

## 1. Uni and multiprogramming

### **(a) Uniprogrammed**

$$20s + 30s + 40s + 60s * 3 = 270 \text{ seconds} = 4 \text{ min } 30 \text{ seconds}$$

### **(b) Multiprogrammed:**

Assuming that there is enough memory for the 3 jobs to be run at the same time, and that there is no resource conflict (i.e. the 3 jobs can do I/O at the same time):

1 minute 40 seconds (1 minute for I/O, 40 seconds for the job with the longest execution time)

## 2. Paging and TLB

TLB look up 100 *ns*, update 200 *ns*

PT lookup 1  $\mu$ s, update 2  $\mu$ s

Load word from Main Memory to the CPU 10  $\mu$ s

Load page from Disk into Main Memory 10 *ms*

### (a) Time it takes to find out the physical address

Assume 100 operations in total. This calculation doesn't include the time it takes to update the page tables & TLB, which is shown in (c) below:

TLB hit

$$0.4 * 100 * 100 \text{ ns} = 4000 \text{ ns}$$

TLB miss (100 *ns*), main memory hit (1  $\mu$ s)

$$(1-0.4) * 0.3 * 100 * (100 \text{ ns} + 1 \mu\text{s}) = 19800 \text{ ns}$$

TLB miss (100 *ns*), main memory miss (1  $\mu$ s), load page from disk (10 *ms*)

$$(1-0.4) * (1-0.3) * 100 * (100 \text{ ns} + 1 \mu\text{s} + 10 \text{ ms}) = 420046200 \text{ ns}$$

Average access time to **find out the physical address**:

$$(4000 \text{ ns} + 19800 \text{ ns} + 420046200 \text{ ns}) / 100 = \mathbf{4200700 \text{ ns} = 4.2007 \text{ ms}}$$

### (b) Time it takes to load the reference word onto the CPU

Assuming 100 operations in total.

TLB hit (100 *ns*), reference word is found in physical memory via TLB (10  $\mu$ s)

$$0.4 * 100 * (100 \text{ ns} + 10 \mu\text{s}) = 404000 \text{ ns}$$

TLB miss (100 *ns*), main memory hit, reference word is found in main memory via PT (1  $\mu$ s + 10  $\mu$ s)

$$(1-0.4) * 0.3 * 100 * (100 \text{ ns} + 1 \mu\text{s} + 10 \mu\text{s}) = 199800 \text{ ns}$$

TLB miss (100 *ns*), main memory miss, reference word is loaded from disk into main memory (10 *ms*), then to CPU via PT (1  $\mu$ s + 10  $\mu$ s)

$$(1-0.4) * (1-0.3) * 100 * (100 \text{ ns} + 1 \mu\text{s} + 10 \mu\text{s} + 10 \text{ ms}) = 420466200 \text{ ns}$$

Average access time to **load the reference word onto the CPU**:

$$(404000 \text{ ns} + 199800 \text{ ns} + 420466200 \text{ ns}) / 100 = \mathbf{4210700 \text{ ns} = 4.2107 \text{ ms}}$$

### (c) Time it takes to perform the necessary updates to the page tables

Assuming 100 operations in total:

TLB hit: no update to TLB/page table

$$0 \text{ ns}$$

TLB miss, main memory hit: update to TLB (200 *ns*) via PT lookup (1  $\mu$ s), no update to page table

$$(1-0.4) * 0.3 * 100 * (200 \text{ ns} + 1 \mu\text{s}) = 21600 \text{ ns}$$

TLB miss, main memory miss (page fault): update to TLB (200 *ns*) via PT look up, update to PT through loading page from disk (10 *ms*)

$$(1-0.4) * (1-0.3) * 100 * (200 \text{ ns} + 1 \mu\text{s} + 2 \mu\text{s} + 10 \text{ ms}) = 420134400 \text{ ns}$$

Average access time to **perform the necessary updates to the page tables**:

$$(0 + 21600 \text{ ns} + 420134400 \text{ ns}) / 100 = \mathbf{4201560 \text{ ns} = 4.20156 \text{ ms}}$$

3. Compute the average turnaround time using the multilevel queues (round robin) scheduling algorithm.

	Arrival Time	Run Time	Run Time (Total)	Priority
A	40	1	20	1
B	50	2	60	1
C	40	1	20	0
D	0	2	160	0

I'm using quantum of 1 here:

0 - 40 : D (120)

40 - 50 : A (10), C(20), D(120)

50 - 70: A(0), B (50), C(20), D(120) ← Runtime for A:  $70 - 40 = 30$

70 - 120: B(0), C(20), D(120) ← Runtime for B:  $120 - 50 = 70$

120 - 160: C(0), D(100) ← Runtime for C:  $160 - 40 = 120$

160 - 260: D(0) ← Runtime for D:  $260 - 0 = 260$

Average runtime:

$$(30 + 70 + 120 + 260) / (20 + 30 + 20 + 80) = \mathbf{3.2 \text{ seconds}}$$