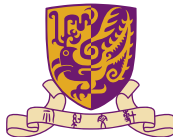


One-Shot Coding over General Noisy Networks

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Overview: Our Contributions

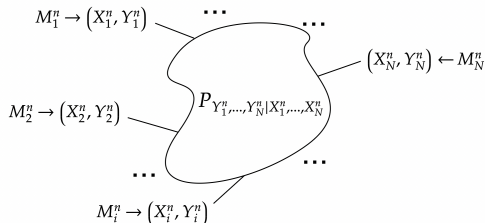


Our Contributions

- ① We consider the general **one-shot** coding problem.
- ② We consider communication and compression of messages among multiple nodes across **general acyclic noisy networks**.
- ③ We design proof techniques based on Poisson functional representations.
- ④ Our coding framework is applicable to **any** combination of source coding, channel coding and coding for computing problems (with special cases presented).



Background: Noisy Network Coding



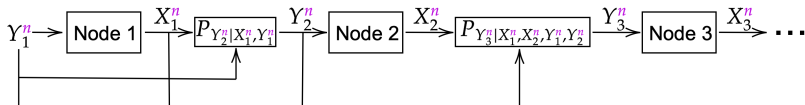
Noisy Network Coding

- **Noisy network coding**^a: communicating messages between **multiple** sources and destinations over a general **noisy** network.
- Generalizing:
 - 1 Noiseless network coding by Ahlswede, Cai, Li and Yeung.
 - 2 Compress-forward coding for relay channels by Cover and El Gamal.
 - 3 Coding for relay networks, coding for erasure networks, etc.

^aLim, Sung Hoon, Young-Han Kim, Abbas El Gamal, and Sae-Young Chung. "Noisy network coding." IEEE Transactions on Information Theory 57, no. 5 (2011): 3132-3152.



Background: A Unified Random Coding Bound



A Unified Asymptotic Random Coding Bound

- ① Unified random coding bound^a: work for **any** combination of channel coding and source coding problems.
- ② Unifying and generalizing known relaying strategies; can yield bounds without complicated error analysis.
- ③ Useful for designing automated theorem proving tools^b.

^aLee, Si-Hyeon, and Sae-Young Chung. "A unified random coding bound." IEEE Transactions on Information Theory 64, no. 10 (2018): 6779-6802.

^bLi, Cheuk Ting. "An automated theorem proving framework for information-theoretic results." IEEE Transactions on Information Theory (2023).

Background: One-Shot Information Theory

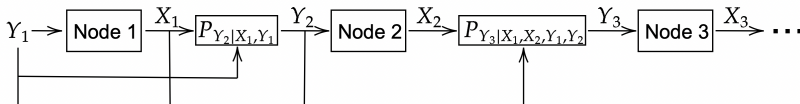


One-Shot Information Theory

What if each source and channel is only used once, i.e., $n = 1$ (Feinstein, [1954]; Shannon, [1957]; Verdú, [2012]; Yassaee et al. [2013]; Li and Anantharam [2021])?

- 1 Sources and channels can be **arbitrary**: no need to be memoryless or ergodic.
- 2 Goal: obtain one-shot results that can recover existing (first-order and second-order) **asymptotic** results when applied to memoryless sources and channels and also **finite blocklength** results (Polyanskiy et al. [2010]; Kostina and Verdú [2012]).

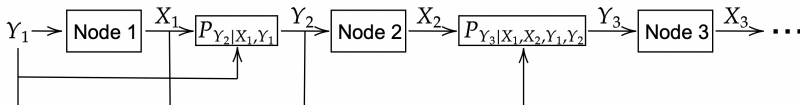
Overview



Our Contributions: One-Shot Coding Framework over Noisy Networks

- 1 A unified **one-shot** coding scheme
- 2 over general **noisy** acyclic discrete networks (ADN)
- 3 that is applicable to **any** combination of source coding, channel coding and coding for computing problems,
- 4 proved by our **exponential process refinement lemma**.

Overview



Our Contributions: Specific Network Information Theory Settings

- **Novel** one-shot achievability results for:
 - 1 One-shot relay channels
 - 2 One-shot primitive relay channels
 - Compress-and-forward bound
 - Partial-decode-and-forward bound
- **Recovered** one-shot & asymptotic results for:
 - 1 Source and channel coding
 - 2 Gelfand-Pinsker, Wyner-Ziv and coding for computing
 - 3 Multiple access channels
 - 4 Broadcast channels



Preliminaries: Poisson Functional Representation

Poisson Functional Representation

- For a finite set \mathcal{U} , let $\mathbf{U} := (Z_u)_{u \in \mathcal{U}}$ be i.i.d. $\text{Exp}(1)$ random variables^a.
- Given a distribution P over \mathcal{U} , **Poisson functional representation**^b:

$$\mathbf{U}_P := \operatorname{argmin}_u \frac{Z_u}{P(u)} \quad (1)$$

- $\mathbf{U}_P \sim P$
- Various applications: minimax learning, neural network compression, etc.

^aWhen the space \mathcal{U} is continuous, a Poisson process is used instead.

^bLi, Cheuk Ting, and Abbas El Gamal. "Strong functional representation lemma and applications to coding theorems." IEEE Transactions on Information Theory 64, no. 11 (2018): 6967-6978.



Preliminaries: Poisson Matching Lemma

Poisson Functional Representation

- Given a distribution P over \mathcal{U} , **Poisson functional representation**:

$$\mathbf{U}_P := \operatorname{argmin}_u \frac{Z_u}{P(u)}$$

Generalized Poisson Matching Lemma

- Let $\mathbf{U}_P(1), \dots, \mathbf{U}_P(|\mathcal{U}|) \in \mathcal{U}$ be the elements of \mathcal{U} sorted in ascending order of $Z_u/P(u)$, let $\mathbf{U}_P^{-1} : \mathcal{U} \rightarrow [|\mathcal{U}|]$ for the inverse function of $i \mapsto \mathbf{U}_P(i)$.
- Generalized Poisson matching lemma**^a: For distributions P, Q over \mathcal{U} , we have the following almost surely:

$$\mathbf{E} \left[\mathbf{U}_Q^{-1}(\mathbf{U}_P) \mid \mathbf{U}_P \right] \leq \frac{P(\mathbf{U}_P)}{Q(\mathbf{U}_P)} + 1.$$

^aLi, Cheuk Ting, and Venkat Anantharam. "A unified framework for one-shot achievability via the Poisson matching lemma." IEEE Transactions on Information Theory 67, no. 5 (2021): 2624-2651.

New Techniques



Refining a distribution by an exponential process

- For a joint distribution $Q_{V,U}$ over $\mathcal{V} \times \mathcal{U}$, the **refinement** of $Q_{V,U}$ by \mathbf{U} :

$$Q_{V,U}^{\mathbf{U}}(v, u) := \frac{Q_V(v)}{\mathbf{U}_{Q_U|V(\cdot|v)}^{-1}(u) \sum_{i=1}^{|\mathcal{U}|} i^{-1}} \quad (2)$$

for all (v, u) in the support of $Q_{V,U}$.

- The refinement is for the **soft decoding**.
- If the distribution $Q_{V,U}$ represents our “**prior distribution**” of (V, U) , then the refinement $Q_{V,U}^{\mathbf{U}}$ is our updated “**posterior distribution**” after taking the exponential process \mathbf{U} into account.



New Techniques

Exponential Process Refinement Lemma

- For a distribution P over \mathcal{U} and a joint distribution $Q_{V,U}$ over a finite $\mathcal{V} \times \mathcal{U}$, for every $v \in \mathcal{V}$, we have, almost surely,

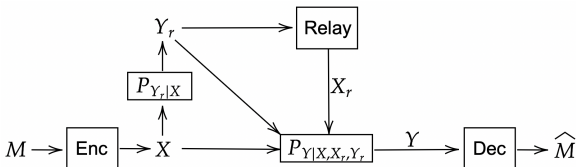
$$\mathbb{E} \left[\frac{1}{Q_{V,U}^U(v, \mathbf{U}_P)} \middle| \mathbf{U}_P \right] \leq \frac{\ln |\mathcal{U}| + 1}{Q_V(v)} \left(\frac{P(\mathbf{U}_P)}{Q_{U|V}(\mathbf{U}_P|v)} + 1 \right). \quad (3)$$

Purpose

It keeps track of the evolution of the “posterior probability” of the correct values of a large number of random variables through the refinement process.



One-Shot Relay Channel



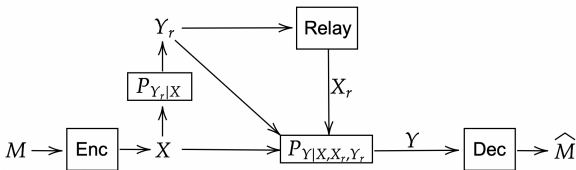
One-Shot Relay Channel

- One-shot version of **relay-with-unlimited-look-ahead**^a
- Limitation of one-shot settings: unable to model “networks with causality”, e.g., conventional relay channel (Van Der Meulen, [1971]; Cover, [1979]; Kim, [2007])
- “**Best one-shot approximation**” of the conventional relay channel

^aEl Gamal, Abbas, Navid Hassanpour, and James Mammen. "Relay networks with delays." IEEE Transactions on Information Theory 53, no. 10 (2007): 3413-3431.



One-Shot Relay Channel



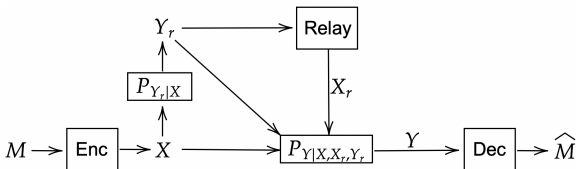
One-Shot Relay Channel

- ① Encoder observes $M \sim \text{Unif}[L]$ and outputs X , which is passed through the channel $P_{Y_r|X}$.
- ② Relay observes Y_r and outputs X_r .
- ③ (X, X_r, Y_r) is passed through the channel $P_{Y|X,X_r,Y_r}$.
 - Y depends on all of X, X_r, Y_r . X_r may interfere with (X, Y_r) .
- ④ Decoder observes Y and recovers \hat{M} .

Practical in scenarios where the relay outputs X_r instantaneously or the channel has a long memory, or it is a storage device.



One-Shot Relay Channel



Theorem (One-Shot Achievable Bound)

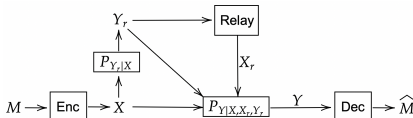
For any P_X , $P_{U|Y_r}$, function $x_r(y_r, u)$, there is a coding scheme for the one-shot relay channel such that the error probability satisfies

$$P_e \leq \mathbf{E} \left[\min \left\{ \gamma L 2^{-\iota(X; U, Y)} \left(2^{-\iota(U; Y) + \iota(U; Y_r)} + 1 \right), 1 \right\} \right],$$

where $(X, Y_r, U, X_r, Y) \sim P_X P_{Y_r|X} P_{U|Y_r} \delta_{x_r(Y_r, U)} P_{Y|X, Y_r, X_r}$, and $\gamma := \ln |\mathcal{U}| + 1$.



One-Shot Relay Channel



Proof

- ① “Random codebooks” $\mathbf{U}_1, \mathbf{U}_2$: independent exponential processes.
- ② Encoder: $U_1 = (\mathbf{U}_1)_{P_{U_1} \times \delta_M}$.
- ③ Relay: $U_2 = (\mathbf{U}_2)_{P_{U_2|Y_r}(\cdot|Y_r)}$, then outputs $X_r = x_r(Y_r, U_2)$.
- ④ Decoder observes Y , and:
 - Refine $P_{U_2|Y}(\cdot|Y)$ to $Q_{U_2} := P_{U_2|Y}^{\mathbf{U}_2}$. By Exponential Process Refinement Lemma:

$$\mathbb{E} \left[\frac{1}{Q_{U_2}(U_2)} \mid U_2, Y, Y_r \right] \leq (\ln |\mathcal{U}_2| + 1) \left(\frac{P_{U_2|Y_r}(U_2)}{P_{U_2|Y}(U_2)} + 1 \right).$$

- Compute $Q_{U_2} P_{U_1|U_2,Y}$ over $\mathcal{U}_1 \times \mathcal{U}_2$, and let its U_1 -marginal be \tilde{Q}_{U_1} .
- Let $\tilde{U}_1 = (\mathbf{U}_1)_{\tilde{Q}_{U_1} \times P_M}$, and output its M -component.



One-Shot Relay Channel

Proof

$$\begin{aligned}
 & \mathbf{P}(\tilde{U}_1 \neq U_1 \mid X, Y_r, U_2, X_r, Y, M) \\
 & \stackrel{(a)}{\leq} \mathbf{E} \left[\min \left\{ \frac{P_{U_1}(U_1) \delta_M(M)}{P_{U_1|U_2,Y}(U_1|U_2, Y) Q_{U_2}(U_2) P_M(M)}, 1 \right\} \mid X, Y_r, U_2, X_r, Y, M \right] \\
 & \stackrel{(b)}{\leq} \min \left\{ L \frac{P_{U_1}(U_1)}{P_{U_1|U_2,Y}(U_1|U_2, Y)} (\ln |\mathcal{U}_2| + 1) \left(\frac{P_{U_2|Y_r}(U_2)}{P_{U_2|Y}(U_2)} + 1 \right), 1 \right\} \\
 & = \min \left\{ (\ln |\mathcal{U}_2| + 1) L 2^{-\iota(X; U_2, Y)} (2^{-\iota(U_2; Y) + \iota(U_2; Y_r)} + 1), 1 \right\}.
 \end{aligned}$$

(a) is by the Poisson matching lemma;

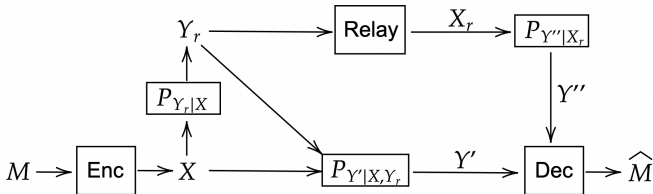
(b) is by the refinement step and Jensen's inequality.

For some $P_{U|Y_r}$ and function $x_r(y_r, u_2)$, it yields the asymptotic achievable rate:

$$R \leq I(X; U, Y) - \max \{ I(U; Y_r) - I(U; Y), 0 \}.$$



One-Shot Primitive Relay Channel



One-shot version of primitive relay channels (Kim, [2007]; Mondelli et al. [2019]; El Gamal et al. [2021]; El Gamal et al. [2022]):

$Y = (Y', Y'')$ and the channel $P_{Y|X, X_r, Y_r} = P_{Y'|X, Y_r} P_{Y''|X_r}$ can be decomposed into two orthogonal components.

Theorem

For any $P_X, P_{X_r}, P_{U'|Y_r}$, there is a coding scheme for the one-shot primitive relay channel with $M \sim \text{Unif}[\mathcal{L}]$ such that

$$P_e \leq \mathbf{E} \left[\min \left\{ \left(\ln(|\mathcal{U}'||\mathcal{X}_r|) + 1 \right) L 2^{-\iota(X; U', Y')} \left(2^{-\iota(X_r; Y'')} + \iota(U'; Y_r | Y') + 1 \right), 1 \right\} \right],$$

$(X, Y_r, U', Y') \sim P_X P_{Y_r|X} P_{U'|Y_r} P_{Y'|X, Y_r}$ independent of $(X_r, Y'') \sim P_{X_r} P_{Y''|X_r}$.



One-Shot Primitive Relay Channel

Theorem

For any $P_X, P_{X_r}, P_{U'|Y_r}$, there is a coding scheme for the one-shot primitive relay channel with $M \sim \text{Unif}[\mathcal{L}]$ such that

$$P_e \leq \mathbf{E} \left[\min \left\{ \left(\ln(|\mathcal{U}'| |\mathcal{X}_r|) + 1 \right) L 2^{-\iota(X; U', Y')} \left(2^{-\iota(X_r; Y'')} + \iota(U'; Y_r | Y') + 1 \right), 1 \right\} \right],$$

$(X, Y_r, U', Y') \sim P_X P_{Y_r|X} P_{U'|Y_r} P_{Y'|X, Y_r}$ independent of $(X_r, Y'') \sim P_{X_r} P_{Y''|X_r}$.

Asymptotic rate

$$R \leq I(X; U', Y') - \max\{I(U'; Y_r | Y') - C_r, 0\}$$

where $C_r = \max_{P_{X_r}} I(X_r; Y'')$.

- It recovers the **compress-and-forward bound**^a.

^aKim, Young-Han. "Coding techniques for primitive relay channels." In Proc. Forty-Fifth Annual Allerton Conf. Commun., Contr. Comput, p. 2007. 2007.



One-Shot Relay Channel

Corollary (Partial-Decode-and-Forward Bound)

Fix any $P_{X,V}$, $P_{U|Y_R,V}$, function $x_R(y_R, u, v)$, and J which is a factor of L . There exists a deterministic coding scheme for the one-shot relay channel with

$$P_e \leq \mathbf{E} \left[\min \left\{ J 2^{-\iota(V; Y_R)} + (\ln(J|\mathcal{U}|) + 1)(\ln(J|\mathcal{V}|) + 1) L J^{-1} 2^{-\iota(X; U, Y|V)} \right. \right. \\ \left. \left. \cdot \left(2^{-\iota(U; V, Y) + \iota(U; V, Y_R)} + 1 \right) \left(J 2^{-\iota(V; Y)} + 1 \right), 1 \right\} \right],$$

where $(X, V, Y_R, U, X_R, Y) \sim P_{X,V} P_{Y_R|X,V} P_{U|Y_R,V} \delta_{x_R(y_R, u, v)} P_{Y|X, Y_R, X_R}$.

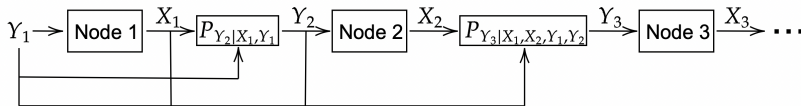
- It recovers existing asymptotic partial-decode-and-forward bounds on primitive relay channel^a and on relay-with-unlimited-look-ahead^b.

^aCover, Thomas, and Abbas El Gamal. "Capacity theorems for the relay channel." IEEE Transactions on information theory 25, no. 5 (1979): 572-584.

^bEl Gamal, Abbas, Navid Hassanpour, and James Mammen. "Relay networks with delays." IEEE Transactions on Information Theory 53, no. 10 (2007): 3413-3431.



General Acyclic Discrete Network



Acyclic discrete network (ADN)

- Nodes are labelled by $1, \dots, N$; node i sees $Y_i \in \mathcal{Y}_i$ and produces $X_i \in \mathcal{X}_i$.
- Y_i depends on all previous inputs and outputs X^{i-1}, Y^{i-1} .
- **ADN**: a collection of channels $(P_{Y_i|X^{i-1}, Y^{i-1}})_{i \in [M]}$, where $P_{Y_i|X^{i-1}, Y^{i-1}}$ is a conditional distribution from $\prod_{j=1}^{i-1} \mathcal{X}_j \times \prod_{j=1}^{i-1} \mathcal{Y}_j$ to \mathcal{Y}_i .



General Acyclic Discrete Network

- ① \tilde{X}_i, \tilde{Y}_i : **actual** random variables from the coding scheme.
- ② X_i, Y_i : random variables following an **ideal** distribution.
 - Example 1 (channel coding): the ideal distribution is $Y_1 = X_2 \sim \text{Unif}[\mathcal{L}]$ (decoding without error), independent of $(X_1, Y_2) \sim P_{X_1} P_{Y_2|X_1}$. If we ensure \tilde{X}^2, \tilde{Y}^2 is “close to” the ideal X^2, Y^2 , it implies $\tilde{Y}_1 = \tilde{X}_2$ with high probability, i.e., a small error probability.
- ③ Take an “error set” \mathcal{E} that we do not want $(\tilde{X}^N, \tilde{Y}^N)$ to fall into.
 - Example 2 (channel coding): \mathcal{E} is the set where $\tilde{Y}_1 \neq \tilde{X}_2$, i.e., an error occurs.
 - Example 3 (lossy source coding): \mathcal{E} is the set where $d(\tilde{Y}_1, \tilde{X}_2) > D$, i.e., the distortion exceeds the limit.
- ④ **Goal**: make $P_{\tilde{X}^N, \tilde{Y}^N}$ “approximately as good as” the P_{X^N, Y^N} , i.e.,

$$\mathbf{P}((\tilde{X}^N, \tilde{Y}^N) \in \mathcal{E}) \lesssim \mathbf{P}((X^N, Y^N) \in \mathcal{E}), \quad (4)$$

which can be guaranteed by ensuring the closeness in TV distance:

$$\delta_{\text{TV}}(P_{X^N, Y^N}, P_{\tilde{X}^N, \tilde{Y}^N}) \approx 0. \quad (5)$$



Coding Scheme

Deterministic coding scheme $(f_i)_{i \in [M]}$

A sequence of encoding functions $(f_i)_{i \in [M]}$, where $f_i : \mathcal{Y}_i \rightarrow \mathcal{X}_i$. For $i = 1, \dots, N$:

- $\tilde{X}_i = f_i(\tilde{Y}_i)$.
- \tilde{Y}_i follows $P_{Y_i|X^{i-1}, Y^{i-1}}$ conditional on $\tilde{X}^{i-1}, \tilde{Y}^{i-1}$.

Goal: $\mathbf{P}((\tilde{X}^N, \tilde{Y}^N) \in \mathcal{E}) \lesssim \mathbf{P}((X^N, Y^N) \in \mathcal{E})$

To construct a deterministic coding scheme, we first construct a randomized coding scheme:

Public-randomness coding scheme $(P_W, (f_i)_{i \in [M]})$

- 1 Generate **public randomness** $W \in \mathcal{W}$ available to all nodes;
- 2 **Encoding function** of node i : $f_i : \mathcal{Y}_i \times \mathcal{W} \rightarrow \mathcal{X}_i$, $\tilde{X}_i = f_i(\tilde{Y}_i, W)$.

Goal: $\delta_{\text{TV}}(P_{X^N, Y^N}, P_{\tilde{X}^N, \tilde{Y}^N}) \approx 0$

If there is a good public-randomness coding scheme, then there is a good deterministic coding scheme by fixing the value of W .



Main Theorem

Theorem

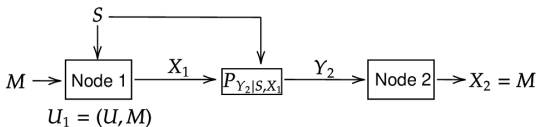
Fix an ADN $(P_{Y_i|X^{i-1}, Y^{i-1}})_{i \in [M]}$. For any collection of indices $(a_{i,j})_{i \in [M], j \in [d_i]}$ where $(a_{i,j})_{j \in [d_i]}$ is a sequence of distinct indices in $[i-1]$ for each i , any sequence $(d'_i)_{i \in [M]}$ with $0 \leq d'_i \leq d_i$ and any collection of conditional distributions $(P_{U_i|Y_i, \bar{U}'_i}, P_{X_i|Y_i, U_i, \bar{U}'_i})_{i \in [M]}$ (where $\bar{U}_{i,S} := (U_{a_{i,j}})_{j \in S}$ for $S \subseteq [d_i]$ and $\bar{U}'_i := \bar{U}_{i,[d'_i]}$), which induces the joint distribution of X^N, Y^N, U^N (the “ideal distribution”), there exists a public-randomness coding scheme s.t.

$$\delta_{\text{TV}}(P_{X^N, Y^N}, P_{\tilde{X}^N, \tilde{Y}^N}) \leq \mathbf{E} \left[\min \left\{ \sum_{i=1}^N \sum_{j=1}^{d'_i} B_{i,j}, 1 \right\} \right],$$

where $\gamma_{i,j} := \prod_{k=j+1}^{d_i} (\ln |\mathcal{U}_{a_{i,k}}| + 1)$ and

$$B_{i,j} := \gamma_{i,j} \prod_{k=j}^{d_i} \left(2^{-\iota(\bar{U}_{i,k}; \bar{U}_{i,[d_i] \setminus [j..k]}, Y_i) + \iota(\bar{U}_{i,k}; \bar{U}'_{a_{i,k}}, Y_{a_{i,k}})} + \mathbf{1}\{k > j\} \right).$$

ADN: Gelfand-Pinsker Problem (Gelfand and Pinsker [1980], Heegard and El Gamal [1983])



Gelfand-Pinsker Problem

- **ADN:** $Y_1 := (M, S)$, $Y_2 := Y$, $P_{Y_2|Y_1, X_1}$ be $P_{Y|S, X}$, and $X_2 := M$.
- **Auxiliary** on node 1: $U_1 = (U, M)$ for some U following $P_{U|S}$ given S .
- **Decoding order:** on node 2 “ U_1 ” (i.e., it only wants U_1).

Corollary (Gelfand-Pinsker)

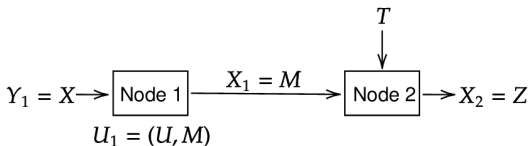
Fix $P_{U|S}$ and function $x : \mathcal{U} \times \mathcal{S} \rightarrow \mathcal{X}$. There exists a coding scheme for the channel $P_{Y|X, S}$ with $S \sim P_S$, $M \sim \text{Unif}[L]$ such that

$$P_e \leq \mathbf{E} \left[\min \left\{ L 2^{-\iota(U; Y) + \iota(U; S)}, 1 \right\} \right],$$

where $S, U, X, Y \sim P_S P_{U|S} \delta_{x(U, S)} P_{Y|X, S}$.



ADN: Wyner-Ziv Problem (Wyner and Ziv [1976])



Corollary (Wyner-Ziv)

Fix $P_{U|X}$ and function $z : \mathcal{U} \times \mathcal{Y} \rightarrow \mathcal{Z}$. There exists a coding scheme s.t.

$$P_e \leq \mathbf{E} \left[\min \left\{ \mathbf{1}\{d(X, Z) > D\} + L^{-1} 2^{-\iota(U; T) + \iota(U; X)}, 1 \right\} \right],$$

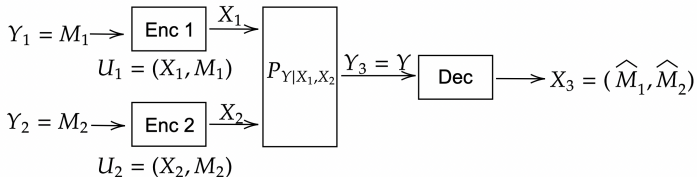
where $X, Y, U, Z \sim P_X P_{Y|X} P_{U|X} \delta_Z(u, Y)$.

Coding for Computing (Yamamoto, [1982])

- Coding for computing: node 2 recovers a function $f(X, T)$,
 $P_e \leq \mathbf{E}[\min\{\mathbf{1}\{d(f(X, T), Z) > D\} + L^{-1} 2^{-\iota(U; T) + \iota(U; X)}, 1\}].$



ADN: Multiple Access Channel (Liao, [1972]; Ahlswede, [1974])



Corollary (Multiple Access Channel)

Fix P_{X_1}, P_{X_2} . There exists a coding scheme for the multiple access channel $P_{Y|X_1, X_2}$ with

$$P_e \leq \mathbf{E} \left[\min \left\{ \gamma L_1 L_2 2^{-\iota(X_1, X_2; Y)} + \gamma L_2 2^{-\iota(X_2; Y|X_1)} + L_1 2^{-\iota(X_1; Y|X_2)}, 1 \right\} \right],$$

where $\gamma := \ln(L_1 | \mathcal{X}_1|) + 1$, $(X_1, X_2, Y) \sim P_{X_1} P_{X_2} P_{Y|X_1, X_2}$.

Asymptotic region: $R_1 < I(X_1; Y|X_2)$, $R_2 < I(X_2; Y|X_1)$, $R_1 + R_2 < I(X_1, X_2; Y)$.



Summary

Summary

- We provide a **unified one-shot coding framework** for communication and compression over general noisy networks.
- We design a proof technique “**exponential process refinement lemma**” that can keep track of a large number of auxiliary random variables.
- We provide **novel one-shot results** for various multi-hop settings.
- We recover existing one-shot and asymptotic results on various settings.

Future Directions

- A unified coding scheme is useful to design automated theorem proving tools, e.g., PSITIP^a. Extensions to one-shot results is left for future study.

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Acknowledgement



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