

```

N3> (format t "~A~&;~v@{~A~:*~}~&" *PART-X* 36 #\*)
STUDY
; *****
NIL
N3>

```

## Untitled #2

unfolding work

### 1 ... as a heuristic of the connectionism ...

In this study, *Neuromuse3* is experimented according to an apriori corpus learned, and interpreted in terms of probabilities involving mainly the Markov processes. The connectionism network thus initiated allows to built sequences according to the emergent characteristic of the network in terms of cliques and *tournois*.

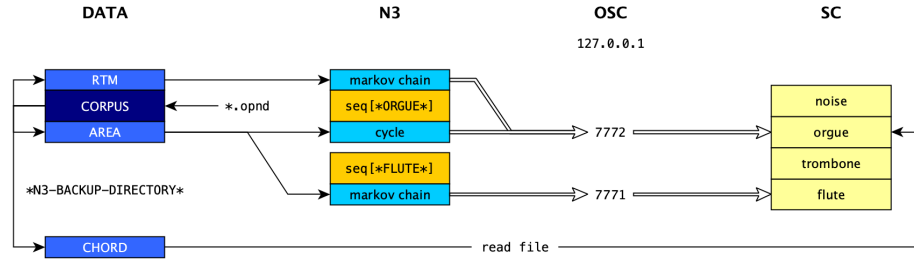


FIGURE 1 – Synoptic overview – data → N3 → SC.

According to the synoptic overview on figure 1, we start from a corpus composed of sequences, which are composed of voices. Then, the parsing of the corpus encodes the duration, degree, and interval to the next note in the N3 AREA, which will learn voices by voices as monody.

Second step, the rhythm of each voice is recorded in a file in order to be used as a corpus dataset of the sequencing in terms of probabilities.

Finally, the harmony context is parsed as a sequence of chords defined by the ordered degrees, in order to interact in the field of this harmony.

N3 as a connectionism network sent by OSC protocol a monophonic Markov chain, plus a combination of emergent cycles of the area.

SuperCollider receives and interprets OSC messages via a mixer (see figure 4 on page 8 and figure 5 on page 9) where each instrument shares or conditions the data with the others (see figures 2 and 3).

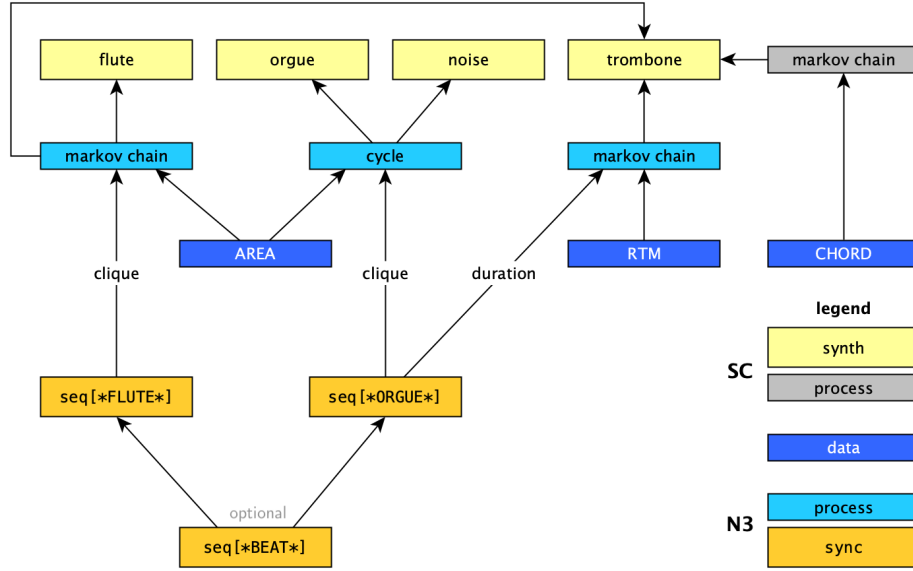


FIGURE 2 – Synoptic overview of the dependencies between components of the global process.

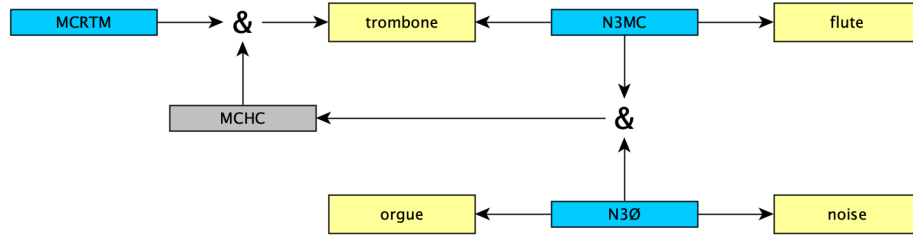


FIGURE 3 – Synoptic overview of which processes are involved at the synthesis level as arguments.

**Legend :**

- MCRTM → markov chain according to the learned rhythms ;
- N3Ø → the emergent cycle of AREA ;
- N3MC → global AREA markov chain ;
- MCHC → markov chain according to the harmonic context.

## 1.1 Learning dataset

Source<sup>1</sup> ... First book of J. S. Bach's *Das Wohltemperirte Klavier* (BWV 846 – 869), 41544 notes ...

```
1 N3> (load (mk-path "OPND" "N3" "opt"))
2 ---> OPND.lisp loaded
3 N3> (defparameter +corpus+
4   (loop
5     for file in
6       (directory ".../bach-database/ps13escomopnd/*-mel.opnd")
7     ;; for this corpus every 4 files the tonality increases by 1
8     ;; ---> (M prelude, M fugue, m prelude, m fugue)
9     ;; so the floor function on 0.25 step allows to transpose
10    ;; all files by 4 to modulo 0 -- i.e. C
11    for tune from 0 by 0.25
12    collect (map-opnd file
13              :tune (floor tune)
14              :out ".../chord.data")))
15 +CORPUS+
16 #|
17 ( ;; list of sequences
18   ( ;; sequence_1
19     ( ;; voice_1
20       (dur_1 deg_1 int_1 chord_1)
21       (dur_2 deg_2 int_2 chord_2)
22       ...
23       (dur_n deg_n int_n chord_n)
24     )
25   )
26 )
27 |#
28 ;; format the file generated previously
29 ;; with the function map-opnd with the key :out
30 N3> (df2sc (".../chord.data"))
31 ;; which generate the SuperCollider file
32 ;; .../chord.scd
33 ;; setting ~chord in SuperCollider environment
34 ; ---> see harmonic context voice 3
35 ;-----
36 ; ---> create and initiate area -- see annex 2.1
37 ;       with :cover-value 5 and :topology 3
38 ; the +CORPUS+ should be a list of sequence of cliques
39 ; then consider it as equal to (flat-once +corpus+)
40 ;-----
41 N3> (defparameter +rtm+ (flat-once (loop for seq in +corpus+
42   collect (loop for voice in seq when (butlast voice)
43     collect (butlast (mapcar #'car voice))))))
42 +RTM+
```

---

1. <http://www.titanmusic.com/data.php>

```

43 #|
44 ( ;; list of rtm by voice
45   (rtm_seq_1_voice_1)
46   (rtm_seq_1_voice_2)
47   ...
48   (rtm_seq_2_voice_1)
49   ...
50   (rtm_seq_n_voice_n)
51 )
52 |#
53 ; ---> see voices 2 and 3
54 ; +RTM+ as 'monnayage' of the voice 2 played by the voice 3

```

The retrieving of learned sequences from the corpus, despite the ‘cover value’ of 5, is not efficient enough because of the lack of discriminative parameters. Nevertheless, this study is rather focusing on an extremely minimalist approach than the ability to recognise sequence snippets from memory. Only, the matrix probabilities cannot reach 100%, which is not required because it is not a question of quotation or reference of the acquired. Then it is currently question to (a) envisage the potential of this AI in context according to the acquired, and (b) to underlining potential issues, such as computation time and interactivity between voices.

```

1 N3> (save corpus)

```

## 1.2 Sequencing instantiation

### 1.2.1 Voice 1

Initialisation of the voice 1 as a physical modeling flute in SC. This instance generates a Markov chain sequence according to two simple rules such as the next degree is evaluated according to the previous interval and avoids more than 4 successive repetitions in terms of duration. The number of repetitions can be modulated, as well as the pulse and the function of :odds.

```

1 ;;-----
2 (create-sequencing
3   :net CORPUS
4   :dub '*flute*
5   :pulse 3
6   :buffer-size 50
7   :port 7771)
8 ;;-----
9 ; this rule set the degree of the next event
10 ; according to the interval of the current one.
11 (set-rule *flute*
12   (let ((nn (mod (+ (cadr (car (buffer-out self)))
13                     ; minus 11 according to the encoding of intervals

```

```

14      (- (caddr (car (buffer-out self))) 11))
15      12)) ; modulo 12
16      ; no more than 4 repetitions duration allowed
17      (rep (remove-duplicates
18            (loop for i from 1 to 4 for c in (buffer-out self)
19              collect (car c))))
20      (if (singleton rep)
21          (list (caadr (pick-other-experience
22                     (locate-clique corpus (list '? nn '?))
23                     (list (car rep) nn '?)) nn '?))
24              (list '? nn '?))))
25      ;; hack to add next event to the OSC message
26      (setf (gethash 'ind (mem-cache *flute*)) :next)
27      ;;-----
28      (set-routine *flute*
29        (markov-chain self :buffer (buffer-out self)
30          :odds #'max-weighted))
31      ;;-----
32      (save *flute*)

```

### 1.2.2 Voice 2

The voice 2 as a physical modeling trombone (from FAUST<sup>2</sup> library as `pm.brass_ui` using `pm.brassModel`) in SC requires preliminary manipulation in order to define relevant descriptors in relation with its basics parameters (i.e. the pressure, the lips tension and the length of the tube).

Three parameters from the *UGen* named **Brass** as :

- `pressure` [0.1..1]
- `lips_tension` [0.1..1]
- `tube_length` [0.1..2.5] (should be done or tested on 0.01 step as 1 cm, but this will increase exponentially the possibility and this against the CPU and RAM resources)

One (plus one as reliability) from also SC with the *UGen* **Pitch** :

- `pitch` [freq|reliability]

And three more parameters (plus two as reliability) from the Praat analysis thanks to the preliminary analysis of the loudness profile and Common Lisp for the computation (see command line *enkode* with the option `-re` – version 7.0) in order to detect emergent frequency – as a kind of roughness indicator – from the peaks of the said loudness profile; the reliability is the standard deviation of the normalised values subtracted to one :

- `roughness` [freq|reliability]
- `loudness` [sone|reliability] (of the emergent frequency)
- `intensity` [dB] (of the sample)

---

2. <https://faust.grame.fr/>

More details about procedures, scripts and parameters in the SuperCollider `tbn2CSV.scd` file, plus annexes page 10, plus FAUST as `SynthDef \tbn` in `synths.scd` file.

On the SuperCollider side, – according to the the switching values of `flute/orgue` (■/□) and `RTM_(on/off)` (■/□) buttons on the SC gui – the trombone plays the following :

- `flute/RTM_off` – unison/octave of the flute ;
- `orgue/RTM_off` – unison/octave of the orgue with the rhythm of the flute ;
- `orgue/RTM_on` – unison/octave of the orgue with its own ‘mint’ rhythm ;
- `flute/RTM_on` – harmonic context of the flute and the orgue with its own ‘mint’ rhythm. The harmonic context is evaluated according to the data file `chord.scd` (see comment in the Section *Learning dataset*) as a dynamic Markov chain with the class `MarkovSet`<sup>3</sup> (see details in documentation of this class plus comment SC file).

### 1.2.3 Voice 3

Initialisation of the voice 3 as a kind of (original) organum in SC. This instance plays a pattern defined by interlacing emergent cycles for each MLT of the AREA.

Note that the rule has to return a *clique* with or without the wild card ‘?’ (without in that case), and the routine fills the buffer with that *clique* – by computation in case of a wild card. This can be done as an external function as `markov-chain`, or like here by coding directly knowing that the current sequencing is called by the argument *self*.

Alternative ‘routine’ for the third voice as a sub-rhythm-pattern<sup>4</sup> according to the corpus (N3 side) and using the contextual harmony (SC side) – i.e. degrees of flute and orgue plus their respective intervals. The corpus is the list of the durations of each voice of each sequence from the initial corpus.

```

1  ;;-----
2  (create-sequencing
3   :dub '*orgue*
4   :pulse 1/3 ;; meaning a pulse of 3 beat hence the value of
       the meter must to be a multiple of (/ 1 pulse)
5   :meter 12
6   :port 7772)
7  ;;-----
8  ;; set pattern
9  (require 'cl-cycle)
10 (set-pattern *orgue* (apply #'cl-cycle:interlace-cycle
11   (loop for s in (soms-list corpus) collect
12    (butlast (lst>trn (car (locate-cycle (id s)))))))

```

3. <https://github.com/yannics/MathLib/tree/yannics-patch-1>

4. Mint (*monnayage*), i.e. a replacement of a term by several more brief ones and overall length equivalent ; in other words fit the same duration.

```

13 ;;-----
14 ;; load alternative rhythm corpus as `monnayage'
15 (set-corpus *orgue* +rtm+)
16 ;; grab event in pattern
17 (set-rule *orgue*
18   (let ((cli (nth (mod (gethash 'pattern-counter
19     (mem-cache self)) (length (pattern self)))
20     (pattern self)))
21     (nextcli (nth (mod (1+ (gethash 'pattern-counter
22     (mem-cache self))) (length (pattern self)))
23     (pattern self))))
24 ;; compute rtm `monnayage'
25   (append cli nextcli (list! (next-event-probability
26     (/ (1+ (car cli)) (* +beat+ (pulse self))) self
27     :opt :sum :remanence :corpus :result :eval
28     :compute #'min-weighted))))))
29 ;;-----
30 (set-routine *orgue*
31   (push (funcall (rule self) self) (buffer-out self))
32   (incf (gethash 'pattern-counter (mem-cache self))))
33 ;;-----
34 (save *orgue*)

```

#### 1.2.4 Voice 4

The fourth voice consists to grab the pitch and incidentally the rhythm of the *\*orgue\** in order to ‘granulate’ by stepping frames through one sample, previously created for analysis, of the trombone. Each sample is selected according to its pitch as degree followed by its related pitch defined by its interval (at half time of the duration) matching (60..72).midicps as indices. (this does not affect the result as such, but allows to renew the sample according to some logical context).

#### 1.2.5 Voice 5

The pitches of the *\*orgue\** are interpreted with the *pseudo-UGen U1am* (See 7.6 in *Journal of Generative Sonic Art* [Ics 2014/24]).

The U1am’s parameters are :

- ar** – an array of frequencies correlated with the current degree of the *\*orgue\** :  
 (~frequencies/~frequencies.minItem).round(0.01)  
 \* (60..72).midicps[~degOrg]
- ind** – ~modeU1am (0 by default – *i.e.* reson and 1 for sine – as sound generator)
- stretch** ~tpsOrg as duration of the event.
- [ **nx** – 0 default value (fit the collatz profile into the duration) ]
- [ **ny** – \max default value (normalize the collatz profile with its max value) ]
- [ **sig** – \norm default value (normalize the output signal between -1 and 1) ]

**detune** –  $\sim\text{detune}$  (0.03) – detune randomly between  $-0.03\%$  and  $+0.03\%$  of each frequency of the input array

**rndAmp** –  $\sim\text{rndAmp}$  (0.1) – each collatz profile as signal is multiplied by a random value between 0.1 and 1

### 1.3 Playing time

```

1 (require 'N3)
2 ;;-----
3 ;; loading AREA and SEQUENCING
4 (progn
5   (load-neural-network "CORPUS")
6   (load-sequencing "flute")
7   (load-sequencing "orgue"))
8 ;;-----
9 ;; ... and play
10 (progn
11   (act-routine *flute*)
12   (act-routine *orgue*))
13 ;;-----
14 ;; ... and stop
15 (progn
16   (kill-routine *flute*)
17   (kill-routine *orgue*))

```

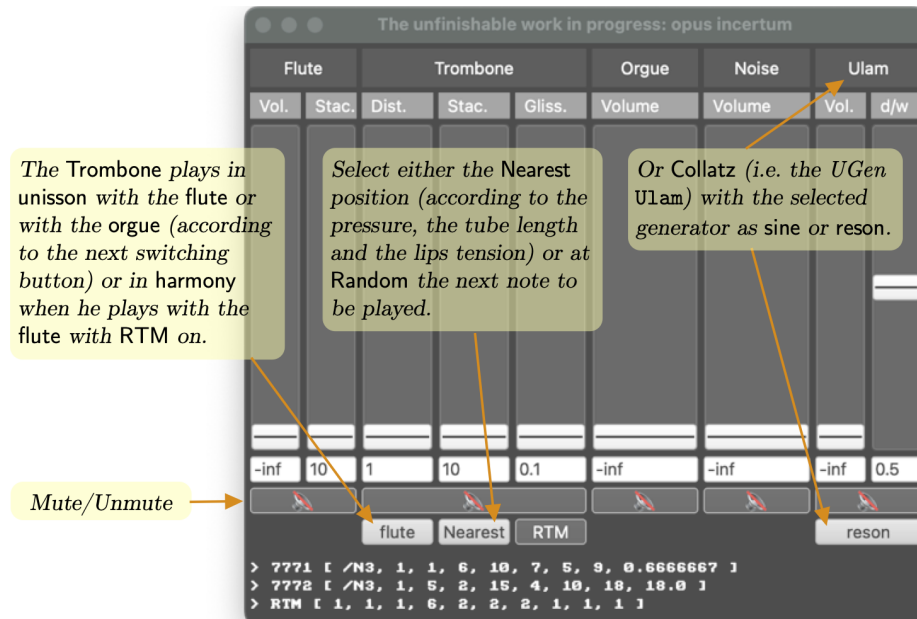


FIGURE 4 – SuperCollider GUI for mixing.



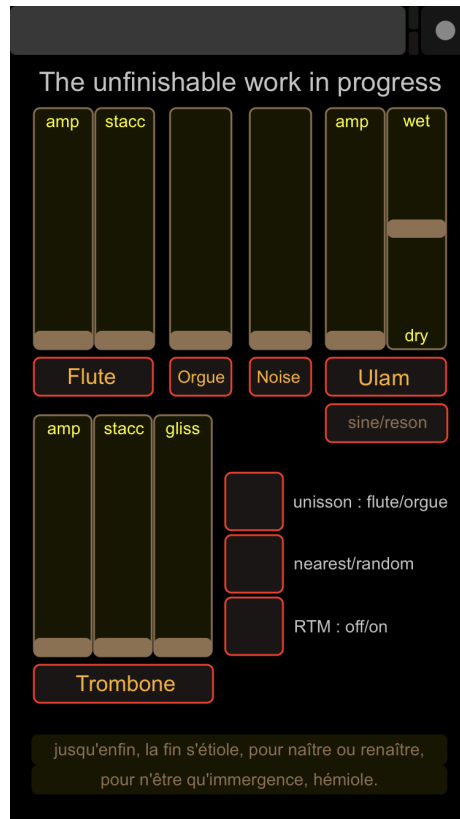
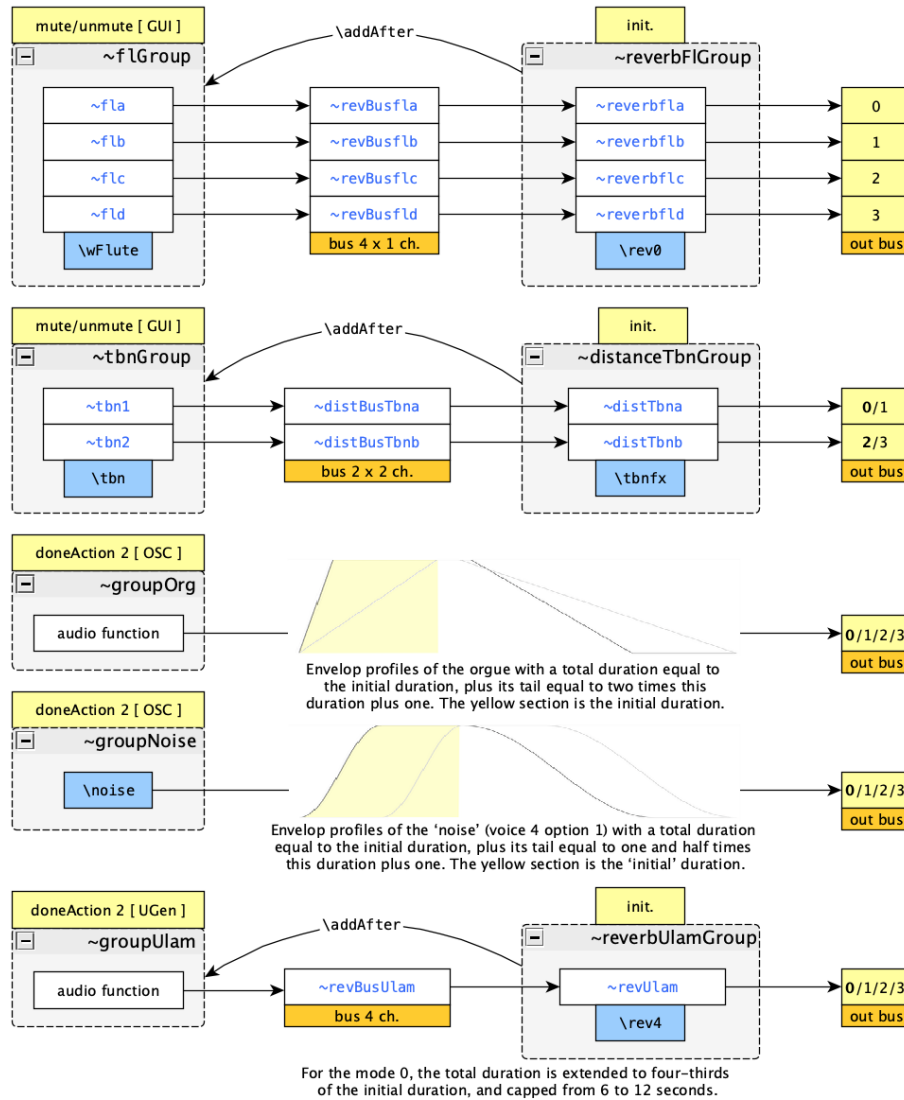


FIGURE 5 – The mixing stage can also be ensured on an iPhone thanks to the application TouchOSC Mk1 <sup>5</sup>.

5. <https://hexler.net/touchosc-mk1>

## Annexes

...



Synoptic overview of the synthesis and effects over busses.

## Psychoacoustics – Roughness

See Ics Y. *Journal of Generative Sonic Art* (2014/2024), Section 1.8.

Online at : <https://github.com/yannics/GSA/blob/master/gsa.pdf> [Accessed 19 décembre 2024]

Source : University of Salford Manchester

<https://hub.salford.ac.uk/sirc-acoustics/psychoacoustics/sound-quality-making-products-sound-better/an-introduction-to-sound-quality-testing/roughness-fluctuation-strength/>

### Next pages

Zwicker E., Fastl H. *Psychoacoustics : Facts and Models* (1990), pp. 247–264.

## 10. Fluctuation Strength

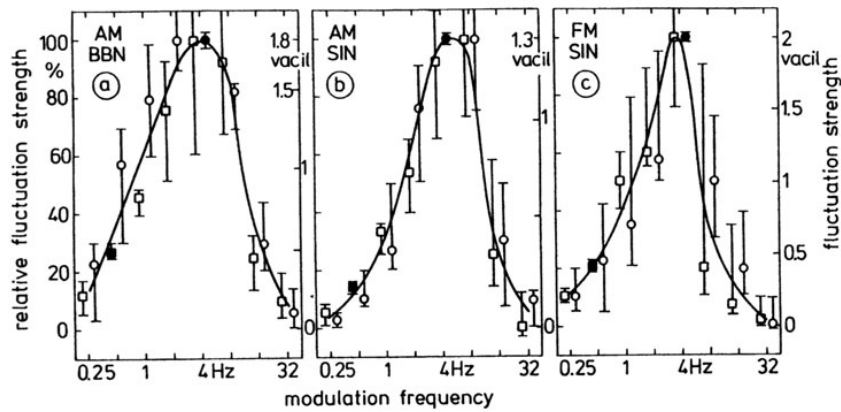
In this chapter, the fluctuation strength of amplitude-modulated broad-band noise, amplitude-modulated pure tones and frequency-modulated pure tones is addressed, and the dependence of fluctuation strength on modulation frequency, sound pressure level, modulation depth, centre frequency, and frequency deviation is assessed. In addition, the fluctuation strength of modulated sounds is compared to the fluctuation strength of narrow-band noises. Finally, a model of fluctuation strength based on the temporal variation of the masking pattern or loudness pattern is proposed.

### 10.1 Dependencies of Fluctuation Strength

Modulated sounds elicit two different kinds of hearing sensations: at low modulation frequencies up to a modulation frequency of about 20 Hz, the hearing sensation of fluctuation strength is produced. At higher modulation frequencies, the hearing sensation of roughness, discussed in detail in Chap. 11, occurs. For modulation frequencies around 20 Hz, there is a transition between the hearing sensation of fluctuation strength and that of roughness. It is a smooth transition rather than a strong border that exists between the two sensations.

Figure 10.1 shows the dependence of fluctuation strength on modulation frequency. The different panels represent the data for amplitude-modulated broad-band noise (AM BBN), amplitude-modulated pure tone (AM SIN) and frequency-modulated pure tone (FM SIN). In each panel, the fluctuation strength was normalized to the maximum value for that sound (left-hand ordinate). Because fluctuation strength is a sensation which one considers separately from other sensations, both absolute and relative values are useful. A fixed point is therefore defined for a 60-dB, 1-kHz tone 100% amplitude-modulated at 4 Hz, as producing 1 vacil (from *vacilare* in Latin, or *vacillate* in English). Using the data of fluctuation strength shown in Fig. 10.7, it is possible to give the absolute values as indicated in the right-hand ordinate scales.

All three panels of Fig. 10.1 clearly show that fluctuation strength shows a band-pass characteristic as a function of modulation frequency, with a maximum around 4 Hz. This means that sounds with a 4-Hz modulation frequency

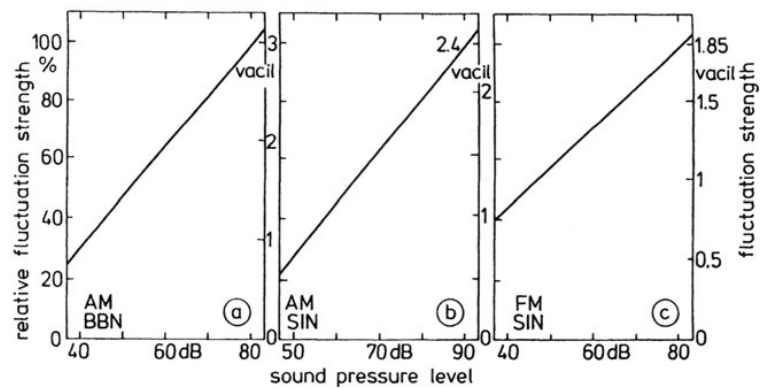


**Fig. 10.1a–c.** Fluctuation strength of three modulated sounds as a function of modulation frequency. (a) Amplitude-modulated broad-band noise of 60-dB SPL and 40-dB modulation depth; (b) amplitude-modulated 1-kHz tone of 70-dB SPL and 40-dB modulation depth; (c) frequency-modulated pure tone of 70-dB SPL, 1500-Hz centre frequency and  $\pm 700$ -Hz frequency deviation

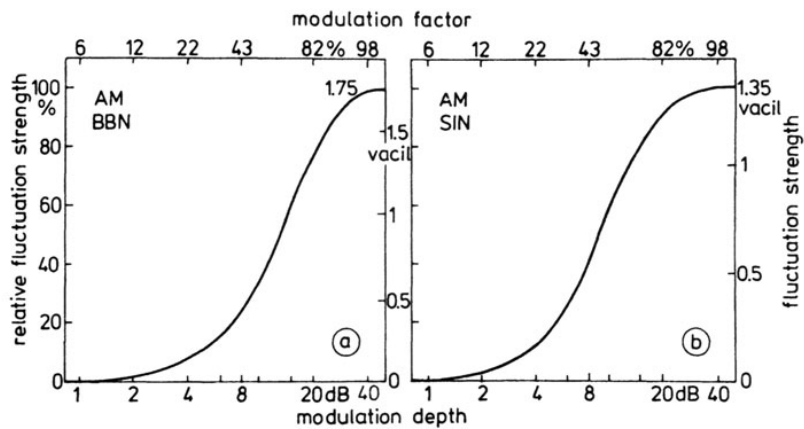
elicit large fluctuation strength, whether amplitude modulation or frequency modulation is used or whether broad-band or narrow-band sounds are modulated. The maximum fluctuation strength for a modulation frequency of about 4 Hz finds its counterpart in the variation of the temporal envelope of fluent speech: at normal speaking rate, 4 syllables/second are usually produced, leading to a variation of the temporal envelope at a frequency of 4 Hz. This may be seen as an indication of the excellent correlation between speech and hearing system.

The dependence of fluctuation strength on sound pressure level is displayed in Fig. 10.2. Again, the three panels show the results for amplitude-modulated broad-band noise, amplitude-modulated pure tone and frequency-modulated pure tone. In each panel, the fluctuation strength is normalized with respect to the corresponding maximum value on the left ordinate scales, and given in absolute values on the right. With increasing sound pressure level and for all sounds considered, the fluctuation strength increases. For amplitude-modulated sounds (Fig. 10.2a and b), the increase is somewhat more prominent than for the frequency-modulated pure tone (Fig. 10.2c). With an increase of 40 dB in sound pressure level, fluctuation strength of modulated sounds increases on average by a factor of about 2.5 (1.7 to 3).

Figure 10.3 shows the dependence of the fluctuation strength of amplitude-modulated broad-band noise and amplitude-modulated pure tones on both the modulation depth and the modulation factor. In each panel, the fluctuation strength is normalized with respect to the corresponding maximum value on the left ordinate scales and given in absolute values on the right ordinate



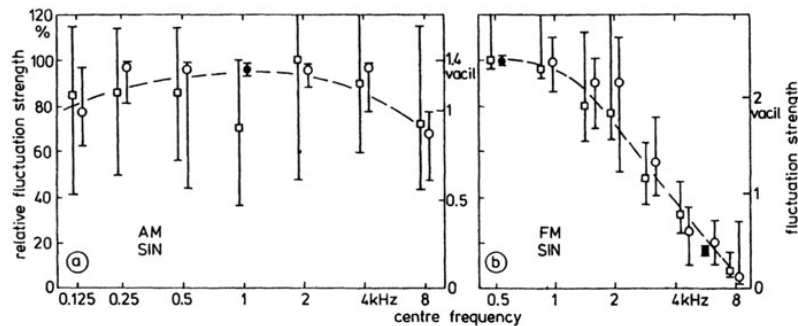
**Fig. 10.2a-c.** Fluctuation strength of modulated sounds as a function of sound pressure level. Stimulus parameters are the same as in Fig. 10.1, but the modulation frequency is 4 Hz



**Fig. 10.3a,b.** Fluctuation strength of two amplitude-modulated sounds as a function of modulation depth (or modulation factor). (a) Amplitude-modulated broadband noise of 60-dB SPL and 4-Hz modulation frequency; (b) amplitude-modulated 1-kHz tone of 70-dB SPL and 4-Hz modulation frequency

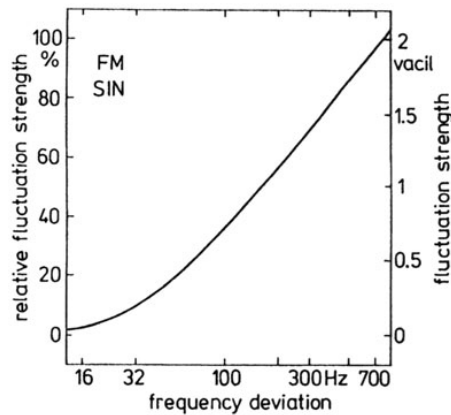
scales. According to the results displayed in Fig. 10.3, fluctuation strength is zero until a modulation depth of about 3 dB, after which it increases approximately linearly with the logarithm of modulation depth. To produce the maximum fluctuation strength of either sound, a modulation depth of at least 30 dB (modulation factor 94%) is necessary. Above that modulation depth, fluctuation strength remains constant at its maximal value.

Figure 10.4 shows the dependence of the fluctuation strength produced by modulated pure tones on centre frequency. In the left panel, results for amplitude-modulated pure tones are shown; the right panel indicates data for frequency-modulated pure tones. In each panel, the data are normalized relative to the respective maximal median fluctuation strength, but are also given in absolute values. The data displayed in Fig. 10.4a suggest that the fluctuation strength of amplitude-modulated pure tones depends very little on their centre frequency; despite the large interquartile ranges, the medians indicate the tendency for amplitude-modulated tones at very low (125 Hz) and very high (8 kHz) frequencies to produce less fluctuation strength than AM tones at medium frequencies. However, the results shown in Fig. 10.4b for FM tones indicate a clear dependence of fluctuation strength on centre frequency so that, although the fluctuation strength of FM tones is almost constant up to about 1 kHz, it decreases approximately linearly with the logarithm of the centre frequency towards higher frequencies.



**Fig. 10.4a,b.** Fluctuation strength of modulated tones as a function of frequency. (a) Amplitude-modulated pure tone of 70-dB SPL, 4-Hz modulation frequency and 40-dB modulation depth; (b) frequency-modulated pure tone of 70-dB SPL, 4-Hz modulation frequency, and  $\pm 200$ -Hz frequency deviation

This decrease can be understood in terms of the number of critical bands encompassed at different centre frequencies by FM tones with a constant frequency deviation of 200 Hz. As an example, the FM tone at 0.5 kHz sweeps between 300 and 700 Hz, i.e. between critical-band rates of 3 and 6.5 Bark, respectively. At the 8-kHz centre frequency, the modulation occurs between frequencies of 7.8 and 8.2 kHz, corresponding to 21.1 and 21.3 Bark, respec-



**Fig. 10.5.** Fluctuation strength of a frequency-modulated tone as a function of frequency deviation. The sound pressure level is 70 dB, the centre frequency 1500 Hz and the modulation frequency 4 Hz

tively. This means that at a centre frequency of 0.5 kHz, the FM tone varies over a critical-band interval of 3.5 Bark, whereas at 8 kHz it varies only over 0.2 Bark. Hence, the critical-band interval at 8 kHz is a factor of 17.5 smaller than the critical-band interval at 0.5 kHz. Regarding Fig. 10.4b, it can be seen that this factor of 17.5 is also found for the difference in the relative fluctuation strength at 0.5 and 8 kHz. This result can be taken as an indication that fluctuation strength of modulated sounds can be described on the basis of the corresponding excitation patterns.

Figure 10.5 shows the dependence of fluctuation strength on frequency deviation of an FM tone at a centre frequency of 1.5 kHz. Fluctuation strength is initially perceived at a frequency deviation of about 20 Hz and increases approximately linearly with the logarithm of frequency deviation. This result applies for an FM tone at 1500 Hz with 70-dB SPL and 4-Hz modulation frequency. For such a tone, the JND for frequency modulation corresponds to about  $2\Delta f = 8$  Hz (see Fig. 7.8). Significant values of fluctuation strength (say 10% relative fluctuation strength) are achieved for frequency deviations larger than about 10 times the magnitude of the JNDFM at 4 Hz. This rule seems to apply also for AM sounds: the modulation depth at which about 10% relative fluctuation strength is reached (see Fig. 10.3), is about 10 times larger than the JNDAM at 4 Hz of about 0.4 dB for a 70-dB AM tone, and about 0.7 dB for the AM broad-band noise as displayed in Fig. 7.1.

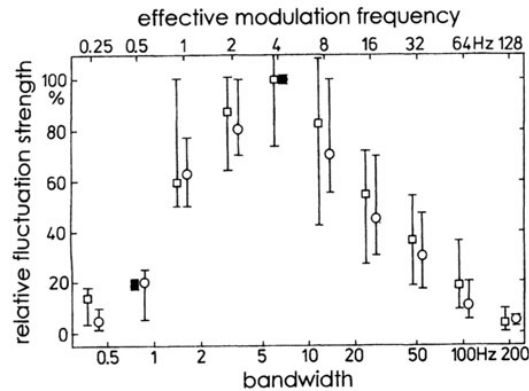
Not only modulated sounds can elicit the hearing sensation fluctuation strength but also unmodulated narrow noise bands.

Figure 10.6 shows the dependence of relative fluctuation strength of narrow-band noise as a function of its bandwidth as well as effective modulation frequency. According to (1.6) this frequency can be calculated as follows:

$$f_{\text{mod}}^* = 0.64 \cdot \Delta f.$$

The comparison of the data displayed in Figs. 10.1 and 10.6 reveals that – irrespective of periodic or stochastic sound fluctuations – fluctuation strength

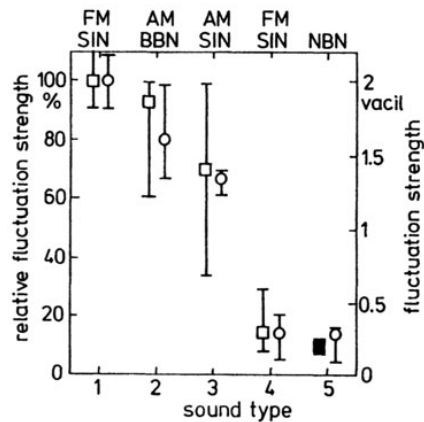




**Fig. 10.6.** Fluctuation strength of narrow-band noise as a function of its bandwidth. Center frequency 1 kHz, level 70 dB

shows a bandpass characteristic with a maximum around 4 Hz (effective) modulation frequency.

For unmodulated narrow-band noise, fluctuation strength increases with level and shows large values for center frequencies around 1 kHz similar to the data displayed for modulated sounds in Figs. 10.2 and 10.4a.



**Fig. 10.7.** Fluctuation strength of the sounds 1–5 as described in Table 10.1

Figure 10.7 enables a comparison of the fluctuation strength of five different sounds whose characteristics are listed in Table 10.1. The largest fluctuation strength is produced by the 70-dB tone with large frequency deviation. Some 10% less fluctuation strength is elicited by a 60-dB, amplitude-modulated broad-band noise. A 70-dB, amplitude-modulated 2-kHz tone pro-

**Table 10.1.** Physical data of sounds 1–5

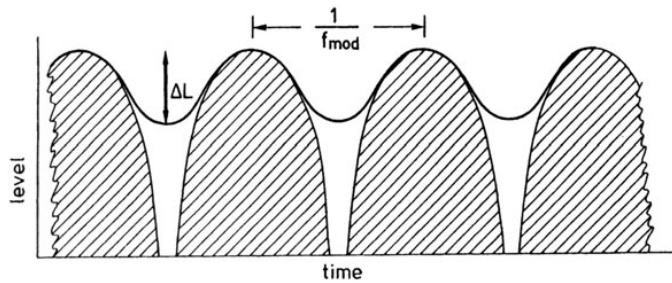
Sound	1	2	3	4	5
Abbreviation	FM SIN	AM BBN	AM SIN	FM SIN	NBN
Frequency [Hz]	1500	-	2000	1500	1000
Level [dB]	70	60	70	70	70
Modulation frequency [Hz]	4	4	4	4	-
Modulation depth [dB]	-	40	40	-	-
Frequency deviation [Hz]	700	-	-	32	-
Bandwidth [Hz]	-	16000	-	-	10

duces a fluctuation strength about 30% down from that of the FM tone. Sound 4, a 70-dB FM tone with small frequency deviation, produces only about 1/10 of the fluctuation strength of sound 1. This result is expected on the basis of the data displayed in Fig. 10.5. Sound 5 represents a narrow-band noise with a bandwidth of 10 Hz. The fluctuation strength elicited by this narrow-band noise can be estimated as follows: as a first approximation, the narrow-band noise can be regarded as an AM tone at 1 kHz with 6.4 Hz modulation frequency (see Sect. 1.1). If an effective modulation factor of 40% for narrow-band noise is assumed, then according to the results displayed in Fig. 10.3, the fluctuation strength of narrow-band noise should be a factor of about 2.5 smaller than the fluctuation strength of AM tones with a 98% modulation factor. A comparison of the relative fluctuation strength of sound 3 and sound 5 in Fig. 10.7, however, reveals that the fluctuation strength of narrow-band noise is smaller by a factor of about 5 than the fluctuation strength of an AM tone. It is apparently the periodic fluctuation of AM tones, in contrast to the random amplitude fluctuations of the noise, that enhances the perceived fluctuation strength of the AM tone.

The large fluctuation strength of amplitude-modulated broad-band noise and frequency-modulated pure tones with large frequency deviation (sounds 2 and 1) can be related to the fact that excitation varies to a large extent along the critical-band rate scale. Therefore, it can be postulated that fluctuation strength is summed up across critical bands. This concept will be explained in more detail in the following section.

## 10.2 Model of Fluctuation Strength

A model of fluctuation strength based on the temporal variation of the masking pattern can be illustrated by Fig. 10.8, where the temporal masking



**Fig. 10.8.** Model of fluctuation strength: temporal masking pattern of sinusoidally amplitude-modulated masker leading to the temporal masking depth  $\Delta L$

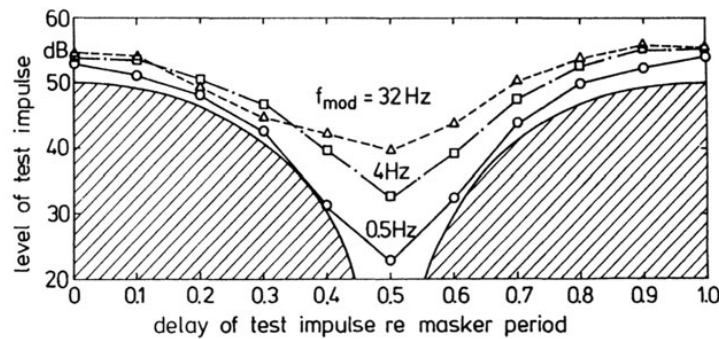
pattern of a sinusoidally amplitude-modulated masker is schematically indicated by the thick solid line. The hatched areas indicate the envelope of a sinusoidally amplitude-modulated masker plotted in terms of sound pressure level. The interval between two successive maxima of the masker envelope corresponds to the reciprocal of the modulation frequency. The temporal variation of the temporal masking pattern can be described by the magnitude  $\Delta L$ , which represents the level difference between the maxima and the minima in the temporal masking pattern. This so-called temporal masking depth,  $\Delta L$ , should not be confused with the modulation depth,  $d$ , of the masker's envelope; the masking depth  $\Delta L$  of the temporal masking pattern is smaller than the modulation depth  $d$  of the masker's envelope due to postmasking.

The equation

$$F \sim \frac{\Delta L}{(f_{\text{mod}}/4\text{Hz}) + (4\text{Hz}/f_{\text{mod}})}, \quad (10.1)$$

shows the relationship between fluctuation strength,  $F$ , and the masking depth of the temporal masking pattern,  $\Delta L$ , as well as the relationship between  $F$  and modulation frequency  $f_{\text{mod}}$ . The denominator clearly shows that a modulation frequency of 4 Hz plays an important part in the description of fluctuation strength: for faster modulation frequencies, the ear exhibits the integrative features evidenced in postmasking; for modulation frequencies lower than 4 Hz, effects of short-term memory become important.

For an amplitude-modulated broad-band noise, the magnitude of the masking depth of the temporal masking pattern,  $\Delta L$ , is largely independent of frequency. For amplitude-modulated pure tones, some frequency dependence occurs because of the nonlinearity of the upper slope in the masking pattern. In addition to those factors, the magnitude of the masking depth shows a strong frequency dependence with frequency-modulated tones. This means that, for describing the fluctuation strength of AM tones and FM tones, the model can be modified as follows: instead of *one* masking depth of the temporal masking pattern  $\Delta L$ , all of the magnitudes of  $\Delta L$  occurring



**Fig. 10.9.** Temporal masking pattern of 100% sinusoidally amplitude-modulated broad-band noise. *Hatched:* temporal envelope of masker; *parameter:* modulation frequency. All data plotted as a function of the temporal location within the period of the modulation of the masker

are integrated along the critical-band rate scale. A more detailed description of this procedure is given in Chap. 11, where the model for roughness is discussed.

A basic feature of the model of fluctuation strength, namely the masking depth of the temporal masking pattern, can be illustrated in Fig. 10.9. The temporal envelope of a sinusoidally amplitude-modulated broad-band noise is indicated by the hatched areas. The different curves represent the temporal masking patterns for the different modulation frequencies indicated. The maximum of the masking pattern shows up at a delay relative to the masker period of 0, the minimum at a delay of 0.5. The difference between maximum and minimum, called the temporal masking depth, clearly decreases with increasing modulation frequency. This means that as a function of modulation frequency, the temporal masking pattern shows a low-pass characteristic, whereas fluctuation strength shows a band-pass characteristic. Equation (10.1) explains how the low-pass characteristic of the temporal envelope is transformed into the band-pass characteristic of fluctuation strength. This bandpass characteristic describes the influence of modulation frequency on fluctuation strength. However, the value  $\Delta L$  in the formula decreases approximately linearly with increasing frequency of modulation. Taking this into account, a relatively simple formula can be given for the fluctuation strength of sinusoidally amplitude-modulated broad-band noise:

$$F_{\text{BBN}} = \frac{5.8(1.25m - 0.25)[0.05(L_{\text{BBN}}/\text{dB}) - 1]}{(f_{\text{mod}}/5\text{Hz})^2 + (4\text{Hz}/f_{\text{mod}}) + 1.5} \text{ vacil} , \quad (10.2)$$

where  $m$  is the modulation factor,  $L_{\text{BBN}}$  the level of the broad-band noise and  $f_{\text{mod}}$  the frequency of modulation. For amplitude- or frequency-modulated tones, fluctuation strength may be approximated by integrating the temporal

masking depth,  $\Delta L$ , along the critical-band rate. This leads to the following approximation:

$$F = \frac{0.008 \int_0^{24\text{Bark}} (\Delta L / \text{dB Bark}) dz}{(f_{\text{mod}} / 4\text{Hz}) + (4\text{Hz} / f_{\text{mod}})} \text{ vacil} , \quad (10.3)$$

where the masking depth,  $\Delta L$ , may be picked up from the masking patterns described in Chap. 4 for the different critical-band rates of 1 Bark distance. The integral is then transformed into a sum of, at most, 24 terms along the whole range of the critical-band rate.

While for most sounds described in this chapter values of  $\Delta L$  are available this is usually not the case for sounds typical for practical applications. Therefore, a computer program was developed which uses instead of the  $\Delta L$  values the corresponding differences in specific loudness. Since the computer models of fluctuation strength and roughness are very similar some more detail is given in Chap. 11 and the related literature.

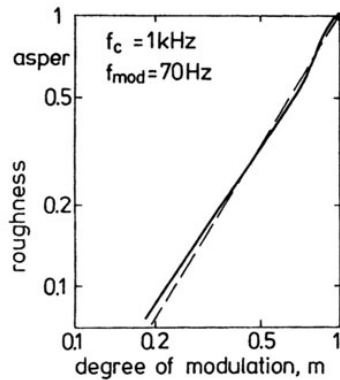
## 11. Roughness

Using a 100% amplitude-modulated 1-kHz tone and increasing the modulation frequency from low to high values, three different areas of sensation are traversed. At very low modulation frequencies the loudness changes slowly up and down. The sensation produced is that of fluctuation. This sensation reaches a maximum at modulation frequencies near 4 Hz and decreases for higher modulation frequencies. At about 15 Hz, another type of sensation, roughness, starts to increase. It reaches its maximum near modulation frequencies of 70 Hz and decreases at higher modulation frequencies. As roughness decreases, the sensation of hearing three separately audible tones increases. This sensation is small for modulation frequencies near 150 Hz; it increases strongly, however, for larger modulation frequencies. This behaviour indicates that roughness is created by the relatively quick changes produced by modulation frequencies in the region between about 15 to 300 Hz. There is no need for exact periodical modulation, but the spectrum of the modulating function has to be between 15 and 300 Hz in order to produce roughness. For this reason, most narrow-band noises sound rough even though there is no periodical change in envelope or frequency. Roughness is again a sensation which we can consider while ignoring other sensations.

### 11.1 Dependencies of Roughness

In order to describe roughness quantitatively, a reference value must be defined. In Latin, the word “asper” characterizes what we call “rough”. To define the roughness of 1 asper, we have chosen the 60-dB, 1-kHz tone that is 100% modulated in amplitude at a modulation frequency of 70 Hz. Three parameters are important in determining roughness. For amplitude modulation, the important parameters are the degree of modulation and modulation frequency. For frequency modulation, it is the frequency modulation index and modulation frequency.

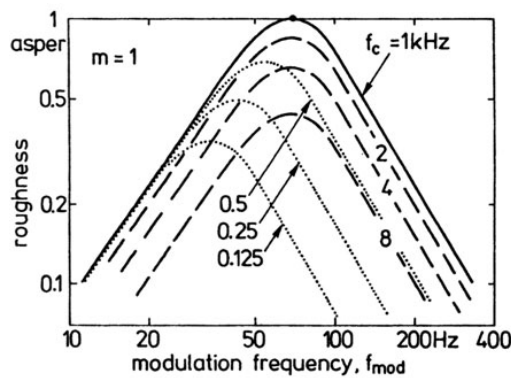
Figure 11.1 shows the roughness of a 1-kHz tone at a modulation frequency of 70 Hz, as a function of the degree of modulation. Values of the degree of modulation larger than 1 are not meaningful here. The data, indicated by the solid line, can be approximated by the dashed line. Because the ordinate and abscissa are given in logarithmic scales, the straight dashed line



**Fig. 11.1.** Roughness as a function of the degree of modulation for a 1-kHz tone, amplitude-modulated at a frequency of 70 Hz. The dot in the right upper corner indicates the standard sound, which produces the roughness of 1 asper. The broken line indicates a useful linear approximation

represents a power law. The exponent is near 1.6 so that a roughness of only 0.1 asper is produced for a degree of modulation of 25%. This roughness is quite small and some subjects classify this as “no longer rough”.

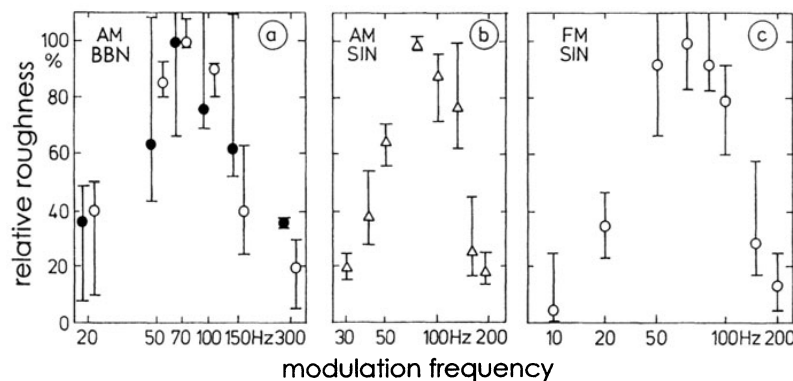
This dependence of roughness on the degree of modulation holds for tones of other centre frequencies also, although the modulation frequency at which the maximum roughness is reached depends on centre frequency. Figure 11.2 shows the dependence of roughness on modulation frequency at different centre frequencies for 100% modulation. This dependence has a band-pass characteristic. Roughness increases almost linearly from low modulation frequencies, in the double-logarithmic coordinates of Fig. 11.2, before it reaches a maximum. The maximum only depends on carrier frequency below 1 kHz where the maximum is shifted towards lower frequency of modulation with decreasing carrier frequency. The lower slope of this band-pass characteristic remains the same for frequencies of modulation below 1 kHz, even though the maximum decreases with decreasing centre frequency. For centre frequencies



**Fig. 11.2.** Roughness of 100% amplitude-modulated tones of the given centre frequency as a function of the frequency of modulation

above 1 kHz, the height of the maximum is reduced although the frequency of modulation at which this maximum is reached remains unchanged. This means that above 1-kHz centre frequency there is a parallel shift downwards of the characteristic with increasing centre frequency.

The upper part of the band-pass characteristic can again be approximated by a straight line, with a relatively quick decay of roughness with increasing modulation frequency. It seems that the width of the critical band at lower centre frequencies plays an important role. At 250 Hz, the critical bandwidth is only 100 Hz. For a modulation frequency of 50 Hz, the two sidebands already have a separation of 100 Hz. For even higher modulation frequencies, the two sidebands fall into different critical bands. For centre frequencies above about 1 kHz, all the dependencies on frequency of modulation have the same shape. Here, the maximal roughness seems to be limited by the temporal resolution of our hearing system. Thus, two characteristics of the ear seem to influence the sensation of roughness: at low centre frequencies, it is frequency selectivity; at high centre frequencies, it is the limited temporal resolution.



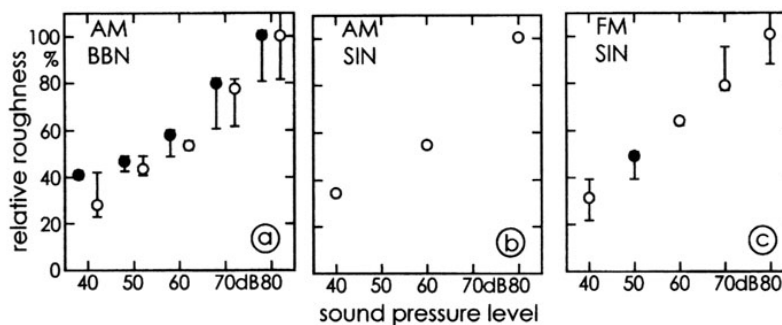
**Fig. 11.3a–c.** Roughness of three modulated sounds as a function of modulation frequency. (a) Amplitude modulated broadband noise of 60 dB SPL and 40 dB modulation depth; (b) amplitude modulated 1 kHz tone of 70 dB SPL and 40 dB modulation depth; (c) frequency modulated pure tone of 70 dB SPL, 1500 Hz center frequency, and  $\pm 700$  Hz frequency deviation

Figure 11.3 shows the dependence of relative roughness on modulation frequency for amplitude modulated broadband noise, amplitude modulated pure tones, and frequency modulated pure tones. In line with the data presented in Fig. 11.2 the maximum of roughness occurs near a modulation frequency of 70 Hz irrespective of bandwidth or type of modulation. As with amplitude modulated pure tones also for amplitude modulated broadband noise or frequency modulated pure tones roughness vanishes for modulation frequencies above about 300 Hz.



Bands of noise often sound rough, although there is no additional amplitude modulation. This is because the envelope of the noise changes randomly. These changes become audible especially for bandwidths in the neighbourhood of 100 Hz, where the average rate of envelope change is 64 Hz (see Sect. 1.1). Therefore, roughness is particularly large at such bandwidths. For increasing bandwidth, the creation of roughness is limited by frequency selectivity. Nonetheless, at very high centre frequencies noises can be produced which are still within the critical band but have a bandwidth of 1 kHz. Such a noise, although it is randomly amplitude modulated, sounds relatively steady and produces only a very small sensation of roughness.

Figure 11.4 shows the dependence of roughness on sound pressure level. Data are given for amplitude-modulated broad-band noise, amplitude-modulated pure tone, and frequency modulated pure tone.



**Fig. 11.4a–c.** Roughness of modulated sounds as a function of sound pressure level. Modulation frequency is 70 Hz. (a) Amplitude-modulated broad-band noise with 40 dB modulation depth, (b) amplitude-modulated 1 kHz-tone with 40 dB modulation depth, (c) frequency-modulated pure tone at 1500 Hz with  $\pm 700$  Hz frequency deviation

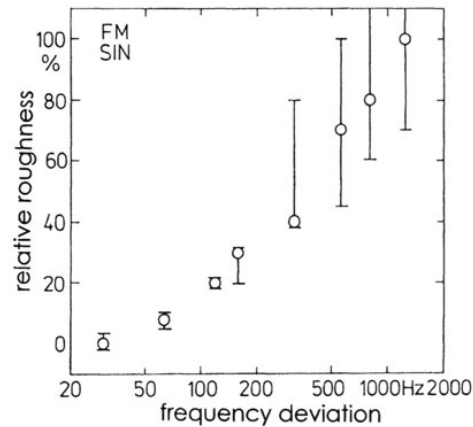
For an increase in sound pressure level by 40 dB roughness increases by a factor of about 3. This dependence of roughness on level is similar to the increase of fluctuation strength with level as displayed in Fig. 10.2.

An increment of roughness becomes audible for an increment in the degree of modulation of about 10%, which corresponds to an increment of about 17% in roughness. For amplitude-modulated 1-kHz tones and a modulation frequency of 70 Hz, a threshold of roughness is reached for values close to 0.07 asper. One asper is close to the maximum roughness for amplitude-modulated tones; there are thus only about 20 audible roughness steps throughout the total range of roughnesses.

Frequency modulation can produce much larger roughness than amplitude modulation. A strong frequency modulation over almost the whole frequency

range of hearing produces a roughness close to 6 asper. Only amplitude modulation of broad-band noises is able to produce such a large roughness.

Figure 11.5 shows the dependence of roughness of an FM-tone on frequency deviation. An FM-tone centered at 1500 Hz with a level of 70 dB was modulated by a modulation frequency of 70 Hz.



**Fig. 11.5.** Roughness of a sinusoidally frequency modulated pure tone as a function of frequency deviation. Center frequency 1500 Hz, sound pressure level 70 dB, modulation frequency 70 Hz

The results displayed in Fig. 11.5 indicate that for frequency deviations up to 50 Hz only negligible values of roughness show up. For larger values of the frequency deviation  $\Delta f$  roughness increases almost linearly with the logarithm of  $\Delta f$ .

## 11.2 Model of Roughness

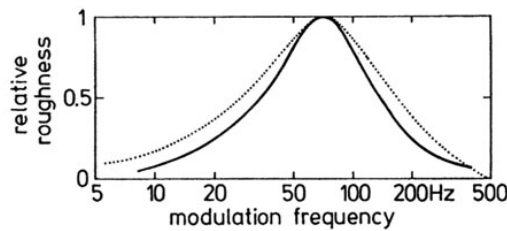
As mentioned above, there are two main factors that influence roughness. These are frequency resolution and temporal resolution of our hearing system. Frequency resolution is modelled by the excitation pattern or by specific-loudness versus critical-band rate pattern.

It is assumed that our hearing system is not able to detect frequency as such, and is only able to process changes in excitation level or in specific loudness at all places along the critical-band rate scale; thus the model for roughness should be based on the differences in excitation level that are produced by the modulation. Starting with amplitude modulation, we can refer to data that describe the masking effect produced by strongly temporally varying maskers. Because masking level is an effective measure for determining excitation, it can be used to estimate the excitation-level differences produced by amplitude modulation. This procedure incorporates the two main effects already discussed, i.e. frequency and temporal resolution.

The temporal masking patterns outlined in Figs. 4.24, 4.25, and 4.27 show the temporal effects and indicate values of  $\Delta L$  that can be used as a measure to estimate differences between the maximum and the minimum of the temporal masking pattern. This temporal masking depth,  $\Delta L$ , becomes larger for lower modulation frequency. If roughnesses were determined only by this masking depth, then one would expect the largest roughness at the lowest modulation frequencies. This is not the case, indicating that roughness is a sensation produced by temporal changes. A very slow change does not produce roughness; a quick periodic change does, however. This means that roughness is proportional to the speed of change, i.e. it is proportional to the frequency of modulation. Together with the value of  $\Delta L$ , this leads to the following approximation:

$$R \sim f_{\text{mod}} \Delta L. \quad (11.1)$$

For very small frequencies of modulation, roughness remains small although  $\Delta L$  is large. In this case  $f_{\text{mod}}$  is small, so that the size of the product remains small. For medium frequencies of modulation around 70 Hz, the value of  $\Delta L$  is smaller than at low modulation frequencies. However,  $f_{\text{mod}}$  is much larger in this case, so that the product of the two values reaches a maximum. At high frequencies of modulation,  $f_{\text{mod}}$  is a large value but  $\Delta L$  becomes small because of the restricted temporal resolution of our hearing system. Thus the product diminishes again. In this context, it should be realized that a modulation frequency of 250 Hz corresponds to a period of 4 ms, and the effective duration of the valley is only about 2 ms. In this case, the temporal masking depth,  $\Delta L$ , becomes almost zero. Consequently, the product of  $\Delta L$  and  $f_{\text{mod}}$  becomes very small and the roughness disappears.



**Fig. 11.6.** Relative roughness as a function of the frequency of modulation as subjectively measured (solid) and calculated (dotted)

This way, roughness can be approximated and compared with the measured data. This is done in Fig. 11.6 by using the maximum roughness at 70 Hz as a reference. Roughness relative to the maximal value reached is plotted as a function of modulation frequency. The solid line corresponds to the data shown in Fig. 11.2 for centre frequencies above 1 kHz. The dotted line corresponds to the calculated values based on the assumption that roughness is proportional to the product of modulation frequency and masking depth. The calculated dependence agrees well with the subjectively measured one,

although there are some differences especially at lower frequencies of modulation. There, subjectively measured roughness disappears more quickly than calculated roughness. In this region, subjects have difficulties differentiating between sensations of roughness and fluctuation strength, and concentrate mostly on one or the other.

For more precise calculations, it has to be realized that the value  $\Delta L$  depends on the critical-band rate. The nonlinear rise of the upper masking slope outlined in Fig. 4.9 produces  $\Delta L$ 's in the region of the upper slope that are much larger than those corresponding to the main excitation. These effects can also be seen in Fig. 4.24. Comparing  $\Delta L$  produced at a test-tone frequency identical to the frequency of the masker (1 kHz), with that produced on the upper slope near 1.6 kHz, it is evident that  $\Delta L$  on the slope is much larger. To account for this effect, the given approximation is changed to:

$$R \sim f_{\text{mod}} \int_0^{24\text{Bark}} \Delta L_E(z) dz . \quad (11.2)$$

Using the boundary condition that a 1-kHz tone at 60 dB and 100%, 70 Hz amplitude-modulated, produces the roughness of 1 asper, the roughness  $R$  of any sound can be calculated using the equation

$$R = 0.3 \frac{f_{\text{mod}}}{\text{kHz}} \int_0^{24\text{Bark}} \frac{\Delta L_E(z) dz}{\text{dB/Bark}} \text{ asper} . \quad (11.3)$$

Unfortunately, we do not have data for  $\Delta L$  as a function of critical-band rate that are as numerous as the data for excitation level or specific loudness. Therefore, the calculations are somewhat limited. Using the data available, however, we have been able to demonstrate that roughness can be calculated precisely as a function of the degree of modulation. In this case, the calculated value is influenced mainly by the dependence of  $\Delta L$  on the degree of modulation, but not by the frequency of modulation. For modulated tones, the nonlinear rise of the upper slope of the masking versus critical-band rate pattern, creates larger contributions to roughness than those produced at the main excitation. This leads to the prediction – in agreement with psychoacoustical data – that the slope of the relationship between roughness and degree of modulation (both on logarithmic scales) is larger for sinusoidal tones (1.6) than for broad-band noises (1.3).

Some data concerning the value  $\Delta L$  with frequency-modulated sounds are available. Approximations based on the equation given follow qualitatively and in many cases even quantitatively the psychoacoustically measured dependencies.

It is of advantage to transfer the  $\Delta L$  values necessary for the calculation of roughness into the corresponding variations of specific loudness. As input to the model, the specific loudness-time function in each channel of a loudness-meter as illustrated in Fig. 8.26 is necessary. Moreover, the correlation between signals in neighboring channels has to be taken into account. On this basis, a computer program was developed which nicely accounts for

the measured psychoacoustic data and can also describe quantitatively the roughness of noise emissions.

A variant of this program which essentially is based on the same features can also quantitatively assess the dependencies of fluctuation strength on relevant stimulus parameters (cf. Chap. 10).