Earth Surf. Dynam., 9, 1301–1322, 2021 https://doi.org/10.5194/esurf-9-1301-2021 © Author(s) 2021. This work is distributed under the Creative Commons Attribution 4.0 License.





Escarpment retreat rates derived from detrital cosmogenic nuclide concentrations

Yanyan Wang and Sean D. Willett

Department of Earth Sciences, ETH Zürich, Zürich, 8092, Switzerland Correspondence: Yanyan Wang (yanyan.wang@erdw.ethz.ch)

Received: 19 March 2021 - Discussion started: 22 April 2021

Revised: 3 August 2021 – Accepted: 30 August 2021 – Published: 30 September 2021

Abstract. High-relief great escarpments at passive margins present a paradoxical combination of high-relief topography but low erosion rates suggesting low rates of landscape change. However, vertical erosion rates do not offer a straightforward metric of horizontal escarpment retreat rates, so we attempt to address this problem in this paper. We show that detrital cosmogenic nuclide concentrations can be interpreted as a directionally dependent mass flux to characterize patterns of non-vertical landscape evolution, e.g., an escarpment characterized by horizontal retreat. We present two methods for converting cosmogenic nuclide concentrations into escarpment retreat rates and calculate the retreat rates of escarpments with published cosmogenic ¹⁰Be concentrations from the Western Ghats of India. Escarpment retreat rates of the Western Ghats inferred from this study vary within a range of hundreds to thousands of meters per Myr. We show that the current position and morphology of the Western Ghats are consistent with an escarpment retreating at a near-constant rate from the coastline since rifting.

1 Introduction

Passive continental margins exhibit a characteristic morphology with a high-relief escarpment separating a low-relief inland high plateau and the low, flat coastal plain (Fig. 1). The edge of an escarpment often coincides with a major, even a continental, water divide. The escarpment that separates the plateau and the coast plain often exhibits local relief of over 1 km, even reaching heights exceeding 2 km. These great escarpments extend hundreds of kilometers parallel to the coast along rift margins and are typically found 30-200 km inland from the coastline (Linari et al., 2017; Persano et al., 2002). Examples of passive margin escarpments and their age of formation include the Red Sea margin (10–5 Ma), the Western Ghats in India (84 Ma) (Eagles and Hoang, 2014), the Serra do Mar escarpment in Brazil (125 Ma), the Drakensberg escarpment (130 Ma) in South Africa, the Queensland escarpment in Australia (150 Ma) and the Blue Ridge escarpment in the US (200 Ma) (Matmon et al., 2002).

The absence of active tectonics at old rift margins makes the formation and persistence of escarpments a long-debated problem. One major dispute is whether an escarpment is geomorphologically static or dynamic in the sense of rates of change of erosion or back-cutting or retreat of the escarpment away from the coast. Most researchers agree that an escarpment originates from rifting-related processes, forming at the edge of a rift graben, and subsequently migrates inland to its modern position (Sacek et al., 2012; Tucker and Slingerland, 1994; Gilchrist and Summerfield, 1990), but it is still debated as to whether this happens as a continuous process or occurs rapidly following rifting with subsequent slowing or stalling, so that the modern geomorphic feature is static (Beauvais et al., 2016; Bonnet et al., 2016; Beauvais et al., 2008). The hypothesized evolution towards relatively static escarpments is supported by the observation of low time-averaged denudation rates. Apatite fission track (AFT) ages and (U-Th) / He ages on the escarpment-side coastal plain are rarely reported to be significantly younger than the break-up age (Persano et al., 2006, 2002; Cockburn et al., 2000), suggesting that escarpments form and retreat rapidly following break-up, but subsequently slow. Erosion rates from in situ cosmogenic nuclides concentrations of escarpment-draining basins are also very low, with rates on the order of tens of meters per million years (Portenga and Bierman, 2011), supporting the idea that older escarpments are geomorphically static.

Alternatively, numerical studies of escarpment topography evolution suggest a much more dynamic and long-lived geomorphic evolution (Braun, 2018; Willett et al., 2018; Sacek et al., 2012; van der Beek et al., 2002; Tucker and Slingerland, 1994; Kooi and Beaumont, 1994). Braun (2018) presented a parameterization of erosion and retreat of an escarpment based on fluvial erosion and diffusion, and showed that this would lead to a constant rate of retreat over time. Willett et al. (2018) also argued that escarpment processes should evolve to maintain a constant form of an escarpment with a constant rate of backward retreat where escarpment slope maintains a balance with rock advection driven by retreat. Given a constant rate of escarpment retreat and formation during rifting, a retreat rate of order $\sim 1 \text{ km/Myr}$ is suggested from the distance of most escarpments from the coastline (Seidl et al., 1996; Oilier, 1982).

Testing of these models is difficult in that measuring a horizontal retreat rate of a geomorphic feature is quite difficult. Direct evidence for escarpment retreat comes from terrace deposits found atop of the Blue Ridge escarpment crest and beheaded drainages on the plateau side of the escarpment (Prince et al., 2010). Erosion rates are easier to measure and have been estimated from sediment budgets measured in the offshore (Campanile et al., 2008) and from concentrations of cosmogenic radionuclides (e.g., de Souza et al., 2019; Linari et al., 2017; Salgado et al., 2014). Detrital cosmogenic nuclide (DCN) ¹⁰Be-derived erosion rates used to calculate retreat rates of the southeastern Australian escarpment yielded rates of 40–80 m/Myr over the last few hundred thousand years (Godard et al., 2019).

The lack of post-rift thermochronometric cooling ages and the very low rates of erosion derived from ¹⁰Be concentrations suggest little geomorphic modification of the landscape and only slow retreat of the escarpment. Given that rocks are exhumed from depths of less than 2 km due to retreat of even the largest escarpments, their cooling is likely to be too small to be measured by thermochronometry except at very high geothermal gradients. It is thus likely that cooling ages reflect conductive cooling associated with lithospheric cooling following rifting or erosional exhumation shortly after rifting when geothermal gradients are elevated but are insensitive to the subsequent erosion associated with escarpment retreat. Cosmogenic isotope concentrations also are problematic, in that escarpment retreat suggests a spatially variable erosion rate so that catchment wide averages, even when correctly measuring mean rates, may not be representative of the local process rates responsible for escarpment retreat.

In this paper, we present a new, systematic method for interpreting detrital cosmogenic isotope concentrations in terms of horizontal retreat rates of an escarpment. The method is based on the physical principle of the models of Braun (2018) and Willett et al. (2018) that argued that an escarpment should evolve into a morphology that drives hor-

izontal retreat at a constant rate. We demonstrate that these conditions are exhibited by the Western Ghats escarpment in India, which shows channel profiles consistent with the concept of a steady, retreating escarpment with occasional river capture from the upper plateau. Under conditions of steady horizontal escarpment retreat, we demonstrate that in situ detrital cosmogenic nuclide concentrations can be interpreted directly in terms of an average horizontal retreat rate of a catchment. We present two methods for the calculation of horizontal retreat rates and demonstrate these methods using published detrital ¹⁰Be concentrations from the Western Ghats in India.

2 Model for escarpment retreat

2.1 Concept of escarpment retreat

High-relief escarpments along rifted continental margins pose a stark morphologic contrast with their neighboring low-relief plateau and coastal plain. The typical width of an escarpment normal to the margin is 5 to 20 km, implying enough drainage area in which a well-developed river network is present and dominates the erosional processes. Normal scaling relationships between slope and area predict high normalized channel steepness for most escarpments, so the observed rates of erosion, which are low, are surprising.

To maintain generality, one can consider two evolution scenarios in terms of river incision: downcutting of the topography with a stationary escarpment (Gunnell and Fleitout, 1998) and back-cutting or retreat of the escarpment with migration of the water divide (Tucker and Slingerland, 1994) (Fig. 1). The downcutting model can be driven by base-level fall or it can involve a change in relief with a fixed base level and a stationary water divide and escarpment. In the stationary escarpment and water divide scenario, the position of an elemental catchment remains stationary. Assuming that erosion rates on the plateau are negligible, the surface of the catchment will downcut only if the escarpment front becomes steeper and shorter. Without a change in the coastal elevation, erosion is focused on the escarpment. In the retreating escarpment scenario, the escarpment front retreats towards the inland plateau. Headward erosion of escarpment rivers drives retreat of the escarpment, widening the coastal plain and enlarging the escarpment-draining basins, although the overall height and morphology of the escarpment remain constant, neglecting the increase in elevation of the base of the escarpment as the coastal plain increases in length (Willett et al., 2018).

These models can be described in terms of a surface moving in either a vertical or horizontal direction with respect to its underlying rock (Fig. 1). Although, as argued by Gunnell and Harbor (2010), the geometry of an escarpment cannot remain strictly self-similar or uniform during its evolution at geological timescales, we assume that morphologic changes are small, and an instantaneous erosion or retreat velocity is

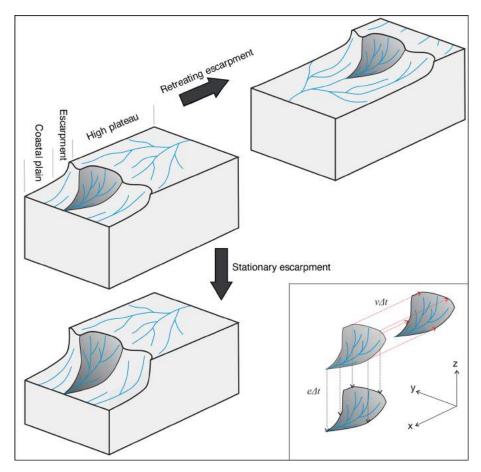


Figure 1. Conceptual diagram showing two scenarios of escarpment evolution: a retreating escarpment or a downcutting escarpment with stationary water divide. The gray surface denotes the surface of an elemental escarpment-draining catchment. Inset is the mathematical representative of the two scenarios as motion relative to the rock. Δt denotes the unit time, v denotes retreat rate, e denotes a vertical erosion rate, red arrows indicate the horizontal retreat vector, and black arrows indicate the vertical erosion vector.

characteristic of the average change over longer timescales. For vertical erosion, this is essentially the assumption made in treating cosmogenic isotope concentrations, converting concentration to catchment average erosion rate. Here, we propose that the retreat velocity should be treated in the same manner, representing it as a horizontal motion of the catchment surface. In this case, the change of the surface can be characterized by a vector in which the magnitude represents the retreat velocity and the direction represents the retreat direction, taken with respect to the solid earth. In this paper, we will investigate the implications of these end-member models for erosional fluxes.

2.2 Southern Western Ghats

2.2.1 Geological and morphological features

The escarpment on the west margin of India is a well-recognized escarpment. It extends parallel to the coast for 1500 km and defines the mountainous region of the Western Ghats (Fig. 2). The western margin of India rifted from

Madagascar at \sim 84 Ma (Eagles and Hoang, 2014), with secondary rifting from the Seychelles affecting the northern segment of the Indian margin (Torsvik et al., 2013). The Western Ghats exhibit relief of 1000 to 2600 m. The escarpment is heterogeneous in terms of bedrock geology and morphology from north to south. The northern Western Ghats (21–16° N) lie on the Deccan igneous province (the Deccan Traps), whilst the southern Western Ghats (16-10° N) are located in the Archean-Proterozoic metamorphic shield. The sinuosity of the escarpment divide varies, with a higher sinuosity of 2.73 in the northern Western Ghats and a value of 2.2 for the southern Western Ghats (Matmon et al., 2002). The southern Western Ghats escarpment (abbreviated as the SWG escarpment hereafter) is 30 to 90 km from the coastline (Fig. 2). The SWG escarpment usually coincides with the continental water divide, but in some areas, the water divide is located inland from the morphologic escarpment. Although the history of the river topological structure is not known, most of the morphologically flat regions currently draining to the west are small in area and are consistent with relatively recent capture of these drainages from east directed to west directed. Consequently, some escarpment-draining basins may have gained drainage area from the plateau, and we distinguish between rivers that have a headwater divide that coincides with the escarpment edge from those that include drainage area from the plateau (e.g., basin A and basin B in Fig. 2).

Escarpment rivers in the SWG are bedrock rivers cutting into the Precambrian metamorphic basement. The morphology of the rivers draining the escarpment differs primarily due to their initiation on the escarpment or landward of the escarpment on the plateau (Fig. 3). Rivers initiating on the escarpment are characterized by a long, low-slope reach on the coastal plain and abrupt steepening at the escarpment front (Fig. 3a). This is particularly evident in transformed χ-elevation river profiles, which normalize the river profiles for drainage area (Perron and Royden, 2013). A typical x-elevation profile of these escarpment front-initiated rivers is composed of two near-linear segments: the coastal plain reach and the short and steeper escarpment-draining reach (Fig. 3b). This characteristic χ-elevation profile indicates the transient state of the escarpment topography and is consistent with the model of a moving escarpment with all erosion focused on the escarpment face (Willett et al., 2018). For plateau-initiated rivers, the channel profile and χ profile have an additional low-slope "tail" at low drainage area, representing the reach on the plateau (Fig. 3c and d).

2.2.2 Methods of river profile analysis

In order to calculate a scaled river profile, it is necessary to assume or estimate the concavity of the profile (Perron and Royden, 2013). We evaluated the slope—area scaling of escarpment-draining rivers (Fig. 4). The channel slope and drainage area data were extracted with the MATLAB-based software TopoToolBox 2 (Schwanghart and Scherler, 2014). We calculated the average slope and drainage area over predefined river segments. River segments were defined with a length of 1 km but break at confluences and were limited by both a threshold slope and drainage area. Recognizing that there were two sets of data, corresponding to the escarpment and the coastal plain, we searched for an optimal break point in slope—area space, searching within the red-dashed-line box in Fig. 4b.

We found concavities of 0.3 to 0.6 for the SWG rivers from a slope–area plot with a mean value of 0.42, which is typical for bedrock rivers (Snyder et al., 2000). Conventionally, normalized steepness index is taken as a proxy for erosion rate (Kirby and Whipple, 2012). However, for an escarpment, uplift rate is likely to be limited to the isostatic response to erosion, and the erosion rate should be reflective rather of the erosion associated with the escarpment retreat. Willett et al. (2018) analyzed this problem and demonstrated that the slope–area scaling for a river retreating in a direction oppo-

site to its flow should scale according to

$$S_{\text{river}} = -\left(\frac{v}{K}\right)^{\frac{1}{n-1}} A_{\text{d}}^{-\frac{m}{n-1}} n > 1,$$
 (1)

where v is the retreat rate, S_{river} is the local channel slope, A_d is the upstream drainage area, K is the erodibility constant, and m and n are positive empirical constants. The steepness of a channel following this scaling would be

$$k_{\rm S} = \left(\frac{v}{K}\right)^{\frac{1}{n-1}} n > 1. \tag{2}$$

This relationship implies a higher concavity (m/n-1) than rivers in equilibrium with vertical uplift, so it is interesting that the concavities we find are close to global averages. This suggests that the assumptions made by Willett et al. (2018) of a steady 1-D river normal to the escarpment with continuous area gain at the channel head might not be appropriate. Sinuous, branching rivers in a transient state due to discrete area capture might fit such a model on average but not for individual escarpment-draining rivers. The slope—area relationship (Fig. 4c) also shows a segmented form as in the channel profiles (Fig. 4b).

2.2.3 Escarpment retreat from river profile analysis

The segmented form of the escarpment-draining rivers is consistent with models of escarpment retreat with a lower reach on the coastal plain, where the gradient is sufficient to transport eroded sediment, but is not incising bedrock. On the upper reach, incision rates are high but have a pattern that results in horizontal retreat of the escarpment as well as the drainage divide. The normalized steepness indices derived from slope-drainage area plots or from the normalized channel profiles show a constant value for the escarpment reaches, consistent with a constant rate of erosion but also consistent with a constant horizontal retreat rate (Willett et al., 2018). Furthermore, river profiles have the same form, but the lengths of the various reaches are highly variable, even scaled into χ space. This suggests that the kinked profile form is not the result of a temporal change in uplift rate common to all rivers, in which case the x scaling would collapse the profiles onto a common form. Rather the profiles are consistent with an escarpment retreat model in which the lower reach is graded to a low slope sufficient to transport sediment from the eroding escarpment reach, and the steep segment is adjusted to erode the escarpment (Willett et al., 2018).

Rivers that include plateau reaches (Fig. 3c and d) are scattered throughout the study area, intermixed with the escarpment rivers. This suggests that they are not the response to temporal variations in uplift rate; i.e., they are not moving knickpoints in response to base-level changes, or they would be clustered together spatially and have common chi profiles, at least within single drainage basins. Rather they appear to

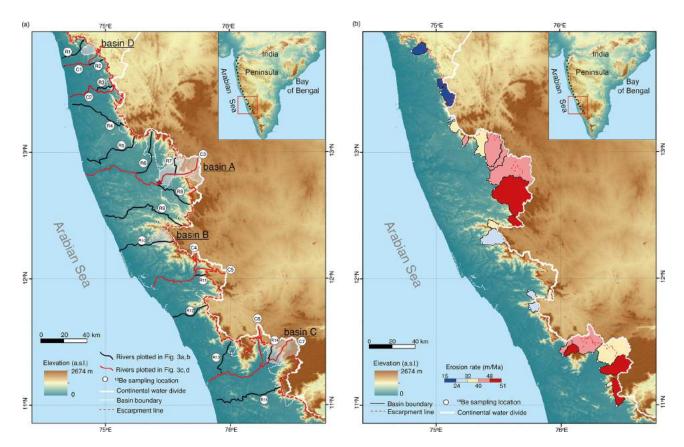


Figure 2. (a) Shuttle Radar Topography Mission (SRTM) 90 m digital elevation model (DEM) (Jarvis et al., 2008) showing the topographic overview of the southern Western Ghats escarpment (location is indicated in the inset figure), escarpment-draining rivers (in solid black and red lines) and the continental water divide (solid white line). The dashed red line denotes the Western Ghats escarpment, and we take the southern limit of the Deccan Traps as the boundary between the northern and southern segments. The ¹⁰Be sample locations of Mandal et al. (2015) are indicated by filled white circles. **(b)** Cosmogenic ¹⁰Be-derived erosion rates. Erosion rate is recalculated from the published concentrations of Mandal et al. (2015) following the method of Lupker et al. (2012). See Table 1 for the data.

be the response to capture of river reaches from the plateau to the coastal plain (Giachetta and Willett, 2018).

The values of the normalized steepness on the escarpment reaches are relatively high compared to other rivers globally but particularly for the observed erosion rates (Fig. 5). In fact, the values of channel steepness from the Western Ghats are amongst the highest in the world at the observed erosion rates. Although the bedrock is relatively resistant to erosion, rainfall is also relatively high, so there is no obvious reason for these high values in a region where the tectonic uplift rates are likely to be low and not localized to the escarpment.

Taken together, these observations suggest that the Ghats escarpment is actively retreating to the east. The high relief is likely to be old and inherited rather than the result of recent uplift, and erosion is focused on the escarpment, driving the escarpment horizontally rather than eroding the entire landscape downward. This suggests that the ¹⁰Be concentration data should be interpreted with this landscape evolution model in mind, and we pursue this approach in the next section.

2.3 Erosional flux and rock velocity from cosmogenic isotope concentrations

The use of cosmogenic isotope concentrations to derive erosion rates makes a key assumption of continuous and steady removal of rocks from the Earth's surface (Lal, 1991). As production of cosmogenic isotope nuclides is fast with respect to erosion rates, steady erosion implies that the concentration profile of a cosmogenic nuclide with depth is also time invariant (Niemi et al., 2005). Catchment-wide detrital cosmogenic-based erosion rates relax this assumption and require only that equilibrium is maintained between the catchment-integrated quantities of production and removal. The appropriate secular equilibrium state implies that over an appropriate timescale, the number of cosmogenic isotope atoms produced is equal to the number lost by erosion, as integrated over the entire catchment. The total rate of production is predictable according to the geographic location, topology and exposed lithology of the catchment (Stone, 2000; Lal, 1991). If we assume well-mixed sediment derived from the entire catchment surface, the measured concentra-

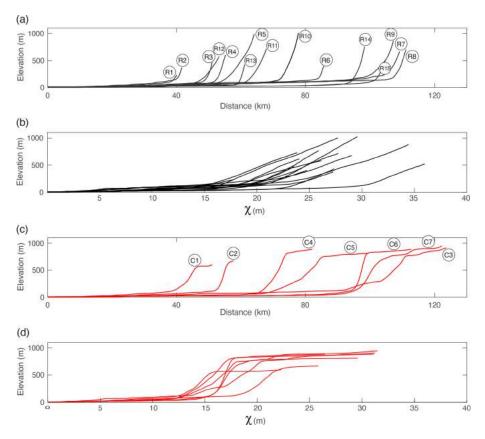


Figure 3. River profiles and corresponding transformed χ profiles in the southern Western Ghats. Locations of these rivers are indicated in Fig. 2a. Rivers are extracted from 90 m SRTM data and use a threshold drainage area of 1 km². The χ value of rivers is calculated using a base level of sea level and concavity of 0.42, and precipitation is not included. (a, b) Profiles of escarpment rivers that initiate from the escarpment. (c, d) Profiles of escarpment rivers that initiate from the plateau interior and drain through the escarpment.

tion of a cosmogenic nuclide within these sediments is equal to the total catchment production divided by the total volume of eroded rock, or more precisely, the volume of the target mineral bearing the cosmogenic nuclide, e.g., quartz (von Blanckenburg, 2005). Production divided by volume can be expressed as the erosional mass flux out of the catchment surface. As a flux, this requires the area of the surface, and in practice this area is calculated from the surface projected onto a horizontal plane, as is done with any standard digital elevation model. This implicitly defines the erosional flux vector to be vertical. However, in general, the mass flux does not need to be treated as a purely vertical flux. In many geomorphic or tectonic settings such as the escarpment problem described above, the change of the surface is better described with a component in the horizontal direction with respect to the underlying rock, thus defining a flux in a non-vertical direction. At rift escarpments, the mass flux of an escarpmentdraining basin can be approximated as purely horizontal and the mass flux is determined by the rate of escarpment retreat with no vertical component. This suggests a need to redefine the expressions describing erosion rates in terms of ¹⁰Be concentrations, generalizing these for a flux of mass through the Earth's surface in a non-vertical direction.

In the following section, we derive a model for catchment-wide mass flux based on the production of cosmogenic nuclides and concentrations measured from river sediments but for the case where the average motion of rock with respect to the Earth's surface is in a horizontal rather than a vertical direction. We then present two methods for calculation of mass flux and velocity from the measured detrital concentration and the catchment-wide nuclide production.

2.3.1 Catchment-averaged erosion rates from cosmogenic nuclide concentrations

Cosmogenic nuclide (CN) concentration of river sediment at a basin outlet represents the basin-integrated production of CNs and the basin-integrated erosion of the rock (Granger et al., 2013):

$$\underline{C} = \frac{P_0}{e\rho/\Lambda + \lambda},\tag{3}$$

where ρ (g/cm³) is the density of the target rock and Λ (g/cm²) is free path absorption length of the CN, and a de-

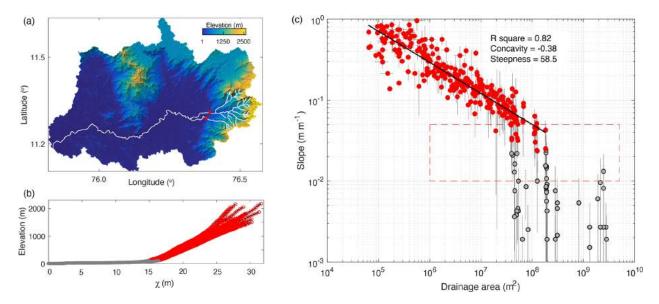


Figure 4. (a) The Chaliyar River catchment in Western Ghats, India. Red squares indicate potential transition point from coastal plain to escarpment channel. The outlet of the drainage basin is at the coast of the Arabian Sea. Channels are extracted from the DEM using a threshold drainage area of $0.5 \,\mathrm{km}^2$ (approximately six DEM grid cells using 90 m resolution DEM). (b) The elevation- χ profiles of channels shown in panel (a). Gray circles indicate coastal plain reaches; open red circles are escarpment reaches and are used in slope—area regression. χ is calculated using a concavity of 0.42. (c) Channel slope–drainage area plot in log space. Uncertainty is 1σ . The box marked by the dashed red line is the range for searching of the threshold point between coastal plain and escarpment (see Methods section).

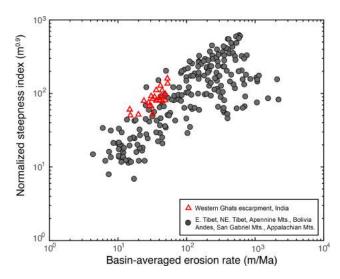


Figure 5. Normalized channel steepness index and cosmogenic ¹⁰Be-derived basin-averaged erosion rates from the southern Western Ghats (red-lined triangles) with comparison to a compilation of global data by Kirby and Whipple (2012) (gray dots). The steepness of Western Ghats rivers is from slope-area analysis using a uniform concavity of 0.45 to be consistent with the global data.

cay constant λ must be considered if the CN is radioactive. The underbars represent integration over the catchment surface (S), which has total area, A, so that each quantity is an integral over the full upstream catchment area (Lupker et al., 2012):

$$\underline{P_0} = \frac{1}{A} \iint_{\mathcal{C}} P_0(x, y) \, \mathrm{d}x \, \mathrm{d}y,\tag{4}$$

$$\underline{P_0} = \frac{1}{A} \iint_S P_0(x, y) dx dy, \qquad (4)$$

$$\underline{e} = \frac{1}{A} \iint_S e(x, y) dx dy, \qquad (5)$$

where a location (x, y) in the catchment is characterized by local erosion rate e(x, y) and a CN surface production rate of $P_0(x, y)$. Estimation of catchment-wide erosion rate is done by solving for e in Eq. (3), given a measurement of C. Complications arise from the calculation of production rates, inclusion of muon production, radioactive decay and topographic shielding. Muon production involves only adding additional production terms, which are integrable. The surface production rate can be estimated from scaling relationships for altitude (or atmosphere pressure) and geographic location (latitude and longitude), taking into account production pathway (from neutron spallation, capture of muons and fast muons) or irradiation geometry (Heisinger et al., 2002a, b; Masarik et al., 2000; Stone, 2000; Lal, 1991).

Radioactive decay is only a factor if erosion rates are low. For CN ¹⁰Be, radioactive decay can be negligible for erosion rates higher than 0.3 m/Myr (von Blanckenburg, 2005). This rule is complicated somewhat if erosion rates are variable across a catchment, as is the case with escarpments, as parts of the basin might exceed this limit.

Shielding of cosmic rays on an individual surface is a function of the surrounding topography on the skyline, as well as by local slope effects. Cosmic ray shielding generally reduces surface production rate $P_0(x, y)$ but extends the free path attenuation length because of the change of irradiation geometry (Dunne et al., 1999). DiBiase (2018) evaluated the counter effects of shielding on catchment-wide production rate (via spallation) and attenuation length, although he found that the combined shielding effect on surface production rate (via spallation) and free path attenuation length is negligible when the valley surface slope is less than 30° (DiBiase, 2018). In this study, we will not apply any shielding correction.

This conventional calculation of basin-averaged erosion rates from CNs concentrations is widely used in many geological studies and can be done using standard software algorithms (e.g., CRONUS) (Balco et al., 2008) to calculate the basin-averaged erosion rate.

2.3.2 Mass fluxes

DCN concentrations as expressed above can be thought of as representing a balance between two fluxes. The flux of cosmic rays into a catchment determines the total production in the basin as given by Eq. (4). With a steady state, this production is balanced by the export of the CNs within eroded sediment. The flux of sediment out of the basin determines the mass through which the CN is distributed and thus the concentration. Concentration can be expressed in terms of the total production over a time interval divided by the total volume of sediment produced over that time interval (von Blanckenburg, 2005):

$$C = \frac{M_{\rm c}}{V_{\rm rock}} = \frac{\iint_{S} \Lambda P_0(x, y) \, dx \, dy}{\iint_{S} e(x, y) \, dx \, dy},\tag{6}$$

where M_c is the total production of CN mass over the catchment with dimensions of moles/time, and $V_{\rm rock}$ is the volume of rock converted to sediment and exported from the catchment. This has dimensions of volume per time and can also be expressed as the integral of the erosion rate over the surface of the catchment, S. Erosion rate in this context can be regarded as a flux, as it is a volume of rock produced per square area per unit time.

This concept can be generalized if we think of the rock within the Earth as moving at a constant velocity, F_s , with respect to the surface. The flux of rock, V_{rock} , through the surface is the scalar (dot) product of the vector F_s and the vector normal to the Earth's surface, S:

$$V_{\text{rock}} = \boldsymbol{F}_{\text{s}} \cdot \boldsymbol{S},\tag{7}$$

If the vector F_s is vertical, we refer to F_s as erosion rate and the projected area of S as the catchment area, A, and we revert to Eq. (3). However, in general, there is no reason for F_s to be vertical. In particular, for the problem of escarpment retreat, the land surface might be better regarded as moving horizontally with respect to the underlying rock (Fig. 1). In this case, we can take F_s as horizontal, but the rock flux is

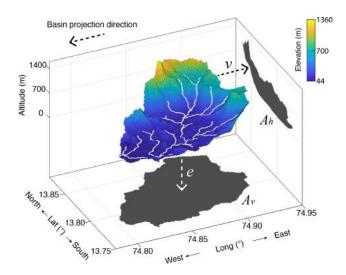


Figure 6. Depiction of the flux of mass through the surface of a drainage basin from the coastal escarpment of the Western Ghats, India. Basin position is indicated as basin D in Fig. 2. Spatial surface of drainage basin and its projection in the vertical and a horizontal direction. Projected areas are $A_{\rm V}$ and $A_{\rm h}$, respectively. Thick white lines denote channels extracted from the DEM for a minimum drainage area of 1 km².

still calculated from the scalar product of F_s and the normal to S. The general form of Eq. (6) for the rock velocity in any direction becomes

$$C = \frac{\iint_{S} \Lambda P_0(x, y) \, dx \, dy}{F_s \cdot S}.$$
 (8)

The concentration of a CN in sediment is still the ratio of the production of CN and the dilution into a flux of sediment, but the flux can be generated by a velocity in any direction, and requires that the catchment surface be projected into a plane normal to the direction of motion. For example, Fig. 6 shows a catchment surface together with its projection onto two planes, one horizontal and one vertical. The projection of the surface onto a horizontal plane produces a surface with an area of $A_{\rm v}$, which we would recognize as the usual catchment area, as calculated from a digital elevation model (DEM), for example, noting that this quantity is also a projection. The projection onto a vertical plane has a different shape and area, denoted as A_h . In either case, Eq. (8) holds and we could infer a velocity, F_s , from a CN concentration and the appropriately projected area. If we assume the velocity is vertical, F_s is equal to the conventional erosion rate, e. If we assume that $\boldsymbol{F}_{\mathrm{s}}$ is horizontal, we would infer a horizontal retreat rate of the landscape at a velocity, v (Fig. 6).

It is important to note that changing the assumed direction of the rock with respect to the surface does not change any of the basic physical processes. Production of a CN is unaffected as it is still produced within the same depth range, Λ , and is determined exclusively by the area, elevation and geometry of the catchment. Provided the assumption of steady

state holds, the total production over the catchment is equal to total export, and this calculation is independent of the direction of rock motion or the path of integration. A concentration measurement is thus constraining the flux of rock, and it is only convention that regards this flux as characteristic of a downward motion of the surface.

Escarpment retreat or other non-vertical motion of Earth's surface can be regarded as being simply a result of spatially variable surface lowering. To illustrate this point, consider the example shown in Fig. 7. A land surface is represented by a one-dimensional profile represented by an exponential function. This surface is back-cutting or retreating to the right, maintaining its form. That motion can be represented by a vertical erosion rate that is variable in space (Fig. 7b) or by a horizontal back-cutting at a constant rate, v (Fig. 7c). Each mathematical description results in the same change in the surface of the Earth with time, the same flux of rock, and the same catchment integrated concentration of detrital CNs. The physical erosion processes would be the same; rock is eroded and removed by gravity processes which operate downslope, and the path through the production zone would have the same vertical component with respect to the surface and so would produce the same surface concentration (Fig. 7d). By changing the assumed direction of the rock flux, we are simply characterizing the change in the land surface with a different metric. We characterize it in terms of a mean horizontal motion rather than as a mean vertical motion.

In two dimensions, the concept of horizontal motion of Earth's surface with respect to the underlying rock is somewhat more complicated. The complex geometry (Fig. 7e) of any catchment surface implies that there will never be perfect horizontal motion of that surface. Any given catchment has facets that dip in all directions (Fig. 7e), so pure, uniform, steady horizontal motion of a catchment is impossible. However, much as the catchment-averaged erosion rate is an average of a spatially variable quantity, the horizontal velocity can also be regarded as an average, where individual facets of the surface lower and retreat at different rates, but the net result can be characterized by an average horizontal velocity. For example, Fig. 7e shows a catchment from the Western Ghats draining the great escarpment. Although the drainage dips dominantly to the SW, there are both channel reaches and hillslopes that dip in all directions, including north or east. If erosion rates in this catchment are higher in the steep escarpment regions in the NE, individual slopes might retreat in any direction or not at all, but the catchment as a whole will expand to the NE, thereby "retreating" in this direction. The "average horizontal velocity" describes the regional motion of the surface by averaging all the individual slope changes. By parameterizing the problem in terms of a horizontal velocity of the surface with respect to its underlying rock, rather than a vertical erosion rate, we do not change any assumptions regarding geomorphic processes, or cosmogenic nuclide production and transport, but we do characterize the change in the landscape with a more representative metric. One important remaining assumption is that all points within the catchment are eroding fast enough that radioactive decay does not contribute significantly to secular equilibrium.

2.3.3 Mass flux in the horizontal direction

We assume that there is no distortion of the surface or rock and that the relative motion can be described as a single Euclidian vector without rotation. We present two methods for the calculation of mass flux and velocity from the measured detrital concentration and the catchment-wide nuclide production.

In the analysis above, we showed that the measured concentration of 10Be in a sediment reflects the total integrated production in mass/time in the upstream catchment, divided by the rate of conversion of rock by erosion into sediment, expressed as a rock mass flux. A measured 10Be concentration gives a unique value for the rock mass flux, but not for the direction of velocity of the rock with respect to the surface. For the escarpment problem, the flux can be converted to a velocity by assuming horizontal rock motion. The calculation of velocity must take into account the complex shape of the catchment as well as uncertainty regarding the azimuthal direction of the rock velocity. We need to convert mass flux to a velocity in the appropriate direction normal to the escarpment, using an area projected normal to that direction. We present two methods for doing the flux to velocity conversion here.

1. Basin projection method

Consider a representative escarpment-draining basin (e.g., the basin in Fig. 6); if the erosion is completely efficient along the escarpment face, the escarpment would form a planar surface retreating horizontally, leaving a flat featureless coastal plain. However, erosion is not completely efficient and although the channel profiles (Fig. 3) show most relief on the escarpment face, lateral variations are significant and catchments show considerable variability in morphology and, presumably, erosion rate. The assumption in the calculation of an average is that inefficiencies in escarpment erosion are balanced by the continued erosion of remnant topography between the escarpment and the coastline. During a unit time period, the mass of rock that is removed from the basin surface can be calculated from the retreat rate vand the area of the catchment projected onto a vertical plane. The retreat vector, \boldsymbol{v} , is normal to the vertical plane. Here, we use A_h to denote the projected area, and the conventional horizontal area is given as A_v (Fig. 6). For a given flux, V_{rock} , we have the following relationship:

$$eA_{\rm v} = vA_{\rm h} = V_{\rm rock}.\tag{9}$$

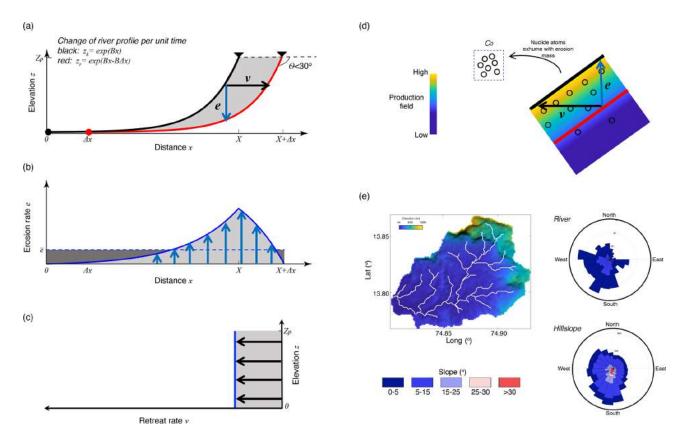


Figure 7. Relationship between mass flux through a surface and the velocity for a retreating escarpment. (a) Land surface, assumed to be exponential in form, retreating into a pre-existing highland at constant velocity, v. The surface lowering at any point is given as e. (b) Surface lowering rate as a function of distance. (c) Horizontal velocity as a function of elevation. Velocity is constant in both elevation and distance. Areas under the curves (light and dark gray) in panels (a), (b) and (c) represent the mass flux and are equal in all cases. (d) CN production zone below a dipping surface. Rock motion in either vertical or horizontal direction brings particles to the surface with an integrated production. For a constant flux, v and e scale so that the time of passage through the production zone is independent of direction, so surface concentration is independent of direction. (e) Elevation of a typical catchment in the Western Ghats with rose diagrams showing frequency and magnitude of slope with direction for channels (upper) and hillslopes (lower).

Equation (9) expresses the relationship between velocity direction and projected area. Projection of a DEM-based catchment surface onto a plane which is orthogonal to the projection direction gives a cluster of scattered points, including some that are identical in projected position. The projected area is given by the enclosed area of the outline that encloses these points on the projection plane.

2. Local scalar product method

As an alternative to full surface projection, we can also calculate the local surface projection. The dot product of the rock velocity and the catchment surface S in Eq. (8) can be calculated by the sum of the scalar product of all elemental surfaces with the mass flux vector:

$$F_{s} \cdot S \approx \sum_{k} F_{s} \cdot n_{k} A_{k} = |F_{s}| \sum_{k} \frac{F_{s}}{|F_{s}|} \cdot n_{k} A_{k},$$
 (10)

where n_k and A_k are the unit normal and the surface area of an elemental surface k in the catchment surface

S. Equation (10) states that the volume of eroded rock is the sum of the scalar product of elemental surfaces with the mass flux vector, and equivalently, a sum of local mass flux from elemental surfaces (Fig. 8). The effective area is calculated from the sum of the scalar product of the unit vector in the direction of $F_{\rm s}$ and elemental surfaces (Eq. 10).

To put this method into practice, we discretize the basin surface into triangular elemental surfaces. The three vertexes of a triangular surface are $\{xi, yi, zi\}_{i=1,2,3}$, which define three vectors in space. The normal of the elemental surface $(n_k \text{ in Eq. } 10)$ is the vector that is normal to the three vectors. This represents the normal to the planar facet connecting three points. The area of this facet is projected onto the plane normal to the flux vector, and this projected area is used for the flux.

With a complex catchment surface and a horizontal velocity, there are many local surfaces which dip towards the direction of rock motion, which implies a local

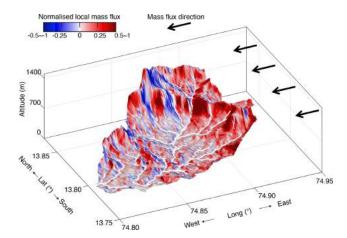


Figure 8. Local mass flux of elemental surfaces of an escarpment-draining basin in the Western Ghats. Basin location is indicated as basin D in Fig. 2 and is also shown in Fig. 6. The basin surface is discretized into elemental surfaces and color-coded with the relative magnitude of the local mass flux for a horizontal rock velocity in the direction indicated. Flux is normalized to the catchment-averaged mass flux. Thick white lines are channels extracted from the DEM for a minimum drainage area of 1 km².

scalar product and a local mass flux $F_s \cdot (n_k A_k)$ that are negative (blue values in Fig. 8). These local negative values do not imply negative mass flux but rather represent the multiple times that a vector in one direction can cross the surface, S. Any local topographic high or transverse valley implies multiple intersections of a vector with the surface, so any negative dot product is compensated for by the multiple positive values.

In both the basin projection and local scalar product methods, it is necessary to select a direction for the velocity or mass flux vector. For the escarpment retreat problem, we can assume that this direction is purely horizontal but with an unknown azimuth. It is practical to sweep through a range of horizontal directions to determine the range of velocities associated with a range of directions. We pick channels that drain through the escarpment but do not appear to be recent captures and take the orientations of these channel segments as an estimate of the potential range of escarpment retreat directions. We then sweep through all possible azimuths within this range. This is visualized by plotting the resulting vector magnitudes as a function of directional azimuth.

An example of the calculation of horizontal retreat rate from ¹⁰Be concentration using each of these methods is shown in Fig. 9. The example basin is from the Western Ghats with ¹⁰Be data published by Mandal et al. (2015). In each case, we test a range of azimuths from N20W to N85E. Inferred horizontal velocities range from 180 to 380 m/Myr, depending on azimuth.

The local scalar product method has the characteristic that the inferred velocity increases rapidly as the direction rotates towards parallel with the dominant catchment flow direction. This is an artifact of the ability of a scalar product to take negative values. A typical catchment has a bowl-shaped geometry, open at the outlet, but as the basin is rotated, the horizontal view eventually sees only the side of the bowl, and with further rotation, would provide a view of only the back of the basin. Through this rotation, the effective area thus goes to zero or even negative, so that the flux goes to infinity for these orientations.

3 Applications and verification

As a demonstration as to how CN data can be used to constrain the geomorphic evolution of a great escarpment, we use the cosmogenic ¹⁰Be data reported by Mandal et al. (2015) combined with our geomorphic analysis and proposed method of analysis in terms of horizontal flux including the basin illustrated in Sect. 2.3 as well as the remaining basins in the Mandal et al. (2015) study. We have reprocessed the data of Mandal et al. (2015) for internal consistency, following the method and scaling relationships used in the method of Lupker et al. (2012) where the cosmogenic production rate is calculated in a pixel-wise manner. Conventional erosion rates are also recalculated from the published DCN concentrations following the method of Lupker et al. (2012).

Mandal et al. (2015) report an average erosion rate of all escarpment-draining basins in the southern Western Ghats to be 48.6 ± 20.9 m/Myr, which is low but can be contrasted to the even lower erosion rates on the plateau to the east (\sim 10 m/Myr). The reported differential erosion rates, as well as the differential steepness across the continental drainage divide, should drive the water divide migration towards the plateau (Mandal et al., 2015).

We evaluated all catchments draining the escarpment for which there are reported detrital ¹⁰Be data (Fig. 2). Each catchment was evaluated using each of the two methods described above; the results are given in Fig. 10 and are summarized in Tables 1 and 2. In all cases, catchments with erosion rates on the order of tens of meters per million years transform into horizontal retreat rates of several hundred meters or a few kilometers per million years.

The two methods yield broadly consistent results (Table 2, Fig. 10). However, the local scalar product method is much more sensitive to azimuth. It always shows a distinct minimum value of velocity, but velocity increases rapidly for other azimuths of velocity. For oddly shaped basins or for flux azimuths oblique to the dominant river direction, there is a strong influence of the negative values from the sides of a basin, and inferred velocities become large and deviate from those obtained from the basin projection method.

The basin geometry can play a large role in the inferred retreat rate. Basin (a1) in Fig. 11 shows an almost symmetrical basin, with a clear flow direction. The retreat rate is between

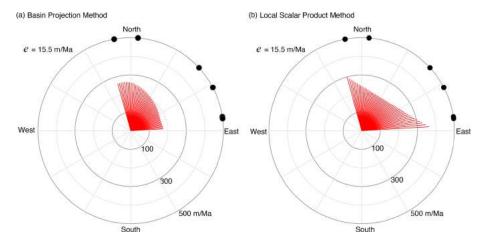


Figure 9. Escarpment retreat rate as a function of azimuth of a horizontal mass flux vector using (a) the basin projection method; (b) the local scalar product method. The basin is from the Western Ghats with location indicated as basin D in Fig. 2. Measured ¹⁰Be concentration is 172 426 (±8125) atoms/g and corresponds to a mean vertical erosion rate of 15.5 m/Myr. The azimuth of the tangential red lines denotes the assumed escarpment retreat direction, and the length of the radial vector is the consequent retreat rate for that direction and the measured ¹⁰Be concentration. Black dots are orientations of characteristic tributaries of the escarpment-draining channels of this basin.

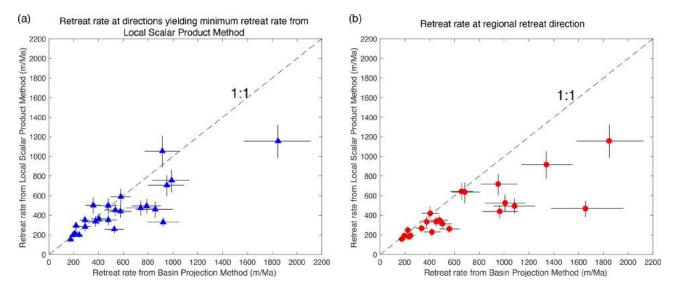


Figure 10. Comparison of retreat rates from the basin projection method and the local scalar product method applied to the data from the Western Ghats escarpment of India. (a) Retreat rates for retreat directions that yield minimum retreat rate from the local scalar product method. Note that direction varies between basins. (b) Rates determined using a constant retreat direction for all basins (N57E).

500 and 600 m/Myr and only weakly dependent on azimuth for the basin projection method. The local scalar product method gives a similar result for the most likely retreat direction of N80E but deviates quickly for other azimuths. In particular, a more northerly azimuth gives very high retreat rates, because high topography on the south margin of the basin provides many negative pixels, reducing the projected area and thus increasing the flux. Basin (c1) in Fig. 11 is strongly asymmetric, with high topography (above \sim 800 m) in the NE. Here, the escarpment is clearly normal to the flow direction of the escarpment rivers (\sim N30E). The basin projection method gives retreat rates between 500 and 600 m/Myr, with

a small variance over the likely range of azimuth. Similar to basin (a1), the higher topography on the plateau (above $\sim 2000\,\mathrm{m}$) provides many negative pixels, leading to high estimated velocities at northeastward azimuths. In Fig. 11, basin (b1) is extremely asymmetric. Retreat rates from the basin projection method are however only weakly dependent on azimuth, suggesting a mean retreat rate of $\sim 1100\,\mathrm{m/Myr}$. The plateau is flat, although the shape is asymmetric; thus, its projected area is small for any azimuth using the basin projection method. The local scalar product method gives much larger retreat rates. Retreat direction of the escarpment is difficult to estimate from the flow directions as there are two

major escarpment valleys oriented obliquely to each other. Surfaces of the four valley flanks intermittently give negative fluxes through rotation of various directions, leading to larger variability but generally larger retreat rates.

In order to compare basins within the Western Ghats, we selected a common retreat direction and calculated retreat rates for all basins in this direction. We selected a direction that is normal to the regional coastline, which is estimated to be trending at N158W. Escarpment retreat rates calculated from both methods vary from 171 m/Myr to 2427 m/Myr and are shown in map view in Fig. 12.

The average value of the retreat rates is close to the retreat rate expected from steady retreat of the escarpment from the coast to its present location since the time of rifting of the margin (Fig. 13). The age of rifting of India from Madagascar is constrained to be between 120 and 100 Ma (Thompson et al., 2019). The important event for the formation of the escarpment is the initial continental rifting that would have formed the new water divides at the crest of escarpments on each margin, so an earlier age is more likely. This event might have even predated other indications of rifting. The majority of retreat rates from ¹⁰Be are lower than the post-rift average, although there are examples of higher rates. The lower rates suggest that the escarpment retreat rate may have been higher in the early post-rift period. Alternatively, the retreat rate might have fluctuated in response to capture of rivers on the plateau surface, so that most observations are of a slower, background retreat rate that is periodically punctuated by more rapid retreat as a portion of the plateau area is captured. There is also significant spatial variation, and this variation co-varies with the shape of the escarpment creating a correlation between the retreat rate and the distance to the coastline (Fig. 13). For example, the large embayment at 13N latitude corresponds to the highest modern retreat rates. This suggests that the modern rates have been sustained since the time of rifting and variations reflect long-lived characteristics of the escarpment or the retreat processes.

We also investigated the relationship between channel steepness of escarpment reaches, escarpment elevation and escarpment retreat rate (Figs. 14 and 15). Steepness is correlated with relief or total height of the escarpment (Fig. 14). Such a relationship was predicted by Willett et al. (2018) for escarpments retreating at a constant velocity; steepness would need to increase with height in order to maintain the higher velocity associated with higher remnant topography. We also plot the predicted relationship between steepness and retreat rate from Eq. (2) for two values of slope exponent, n, and erodibility, K (Fig. 15). A range of K would be necessary to explain the full scatter, but it is also possible that some of the scatter is associated with plateau river capture and transience in the river profiles.

4 Discussion

4.1 Correction for flexural isostatic rebound on ¹⁰Be-inferred retreat rate

One effect not accounted for in our horizontal flux calculation is the vertical uplift and flux that results from flexural compensation of the mass eroded from the escarpment face. Retreat of the escarpment generates a flexural isostatic uplift centered at the escarpment front but spread over a distance that encompasses the nearby plateau and lowland coastal plain. Approximately half of the flexural uplift occurs on the plateau side of the escarpment. This uplift is manifested as surface uplift, not exhumation, and therefore raises the height of the plateau edge above where it would be in the absence of an isostatic response. This increase in the height of the escarpment is accounted for in the projected basin area and thus is accounted for in the horizontal retreat calculation (Fig. 16a). However, uplift of the coastal plain is not part of the horizontal retreat calculations and if this uplift is eroded, it represents a vertical component to the erosional flux that we have not accounted for. Not accounting for this eroded mass implies that we have overestimated escarpment retreat rates, so we assess how large this effect is here.

The flexural uplift rate due to escarpment erosion can be quantified with the isostatic deflection of a simple line load centered on the escarpment. The magnitude of the line load is expressed as

$$N_0 = v \Delta t \Delta y H g \rho_{\text{crust}}, \tag{11}$$

where N_0 is the load and is a function of the escarpment height, H, and the retreat rate, v (Fig. 15a). As we are interested in the velocity, not the cumulative uplift, this is done for a small time, Δt and along-strike unit width of the escarpment, Δy . The density of eroded rock is given by ρ_{crust} . The deflection of this line load is given by (Turcotte and Schubert, 2002)

$$w(x) = w_{\text{max}} \exp\left(-\frac{x}{\alpha}\right) \left(\cos\left(\frac{x}{\alpha}\right) + \sin\left(\frac{x}{\alpha}\right)\right),$$
 (12)

where $w_{\rm max}$ the is the maximum deflection uplift, α is the characteristic wavelength of flexural deflection, given as

$$w_{\text{max}} = \frac{N_0}{2} \cdot \frac{1}{\Delta \rho g \alpha} = \frac{v \Delta t \Delta y H g \rho_{\text{crust}}}{2} \cdot \frac{1}{\Delta \rho g \alpha}$$
$$= \frac{v \Delta t \Delta y H \rho_{\text{crust}}}{2 \Delta \rho \alpha},$$
$$\alpha = \left\{ \frac{4D}{\Delta \rho g} \right\}^{1/4}, \tag{13}$$

where $\Delta \rho$ is the density contrast between mantle and air; and D is the flexural rigidity (Turcotte and Schubert, 2002):

$$D = \frac{ET_{\rm e}^3}{12(1-\zeta^2)},\tag{14}$$

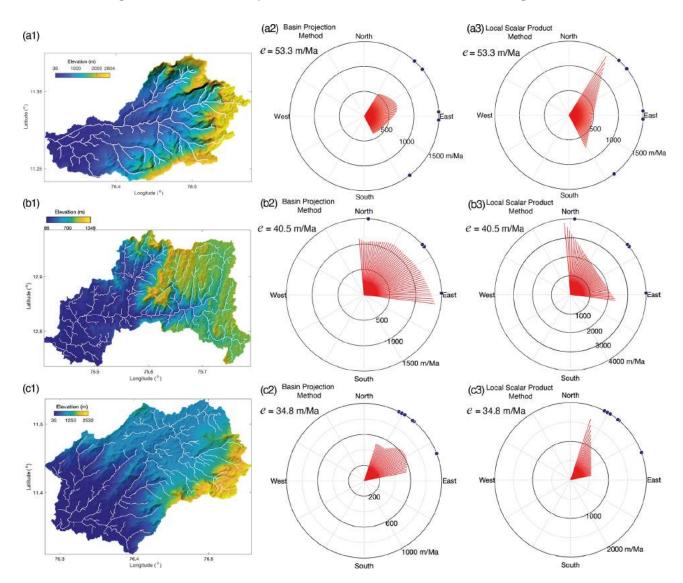


Figure 11. Example basins from the Western Ghats showing the retreat rate as a function of azimuth of a horizontal mass flux vector using (a2, b2, c2) the basin projection method; (a3, b3, c3) the local scalar product method. The azimuth of the red lines denotes the assumed escarpment retreat direction, and the length of the radial vector is the consequent retreat rate for that direction and the measured ¹⁰Be concentration. Black dots are orientations of characteristic tributaries of the escarpment-draining channels of this basin.

where ζ is Poisson's ratio, E is Young's modulus, and $T_{\rm e}$ is the effective elastic thickness that characterizes the lithosphere rigidity.

The effect on our calculations depends on the uplift between the escarpment and the point at which a DCN sample is taken. In Fig. 16b, we show this at the coast, but in practice this will be closer to the escarpment. Assuming complete erosion of uplifted rock, isostatic uplift results in a mass flux through the surface. Mass flux is obtained by integrating the uplift from the escarpment to the sample point at X_s , giving

$$\int_{0}^{X_{s}} w dx = w_{\max} \int_{0}^{X_{s}} \exp\left(-\frac{x}{\alpha}\right) \cdot \left[\cos\left(\frac{x}{\alpha}\right) + \sin\left(\frac{x}{\alpha}\right)\right] dx.$$

Solving this gives the mass flux of eroded material:

$$F_{\text{uplift}} = -\alpha w_{\text{max}} \left(\exp\left(-\frac{X_{\text{s}}}{\alpha}\right) \cos\left(\frac{X_{\text{s}}}{\alpha}\right) - 1 \right). \tag{16}$$

The escarpment retreat implies a mass flux of erosion:

$$F_{\text{retreat}} = v \Delta t H \Delta y. \tag{17}$$

The missing flux due to flexural uplift can be quantified by the ratio of the uplifted mass flux to the retreat mass flux:

$$R_{\rm F} = \frac{F_{\rm uplift}}{F_{\rm retreat}} = \frac{\rho_{\rm crust}}{2\rho_{\rm mantle}} \cdot \left(\exp\left(-\frac{X_s}{\alpha}\right)\cos\left(\frac{X_s}{\alpha}\right) - 1\right). \quad (18)$$

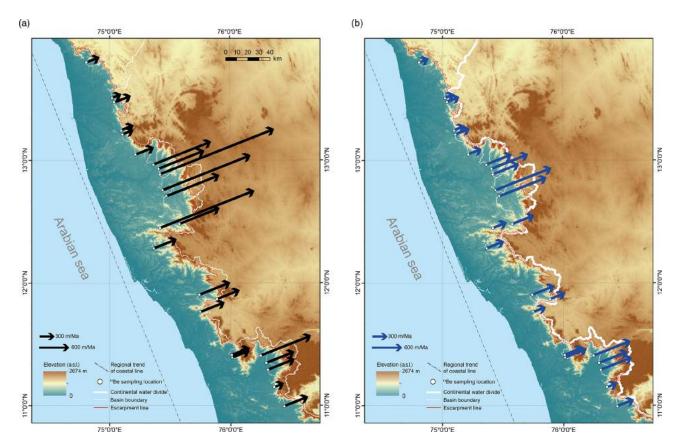


Figure 12. Escarpment retreat rates in the normal direction of the reference coastal line on the topography base map of the southern Western Ghats. Topography is from SRTM 90 m DEM (Jarvis et al., 2008). Rates from **(a)** the local scalar product method and **(b)** from the basin projection method. Arrows represent the escarpment retreat vector: the azimuth denotes the retreat direction while the length denotes the retreat rate in that direction. The dashed black line indicates the trend of the modern coastline and escarpment.

The density contrast between mantle and the upper crust can be constrained to a range of 0.78–0.92 with an average ratio of 0.85 at global scale (Tenzer et al., 2012).

Figure 16b shows the flux ratio $R_{\rm F}$ for a range of $X_{\rm S}$ and the effective elastic thickness at a density contrast of 0.85 between upper crust and mantle. The eroded flux ratio $R_{\rm F}$ decreases as the effective elastic thickness of the lithosphere increases. At a mature passive margin, the lithosphere effective elastic thickness, $T_{\rm e}$, is typically a few tens of kilometers (Audet and Bürgmann, 2011). For the Western Ghats data, most samples are within 20 km of the center of the escarpment (Fig. 3). At a $T_e = 20 \,\mathrm{km}$, the mass flux ratio R_F is below 15 % for $X_s = 20 \,\mathrm{km}$ (Fig. 15b). At the Western Ghats, the DCN ¹⁰Be sampling location is close to the escarpment with variable X_s . The mass flux ratio R_F of the escarpment basins is in the range of 1.7 %–18.5 %, but most of the basins are below 10 % (Table 2). This error is partially offset by the rock uplift that establishes the coastal plain slope, which for this calculation, we assume is flat.

4.2 Methods for converting flux to velocity

The calculation of a horizontal escarpment retreat rate is based on recognition that the concentration of ¹⁰Be in a detrital sediment is proportional to a flux of rock from the Earth, regardless of direction or spatial variation of local flux. Cosmogenic ¹⁰Be concentration provides a measure of the flux of rock from the earth, but this need not be an erosion rate in the sense of a vertical velocity. Measurement of the surface area, projected onto a horizontal plane, can be used to convert the flux into a vertical velocity, which is defined to be the erosion rate, which is what is done in a conventional analysis. The calculation of a horizontal retreat rate is an identical process. A direction must be selected and the surface of the catchment projected onto a plane perpendicular to this direction. The horizontal retreat rate depends on the effective area of a basin in the migration direction. We present two methods to calculate the effective area. The basin projection method calculates the projected area of the overall basin surface onto a vertical plane and the local scalar product method calculates the effective area by summation of the dot product of local elemental surface normal with the velocity. If an escarpment were a perfect uniform plane, these methods would

Table 1. Cosmogenic ¹⁰Be basins of Western Ghats studied in this research.

Published	Lat. (°)	Long. (°)	DCN ¹⁰ Be concentration	Escarpment	Mean slope	Steepness	Slope > 30°	Recalc	ulated ero	osion rate (m/Myr) ^f
basin ^a			(atoms/g) ^b	elevation (m)	(°) ^c	$(m^{0.84})^d$	(%) ^e	Rate	34 %	-34 %
SIN1440	13.7960	74.8034	172426 ± 8125	827	12	34.5	6	15.53	2.35	2.31
SIN1380	13.5069	75.0212	133454 ± 9211	704	13	34.8	7	20.35	3.14	3.23
SIN1435	13.2432	75.0966	102250 ± 5223	909	16	45.2	8	29.5	4.23	4.27
SIN1433	13.2100	75.1062	90233 ± 5261	995	12	44.5	4	31.15	4.49	4.94
SIN1432	13.0480	75.2141	70145 ± 4074	1285	14	52.5	7	45.38	6.2	6.7
SIN1369	12.9638	75.3649	77251 ± 6585	1178	12	53	6	37.14	5.93	6.08
SIN1368	12.9295	75.4067	70502 ± 5028	1226	13	59.8	4	43.42	6.28	6.99
SIN1367	12.8833	75.4181	73573 ± 8296.5	1178	15	52.6	9	41.21	6.89	7.61
SIN1362	12.7566	75.4401	80104 ± 5184	1093	11	55.8	4	40.46	5.77	6.05
SIN1361	12.7098	75.4695	90315 ± 6672	1002	12	54.1	4	32.81	4.93	5.16
SIN1430	12.4804	75.5794	69430 ± 5001	1200	16	53.5	6	49.82	7.15	7.7
SIN1427	12.4466	75.4186	94374 ± 5389	1100	18	52.8	4	36.95	5.16	5.21
SIN1429	12.2815	75.3675	97093 ± 4932	1158	18	59.6	8	31.1	4.47	4.48
SIN1419	11.9043	75.7418	106563 ± 6034	1043	12	52.3	3	24.43	3.83	3.72
SIN1421	11.8677	75.8892	107228 ± 5571	784	17	34.7	13	32.5	4.52	4.6
SIN1416	11.7651	75.7500	109089 ± 6025	920	20	49.7	16	28.48	4.01	4.26
SIN1350	11.4120	76.0106	74345 ± 6593	1512	15	83.6	12	42.31	6.55	7.05
SIN1351	11.3913	76.0130	71843 ± 8383	1234	21	89.5	24	53.75	8.81	9.37
SIN1331	11.4070	76.2507	82246 ± 7018	1194	15	70.7	9	44.77	6.47	7.22
SIN1332	11.3473	76.2947	110089 ± 7370	1513	13	58.5	6	34.77	4.78	4.89
SIN1330	11.2890	76.3074	86695 ± 9867	2405	20	101.8	27	53.32	8.05	9.4
SIN1407	11.1503	76.3591	84821 ± 4828	1238	21	74.1	20	36.79	5.18	5.37
SIN1348	10.9917	76.4440	84696 ± 7081	1480	18	66.7	15	49.79	7.05	7.63
SIN1379	13.4731	75.0358	198955 ± 18234	848	14	40.8	7	15.19	2.41	2.59

^a Basin name is from the published DCN ¹⁰Be sample name in Mandal et al. (2015). ^b DCN ¹⁰Be concentration data are from Mandal et al. (2015). ^c Slope is calculated from MATLAB surfnorm function of surface pixels. ^d Steepness is calculated from slope-area plots with a uniform concavity of 0.42. ^c For the percentage of surface pixels steeper than 30°, the slope is calculated from MATLAB surfnorm function of surface pixels. ^f For internal consistency, conventional erosion rates are recalculated from reported ¹⁰Be concentrations following method of Lupker et al. (2012). The uncertainties of ±34% are propagated from the measured error of ¹⁰Be concentration.

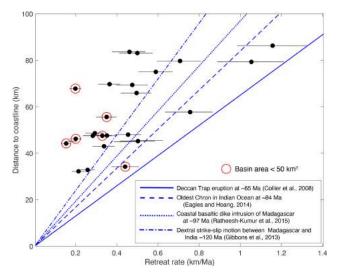


Figure 13. Current distance from the coastline against inferred retreat rate of the Western Ghats escarpment basins from detrital $^{10}\mathrm{Be}$ concentrations with 1σ uncertainty. Retreat rates of the escarpment are calculated using the basin projection method with azimuth taken as N57E. See Table 2 for the data. Age of rifting is constrained by various events as indicated and is expected to be older than these constraints. Basins smaller than $50\,\mathrm{km}^2$ are indicated with open red circles.

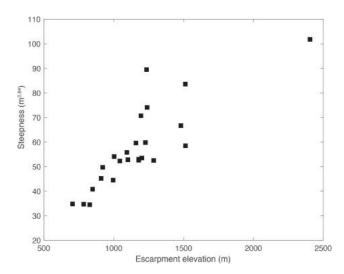


Figure 14. Relationship between channel steepness and escarpment height in the Western Ghats. The channel steepness is calculated from slope—area plots using a uniform concavity of 0.42. Correlation is consistent with the theory that morphology has evolved to erode pre-existing topography at a constant rate of retreat. See Table 1 for the data.

Table 2. ¹⁰Be-inferred escarpment retreat rates of Western Ghats, India.

busin (4m) ³ Local scalar product method Basin projection method Direction Local scalar product method Basin projection method Direction Direction Direction Rate 34% -234% Rate 34% -34% Rate	Published	Distance	R.	etreat rate of re rate from local	e of retreat n local scal	Retreat rate of retreat directions yielding minimum rate from local scalar product method (m/Myr)	elding n ethod (m	ninimum ı/Myr)			Retn	eat rate of retreat dir	Retreat rate of regional escarpment retreat direction (m/Myr)	carpment fyr)			$R_{ m F}$
32.2 31 Rade 34% Rade 34% -34%	basin	(km) ^a	Direction ^b		scalar prod	luct method	Basin	projection	n method	Direction ^b	Local sc	alar produ	ct method	Basin I	projection	method	(%) _c
32.2 31 210 32 31 32 32 32 33 35 35 35 35 36 182 28 27 444.2 53 174 27 28 153 24 24 35 24 35 24 35 34 46 46 37 245 35 35 35 36 48 48 46 57 243 35 36 48 46 57 245 35 36 38 36 48 57 144 57 243 35 36 48 57 144 46 46 77 48 57 149 46 49 57 33 48 46 47 46 77 48 46 77 48 46 77 48 46 77 48 46 77 48 48 46 77 48 48 48 48 48					34 %		Rate	34%	34		Rate	34%		Rate	34 %	-34%	
44.2 53 174 27 28 153 24 24 57 175 27 28 158 24 26 57 175 27 28 158 24 28 48.6 68 218 13 35 20 42 46 57 223 35 28 28 39 55.6 19 20 40 42 35 46 46 49 28 37 40 69.4 11 20 40 49 35 46 46 49 57 149 46 49 46 49	SIN1440	32.2	31	210	32	31	213	32	32	57	233	35	35	182	28	27	8.0
46.2 51 24.3 3.5 3.5 200 2.9 2.9 57 24.5 3.5 3.6 4.9 2.9 4.9 4.5 3.5 3.5 4.9 <td>SIN1380</td> <td>44.2</td> <td>53</td> <td>174</td> <td>27</td> <td>28</td> <td>153</td> <td>24</td> <td>24</td> <td>57</td> <td>175</td> <td>27</td> <td>28</td> <td>158</td> <td>24</td> <td>25</td> <td>4.1</td>	SIN1380	44.2	53	174	27	28	153	24	24	57	175	27	28	158	24	25	4.1
48.6 68 218 31 35 42 46 57 223 32 35 48 46 57 223 32 35 48 46 46 49 26 37 48 46 46 49 26 37 49 46 49 35 48 57 374 46 49 36 37 40 <	SIN1435	46.2	51	243	35	35	200	50	53	57	245	35	35	194	28	28	2.9
55.6 19 290 40 43 350 48 52 334 46 49 268 37 40 69.4 14 73 118 121 474 76 78 57 107 161 165 526 84 86 99.4 14 138 151 147 76 173 118 156 138 161 166 87 1007 161 165 178 166 84 86 86.3 55 148 263 27 165 179 306 469 78 179 168 179 179 179 189 179	SIN1433	48.6	89	218	31	35	293	42	46	57	223	32	35	248	36	39	3.2
694 14 739 118 121 474 76 78 57 1007 161 165 526 84 86 797 354 359 118 123 474 76 114 57 952 138 153 718 104 116 117 165 113 165 118 116 116 173 165 178 169 178 116 117 165 117 165 173 165 178 176 118 176 165 178 167 178 167 178 179 167 178 179 178 179 178 179 178 179 178 179 178 179 178 179 178 179 178 179 178 179 178 179 178 179 178 179 178 179 179 178 179 179 179 179 179	SIN1432	55.6	19	290	40	43	350	48	52	57	334	46	49	268	37	40	4.4
79.7 54 951 138 153 707 102 114 57 952 138 153 718 104 116 83.6 359 857 143 158 461 77 85 277 306 469 78 87 86.3 57 144 163 115 165 173 164 178 168 178 169 78 179 178 178 179 178 178 179 178 179 178 179 178 179 178 179 178 179 178 179 179 179	SIN1369	69.4	14	739	118	121	474	92	78	57	1007	161	165	526	84	98	13.9
83.6 359 857 143 158 461 77 85 57 1655 277 306 469 78 87 86.3 55 1847 263 276 1157 165 173 154 263 276 1158 165 173 1847 263 276 1158 165 173 1847 263 276 1158 165 173 173 173 173 173 173 174 173 174 </td <td>SIN1368</td> <td>79.7</td> <td>54</td> <td>951</td> <td>138</td> <td>153</td> <td>707</td> <td>102</td> <td>114</td> <td>57</td> <td>952</td> <td>138</td> <td>153</td> <td>718</td> <td>104</td> <td>116</td> <td>12.5</td>	SIN1368	79.7	54	951	138	153	707	102	114	57	952	138	153	718	104	116	12.5
86.3 57 1847 263 276 1157 165 173 67 1847 263 276 1158 165 173 1847 263 276 1158 165 173 184 165 173 184 165 173 184 167 188 170 189 170 189 174 173 174 174 175 174 261 271 174 173 174 174 174 174 174 174 261 271 271 474 475 475 475 474 64 64 64 67 676 972 982 471 474 475 <td>SIN1367</td> <td>83.6</td> <td>359</td> <td>857</td> <td>143</td> <td>158</td> <td>461</td> <td>77</td> <td>82</td> <td>57</td> <td>1655</td> <td>277</td> <td>306</td> <td>469</td> <td>78</td> <td>87</td> <td>12.4</td>	SIN1367	83.6	359	857	143	158	461	77	82	57	1655	277	306	469	78	87	12.4
79.3 104 914 137 144 1654 158 166 57 1340 201 211 917 138 144 48 148 138 113 122 496 71 77 57 964 138 149 440 63 68 48 143 535 75 476 644 64	SIN1362	86.3	57	1847	263	276	1157	165	173	57	1847	263	276	1158	165	173	17.6
65.9 93 788 113 122 496 71 77 57 964 138 149 440 63 68 48 143 535 75 75 6964 972 982 291 41 41 47.6 59 478 69 69 57 478 69 69 350 50 50 50 34.2 72 478 69 69 57 478 69 69 50	SIN1361	79.3	104	914	137	144	1054	158	166	57	1340	201	211	917	138	144	18.5
48 143 535 75 454 64 64 64 64 64 64 64 64 67 6964 972 982 291 41 41 47.6 59 478 69 69 67 478 69 69 57 478 69 69 50	SIN1430	62.9	93	788	113	122	496	71	11	57	964	138	149	440	63	89	4.1
47.6 59 478 69 69 47.8 69 69 47.8 47.8 69 69 67 47.8 69 69 67 47.8 69 69 67 47.8 69 69 67 47.8 69 67 57 47.8 69 67 57 47.8 69 49 77 75 47.9 77 75 77 77 77 77 77 77 77 77 77 77 77 78 80	SIN1427	48	143	535	75	75	454	64	2	57	6964	972	982	291	41	41	2.4
34.2 76 90 88 440 69 67 57 1083 170 165 494 77 75 47.5 132 921 128 130 329 46 47 57 503 70 71 313 44 44 32.8 76 52 46 47 57 58 62 38 57 78 83 50 44 <td>SIN1429</td> <td>47.6</td> <td>59</td> <td>478</td> <td>69</td> <td>69</td> <td>352</td> <td>51</td> <td>51</td> <td>57</td> <td>478</td> <td>69</td> <td>69</td> <td>350</td> <td>20</td> <td>20</td> <td>9.2</td>	SIN1429	47.6	59	478	69	69	352	51	51	57	478	69	69	350	20	20	9.2
47.5 132 921 128 130 329 46 47 57 503 70 71 313 44 44 32.8 76 527 74 79 258 36 39 57 57 78 83 261 37 39 43.2 86 35 52 56 57 375 58 62 33 52 56 45.2 86 35 62 88 57 404 66 70 421 69 73 57.7 272 989 143 160 756 109 122 57 404 66 70 421 69 73 57.7 272 88 57 656 90 92 643 89 90 83.1 103 27 28 193 27 28 192 27 28 69.7 30 42 52 <td>SIN1419</td> <td>34.2</td> <td>72</td> <td>576</td> <td>06</td> <td>88</td> <td>440</td> <td>69</td> <td>19</td> <td>57</td> <td>1083</td> <td>170</td> <td>165</td> <td>494</td> <td>77</td> <td>75</td> <td>4.8</td>	SIN1419	34.2	72	576	06	88	440	69	19	57	1083	170	165	494	77	75	4.8
32.8 76 527 74 79 258 36 39 57 557 78 83 261 37 39 43. 58 58 58 56 57 57 58 62 56 57 57 58 62 57 57 404 66 70 421 69 73 56 57 57 404 66 70 421 69 73 56 57 404 66 70 421 69 73 56 73 57 404 66 70 421 69 73 56 73 57 404 66 70 421 69 73 42 57 404 66 70 421 69 73 42 58 73 48 59 73 88 74 88 74 88 74 88 74 88 74 74 74 74 74 <td>SIN1421</td> <td>47.5</td> <td>132</td> <td>921</td> <td>128</td> <td>130</td> <td>329</td> <td>46</td> <td>47</td> <td>57</td> <td>503</td> <td>70</td> <td>71</td> <td>313</td> <td>4</td> <td>44</td> <td>1.7</td>	SIN1421	47.5	132	921	128	130	329	46	47	57	503	70	71	313	4	44	1.7
43 58 375 58 62 38 52 56 57 375 58 62 333 52 56 45.2 86 358 59 62 82 88 57 404 66 70 421 69 73 57.7 272 989 143 160 122 57 -1208 195 175 84 94 73 83.1 103 478 72 84 499 75 83 103 120 83 90 83.1 103 27 28 88 57 683 103 122 89 90 67.8 67.8 193 27 28 29 57 451 64 69 90	SIN1416	32.8	92	527	74	79	258	36	39	57	557	78	83	261	37	39	2.3
45.2 86 358 59 62 82 88 57 404 66 70 421 69 73 57.7 272 989 143 160 756 109 122 57 -1208 195 175 581 84 94 75 72 579 80 82 589 81 83 57 656 90 92 643 88 90 83.1 103 478 72 84 499 75 88 57 683 103 120 636 90 91 112 67.8 63 193 27 28 195 27 28 192 27 28 14 52 56 57 451 64 69 37 48 52 58 54 48 52 58 41 66 71 20 39 39 39 39 39 39	SIN1350	43	58	375	28	62	338	52	26	57	375	28	62	333	52	99	5.6
57.7 272 989 143 160 756 109 122 57 -1208 195 175 581 84 94 75 72 579 80 82 589 81 83 57 656 90 92 643 88 90 83.1 103 478 72 84 499 75 88 57 683 103 120 636 90 112 67.8 67.8 63 28 28 29 57 195 27 28 112 69.7 30 402 57 62 57 451 64 69 37 48 52 47.5 102 292 46 50 283 45 48 57 417 66 71 230 36 39	SIN1351	45.2	98	358	59	62	502	82	88	57	404	99	70	421	69	73	6.4
75 72 579 80 82 589 81 83 57 656 90 92 643 88 90 83.1 103 478 72 84 499 75 88 57 683 103 120 636 96 112 67.8 63.1 193 27 28 198 28 29 57 195 27 28 192 27 28 69.7 30 402 57 62 364 52 56 57 451 64 69 37 48 52 47.5 102 292 46 50 283 45 48 57 417 66 71 230 36 39	SIN1331	57.7	272	686	143	160	756	109	122	57	-1208	195	175	581	84	94	6.3
83.1 103 478 72 84 499 75 88 57 683 103 120 636 96 112 67.8 63.8 63 40 57 28 195 27 28 192 27 28 69.7 30 402 57 62 364 52 56 57 451 64 69 337 48 52 47.5 102 292 46 50 283 45 48 57 417 66 71 230 36 39	SIN1332	75	72	579	80	82	589	81	83	57	959	90	92	643	88	06	9.2
67.8 63 193 27 28 194 28 29 57 195 27 28 192 27 28 69.7 30 402 57 62 364 52 56 57 451 64 69 337 48 52 47.5 102 292 46 50 283 45 48 57 417 66 71 230 36 39	SIN1330	83.1	103	478	72	8	499	75	88	57	683	103	120	989	96	112	10.1
69.7 30 402 57 62 364 52 56 57 451 64 69 337 48 52 47.5 102 292 46 50 283 45 48 57 417 66 71 230 36 39	SIN1407	67.8	63	193	27	28	198	28	53	57	195	27	28	192	27	28	2.5
, 47.5 102 292 46 50 283 45 48 57 417 66 71 230 36 39	SIN1348	69.7	30	402	27	62	364	52	99	57	451	64	69	337	48	52	5.4
	SIN1379	47.5	102	292	46	20	283	45	48	57	417	99	71	230	36	39	5.9

^a Distance is calculated using a reference retreating direction that is perpendicular to the regional escarpment. ^b The angle is defined as clockwise from the geographic north (0°). ^c The mass flux ratio in Eq. (18) for a density ratio of 0.85 and effective elastic thickness $T_6 = 20 \,\mathrm{km}$.

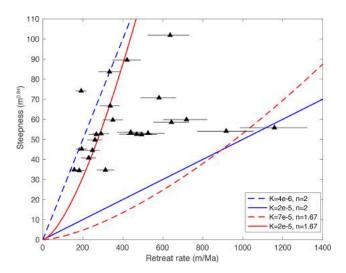


Figure 15. Channel steepness against escarpment retreat rates with 1σ uncertainty for catchments in the Western Ghats. Retreat rates of the escarpment are calculated using the basin projection method with an azimuth of N57E. Lines are model prediction of steepness and retreat rates from Eq. (2) for a range of the slope exponent n and K where the dimensions of K are $m^{1-0.84n}/yr$.

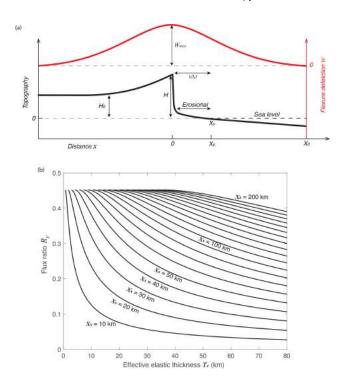


Figure 16. (a) Schematic model of isostatic flexural uplift due to escarpment erosion and retreat. Flexural uplift is calculated assuming removal of mass $v\Delta t\Delta yH$ treated as a line load at x=0; (b) flux ratio showing vertical erosion of coastal plain not accounted for in our horizontal retreat model. The ratio represents an overestimate of our retreat rates and is up to a few tens of percent at small $T_{\bf e}$ if the DCN sample is taken distant from escarpment.

give identical predictions, but for real landscapes, deviations of the land surface from a single plane result in differences in the velocity calculation, based on how the normal to the surface is calculated.

In practice, there are some disadvantages to the local scalar method. The primary of these is the strong effect of blocking of flux by neighboring basins. If the flux direction is such that the sides of the basin overlap with neighboring basins, a negative flux results from these sides, canceling the corresponding flux from the escarpment surface. This is the "edge of the bowl" problem discussed above, where if one viewed the basin in the direction of the flux vector, one could see only the outside of the basin. This is not necessarily an error, depending on the geometry of the basins and the erosive role of the neighboring basin, so this approach may or may not be correct, but the basin projection method is less sensitive to this effect, and so gives a more robust, if not more accurate, result.

4.2.1 Remnant topography in an escarpment-draining basin

Within a given escarpment-draining basin, the dependence of retreat rate on retreat direction (e.g., Fig. 9) comes directly from the geometry of the basin surface. Isolated buttes, inselbergs or other topography internal to the drainage basin such as escarpment-normal interfluvial ridges, define a type of remnant topography due to inefficient retreat of the escarpment. Buttes are generally regarded to be part of the ancient escarpment but now are erosion residuals (Gunnell and Harbor, 2010). Their existence attests to some inefficiency in the past escarpment erosion, such that a portion of the high topography is not removed as the escarpment passes. If the erosional efficiency of the escarpment is variable along strike, we would expect the low efficiency segments of the escarpment to lag and potentially become isolated from the escarpment forming a butte. An important question for our analysis is how this impacts the ¹⁰Be concentrations and inferred retreat rates.

By calculating the mean retreat rate, we are implicitly assuming that anomalously slow-retreating escarpment segments, including incipient buttes, are balanced by segments elsewhere in the same catchment that have higher retreat rates. As with vertical erosion rate calculations, spatial variation will not impact the mean unless it has an extreme variation that affects the assumptions regarding production or radioactive decay. This is also valid for the formation of remnant topography. For example, a butte forms because part of the escarpment was eroding at a retreat rate slower than the average. After a butte has formed as an isolated topographic feature, it continues to erode, thus contributing sediment (and ¹⁰Be atoms) to the net total of the basin. The principle of the average rate is that the extra sediment coming from the butte balances the "missing" sediment that does not arrive from a slow-eroding segment of the current escarpment. Provided the rate of remnant topography formation remains constant, the variance of retreat rate on the escarpment remains constant, and if the basin is large enough to average this process, we will obtain the correct average ¹⁰Be concentration and the correct retreat rate.

4.2.2 Retreat direction

Pure horizontal mass flux is an end-member flux direction; the other end-member is purely vertical. Horizontal flux requires assuming an azimuth direction. Both methods for calculating a purely horizontal mass flux have an important azimuthal dependence. The local scalar product method is more sensitive than the basin projection method to the assumed direction. Drainage basins have surfaces dipping in all directions but dominant directions are evident (e.g., Fig. 7e). A perfect escarpment basin would have rivers and hillslopes dipping nearly normal to the escarpment, in which case the direction of propagation is easy to determine, but most basins have geometry that is more complex (Fig. 7e) and this leads to sensitivity to the selected azimuth. Inferred rates deviate if the azimuth varies far from the dominant direction, particularly with the local scalar product method. The basin projection method displays less azimuthal sensitivity. At the largest scale, a rift margin escarpment is sinuous, implying variations in its average long-term retreat rate and local direction. The Western Ghats is assumed to be retreating at N57E, but locally, there is likely to be considerable variation in retreat direction.

4.2.3 Temporal variations in retreat rates

Retreat rates from our analysis are on the order of 100 m/Myr to 1 km/Myr. The retreat rates are horizontal, but the dominant physical process is still vertical incision of rivers (Fig. 7a–c). As we use DCN 10 Be concentrations for retreat rate calculations, these retreat rates are valid through the vertical erosion of one attenuation length of rock (Fig. 7d), providing an integration time for the measurement. In the Western Ghats, the basin-averaged erosion rate of escarpment-draining basins is tens to hundreds of meters per Myr. An erosion rate of hundreds of meters per Myr implies an integration time of $\sim 10^3$ years, which means the escarpment retreat rates are integrating over thousand-year timescales.

Using the current coastline and the rifting age as reference position and time also gives an average retreat rate of hundreds to thousands of meters per Myr since continental break-up. For this calculation, the modern coastline is assumed to represent the locus of the break-up structures, which may not always be true, although the western margin of India shows that the structural hinge between uplift and subsidence is close to the modern coast (Campanile et al., 2008; Chaubey et al., 2002). Average retreat rates are in the same range but systematically higher than DCN ¹⁰Beinferred retreat rates (Fig. 13), suggesting that the modern

escarpment is moving slower than its average since rifting. This difference becomes larger if we correct our retreat rates for flexural compensation. However, the majority of points are within a factor of 2 for an initiation of rifting at 120 Ma. Small escarpment basins have a higher probability of reflecting local effects, e.g., resistant lithology, and structural or metamorphic fabrics, and these basins show larger variance. Taking these small basins out of the analysis, the Western Ghats has a long-term retreat rate well represented by the DCN ¹⁰Be-inferred rate.

Although offshore sedimentation records are difficult to interpret given that basins are open to sediment export and recycling of sediment by subsequent erosion, records do not generally support steady rates of sediment supply with time since rifting. The offshore Konkan and Kerala basins abutting the Western Ghats record two pulses of intensive sedimentation: a Paleocene phase and a Pliocene phase (Campanile et al., 2008). If these sediment records are correct reflections of sediment supply from the eroding escarpment, they suggest that the correspondence between modern and long-term retreat rates might be fortuitous. However, the cause of the variations in erosion rate remains unclear. Escarpment relief might have changed over time if there has been significant continental uplift or tilting due to mantle dynamic flow, but there is no evidence for this aside from the variations in offshore sediment volume. The consistency in escarpment morphology and lack of along-strike variations in height, morphology or distance from the coast suggests that escarpment retreat has been the dominant process since rifting and any dynamic uplift would need to affect the entire margin nearly uniformly. A role for dynamic uplift, however, does remain possible and would affect the temporal variability of escarpment retreat. The other possibility is climate change; changing precipitation rates through the Cenozoic would also affect the erosional efficiency and thus retreat rate of the escarpment. Given India's migration from the tropics to its current midlatitude position and global climate changes over the Cenozoic (Kent and Muttoni, 2008), climate change certainly occurred and some impact on temporal variations in retreat rate is likely.

5 Conclusions

Large escarpments such as those that occur on many passive margins represent disequilibrium landscapes that have a long timescale of response and are characterized by erosion rates localized onto the escarpment, thereby driving retreat of the escarpment inland. Erosion rates are strongly variable in space, so an average erosion rate, as derived from detrital cosmogenic nuclides for catchments draining the escarpment, does not give an effective characterization of the rates of landscape change. We have addressed this issue by showing how ¹⁰Be concentrations can be used to measure the average rate of escarpment retreat. Retreat rates obtained from

¹⁰Be data from the Western Ghats of India gave retreat rates of up to more than 2 km/Myr. These rates are broadly consistent with the distance of the escarpment from the coast, suggesting that they are representative of the long-term rates.

Study of the Western Ghats demonstrates that the morphology of the escarpment rivers is consistent with evolution of the escarpment to a form driving escarpment retreat at a constant rate with a low-steepness coastal reach keeping up with sediment transport and isostatic uplift, and a steep-escarpment reach driving landward retreat. Escarpment retreat leads to episodic capture of plateau rivers, and we found numerous examples of rivers with high flat reaches characteristic of capture. These examples were distributed randomly along the escarpment, inconsistent with the alternative model of constant catchment geometry and transient uplift.

The general conclusion of this study is that great escarpments on passive margins are dynamic features with significant rates of retreat and high local rates of mass removal by erosion. Although rates are likely to be variable in time, escarpment retreat appears to be active from the time of rifting to the modern with current and average rates at hundreds to thousands of meters per million years, and these rates can be estimated by analysis of cosmogenic isotope concentrations.

Code availability. Related codes are available at https://gitlab. ethz.ch/yanywang/mass_flux_from_cosmo (last access: 31 August 2021) or upon request to the corresponding author.

Data availability. Data used in this paper are available at https://doi.org/10.5281/zenodo.5521585 (Wang and Willett, 2021).

Author contributions. YW and SDW conceptualized and designed the research. YW analyzed morphological features, developed the theory, developed the codes, conducted calculations, analyzed the data, wrote the manuscript and prepared the figures. SDW contributed to theory development and data interpretation, and provided input on the manuscript.

Competing interests. The authors declare that they have no conflict of interest.

Acknowledgements. We thank Maarten Lupker for valuable discussions.

Disclaimer. Publisher's note: Copernicus Publications remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Review statement. This paper was edited by Jens Turowski and reviewed by Greg Balco and one anonymous referee.

References

- Audet, P. and Bürgmann, R.: Dominant role of tectonic inheritance in supercontinent cycles, Nat. Geosci., 4, 184–187, https://doi.org/10.1038/ngeo1080, 2011.
- Balco, G., Stone, J. O., Lifton, N. A., and Dunai, T. J.: A complete and easily accessible means of calculating surface exposure ages or erosion rates from 10Be and 26Al measurements, Quat. Geochronol., 3, 174–195, https://doi.org/10.1016/j.quageo.2007.12.001, 2008.
- Beauvais, A., Ruffet, G., Hénocque, O., and Colin, F.: Chemical and physical erosion rhythms of the West African Cenozoic morphogenesis: the ³⁹Ar–⁴⁰Ar dating of supergene K-Mn oxides, J. Geophys. Res.-Earth Surf., 113, F04007, https://doi.org/10.1029/2008JF000996, 2008.
- Beauvais, A., Bonnet, N. J., Chardon, D., Arnaud, N., and Jayananda, M.: Very long-term stability of passive margin escarpment constrained by 40Ar/39Ar dating of K-Mn oxides, Geology, 44, 299–302, https://doi.org/10.1130/G37303.1, 2016.
- Bonnet, N. J., Beauvais, A., Arnaud, N., Chardon, D., and Jayananda, M.: Cenozoic lateritic weathering and erosion history of Peninsular India from ⁴⁰Ar/³⁹Ar dating of supergene K-Mn oxides, Chem. Geol., 446, 33–53, https://doi.org/10.1016/j.chemgeo.2016.04.018, 2016.
- Braun, J.: A review of numerical modeling studies of passive margin escarpments leading to a new analytical expression for the rate of escarpment migration velocity, Gondwana Res., 53, 209–224, https://doi.org/10.1016/j.gr.2017.04.012, 2018.
- Campanile, D., Nambiar, C., Bishop, P., Widdowson, M., and Brown, R.: Sedimentation record in the Konkan-Kerala Basin: implications for the evolution of the Western Ghats and the Western Indian passive margin, Basin Res., 20, 3–22, https://doi.org/10.1111/j.1365-2117.2007.00341.x, 2008.
- Chaubey, A., Rao, D. G., Srinivas, K., Ramprasad, T., Ramana, M., and Subrahmanyam, V.: Analyses of multichannel seismic reflection, gravity and magnetic data along a regional profile across the central western continental margin of India, Mar. Geol., 182, 303–323, https://doi.org/10.1016/S0025-3227(01)00241-9, 2002.
- Cockburn, H., Brown, R., Summerfield, M., and Seidl, M.: Quantifying passive margin denudation and landscape development using a combined fission-track thermochronology and cosmogenic isotope analysis approach, Earth Planet. Sc. Lett., 179, 429–435, https://doi.org/10.1016/S0012-821X(00)00144-8, 2000.
- Collier, J., Sansom, V., Ishizuka, O., Taylor, R., Minshull, T., and Whitmarsh, R.: Age of Seychelles-India break-up, Earth Planet. Sc. Lett., 272, 264–277, https://doi.org/10.1016/j.epsl.2008.04.045, 2008.
- de Souza, D. H., Stuart, F. M., Á., Rodés, Pupim, F. N., and Hackspacher, P. C.: Controls on the erosion of the continental margin of southeast Brazil from cosmogenic 10Be in river sediments, Geomorphology, 330, 163–176, https://doi.org/10.1016/j.geomorph.2019.01.020, 2019.
- DiBiase, R. A.: Short communication: Increasing vertical attenuation length of cosmogenic nuclide production on

- steep slopes negates topographic shielding corrections for catchment erosion rates, Earth Surf. Dynam., 6, 923–931, https://doi.org/10.5194/esurf-6-923-2018, 2018.
- Dunne, J., Elmore, D., and Muzikar, P.: Scaling factors for the rates of production of cosmogenic nuclides for geometric shielding and attenuation at depth on sloped surfaces, Geomorphology, 27, 3–11, https://doi.org/10.1016/S0169-555X(98)00086-5, 1999.
- Eagles, G. and Hoang, H. H.: Cretaceous to present kinematics of the Indian, African and Seychelles plates, Geophys. J. Int., 196, 1–14, https://doi.org/10.1093/gji/ggt372, 2014.
- Giachetta, E. and Willett, S. D.: Effects of river capture and sediment flux on the evolution of plateaus: insights from numerical modeling and river profile analysis in the upper Blue Nile catchment, J. Geophys. Res.-Earth Surf., 123, 1187–1217, https://doi.org/10.1029/2017JF004252, 2018.
- Gibbons, A. D., Whittaker, J. M., and Muller, R. D.: The breakup of East Gondwana: Assimilating constraints from Cretaceous ocean basins around India into a best-fit tectonic model, J. Geophys. Res.-Sol. Ea., 118, 808–822, https://doi.org/10.1002/jgrb.50079, 2013.
- Gilchrist, A. and Summerfield, M.: Differential denudation and flexural isostasy in formation of rifted margin upwarps, Nature, 346, 739–742, https://doi.org/10.1038/346739a0, 1990.
- Godard, V., Dosseto, A., Fleury, J., Bellier, O., Siame, L., and ASTER Team: Transient landscape dynamics across the Southeastern Australian Escarpment, Earth Planet. Sc. Lett., 506, 397– 406, https://doi.org/10.1016/j.epsl.2018.11.017, 2019.
- Granger, D. E., Lifton, N. A., and Willenbring, J. K.: A cosmic trip: 25 years of cosmogenic nuclides in geology, Geol. Soc. Am. Bull., 125, 1379–1402, https://doi.org/10.1130/B30774.1, 2013.
- Gunnell, Y. and Fleitout, L.: Shoulder uplift of the Western Ghats passive margin, India: a denudational model, Earth Surf. Process. Landf., 23, 391–404, 1998.
- Gunnell, Y. and Harbor, D.: Butte detachment: how pre-rift geological structure and drainage integration drive escarpment evolution at rifted continental margins, Earth Surf. Process. Landf., 35, 1373–1385, https://doi.org/10.1002/esp.1973, 2010.
- Heisinger, B., Lal, D., Jull, A., Kubik, P., Ivy-Ochs, S., Knie, K., and Nolte, E.: Production of selected cosmogenic radionuclides by muons: 2. Capture of negative muons, Earth Planet. Sc. Lett., 200, 357–369, https://doi.org/10.1016/S0012-821X(02)00641-6, 2002a.
- Heisinger, B., Lal, D., Jull, A., Kubik, P., Ivy-Ochs, S., Neumaier, S., Knie, K., Lazarev, V., and Nolte, E.: Production of selected cosmogenic radionuclides by muons: 1. Fast muons, Earth Planet. Sc. Lett., 200, 345–355, https://doi.org/10.1016/S0012-821X(02)00640-4, 2002b.
- Jarvis, A., Reuter, H., Nelson, A., and Guevara, E.: Hole-filled seamless SRTM data, Version 4, International Centre for Tropical Agriculture (CIAT), available at: http://srtm.csi.cgiar.org (last access: 11 October 2016), 2008.
- Kent, D. V. and Muttoni, G.: Equatorial convergence of India and early Cenozoic climate trends, P. Natl. Acad. Sci. USA, 105, 16065–16070, https://doi.org/10.1073/pnas.0805382105, 2008.
- Kirby, E. and Whipple, K. X.: Expression of active tectonics in erosional landscapes, J. Struct. Geol., 44, 54–75, https://doi.org/10.1016/j.jsg.2012.07.009, 2012.
- Kooi, H. and Beaumont, C.: Escarpment evolution on highelevation rifted margins: Insights derived from a surface

- processes model that combines diffusion, advection, and reaction, J. Geophys. Res.-Sol. Ea., 99, 12191–12209, https://doi.org/10.1029/94JB00047, 1994.
- Lal, D.: Cosmic ray labeling of erosion surfaces: in situ nuclide production rates and erosion models, Earth Planet. Sc. Lett., 104, 424–439, https://doi.org/10.1016/0012-821X(91)90220-C, 1991.
- Linari, C. L., Bierman, P. R., Portenga, E. W., Pavich, M. J., Finkel, R. C., and Freeman, S. P.: Rates of erosion and landscape change along the Blue Ridge escarpment, southern Appalachian Mountains, estimated from in situ cosmogenic ¹⁰Be, Earth Surf. Process. Landf., 42, 928–940, https://doi.org/10.1002/esp.4051, 2017.
- Lupker, M., Blard, P.-H., Lavé, J., France-Lanord, C., Leanni, L., Puchol, N., Charreau, J., and Bourles, D.: 10Bederived Himalayan denudation rates and sediment budgets in the Ganga basin, Earth Planet. Sc. Lett., 333, 146–156, https://doi.org/10.1016/j.epsl.2012.04.020, 2012.
- Mandal, S. K., Lupker, M., Burg, J.-P., Valla, P. G., Haghipour, N., and Christl, M.: Spatial variability of ¹⁰Be-derived erosion rates across the southern Peninsular Indian escarpment: A key to land-scape evolution across passive margins, Earth Planet. Sc. Lett., 425, 154–167, https://doi.org/10.1016/j.epsl.2015.05.050, 2015.
- Masarik, J., Kollar, D., and Vanya, S.: Numerical simulation of in situ production of cosmogenic nuclides: Effects of irradiation geometry, Nucl. Instrum. Methods Phys. Res. Sect. B, 172, 786– 789, https://doi.org/10.1016/S0168-583X(00)00121-X, 2000.
- Matmon, A., Bierman, P., and Enzel, Y.: Pattern and tempo of great escarpment erosion, Geology, 30, 1135–1138, https://doi.org/10.1130/0091-7613(2002)030<1135:PATOGE>2.0.CO;2, 2002.
- Niemi, N. A., Oskin, M., Burbank, D. W., Heimsath, A. M., and Gabet, E. J.: Effects of bedrock landslides on cosmogenically determined erosion rates, Earth Planet. Sc. Lett., 237, 480–498, https://doi.org/10.1016/j.epsl.2005.07.009, 2005.
- Oilier, C.: The Great Escarpment of eastern Australia: tectonic and geomorphic significance, J. Geo. Soc. Aus., 29, 13–23, https://doi.org/10.1080/00167618208729190, 1982.
- Perron, J. T. and Royden, L.: An integral approach to bedrock river profile analysis, Earth Surf. Process. Landf, 38, 570–576, https://doi.org/10.1002/esp.3302, 2013.
- Persano, C., Stuart, F. M., Bishop, P., and Barfod, D. N.: Apatite (U-Th)/He age constraints on the development of the Great Escarpment on the southeastern Australian passive margin, Earth Planet. Sc. Lett., 200, 79–90, https://doi.org/10.1016/S0012-821X(02)00614-3, 2002.
- Persano, C., Bishop, P., and Stuart, F.: Apatite (U-Th)/He age constraints on the Mesozoic and Cenozoic evolution of the Bathurst region, New South Wales: evidence for antiquity of the continental drainage divide along a passive margin, Aust. J. Earth Sci., 53, 1041–1050, https://doi.org/10.1080/08120090600923303, 2006.
- Portenga, E. W. and Bierman, P. R.: Understanding Earths eroding surface with ¹⁰Be, GSA Today, 21, 4–10, https://doi.org/10.1130/G111A.1, 2011.
- Prince, P. S., Spotila, J. A., and Henika, W. S.: New physical evidence of the role of stream capture in active retreat of the Blue Ridge escarpment, southern Appalachians, Geomorphology, 123, 305–319, https://doi.org/10.1016/j.geomorph.2010.07.023, 2010.

- Ratheesh-Kumar, R., Ishwar-Kumar, C., Windley, B., Razakamanana, T., Nair, R. R., and Sajeev, K.: India-Madagascar paleofit based on flexural isostasy of their rifted margins, Gondwana Res., 28, 58–600, https://doi.org/10.1016/j.gr.2014.06.008, 2015.
- Sacek, V., Braun, J., and Van Der Beek, P.: The influence of rifting on escarpment migration on high elevation passive continental margins, J. Geophys. Res.-Sol. Ea., 117, B04407, https://doi.org/10.1029/2011JB008547, 2012.
- Salgado, A. A., Marent, B. R., Cherem, L. F., Bourles, D., Santos, L. J., Braucher, R., and Barreto, H. N.: Denudation and retreat of the serra do mar escarpment in Southern Brazil derived from in situ produced ¹⁰Be concentration in river sediment, Earth Surf. Process. Landf., 39, 311–319, https://doi.org/10.1002/esp.3448, 2014
- Schwanghart, W. and Scherler, D.: Short Communication: Topo-Toolbox 2 – MATLAB-based software for topographic analysis and modeling in Earth surface sciences, Earth Surf. Dynam., 2, 1–7, https://doi.org/10.5194/esurf-2-1-2014, 2014.
- Seidl, M. A., Weissel, J. K., and Pratson, L. F.: The kinematics and pattern of escarpment retreat across the rifted continental margin of SE Australia, Basin Res., 8, 301–316, https://doi.org/10.1046/j.1365-2117.1996.00266.x, 1996.
- Snyder, N. P., Whipple, K. X., Tucker, G. E., and Merritts, D. J.: Landscape response to tectonic forcing: Digital elevation model analysis of stream profiles in the Mendocino triple junction region, northern California, Geol. Soc. Am. Bull., 112, 1250–1263, https://doi.org/10.1130/0016-7606(2000)112<1250:LRTTFD>2.0.CO;2, 2000.
- Stone, J. O.: Air pressure and cosmogenic isotope production, J. Geophys. Res.-Sol. Ea., 105, 23753–23759, https://doi.org/10.1029/2000JB900181, 2000.
- Tenzer, R., Novák, P., Gladkikh, V., and Vajda, P.: Global crust-mantle density contrast estimated from EGM2008, DTM2008, CRUST2. 0, and ICE-5G. Pure Appl. Geophys., 169, 1663–1678, https://doi.org/10.1007/s00024-011-0410-3, 2012.

- Thompson, J. O., Moulin, M., Aslanian, D., De Clarens, P., and Guillocheau, F.: New starting point for the Indian Ocean: Second phase of breakup for Gondwana, Earth-Sci. Rev., 191, 26–56, https://doi.org/10.1016/j.earscirev.2019.01.018, 2019.
- Torsvik, T. H., Amundsen, H., Hartz, E. H., Corfu, F., Kusznir, N., Gaina, C., Doubrovine, P. V., Steinberger, B., Ashwal, L. D., and Jamtveit, B.: A Precambrian microcontinent in the Indian Ocean, Nat. Geosci., 6, 223–227, https://doi.org/10.1038/ngeo1736, 2013.
- Tucker, G. E. and Slingerland, R. L.: Erosional dynamics, flexural isostasy, and long-lived escarpments: A numerical modeling study, J. Geophys. Res.-Sol. Ea., 99, 12229–12243, https://doi.org/10.1029/94JB00320, 1994.
- Turcotte, D. and Schubert, G.: Elasticity and Flexure, in: Geodynamics, Cambridge University Press, Cambridge, 105–131, https://doi.org/10.1017/CBO9780511807442.005, 2002.
- van der Beek, P., Summerfield, M. A., Braun, J., Brown, R. W., and Fleming, A.: Modeling postbreakup landscape development and denudational history across the southeast African (Drakensberg Escarpment) margin, J. Geophys. Res.-Sol. Ea., 107, ETG-11, https://doi.org/10.1029/2001JB000744, 2002.
- Von Blanckenburg, F.: The control mechanisms of erosion and weathering at basin scale from cosmogenic nuclides in river sediment. Earth Planet. Sc. Lett., 237, 462–479, https://doi.org/10.1016/j.epsl.2005.06.030, 2005.
- Wang, Y. and Willett, D. S.: Dataset to paper YWang and SWillett Escarpment retreat rates derived from detrital cosmogenic nuclide concentrations, in: Earth Surface Dynamics, Zenodo [data set], https://doi.org/10.5281/zenodo.5521585, 2021.
- Willett, S. D., McCoy, S. W., and Beeson, H. W.: Transience of the North American High Plains landscape and its impact on surface water, Nature, 561, 528–532, https://doi.org/10.1038/s41586-018-0532-1, 2018.