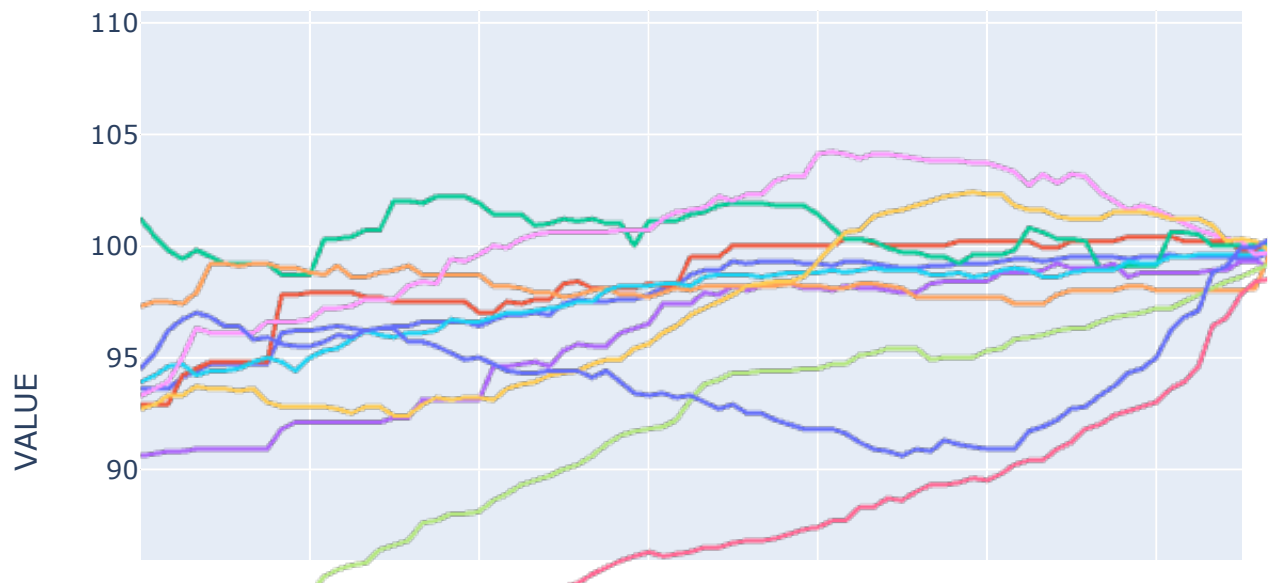
Out[80]:

	Date	VALUE	GEO
0	2010-01-01	93.6	Atlantic Region
1	2010-01-01	92.9	Newfoundland and Labrador
2	2010-01-01	101.2	Prince Edward Island
3	2010-01-01	90.6	Nova Scotia
4	2010-01-01	97.3	New Brunswick

```

In [81]: 1 # - 2b. plot time series by region
2 import plotly.express as px
3 import plotly.graph_objects as go
4
5
6 housing_index_plot = px.line(housing_data_small_plotting ,
7                             x="Date",
8                             y="VALUE",
9                             color="GEO",
10                             line_group="GEO",
11                             hover_name="GEO")
12
13 # write to html
14 housing_index_plot.write_html("cleaned_data/housing_index_plot.html")
15
16 housing_index_plot.show()
17
18 # (sometimes the plot doesn't show)
19
20 # it usually works better when the zoom on the top right hand corner
21
22 # the data was standardized using 2017 as index, which is why the li

```



3. Multivariate Linear Regression

- Regress housing index for each province on all other factors
- Compute R squared value for each province, which gives measure of how integrated the province's housing returns are with the rest of the economy

```
In [82]: 1 # - 3a. write regression function to get R squared value for Alberta
2
3 # - get explanatory vars
4 X = regression_data.drop(["Alberta",
5                           "British Columbia",
6                           "Saskatchewan",
7                           "Manitoba",
8                           "Quebec",
9                           "Ontario",
10                          "Newfoundland and Labrador",
11                          "Nova Scotia",
12                          "Atlantic Region",
13                          "New Brunswick",
14                          "Prince Edward Island"], axis = 1).copy()
15
16 # - get y for Alberta
17 ab_true = regression_data["Alberta"]
18
19 # - set the model instance for Alberta
20 alberta_model = linear_model.LinearRegression()
21 alberta_model.fit(X, ab_true)
22
23 # - print coefficients to check
24 alberta_model.intercept_
25 # intercept : -101.25278654861009
26 alberta_coefs = pd.Series(dict(zip(list(X), alberta_model.coef_)))
27 alberta_coefs
```

```
Out[82]: Mortgage Rate          1.481234
TSX Pct Change          0.015356
Total expenditure       0.003602
Total current consumption -0.004274
Debt to disposable income ratio -0.019740
dtype: float64
```

```
In [83]: 1 # - get R-squared value for Alberta :
        2 # - higher. R squared value means higher cointegration of Alberta's
        3 ab_r2 = alberta_model.score(X, ab_true)
        4 ab_r2
```

Out[83]: 0.9588117090190931

```
In [84]: 1 # - 3b. get r2 score for all other variables
        2
        3 def get_r2_score(province:str, df:pd.DataFrame, x:pd.DataFrame):
        4     """
        5     get r2 value for each province
        6     """
        7     # explanatory vars
        8     province_true = df[province]
        9
        10    # set model instance
        11    province_model = linear_model.LinearRegression()
        12    province_model.fit(X, province_true)
        13
        14    # get r2
        15    r2 = province_model.score(X, province_true)
        16
        17    return r2
```

```
In [85]: 1 get_r2_score("Quebec", regression_data, X)
```

Out[85]: 0.9234561210118982

In [86]:

```
1  # - get dataframe of r2 scores
2
3  province = ["Alberta",
4              "British Columbia",
5              "Saskatchewan",
6              "Manitoba",
7              "Quebec",
8              "Ontario",
9              "Newfoundland and Labrador",
10             "Nova Scotia",
11             "Atlantic Region",
12             "New Brunswick",
13             "Prince Edward Island"]
14
15  r2 = []
16  for p in province:
17      score = get_r2_score(p, regression_data, X)
18      r2.append(score)
19  print (r2)
20
21  r2_scores = pd.DataFrame({"province":province,
22                           "r2score":r2})
23
24  # - write to csv
25  r2_scores.to_csv("cleaned_data/r2_data.csv")

[0.9588117090190931, 0.8363669273456951, 0.8070086015414639, 0.9536842
03647346, 0.9234561210118982, 0.9637419690886144, 0.7309201814771507,
0.9620597630269168, 0.9077251256117037, 0.6178935456376443, 0.22304545
44530599]
```

```
In [87]: 1 # - Alberta, Manitoba, Ontario, Nova Scotia and New Brunswick are high
        2 # - Saskatchewan, Newfoundland & Labrador, and PEI are the least inter
        3 r2_scores
```

Out[87]:

	province	r2score
0	Alberta	0.958812
1	British Columbia	0.836367
2	Saskatchewan	0.807009
3	Manitoba	0.953684
4	Quebec	0.923456
5	Ontario	0.963742
6	Newfoundland and Labrador	0.730920
7	Nova Scotia	0.962060
8	Atlantic Region	0.907725
9	New Brunswick	0.617894
10	Prince Edward Island	0.223045

5. Load results onto map

```
In [88]: 1 # - clean boundary file
        2 boundary_data = gpd.read_file("project_data/boundary_clean.json")
        3 boundary_data = boundary_data.set_index("PRENAME")
        4
        5 boundary_data_small = boundary_data.loc[["Alberta",
        6                                         "British Columbia",
        7                                         "Saskatchewan",
        8                                         "Manitoba",
        9                                         "Quebec",
        10                                        "Ontario",
        11                                        "Newfoundland and Labrador",
        12                                        "Nova Scotia",
        13                                        "New Brunswick",
        14                                        "Prince Edward Island"]]
        15
        16 # - write to geojson file
        17 boundary_data_small.to_file("cleaned_data/boundary_clean.json", driver="GeoJSON")
```

```

In [89]: 1 # - get colours by r2 value
          2 r2_scores_plotting = r2_scores.set_index("province")
          3 r2_scores_plotting = r2_scores_plotting.drop(["Atlantic Region"], ax:
          4
          5 r2_scores_plotting["hue"] = np rint((r2_scores_plotting["r2score"]-0
          6
          7 r2_scores_plotting["hue"] = r2_scores_plotting["hue"].astype(int)
          8
          9 r2_scores_plotting

```

Out[89]:

	r2score	hue
province		
Alberta	0.958812	152
British Columbia	0.836367	127
Saskatchewan	0.807009	121
Manitoba	0.953684	151
Quebec	0.923456	145
Ontario	0.963742	153
Newfoundland and Labrador	0.730920	106
Nova Scotia	0.962060	152
New Brunswick	0.617894	84
Prince Edward Island	0.223045	5

```
In [90]: 1 # - get rgb values
2 rgb = []
3 for c in r2_scores_plotting["hue"]:
4     rgb_cols = '#%02x%02x%02x' % (255-c, c, 255)
5     rgb = rgb + [rgb_cols]
6 print (rgb)
7
8
9 r2_scores_plotting["rgb"] = rgb
10 r2_scores_plotting
```

```
['#6798ff', '#807fff', '#8679ff', '#6897ff', '#6e91ff', '#6699ff', '#956aff', '#6798ff', '#ab54ff', '#fa05ff']
```

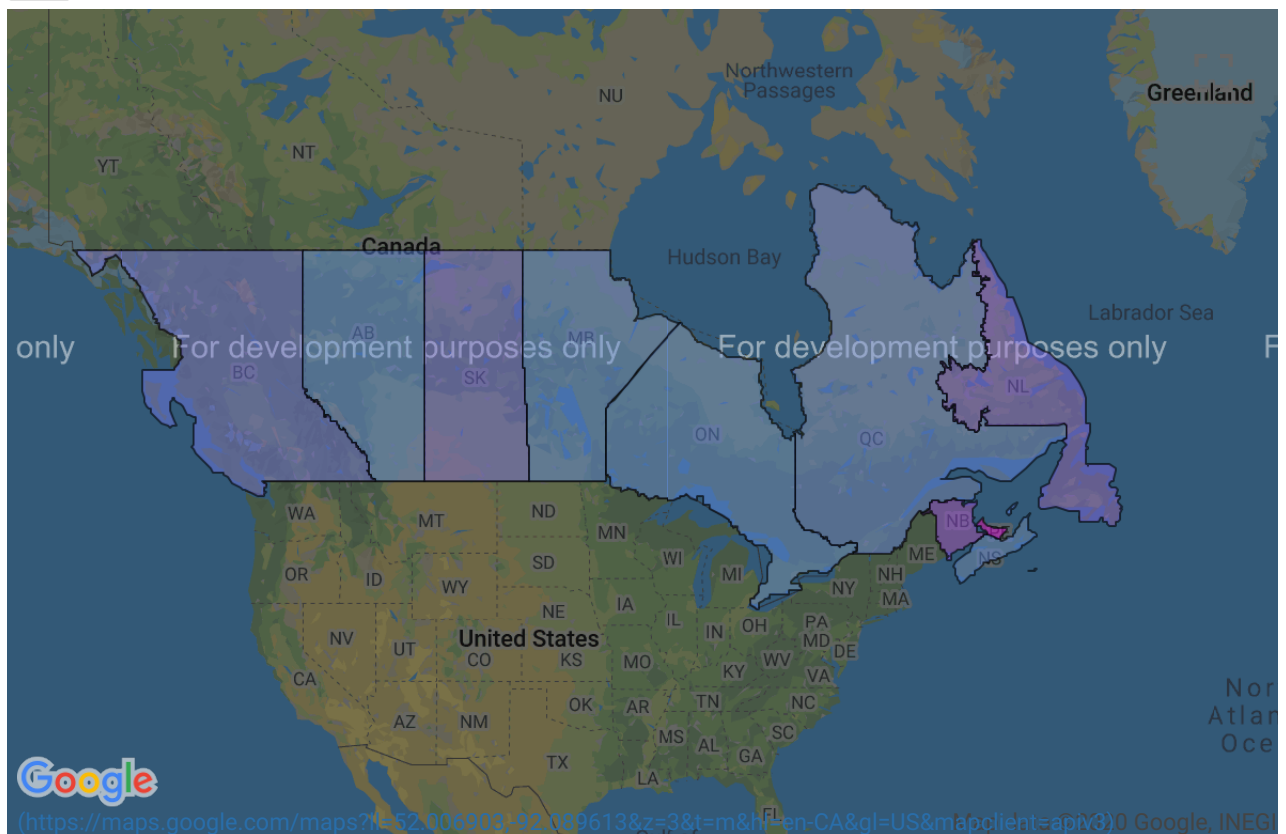
Out[90]:

	r2score	hue	rgb
province			
Alberta	0.958812	152	#6798ff
British Columbia	0.836367	127	#807fff
Saskatchewan	0.807009	121	#8679ff
Manitoba	0.953684	151	#6897ff
Quebec	0.923456	145	#6e91ff
Ontario	0.963742	153	#6699ff
Newfoundland and Labrador	0.730920	106	#956aff
Nova Scotia	0.962060	152	#6798ff
New Brunswick	0.617894	84	#ab54ff
Prince Edward Island	0.223045	5	#fa05ff

```

In [91]: 1 # - load onto google maps
          2
          3 # - get google maps api
          4 apikey = "AIzaSyDzJhxiVPyQ4y0Ycb9f3hJ5vyzxMbjmdB4"
          5 gmaps.configure(api_key = apikey)
          6
          7 # - get figure
          8 fig = gmaps.figure()
          9
         10 # - get canada boundaries
         11 canada_boundaries = open("cleaned_data/boundary_clean.json")
         12 canada_boundaries = json.load(canada_boundaries)
         13
         14 colours = []
         15
         16 boundary_layer = gmaps.geojson_layer(canada_boundaries,
         17                                     fill_color = rgb)
         18 fig.add_layer(boundary_layer)
         19 # - we see that PEI, Newfoundland, Sask, and (surprisingly) British
         20 #   less integrated with the Canadian economy
         21
         22 fig

```



```

In [92]: 1 # - plot population onto map to see where people are moving to as he

```

```

2
3 # - read in data
4 population_data = pd.read_csv("project_data/employment.csv", delimiter=";", encoding="utf-8")
5 population_data
6
7 # - clean data
8 population_data_small = population_data.loc[population_data["Statistic"] == "Population"]
9 population_data_small["Year"] = population_data_small["REF_DATE"].str[:4]
10
11 population_data_small = population_data_small.loc[population_data_small["Year"] != 2015]
12
13 population_data_small = population_data_small.loc[population_data_small["Year"] != 2020]
14
15 population_data_small = population_data_small[[ "REF_DATE",
16                                                  "GEO",
17                                                  "Labour force characteristics",
18                                                  "VALUE" ]]
19
20 # - get population change over last 5 years
21 relevant_2015 = (population_data_small["REF_DATE"] == "2015-03")
22 population_data_2015 = population_data_small.loc[relevant_2015]
23 population_data_2015.rename(columns = {'VALUE': 'Population 2015'}, inplace=True)
24
25 relevant_2020 = (population_data_small["REF_DATE"] == "2020-03")
26 population_data_2020 = population_data_small.loc[relevant_2020]
27 population_data_2020.rename(columns = {'VALUE': 'Population 2020'}, inplace=True)
28
29 population_clean = pd.merge(population_data_2020, population_data_2015, on="GEO", how="left")
30
31 population_clean["Population_change"] = (1.5 + 100*(population_clean["Population 2020"] - population_clean["Population 2015"])/population_clean["Population 2015"])
32
33 population_clean = population_clean.set_index("GEO")
34 population_clean = population_clean.drop(["Canada",
35                                           "Alberta",
36                                           "British Columbia",
37                                           "Saskatchewan",
38                                           "Manitoba",
39                                           "Quebec",
40                                           "Ontario",
41                                           "Newfoundland and Labrador",
42                                           "Nova Scotia",
43                                           "New Brunswick",
44                                           "Prince Edward Island",
45                                           "Ottawa-Gatineau, Ontario/Quebec",
46                                           "Ottawa-Gatineau, Quebec province",
47                                           "Ottawa-Gatineau, Ontario province"])

```

/opt/anaconda3/lib/python3.7/site-packages/IPython/core/interactiveshell.py:3063: DtypeWarning: Columns (12) have mixed types. Specify dtype option on import or set pd.options.infer_datetime_from_object = False

columns (13) have mixed types. Specify dtype option on import or set to w_memory=False.

/opt/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:9: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
(https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy)

/opt/anaconda3/lib/python3.7/site-packages/pandas/core/frame.py:4133:

In [93]:

```

1 # convert to geodataframe
2 import geopandas as gpd
3 import geopy as gpy
4 from geopandas.tools import geocode
5 from geopy.geocoders import Nominatim
6
7 population_geo = gpd.GeoDataFrame(population_clean)
8 population_geo = population_geo.reset_index()
9
10 population_geo = population_geo.replace({"GEO": "St. Catharines-Niagara",
11 population_geo = population_geo.replace({"GEO": "Kitchener-Cambridge",
12 population_geo = population_geo.replace({"GEO": "Abbotsford-Mission",
13 population_geo

```

Out[93]:

	GEO	REF_DATE_x	Labour force characteristics_x	Population 2020	REF_DATE_y	Labour force characteristics_y	Pop
0	St. John's, Newfoundland and Labrador	2020-03	Population	187.0	2015-03	Population	
1	Halifax, Nova Scotia	2020-03	Population	379.6	2015-03	Population	
2	Moncton, New Brunswick	2020-03	Population	133.0	2015-03	Population	
3	Saint John, New Brunswick	2020-03	Population	107.7	2015-03	Population	
4	Saguenay, Quebec	2020-03	Population	133.4	2015-03	Population	
5	Québec, Quebec	2020-03	Population	690.1	2015-03	Population	

In [94]:

```

1 # convert to geodataframe
2 import geopandas as gpd
3 import geopy as gpy
4 from geopandas.tools import geocode
5 from geopy.geocoders import Nominatim
6
7 population_geo = gpd.GeoDataFrame(population_clean)
8 population_geo = population_geo.reset_index()
9
10 population_geo.replace({"GEO": "St. Catharines-Niagara, Ontario"}, "St. Catharines-Niagara, Ontario")
11 population_geo.replace({"GEO": "Kitchener-Cambridge-Waterloo, Ontario"}, "Kitchener-Cambridge-Waterloo, Ontario")
12 population_geo.replace({"GEO": "Kitchener-Cambridge-Waterloo, Ontario"}, "Kitchener-Cambridge-Waterloo, Ontario")

```

Out[94]:

	GEO	REF_DATE_x	Labour force characteristics_x	Population 2020	REF_DATE_y	Labour force characteristics_y	Pop
0	St. John's, Newfoundland and Labrador	2020-03	Population	187.0	2015-03	Population	
1	Halifax, Nova Scotia	2020-03	Population	379.6	2015-03	Population	
2	Moncton, New Brunswick	2020-03	Population	133.0	2015-03	Population	
3	Saint John, New Brunswick	2020-03	Population	107.7	2015-03	Population	
4	Saguenay, Quebec	2020-03	Population	133.4	2015-03	Population	
5	Québec, Quebec	2020-03	Population	690.1	2015-03	Population	

In [95]:

```

1 # convert to geodataframe
2 import geopandas as gpd
3 import geopy as gpy
4 from geopandas.tools import geocode
5 from geopy.geocoders import Nominatim
6
7 population_geo = gpd.GeoDataFrame(population_clean)
8 population_geo = population_geo.reset_index()
9
10 population_geo.replace({"GEO": "St. Catharines-Niagara, Ontario"}, "St. Catharines-Niagara, Ontario")
11 population_geo.replace({"GEO": "Kitchener-Cambridge-Waterloo, Ontario"}, "Kitchener-Cambridge-Waterloo, Ontario")
12 population_geo.replace({"GEO": "Kitchener-Cambridge-Waterloo, Ontario"}, "Kitchener-Cambridge-Waterloo, Ontario")

```

Out[95]:

	GEO	REF_DATE_x	Labour force characteristics_x	Population 2020	REF_DATE_y	Labour force characteristics_y	Pop
--	-----	------------	--------------------------------	-----------------	------------	--------------------------------	-----

0	St. John's, Newfoundland and Labrador	2020-03	Population	187.0	2015-03	Population
1	Halifax, Nova Scotia	2020-03	Population	379.6	2015-03	Population
2	Moncton, New Brunswick	2020-03	Population	133.0	2015-03	Population
3	Saint John, New Brunswick	2020-03	Population	107.7	2015-03	Population
4	Saguenay, Quebec	2020-03	Population	133.4	2015-03	Population
5	Québec, Quebec	2020-03	Population	690.1	2015-03	Population
6	Sherbrooke, Quebec	2020-03	Population	189.4	2015-03	Population
7	Trois-Rivières, Quebec	2020-03	Population	135.6	2015-03	Population
8	Montréal, Quebec	2020-03	Population	3546.1	2015-03	Population
9	Kingston, Ontario	2020-03	Population	147.4	2015-03	Population
10	Peterborough, Ontario	2020-03	Population	108.4	2015-03	Population
11	Oshawa, Ontario	2020-03	Population	350.0	2015-03	Population
12	Toronto, Ontario	2020-03	Population	5649.2	2015-03	Population
13	Hamilton, Ontario	2020-03	Population	684.6	2015-03	Population
14	St. Catharines- Niagara, Ontario	2020-03	Population	360.2	2015-03	Population
15	Kitchener, Ontario	2020-03	Population	454.0	2015-03	Population
16	Brantford, Ontario	2020-03	Population	119.2	2015-03	Population
17	Guelph, Ontario	2020-03	Population	141.5	2015-03	Population
18	London, Ontario	2020-03	Population	452.6	2015-03	Population
	Windsor,					

19	Ontario	2020-03	Population	298.3	2015-03	Population
20	Barrie, Ontario	2020-03	Population	182.4	2015-03	Population
21	Greater Sudbury, Ontario	2020-03	Population	141.3	2015-03	Population
22	Thunder Bay, Ontario	2020-03	Population	104.6	2015-03	Population
23	Winnipeg, Manitoba	2020-03	Population	704.3	2015-03	Population
24	Regina, Saskatchewan	2020-03	Population	215.0	2015-03	Population
25	Saskatoon, Saskatchewan	2020-03	Population	279.9	2015-03	Population
26	Calgary, Alberta	2020-03	Population	1292.8	2015-03	Population
27	Edmonton, Alberta	2020-03	Population	1203.0	2015-03	Population
28	Kelowna, British Columbia	2020-03	Population	168.5	2015-03	Population
29	Abbotsford-Mission, British Columbia	2020-03	Population	160.1	2015-03	Population
30	Vancouver, British Columbia	2020-03	Population	2302.5	2015-03	Population
31	Victoria, British Columbia	2020-03	Population	324.8	2015-03	Population

In [96]:

```

1 # - the following code will time out, so the file was loaded in and
2 # geo = geocode(population_geo["GEO"], provider = "nominatim")
3 # geo

```

In [97]:

```

1 # - write to file
2 geo.to_file("cleaned_data/city_coords.json", driver="GeoJSON")

-----
-----
NameError                                Traceback (most recent call
last)
<ipython-input-97-d11604e34d95> in <module>
      1 # - write to file
----> 2 geo.to_file("cleaned_data/city_coords.json", driver="GeoJSON")

NameError: name 'geo' is not defined

```

In [98]:

```

1 # - merge population change as weights for heatmap
2 population_locations = gpd.read_file("cleaned_data/city_coords.json")
3 population_locations["Population change"] = population_geo["Population change"]
4 population_locations["coordinates"] = (population_locations["geometry"].to_wkt()
5 # population_locations.to_file("cleaned_data/copied_data/city_coords.json")
6 population_locations.head()

```

Out[98]:

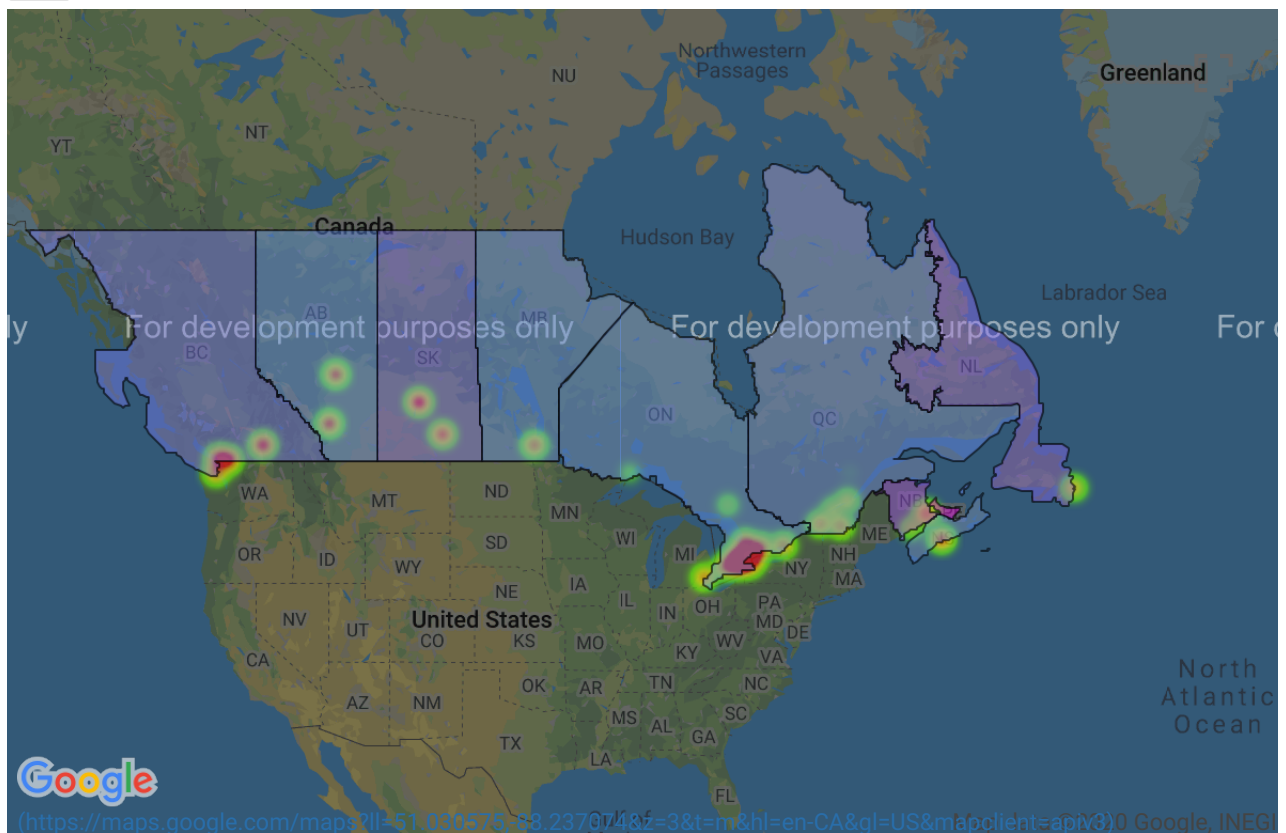
	address	geometry	Population change	coordinates
0	St. John's, Newfoundland, Newfoundland and Lab...	POINT (-52.71515 47.56170)	65.561798	POINT (-52.71515 47.56170)
1	Halifax, Halifax County, Nova Scotia, Canada	POINT (-63.58595 44.64862)	109.894722	POINT (-63.58595 44.64862)
2	Moncton, Moncton Parish, New Brunswick, Canada	POINT (-64.80011 46.09799)	94.545455	POINT (-64.80011 46.09799)
3	Saint John, City of Saint John, Saint John Cou...	POINT (-66.05804 45.27875)	34.886364	POINT (-66.05804 45.27875)
4	Saguenay, Saguenay-Lac-Saint-Jean, Québec, G7H...	POINT (-71.06918 48.40596)	2.416728	POINT (-71.06918 48.40596)

In [99]:

```

1 # add population flow layer
2 s = gpd.GeoSeries(population_locations["geometry"])
3 x_coords = s.apply(lambda p: p.x)
4
5 s = gpd.GeoSeries(population_locations["geometry"])
6 y_coords = s.apply(lambda p: p.y)
7
8 locations = pd.DataFrame(y_coords)
9 locations["longitude"] = x_coords
10 locations.rename(columns = {"geometry": 'latitude'}, inplace = True)
11
12
13 weights = population_locations["Population change"]
14
15 fig.add_layer(gmaps.heatmap_layer(locations, weights = weights))
16
17 fig
18 # more intense colours show that more people have immigrating been t.

```



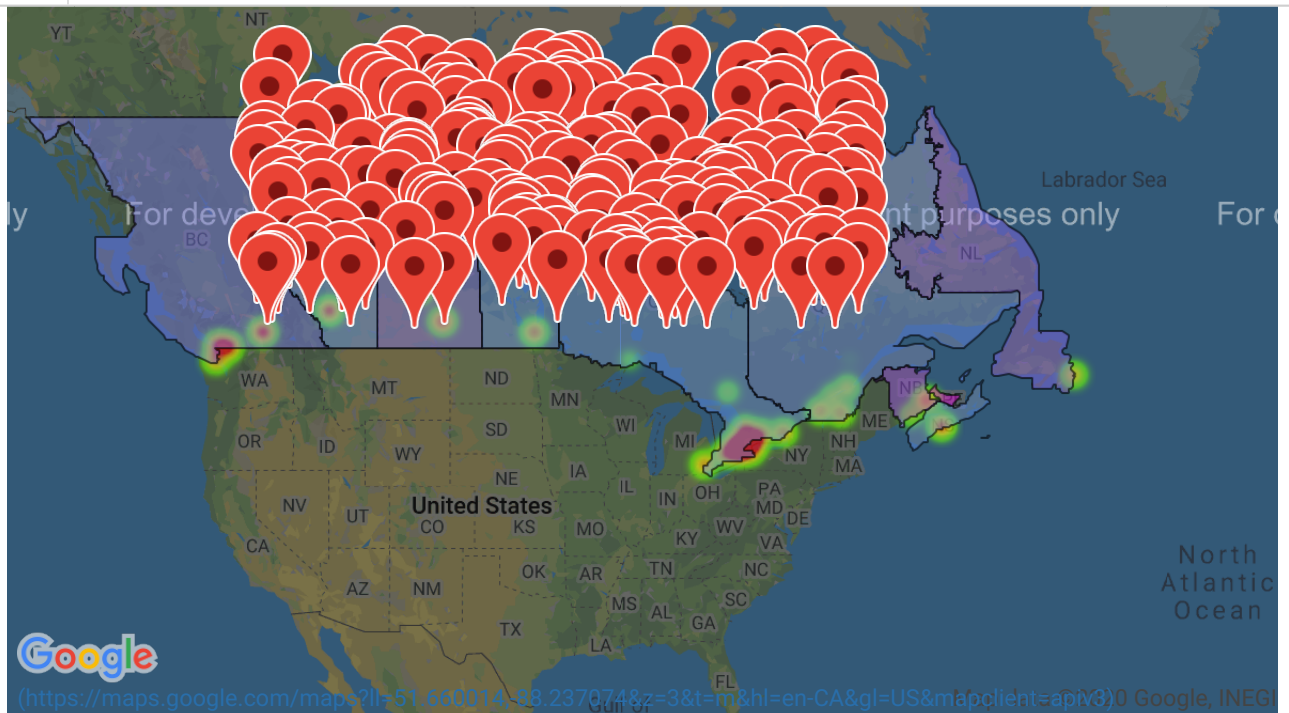
In [100]:

```

1  # - plotting an arbitrary portfolio
2
3  # get random real estate portfolio
4
5  np.random.seed(123)
6  # get holding_type column
7  holding_type = ["Residential"]*50 + ["Industrial"]*50 + ["Office"]*50
8  portfolio = {"holding_type": holding_type}
9  portfolio = pd.DataFrame.from_dict(portfolio)
10
11 # get market value column
12 portfolio['mkt_value'] = np.random.randint(100_000, 50_000_000, port:
13
14
15 #get random coordinates x
16 x_coords = np.random.randint(5000, 6000, 200)/100
17 portfolio['x_coords'] = x_coords
18
19
20 #get random coordinates y
21 y_coords = np.random.randint(-12000, -7000, 200)/100
22 portfolio['y_coords'] = y_coords
23
24
25 # get in point format
26 portfolio["coords"] = gpd.GeoSeries([Point(x, y) for x, y in zip(x_co
27 portfolio["location"] = [(x, y) for x, y in zip(x_coords, y_coords)
28
29 portfolio.to_csv("cleaned_data/portfolio")
30
31 locs = portfolio["location"]
32
33 mkt_vals = [f"${str(i)}" for i in list(portfolio["mkt_value"])]
34
35 holding_type = list(portfolio["holding_type"])
36
37 def join_lists(list1, list2):
38     n = 0
39     acc = []
40     for i in list1:
41         info = (f"Type = {list1[n]}, Price = {list2[n]}")
42         acc = acc + [info]
43         n = n + 1
44     return acc
45
46 holding_info = join_lists(holding_type, mkt_vals)
47
48 fig.add_layer(gmaps.marker_layer(locations = locs, info_box_content =

```

```
In [101]: 1 # show figure  
          2 fig
```



```
In [ ]:
```

```
1
```