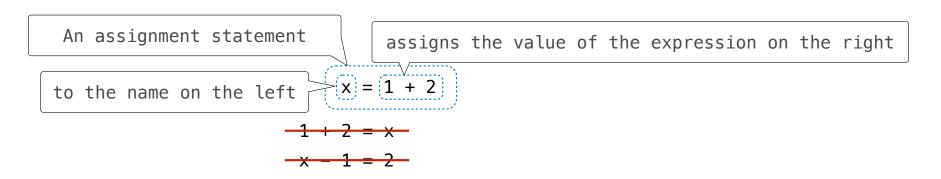


Assignment Statements



The expression (right) is evaluated, and its value is assigned to the name (left).

```
>>> x = 2

>>> y = x + 1

>>> y

3

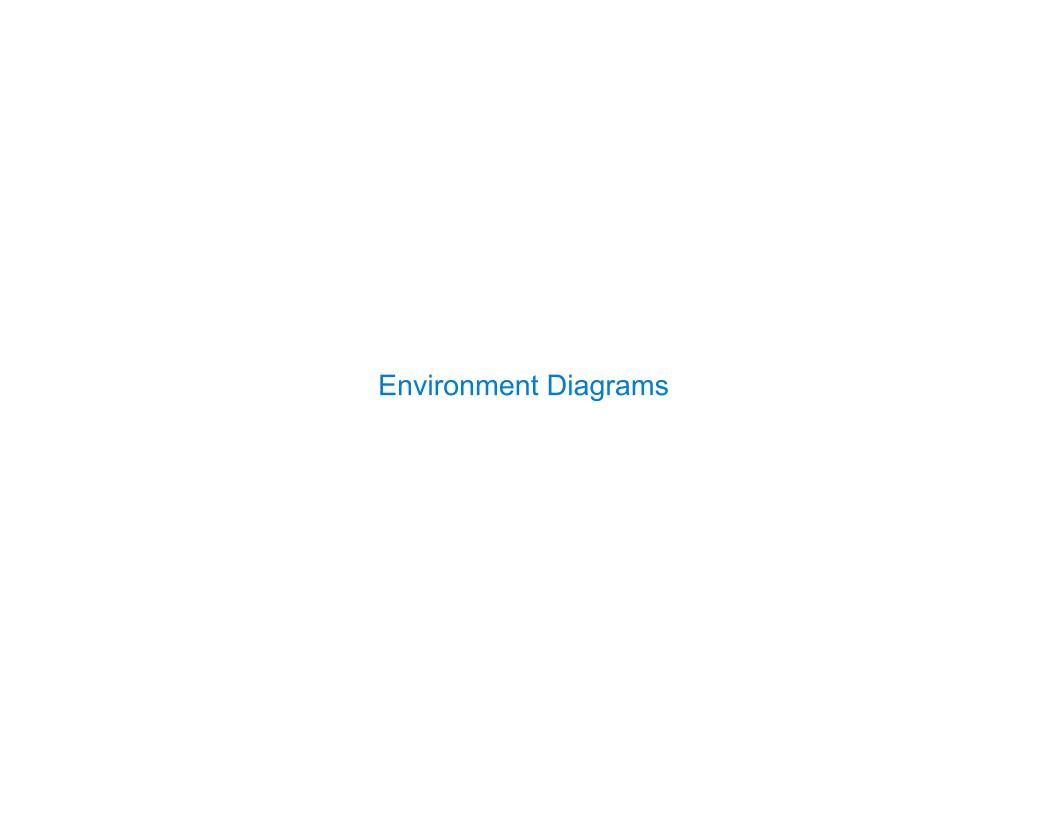
>>> x = 5

>>> x

5

>>> y
```

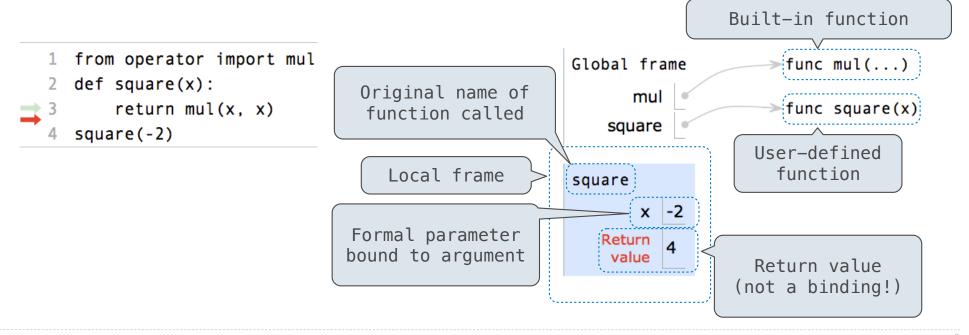
4



Calling User-Defined Functions

Procedure for calling/applying user-defined functions (version 1):

- 1. Add a local frame, forming a new environment
- 2. Bind the function's formal parameters to its arguments in that frame
- 3. Execute the body of the function in that new environment



http://pythontutor.com/composingprograms.html#code=from%20pperator%20import%20mu%40def%20square%28%429%3A%40%20%20%20retur%20mu%428%2%39%Asquare%28%29%30retur%20mu%20retur%20

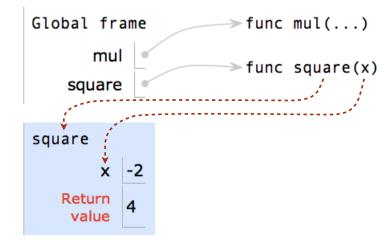
Calling User-Defined Functions

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- 1. Add a local frame, forming a new environment
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- 3. Execute the body of the function in that new environment

```
1 from operator import mul
2 def square(x):
3    return mul(x, x)
4 square(-2)
```

A function's signature has all the information needed to create a local frame



Frames & Environments

Frame: Holds name-value bindings; looks like a box; no repeated names allowed!

Global frame: The frame with built-in names (min, pow, etc.)

Environment: A sequence of frames that always ends with the global frame

Lookup: Find the value for a name by looking in each frame of an environment

A name (which is a type of expression) such as \mathbf{x} is evaluated by looking it up

Why organize information this way?

- Local context before global context
- Calling or returning changes the local context

2 def square(x):

1 from operator import mul

- z dei square(x).
- \Rightarrow 3 return mul(x, x)
 - 4 square(-2)

• Assignment within a function's local frame doesn't affect other frames

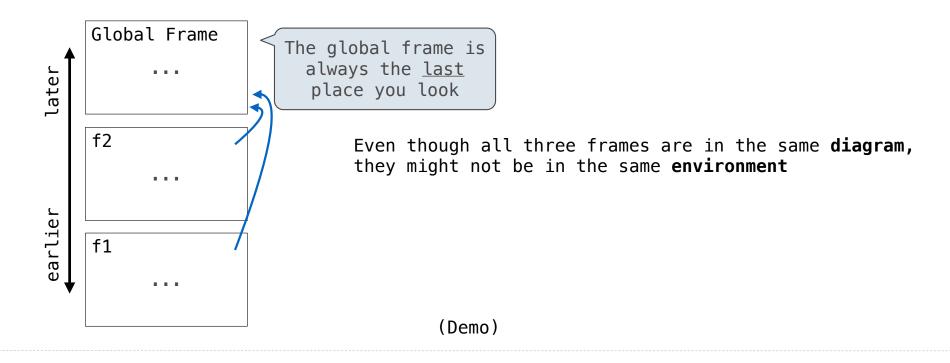
8

A Sequence of Frames

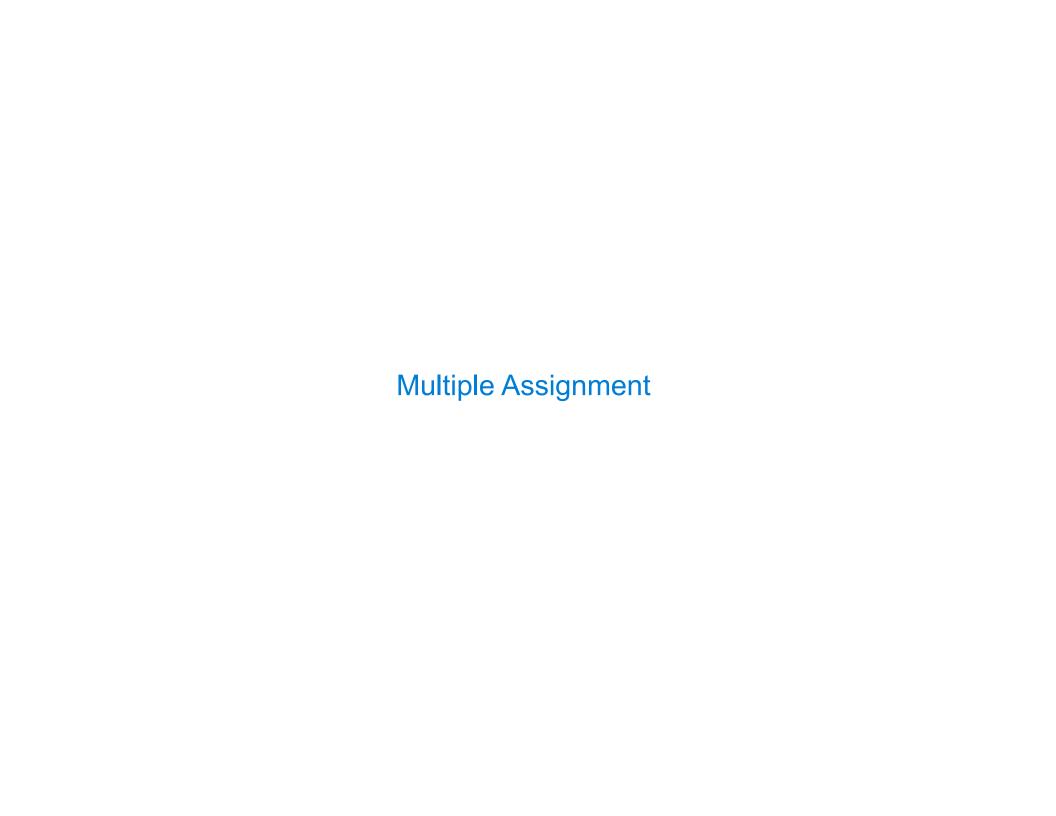
An environment is a sequence of frames. <

A sequence is a first frame and then the rest of the sequence

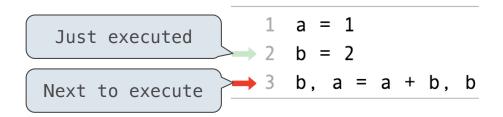
A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.



9



Multiple Assignment



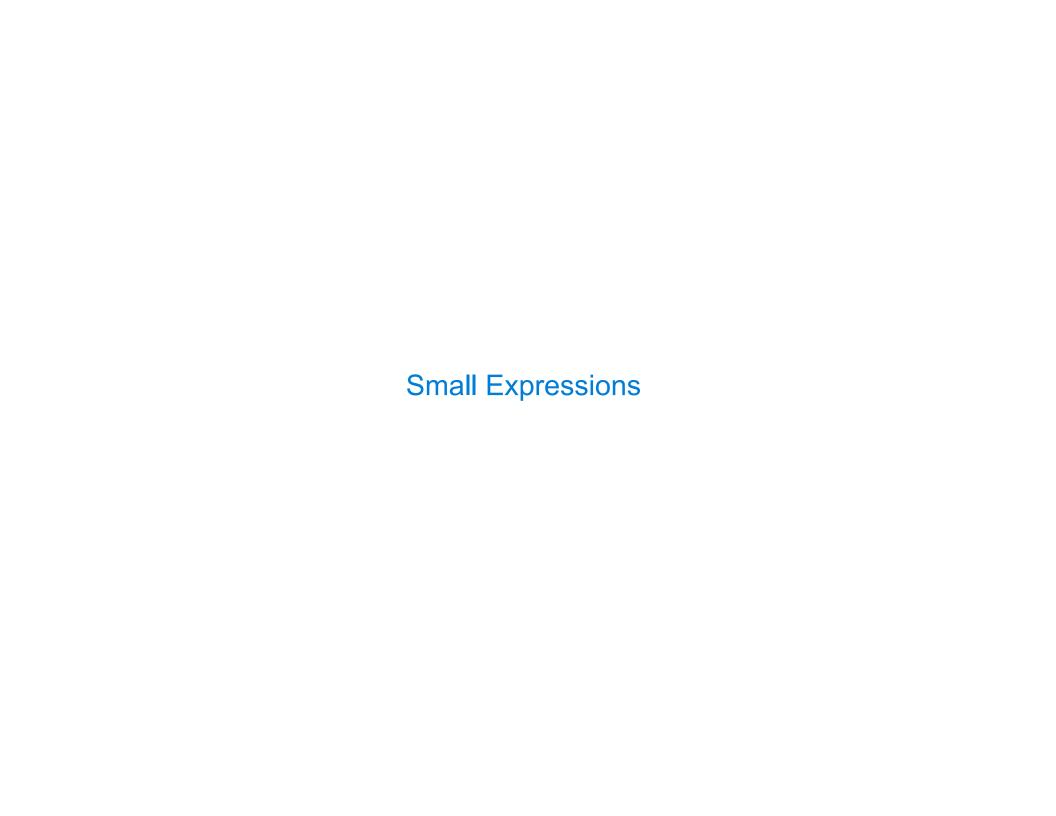
Execution rule for assignment statements:

- 1. Evaluate all expressions to the right of = from left to right.
- 2. Bind all names to the left of = to those resulting values in the current frame.

(Demo)

Print and None

(Demo)



Problem Definition

From Discussion 0:

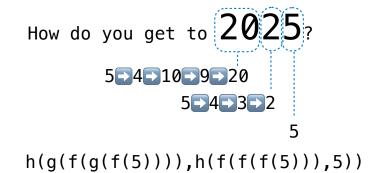
Imagine you can call only the following three functions:

- f(x): decrement an integer x to get x-1
- g(x): increment then double an integer x to get 2*(x+1)
- h(x, y): Concatenates the digits of two different positive integers x and y. For example, h(789, 12) evaluates to 78912 and h(12, 789) evaluates to 12789.

Definition: A *small expression* is a call expression that contains only f, g, h, the number 5, and parentheses. All of these can be repeated. For example, h(g(5), f(f(5))) is a small expression that evaluates to 103.

What's the shortest *small expression* you can find that evaluates to 2024?

Fewest calls?
Shortest length when written?

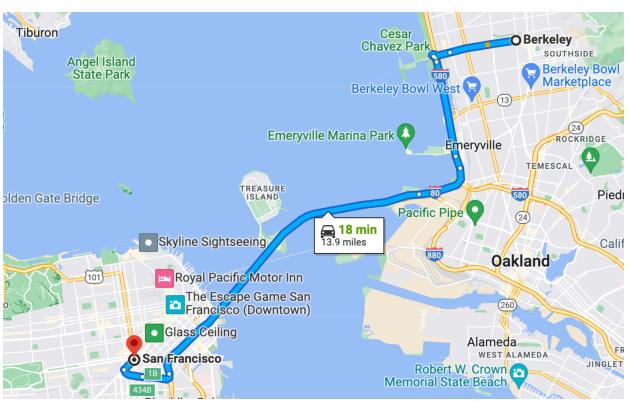


Effective problem solving:

- Understand the problem
- Come up with ideas
- Turn those ideas into solutions

Search





A common strategy: try a bunch of options to see which is best Computer programs can evaluate many alternatives by repeating simple operations

A Computational Approach

Try all the small expressions with 3 function calls, then 4 calls, then 5 calls, etc.

```
f(f(f(5))) \rightarrow 2
                         f(f(h(5,5))) \rightarrow 53
                                                              h(5,f(f(5))) \rightarrow 53
                                                                                                    h(q(5),f(5)) \rightarrow 124
q(f(f(5))) -> 8
                         q(f(h(5,5))) \rightarrow 110
                                                              h(5,q(f(5))) \rightarrow 510
                                                                                                    h(g(5),g(5)) \rightarrow 1212
f(q(f(5))) -> 9
                          f(q(h(5,5))) \rightarrow 111
                                                              h(5,f(q(5))) \rightarrow 511
                                                                                                    h(g(5),h(5,5)) \rightarrow 1255
                         g(g(h(5,5))) \rightarrow 226
                                                              h(5,g(g(5))) \rightarrow 526
q(q(f(5))) -> 22
                                                                                                    h(h(5,5),f(5)) \rightarrow 554
                                                                                                    h(h(5,5),g(5)) \rightarrow 5512
f(f(q(5))) \rightarrow 10
                         f(h(5,f(5))) \rightarrow 53
                                                              h(5,f(h(5,5))) \rightarrow 554
q(f(q(5))) \rightarrow 24
                         g(h(5,f(5))) \rightarrow 110
                                                              h(5,q(h(5,5))) \rightarrow 5112
                                                                                                    h(h(5,5),h(5,5)) \rightarrow 5555
f(q(q(5))) \rightarrow 25
                         f(h(5,q(5))) \rightarrow 511
                                                              h(5,h(5,f(5))) \rightarrow 554
                                                                                                    h(f(f(5)),5) \rightarrow 35
q(q(5))) -> 54
                          q(h(5,q(5))) \rightarrow 1026
                                                              h(5,h(5,q(5))) \rightarrow 5512
                                                                                                    h(q(f(5)),5) \rightarrow 105
                          f(h(5,h(5,5))) \rightarrow 554
                                                              h(5,h(5,h(5,5))) \rightarrow 5555
                                                                                                    h(f(q(5)),5) \rightarrow 115
                          q(h(5,h(5,5))) \rightarrow 1112
                                                              h(5,h(f(5),5)) \rightarrow 545
                                                                                                    h(q(q(5)),5) \rightarrow 265
                          f(h(f(5),5)) \rightarrow 44
                                                              h(5,h(q(5),5)) \rightarrow 5125
                                                                                                    h(f(h(5,5)),5) \rightarrow 545
                          q(h(f(5),5)) \rightarrow 92
                                                              h(5,h(h(5,5),5)) \rightarrow 5555
                                                                                                    h(q(h(5,5)),5) \rightarrow 1125
                          f(h(q(5),5)) \rightarrow 124
                                                              h(f(5),f(5)) \rightarrow 44
                                                                                                    h(h(5,f(5)),5) \rightarrow 545
                          q(h(q(5),5)) \rightarrow 252
                                                              h(f(5),g(5)) \rightarrow 412
                                                                                                     h(h(5,q(5)),5) \rightarrow 5125
                          f(h(h(5,5),5)) \rightarrow 554
                                                                                                     h(h(5,h(5,5)),5) \rightarrow 5555
                                                              h(f(5),h(5,5)) \rightarrow 455
                          q(h(h(5,5),5)) \rightarrow 1112
                                                                                                    h(h(f(5),5),5) \rightarrow 455
                                                                                                    h(h(g(5),5),5) \rightarrow 1255
                                                                                                    h(h(h(5.5).5).5) \rightarrow 5555
```

Reminder: f(x) decrements; g(x) increments then doubles; h(x, y) concatenates

A Computational Approach

Try all the small expressions with 3 function calls, then 4 calls, then 5 calls, etc.

Reminder: f(x) decrements; g(x) increments then doubles; h(x, y) concatenates

A Computational Approach

Try all the small expressions with 3 function calls, then 4 calls, then 5 calls, etc.

```
def f(x):
                   Functions
   return x - 1
def q(x):
                                                                                           Generators
                                                               def smalls(n):
   return 2 * (x + 1)
                                                                   if n == 0:
def h(x, y):
                                                                       vield Number(5)
                                 Containers
   return int(str(x) + str(y))\langle
                                                                   else:
                                                                                                    Recursion
                                                                       for operand in smalls(n-1):
class Number:
                                                                           yield Call(f, [operand])
   def __init__(self, value):
                                 Objects
                                                                           yield Call(g, [operand])
       self.value = value
                                                                                                                Tree
                                                                       for k in range(n):
                                                                           for first in smalls(k):
                                                                                                             Recursion
   def __str__(self):
                                                                               for second in smalls(n-k-1):
                                 Representation
       return str(self.value)
                                                                                  if first.value > 0 and second.value > 0:
                                                                                      yield Call(h, [first, second]) √
   def calls(self):
                                                                                                                      Control
       return 0
                                                               result = []
class Call:
                                                               for i in range(9):
   """A call expression."""
                                                                   result.extend([e for e in smalls(i) if e.value == 2024])
   def __init__(self, f, operands):
       self.f = f
                                                                                  Mutability
       self.operands = operands
                                                     Sequences
       self.value = f(*[e.value for e in operands]) <
   def __str__(self):
                                                                       Higher-Order Functions
       return f'{self.f. name }({",".join(map(str, self.operands))})'
   def calls(self):
                                                         Iterators
       return 1 + sum(o.calls() for o in self.operands)
                                                                                    By Midterm 2, you can do this.
```