

Lecture 11 : Supercon

10/29

Below T_c , $R_{DC}(T) = 0$

Transition to SC state due to Cooper Pairs

two e^- make a quasiparticles boson with $\vec{k}_{net} = 0$ in zero field

in $H=0$ second order

$H \neq 0$ first order

Define H_c - critical field :

$$\frac{H_c^2}{8\pi} = f_n(T) - f_s(T)$$

Empirically : $H_c(T) = H_c(0) \left[1 - \left(\frac{T}{T_c} \right)^2 \right]$

$$\vec{B} = \vec{H} + 4\pi \vec{M}$$

$$\vec{B}=0 \rightarrow \vec{H} = -4\pi \vec{M}$$

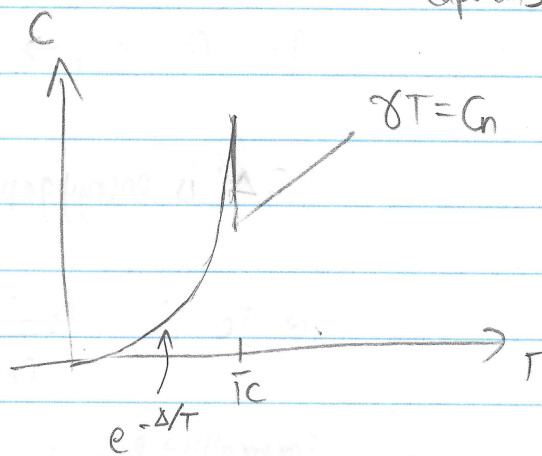
$$\chi = \frac{\vec{M}}{\vec{H}} = -\frac{1}{4\pi}$$

Penetration : $B(x) = B_0 \cdot e^{-x/\lambda}$

$$\lambda(T) = \frac{\lambda(0)}{\left[1 - \left(\frac{T}{T_c} \right)^4 \right]^{1/2}}$$

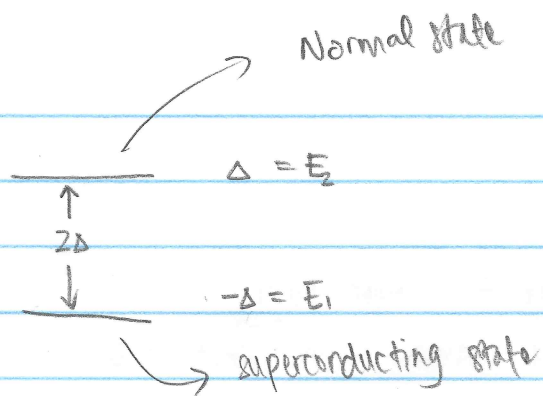
$$\lambda(0) = \left(\frac{mc^2}{4\pi ne^2} \right)^{1/2}$$

Electronic Heat Capacity



$$\Delta S = \int_0^{T_c} \frac{C}{T} dT$$

$$\int_0^{T_c} \frac{C_n}{T} dT = \int_0^{T_c} \frac{C_s}{T} dT$$



$$Z = \sum_n e^{-\beta \epsilon_n} = -e^{-\beta \Delta} + e^{-\beta (-\Delta)} \\ = 2 \cosh(\beta \Delta)$$

$$U = -\frac{\partial}{\partial \beta} \ln Z = -\frac{1}{Z} \frac{\partial Z}{\partial \beta} \\ = -\Delta \tanh \beta \Delta$$

$$\beta = \frac{1}{kT} \quad C = \frac{\partial U}{\partial T} = -k\beta^2 \frac{\partial U}{\partial \beta} \\ C = +k\Delta^2 \operatorname{sech}^2 \beta \Delta$$

$$T \rightarrow 0 \rightarrow \beta \rightarrow \infty \rightarrow C \propto e^{-\Delta/T}$$

2Δ is energy gap (E_g) bt

$$\text{at } T_c : \frac{C_s - C_n}{C_n} = 1.43$$

$$\text{Empirically + BCS : } \frac{\Delta(0)}{kT_c} = 1.76$$

$$\Delta(T) = \Delta(0) \left[1 - \frac{T}{T_c}\right]^{\frac{1}{2}} \text{ near } T_c$$