

VE311 RC1

Jiaying Li

University of Michigan-Shanghai Jiao Tong University Joint Institute

June 12, 2023



JOINT INSTITUTE
交大密西根学院

Overview

1 Diode and Diode Circuit

mid

2 BJT

1. diode

3 BJT Common-Emitter Amplifier

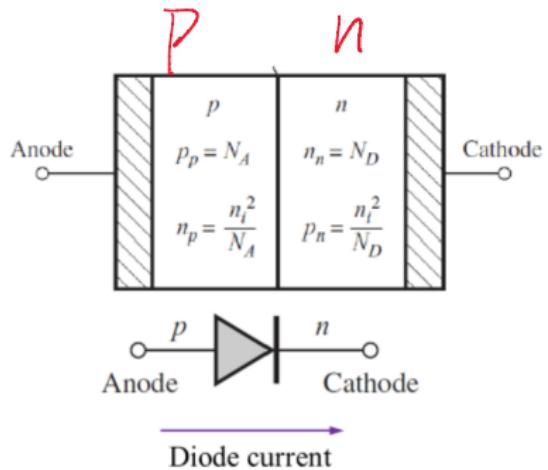
2. op-amp

3. BJT

4. MOSFET Big Signal

MOSFET SS X

PN Junction Diode



N_A, N_D : doping densities

n_i : intrinsic carrier concentration

hole in p: *majority*

$$p_p = N_A \quad (1)$$

electron in p: *minority*

$$n_p = \frac{n_i^2}{N_A} \quad (2)$$

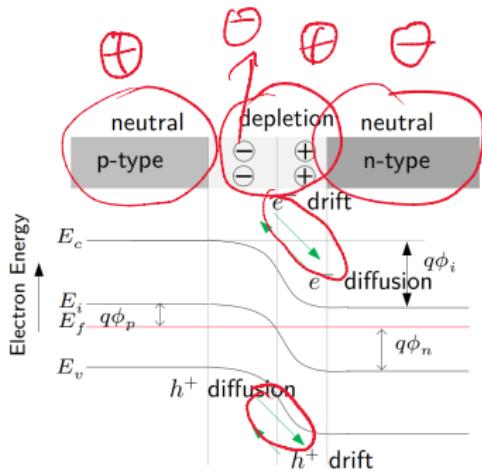
electron in n: *majority*

$$n_n = N_D \quad (3)$$

hole in n: *minority*

$$p_n = \frac{n_i^2}{N_D} \quad (4)$$

PN Junction Diode



built-in potential:

$$V_{bi} = V_T \ln\left(\frac{N_A N_D}{n_i^2}\right) \quad (5)$$

- ▶ Some electrons/holes in the **neutral regions** with sufficient energy continuously diffuse to the opposite sides. → Formation of diffusion *high concentration \rightarrow low*
- ▶ Some electrons/holes wandering into the in the **depletion region** get swept by the built-in electric field. → Formation of drift current
- ▶ Diffusion current cancels drift current. No net current flowing. *at equilibrium*

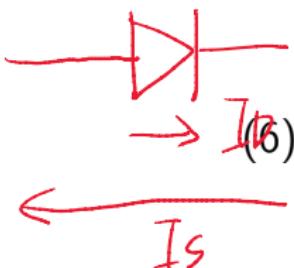
Diode Equation



- ▶ **Forward Bias:** Diode is on. Current flows from p to n.
- ▶ **Reverse Bias:** Diode is off. Current doesn't flow, but saturation current exists.

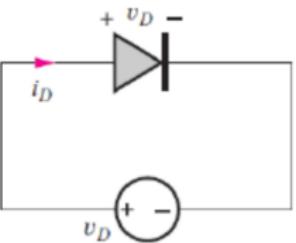
$$V_T = \frac{kT}{q} \quad \text{can be ignored}$$

$$I_D = I_S \left(e^{\frac{qV_D}{kT}} - 1 \right) = I_S \left(e^{\frac{V_D}{V_T}} - 1 \right)$$



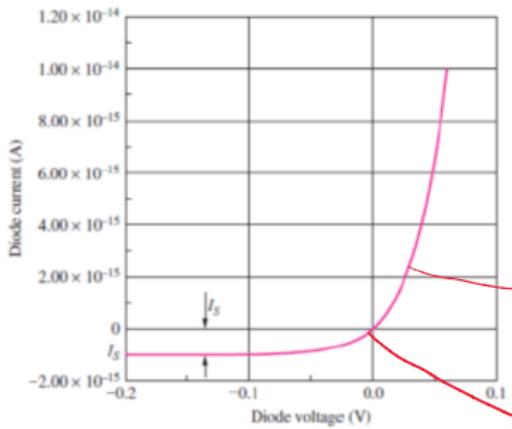
Note:

- ▶ k = Boltzmann's constant, $8.62 \times 10^{-5} \text{ eV/K}$
- ▶ $\frac{kT}{q} = 0.026(0.025875)\text{V}$ at 300K when calculation.



IV Characteristics of Diode

ideal condition



Non-linear, or rectifying, behavior

- ▶ Non-linear behavior
- ▶ turn-on voltage > V_{bi}

$$I_D = I_S \left(e^{\frac{V_D}{V_T}} - 1 \right)$$

rectifying behavior

let current flow in one direction,

$V_{on} : 0.5V \sim 0.7V$ but
due to the V_{bi}
 $V_{on} > V_{bi}$

prevent it
flowing to
the opposite
direction

Exercise 1

(23FA Mid/1) Choose one description that is not right. (5)

- (1) At equilibrium, a PN diode current is zero. ✓ drift and diffusion cancel out $I_D = I_s(e^{\frac{V}{T}} - 1)$
- (2) Under a forward bias, a PN diode current increases exponentially. ✓
- (3) Under a forward bias, a PN diode current is from P to N. ✓ P-DIODE N I_D
- (4) Under a moderate reverse bias (before the breakdown), a PN diode current is almost zero. ✓
- (5) A PN diode shows a rectifying behavior, i.e. nonlinear I-V curve, because a drift current is dominant over a diffusion current under a forward bias. X
internal structure

Diode Simplification

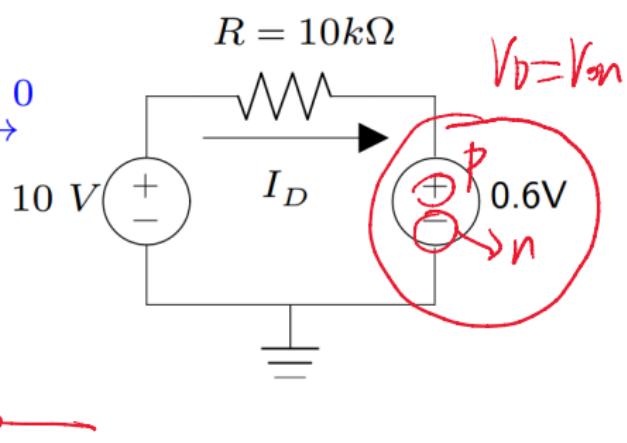
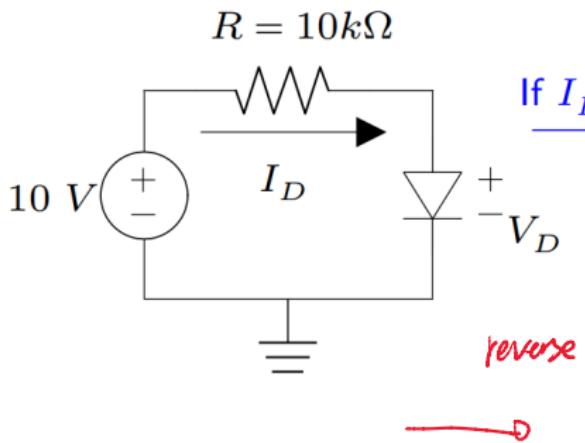
Forward bias
 $I_D > 0$



reverse
 $I_D \leq 0$
 $V_D = e$



- Ideal Diode Model: **Short circuit** for Forward Bias and **Open Circuit** for Reverse Bias
- Constant Voltage Drop Model: Replace Diode with a voltage source for Forward Bias and **Open Circuit** for Reverse Bias.



Diode Simplification more than 1 diode

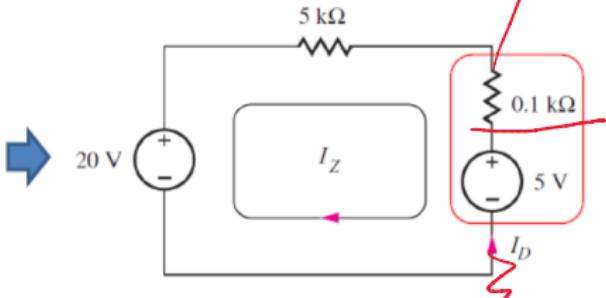
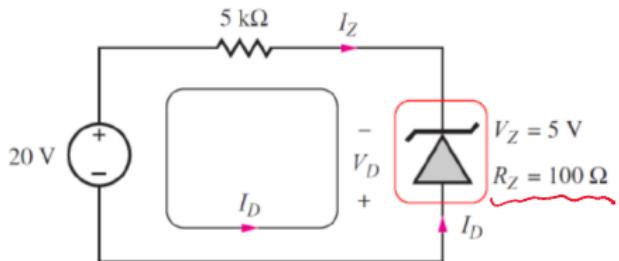
1. Identify the model for simplification. *Ideal or CVD*
2. Assume the voltage applied on the diode *Assume diode is on*
3. Transform the diode to source and resistor according to the assumption.
4. Validate that the assumption is correct or not.

judge $I_D > 0 \rightarrow$ *Assumption is right*

$I_D \approx 0 \rightarrow$ *wrong, calculate again assuming diode is off*

Diodes (Zener) in Breakdown Region

Method: Replace the Diode with a "Reverse" voltage source and a resistance.



forward:

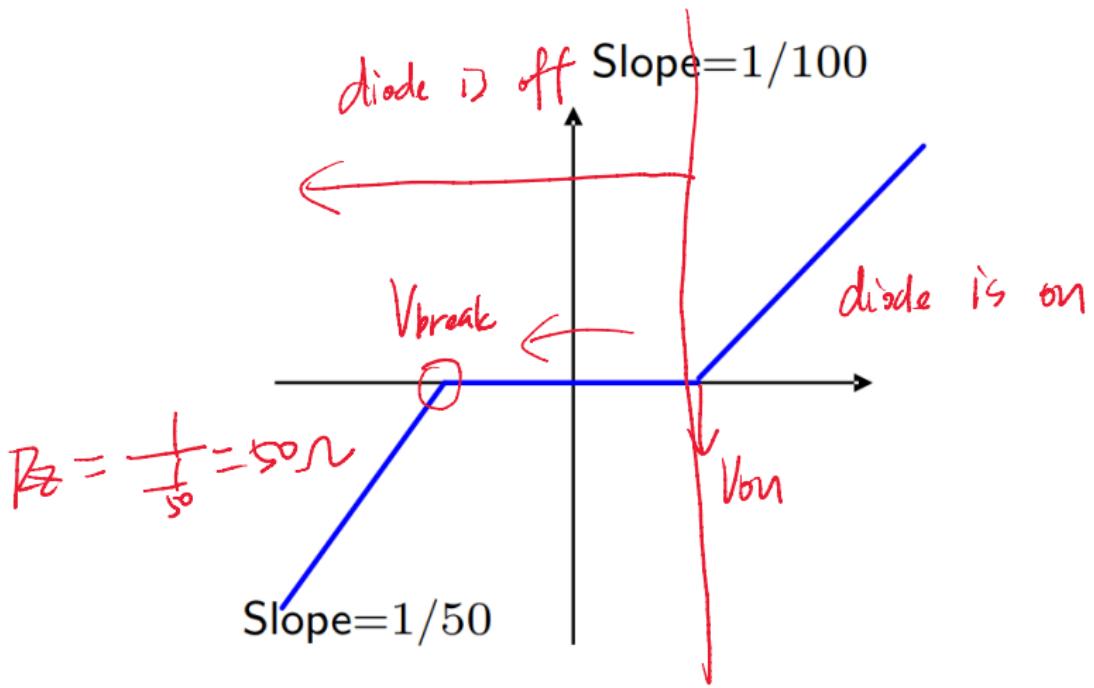


zener:



IV Characteristics

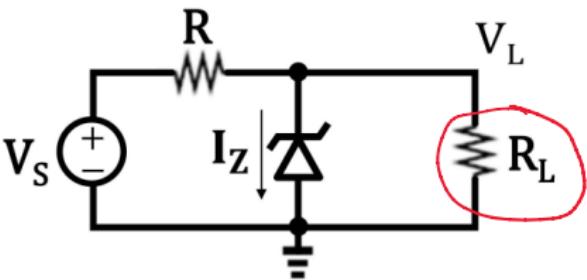
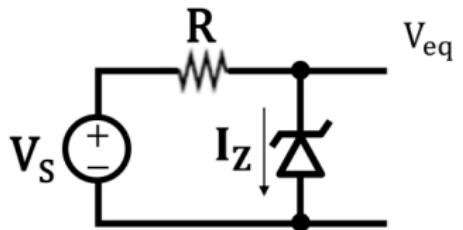
When $V_D < V_{break}$, voltage source is V_{break} , slope is $\frac{1}{R_Z}$.



Voltage Regulator

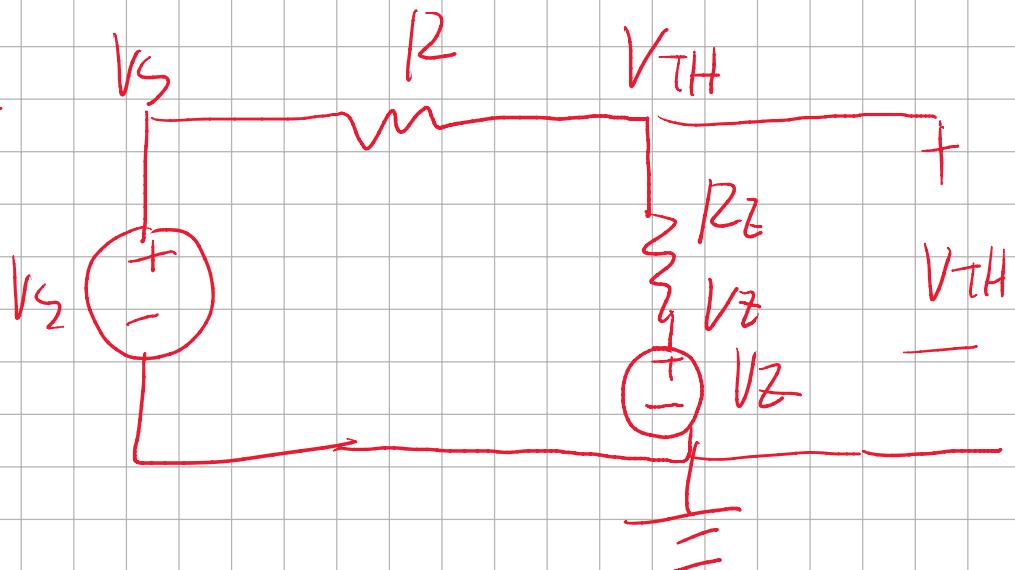
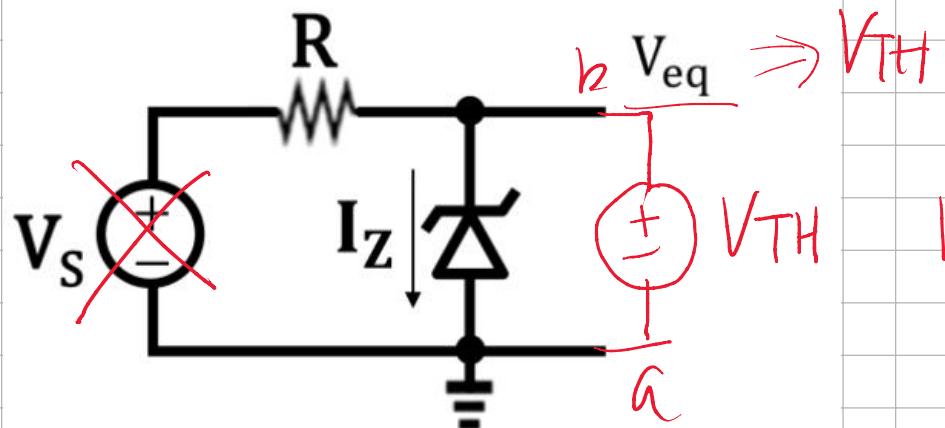
maintain a constant voltage
of the load resistor

Assume the zener diode operates in reverse breakdown region.



$$V_{eq} = V_{break} + \frac{V_s - V_{break}}{R + R_Z} R_Z \quad (7)$$

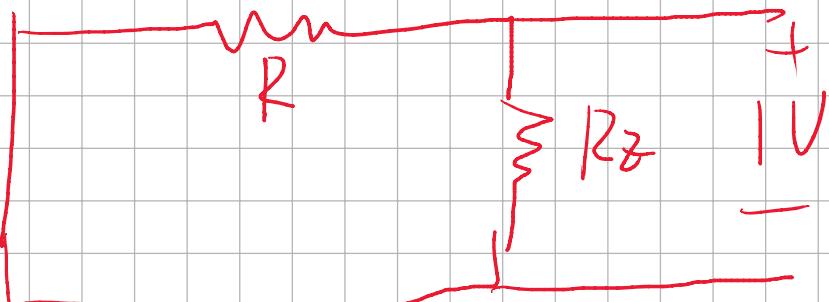
$$V_L = V_{eq} \frac{R_L}{(R || R_Z) + R_L} \quad (8)$$



① V_{TH}

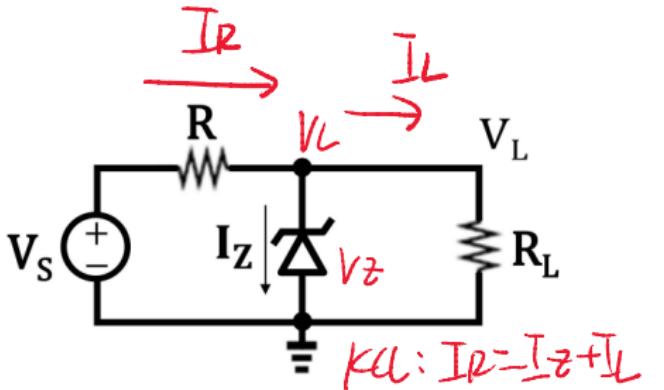
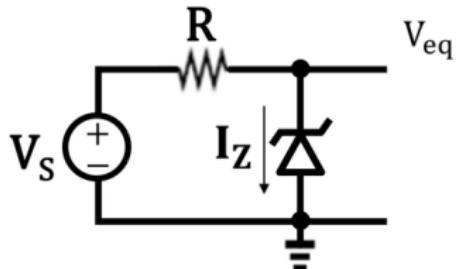
② R_{TH} : add a voltage source of 1V on a-b

and X turn off the independent sources



$$R_{TH} = R \parallel R_Z$$

Voltage Regulator



how sensitive V_L is to V_S when $R_L \rightarrow \infty$

$$\text{Line Regulation} = \frac{dV_L}{dV_S} = \frac{R_Z}{R + R_Z} \quad (R_L = \infty) \quad (9)$$

Load Regulation = $\frac{dV_L}{dI_L} = \underline{R \parallel R_Z}$ (10)

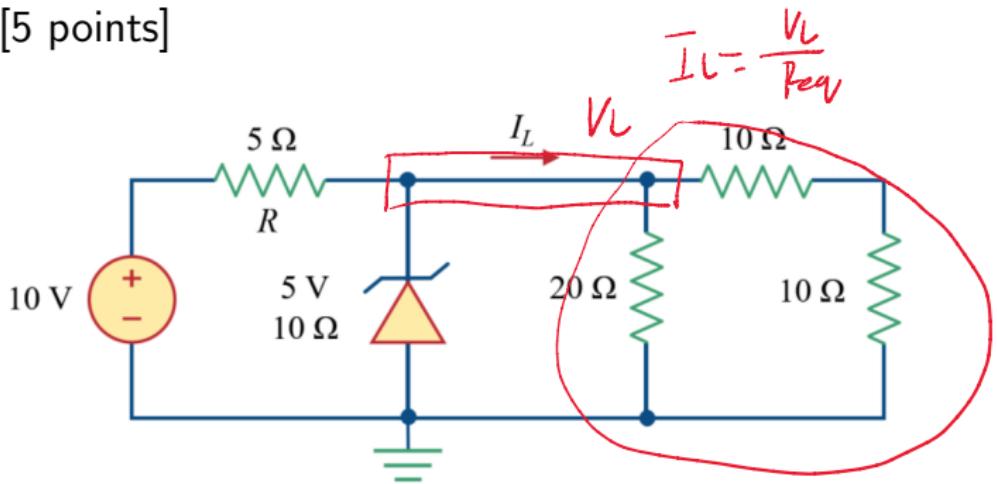
Exercise 2

(23FA Mid/6) For the diode circuit below:

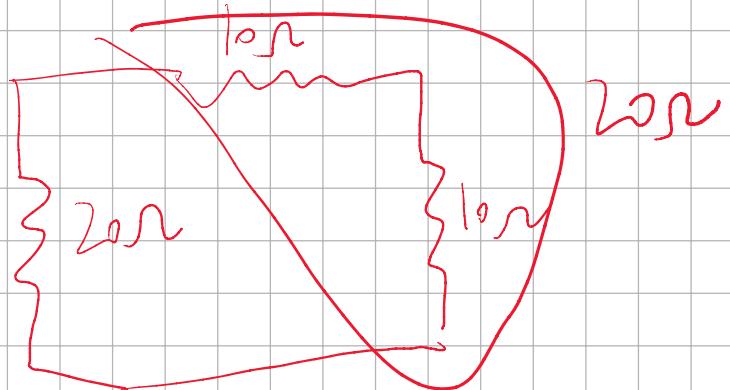
(1) Calculate the value I_L . [10 points]

(2) Find the maximum value of R required for reverse breakdown to happen. [5 points]

extreme condition: $I_Z > 0$



1)



$$I_L = \frac{V_L - 0}{R_{\text{Req}}} = \frac{\frac{25}{4}}{10} = \frac{5}{8} \text{ A}$$

$$2) I_Z = \frac{V_L - 5}{10} > 0$$

$$\frac{10 - V_L}{R} = \frac{V_L - 5}{10} + \frac{V_L - 0}{10}$$

$$\Rightarrow V_L = \frac{5R + 100}{2R + 10}$$

$$V_L - 5 = \frac{50 - 5R}{2R + 10} > 0$$

$$\Rightarrow R < 10$$

$$\text{KCL: } I_R = I_Z + I_L$$

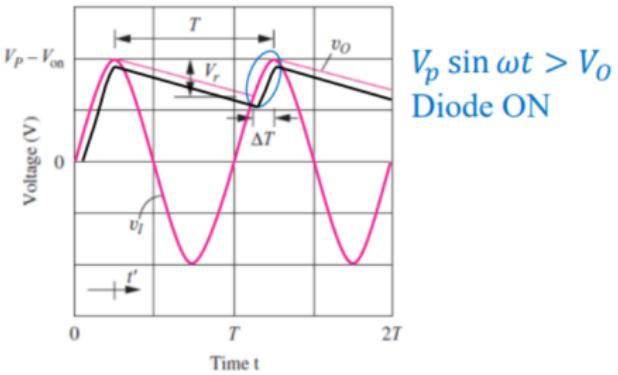
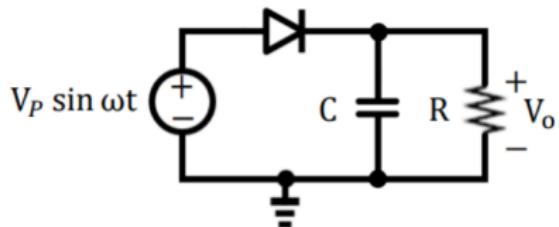
$$\frac{10 - V_L}{5} = \frac{V_L - 5}{10} + \frac{V_L - 0}{10}$$

$$\Rightarrow V_L = \frac{25}{4} \text{ V}$$

$$R_{\text{MAX}} = 10 \Omega$$

Half-Wave Rectifier

The basic rectifier circuit converts an AC voltage to a pulsating DC voltage.



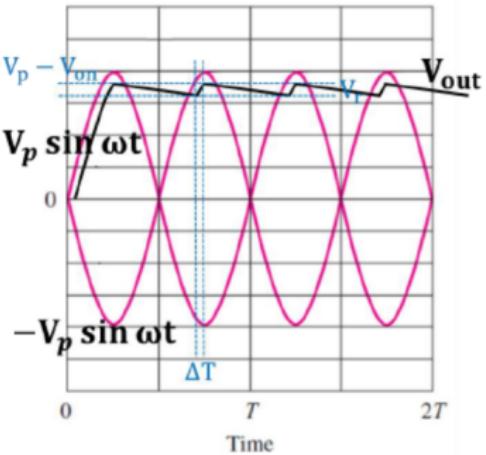
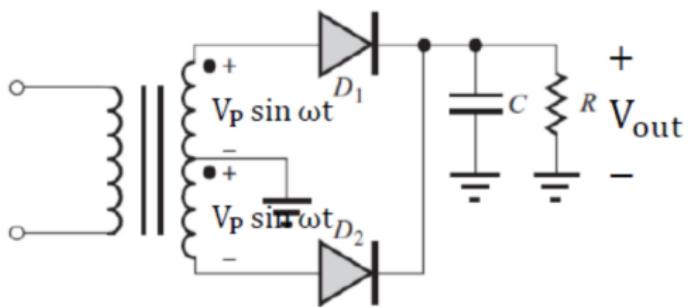
Half-Wave Rectifier

CTPP Time!

1. $V_{dc} = V_s - V_{on}$
2. $I_{dc} = \frac{V_{dc}}{R}$
3. Ripple Voltage: $V_r = V_{dc}(1 - e^{\frac{T-\Delta T}{RC}}) \approx V_{dc} \frac{T}{RC}$
4. Conduction Angle: $\theta_c = \sqrt{\frac{2V_r}{V_s}}$
5. Conduction Interval: $\Delta T = \frac{\theta_c}{\omega}$
6. Diode Current: $I_{peak} = \frac{2I_{dc}T}{\Delta T}$
7. Surge Current: $I_{surge} = C \frac{dV}{dt} = \omega C V_s(t=0)$
8. Peak Inverse Voltage (PIV): $PIV = 2V_s - V_{on}$

Full-Wave Rectifier

Full-wave rectifier circuits cut the capacitor discharge time in half and offer the advantage of requiring only one-half the filter capacitance to achieve a given ripple voltage



Full-Wave Rectifier

CTPP Time!

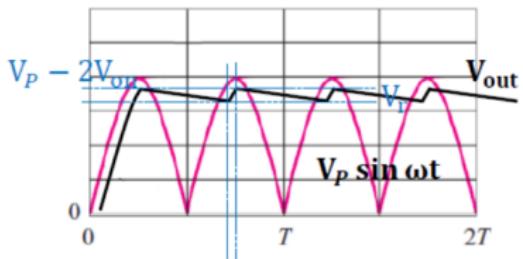
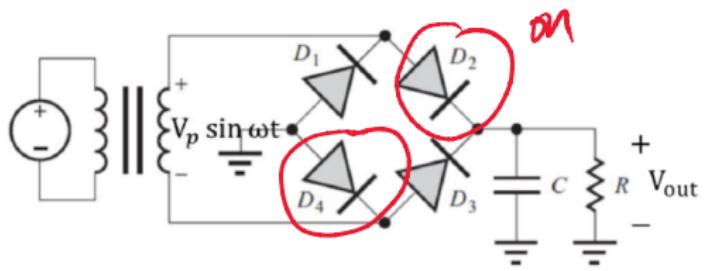
$T \rightarrow \frac{T}{2}$

Just replace T with $\frac{T}{2}$ in the Half-Wave rectifier.

1. $V_{dc} = V_s - V_{on}$
2. $I_{dc} = \frac{V_{dc}}{R}$
3. Ripple Voltage: $V_r = V_{dc}(1 - e^{\frac{T/2-\Delta T}{RC}}) \approx V_{dc} \frac{T}{2RC}$
4. Conduction Angle: $\theta_c = \sqrt{\frac{2V_r}{V_s}}$
5. Conduction Interval: $\Delta T = \frac{\theta_c}{\omega}$
6. Diode Current: $I_{peak} = \frac{I_{dc}T}{\Delta T}$
7. Surge Current: $I_{surge} = C \frac{dV}{dt} = \omega C V_s(t=0)$
8. Peak Inverse Voltage (PIV): $PIV = 2V_s - V_{on}$

Full-Wave Bridge Rectifier

- ▶ For $v_I > 0$, D_2 and D_4 will be on and D_1 and D_3 will be off.
- ▶ For $v_I < 0$, D_2 and D_4 will be off and D_1 and D_3 will be on.



Full-Wave Bridge Rectifier

CTPP Time!

Just replace V_{on} with $2V_{on}$ in the Full-Wave rectifier and change PIV.

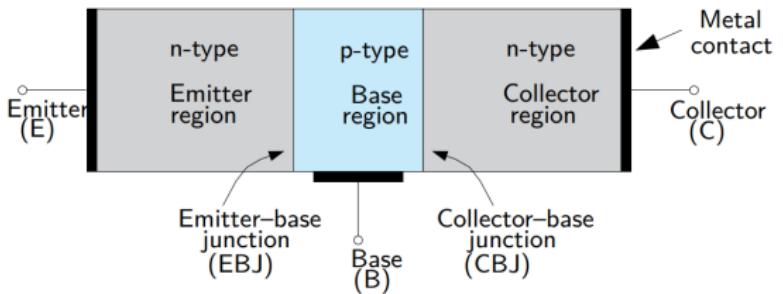
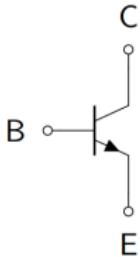
1. $V_{dc} = V_s - 2V_{on}$
2. $I_{dc} = \frac{V_{dc}}{R}$
3. Ripple Voltage: $V_r = V_{dc}(1 - e^{\frac{T/2-\Delta T}{RC}}) \approx V_{dc} \frac{T}{2RC}$
4. Conduction Angle: $\theta_c = \sqrt{\frac{2V_r}{V_s}}$
5. Conduction Interval: $\Delta T = \frac{\theta_c}{\omega}$
6. Diode Current: $I_{peak} = \frac{I_{dc}T}{\Delta T}$
7. Surge Current: $I_{surge} = C \frac{dV}{dt} = \omega C V_s(t=0)$
8. Peak Inverse Voltage (PIV): $PIV = V_s - V_{on}$

Overview

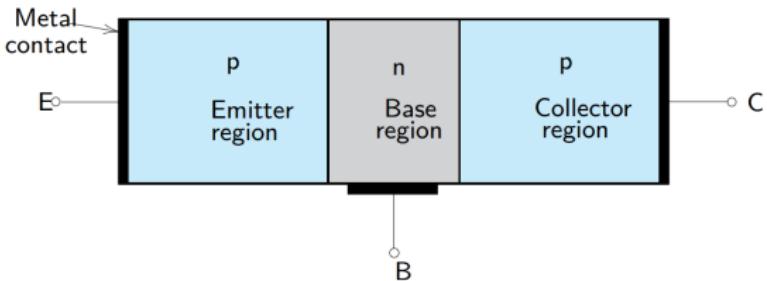
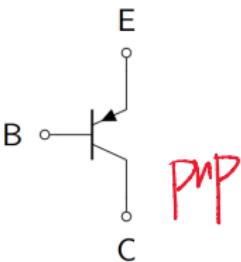
- 1 Diode and Diode Circuit
- 2 BJT
- 3 BJT Common-Emitter Amplifier

npn and pnp

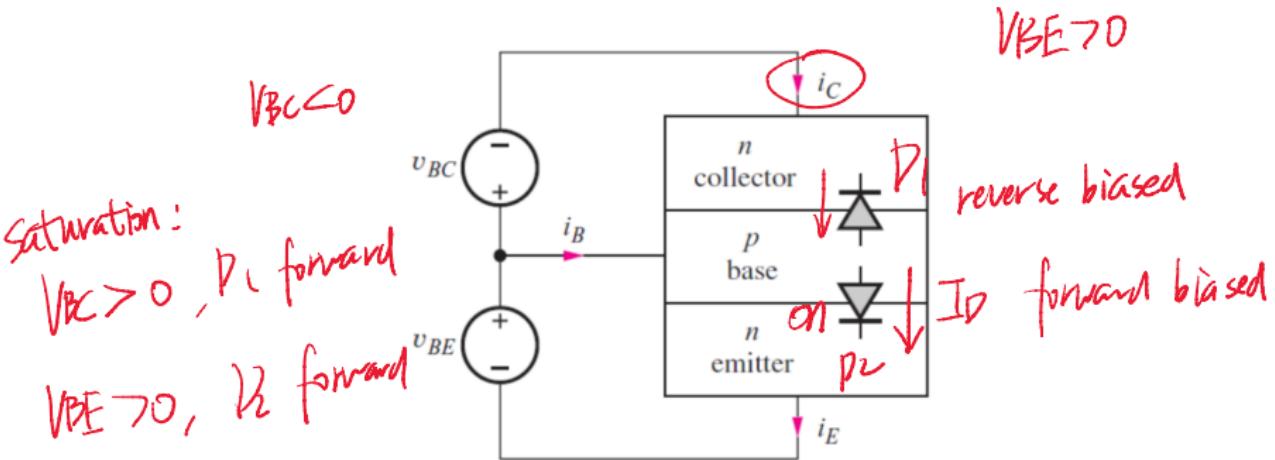
npn



B doesn't change, $C \rightarrow E$

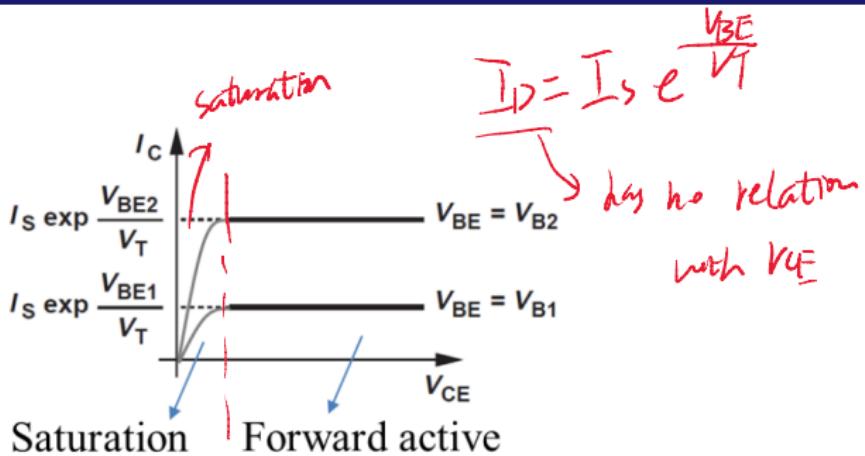


Forward Active Mode



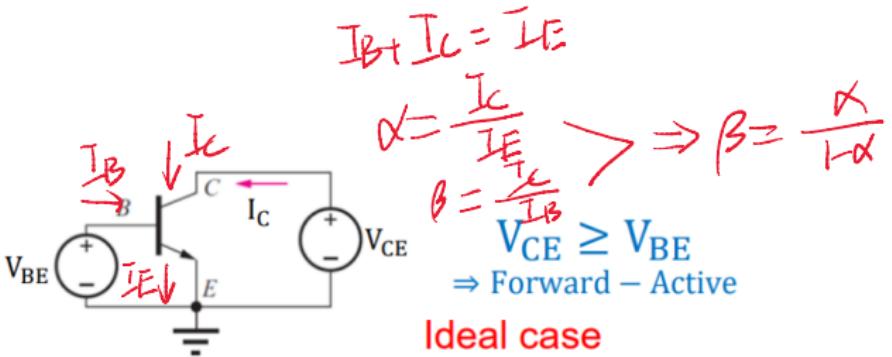
- EB diode is forward biased ($V_{BE} > 0$ or $V_{EB} < 0$)
- BC diode is reversed biased ($V_{BC} < 0$ or $V_{CB} > 0$)

Saturation v.s. Forward Active



- ▶ $V_{CE} < V_{BE}$, then $V_{CB} < 0$ or $V_{BC} > 0$, meaning that BC diode is forward biased. Both diodes are on, which is called as saturation.
- ▶ $V_{CE} > V_{BE}$, then $V_{CB} > 0$ or $V_{BC} < 0$, meaning that BC diode is reverse biased. → Forward Active

Summary:



Ideal case

$$I_C = I_S \left(e^{\frac{qV_{BE}}{kT}} - 1 \right)$$

$$\alpha = \frac{I_C}{I_E} \cong 1$$

$$\beta = \frac{I_C}{I_B} = \frac{\alpha}{1 - \alpha}$$

$$I_C = I_S \left(e^{\frac{qV_{BE}}{kT}} - 1 \right)$$

$$\alpha = \frac{I_C}{I_E} = 1$$

$$\beta = \frac{I_C}{I_B} = \infty$$

Don't forget this: $I_E = I_C + I_B$

Early effect

Early effect: V_A is called the Early voltage

*limit the gain of
BJT amplifier*

$$I_C = I_S \left(e^{\frac{qV_{BE}}{kT}} - 1 \right) \left(1 + \frac{V_{CE}}{V_A} \right) \quad (11)$$

or

$$I_C = I_S \left(e^{\frac{qV_{BE}}{kT}} \right) \left(1 + \frac{V_{CE}}{V_A} \right) \quad (12)$$

Small Signal

$$V_{out} = V_{OUT} + v_{out}$$

V_{out} : DC+AC, V_{OUT} : DC, v_{out} : AC

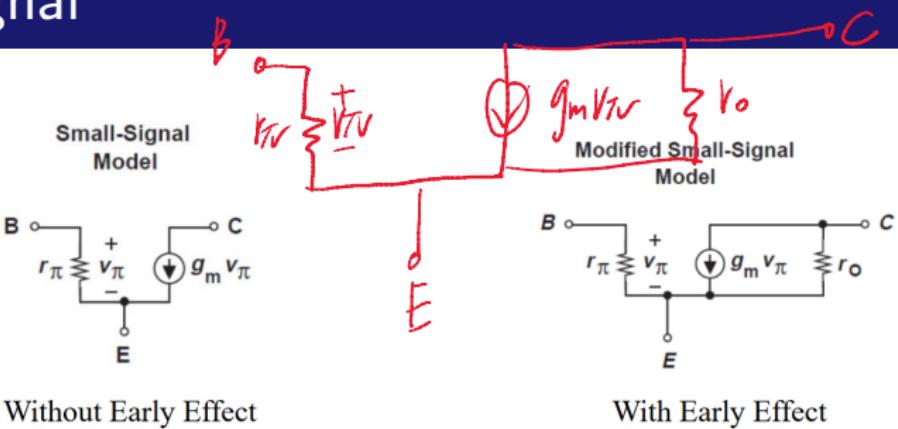
It is important to bear in mind that small-signal analysis deals with only (small) changes in voltages and currents in a circuit around their quiescent values. Thus, all constant sources, i.e., **voltage and current sources that do not vary with time (independent sources)**, must be set to zero for small-signal analysis.

Small Signal

How to get a small signal circuit:

- ▶ DC voltage source: short circuit
- ▶ DC current source: open circuit
- ▶ Capacitor: short circuit (short in AC, open in DC)

Small Signal

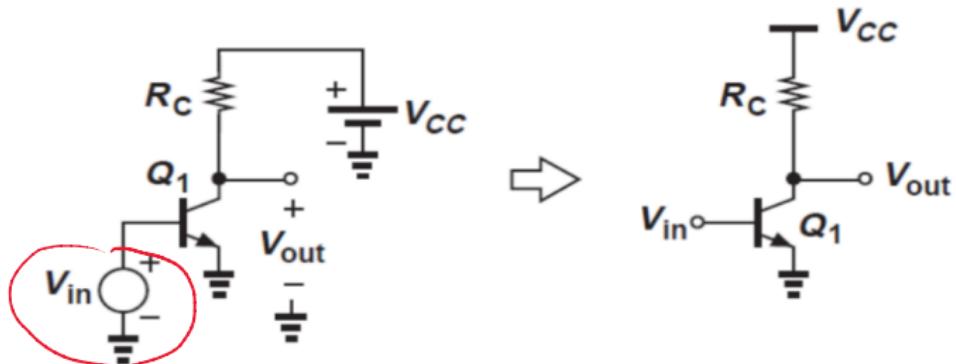


$$r_\pi = \frac{dV_{BE}}{dl_B} = \frac{1}{\frac{dl_C}{\beta dV_{BE}}} = \frac{1}{\frac{g_m}{\beta}} = \frac{\beta}{g_m} \quad (13)$$

$$g_m = \frac{dl_C}{dV_{BE}} \cong \frac{l_C}{kT/q} \quad (14)$$

$$r_o = \frac{1}{\frac{dl_C}{dV_{CE}}} \cong \frac{V_A}{l_C} \quad (15)$$

Small Signal



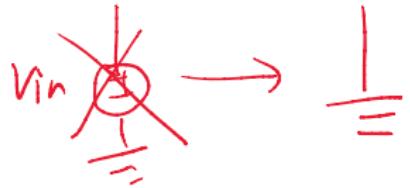
Attention:

- ▶ V_{out} is not connected in the circuit! There is no current to it.
- ▶ V_{in} is connected. There is current from it.

Tips: See V_{out} as a voltmeter, V_{in} as a voltage source.

How to calculate R_{out} ?

1. Draw small signal model.
2. Connect port with V_{in} to ground. Connect a test voltage v_t on port with V_{out} .
3. Derive i_t .
4. Calculate $R_{out} = \frac{v_t}{i_t}$



R_{in}

How to calculate R_{in} ?

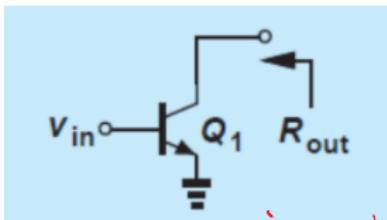
1. Draw small signal model.
2. Connect a test voltage v_t on port with V_{in} . Do nothing on output port.
3. Derive i_t .
4. Calculate $R_{in} = \frac{v_t}{i_t}$

Exercise 3

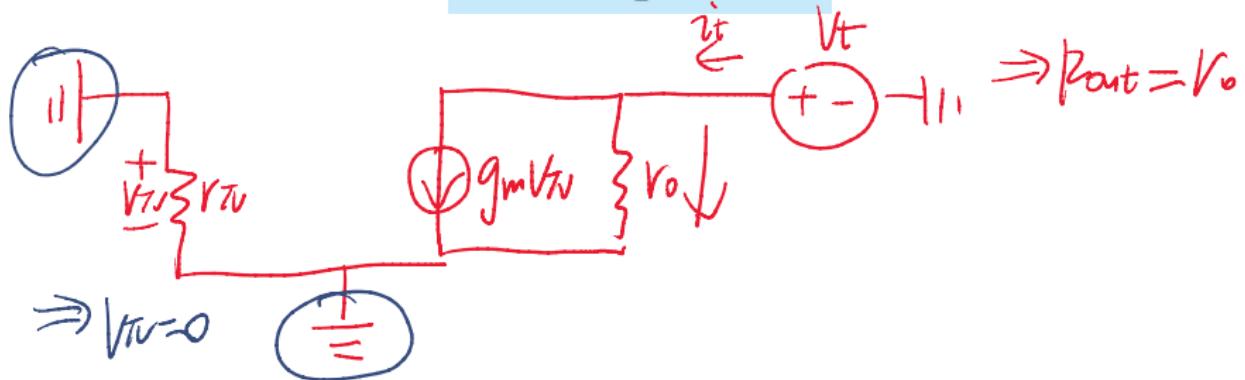
Assuming that the BJT operates in the forward active region, determine the impedance seen into the collector of Q1. Please consider the Early effect ($\beta V_A \gg 1$)

$$\textcircled{1} \quad V_{in} \rightarrow \text{ground}$$

$$\textcircled{2} \quad V_{out} \rightarrow V_t$$



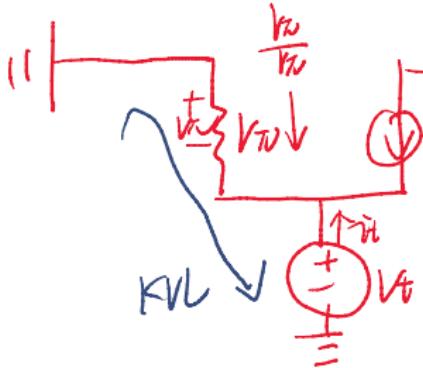
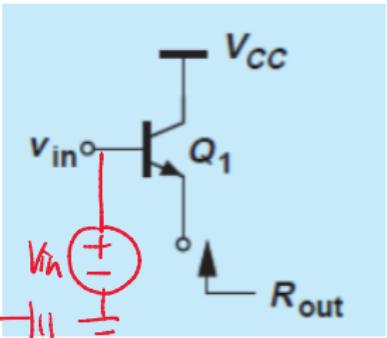
$$\begin{aligned} \text{rel: } i_t &= \frac{V_t}{R_o} + g_m V_{in} \\ &= \frac{V_t}{R_o} \end{aligned}$$



Exercise 4

Assuming that the BJT operates in the forward active region, determine the impedance seen at the emitter. Please neglect the Early effect for simplicity.

V_A is infinite



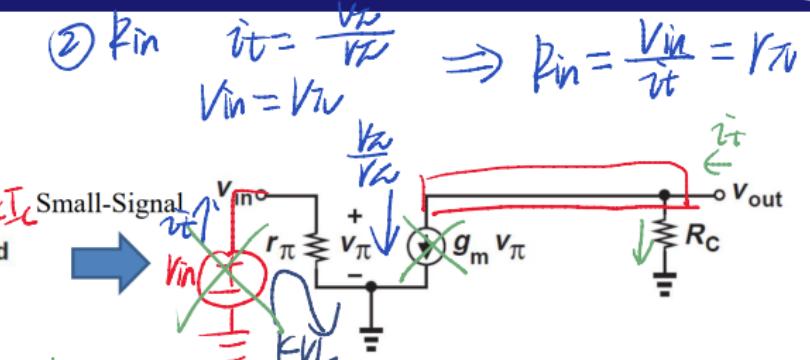
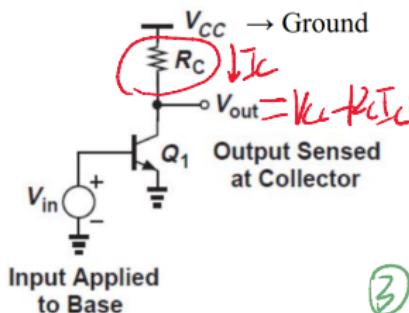
$$\begin{aligned} \text{KCL: } i_t + \frac{V_{BE}}{V_A} + g_m V_B &= 0 \\ \Rightarrow i_t &= -\frac{V_{BE}}{V_A} - g_m V_B \end{aligned}$$

$$\begin{aligned} \text{KVL: } V_{BE} + V_t &= 0 & = \frac{1}{\frac{1}{V_A} + g_m} \\ \Rightarrow V_{BE} &= -V_t & = V_{BE} || \frac{1}{g_m} \\ \therefore f_{out} &= \frac{V_t}{V_t} = \frac{V_t}{V_{BE} + g_m V_B} & = V_{BE} || \frac{1}{g_m} \end{aligned}$$

Overview

- 1 Diode and Diode Circuit
- 2 BJT
- 3 BJT Common-Emitter Amplifier

CE Amplifier (Without Early Effect)



① A_v

$$KVL: -V_{in} + V_{in} = 0$$

$$\Rightarrow V_{in} = V_{in}$$

$$KCL: \frac{V_{out}}{R_C} + g_m V_{in} = 0$$

$$③ R_{out}$$

$$i_t = \frac{V_{out}}{R_C}$$

$$\Rightarrow R_{out} = R_C$$

$$A_v = \frac{V_{out}}{V_{in}} = -g_m R_C \quad (16)$$

$$R_{in} = r_\pi = \frac{\beta}{g_m} = \frac{\beta V_T}{I_C}$$

$$\Rightarrow V_{out} = -g_m V_{in} R_C$$

$$\Rightarrow A_v = \frac{V_{out}}{V_{in}} = -g_m R_C \quad (18)$$

CE Amplifier (Without Early Effect)



$$A_v = -g_m R_C$$

$$\uparrow I_C = I_S e^{\frac{V_{BE}}{V_T}}$$

$$\downarrow V_{out} = V_{CC} - R_C I_C \uparrow$$

Important properties of the CE stage:

1. The small-signal gain is negative, i.e. $V_{BE} \uparrow$ and $I_C \uparrow$ lower V_{out} .
2. The voltage gain of the stage is limited by the supply voltage.

$$g_m = \frac{I_C}{V_T} \quad \text{voltage drop across } R_C$$

$$|A_v| = g_m R_C = \frac{I_C R_C}{V_T} \quad I_C R_C < V_{CC} \quad (19)$$

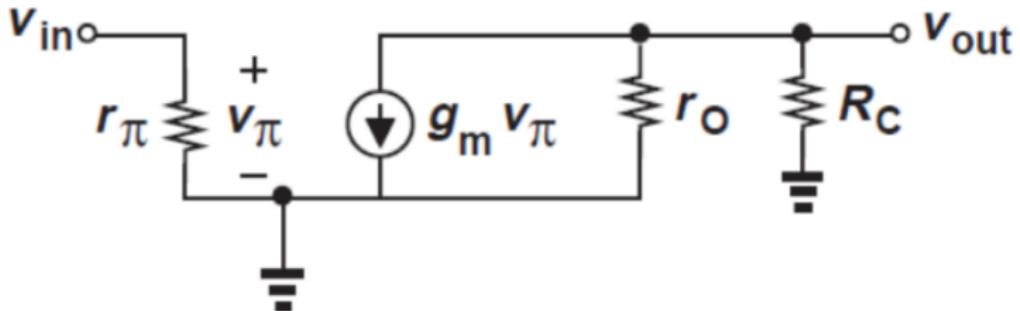
$I_C R_C$ indicates the voltage drops at the collector resistor R_C . Because $I_C R_C < V_{CC}$, $|A_v| < \frac{V_{CC}}{V_T}$. Finally, as the BJT is in the active region, we can say that, $|A_v| < \frac{V_{CC} - V_{BE}}{V_T}$.

However, when $R_C \rightarrow \infty$, $|A_v| \rightarrow \infty$. Contradiction!

$$|A_v| < \frac{V_{CC}}{V_T} \quad \begin{matrix} \text{finite} \\ \text{value} \end{matrix}$$

$R_C \rightarrow \infty$, $|A_v| = g_m R_C \rightarrow \infty$
Contradiction
 \Rightarrow early effect

CE Amplifier (With Early Effect)



$$A_v = \frac{V_{out}}{V_{in}} = -g_m \underbrace{(R_C \parallel r_o)}_{(20)}$$

$$\underline{R_{in} = r_\pi} = \frac{\beta}{g_m} = \frac{\beta V_T}{I_C} \quad (21)$$

$$\underline{R_{out} = R_C \parallel r_o} \quad (22)$$

CE Amplifier (With Early Effect)

$$R_{out} = R_C \| r_o \rightarrow r_o \quad A_v = -g_m (R_C \| r_o) \rightarrow -g_m r_o$$

If $R_C \rightarrow \infty$, $A_v = \underline{-g_m r_o}$ → intrinsic gain

Because

$$g_m = \frac{I_C}{V_T} \quad (23)$$

and

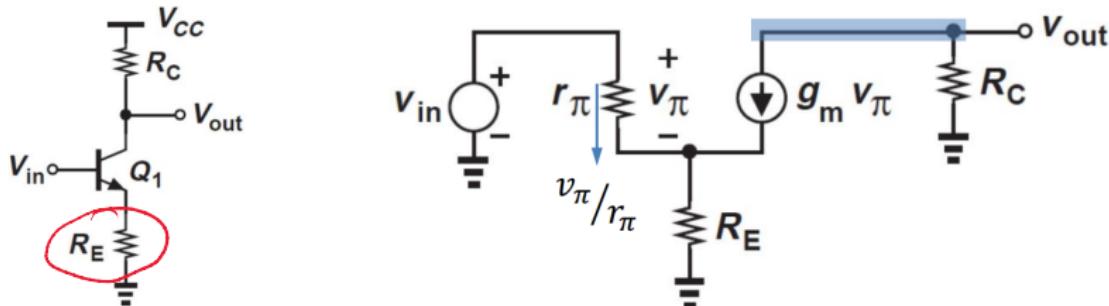
$$r_o = \frac{V_A}{I_C}, \quad (24)$$

we can get

$$\underline{A_v = -\frac{V_A}{V_T}} \quad \text{finite} \quad (25)$$

The Early effect limits the voltage gain even if R_C approaches infinity.

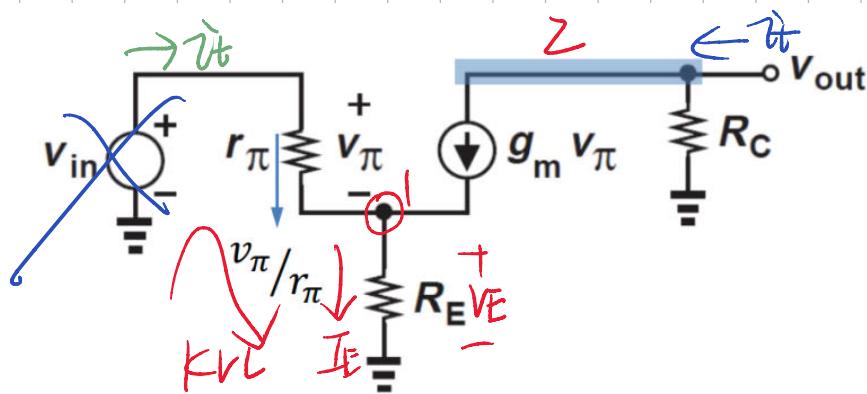
CE Stage With Emitter Degeneration (Without Early Effect)



$$A_v = \frac{V_{out}}{V_{in}} = \frac{-g_m R_C}{1 + (\frac{1}{r_\pi} + g_m) R_E} \quad (26)$$

$$R_{in} = r_\pi + (\beta + 1) R_E \quad (27)$$

$$R_{out} = R_C \quad (28)$$



① A_v

$$KVL: -V_{in} + V_{\pi} + \underline{V_E} = 0 \quad \checkmark$$

$$KCL1: \frac{V_{\pi}}{r_{\pi}} + g_m V_{\pi} = I_E \quad \checkmark$$

$$KCL2: \frac{V_{out}}{R_C} + g_m V_{\pi} = 0 \Rightarrow V_{out} = -g_m R_C V_{\pi}$$

$$V_{in} = V_{\pi} + R_E \left(\frac{V_{\pi}}{r_{\pi}} + g_m V_{\pi} \right)$$

$$= V_{\pi} \left[1 + R_E \left(\frac{1}{r_{\pi}} + g_m \right) \right]$$

$$V_{out} = -g_m R_C \frac{V_{in}}{1 + R_E \left(\frac{1}{r_{\pi}} + g_m \right)}$$

$$\Rightarrow A_v = - \frac{g_m R_C}{1 + R_E \left(\frac{1}{r_{\pi}} + g_m \right)}$$

② R_{in}

$$\hat{i}_t = \frac{V_{in}}{r_{\pi}}$$

$$KVL: -V_{in} + V_{\pi} + V_E = 0$$

$$KCL: \frac{V_{\pi}}{r_{\pi}} + g_m V_{\pi} = I_E$$

$$\Rightarrow V_{in} = V_{\pi} + \underline{V_E} = R_E I_E$$

$$= V_{\pi} \left[1 + R_E \left(\frac{1}{r_{\pi}} + g_m \right) \right]$$

$$\Rightarrow R_{in} = \frac{V_{in}}{\hat{i}_t} = r_{\pi} \left[1 + R_E \left(\frac{1}{r_{\pi}} + g_m \right) \right]$$

$$= r_{\pi} + R_E \left(1 + \cancel{r_{\pi} g_m} \right) = \beta$$

$$= r_{\pi} + R_E (1 + \beta)$$

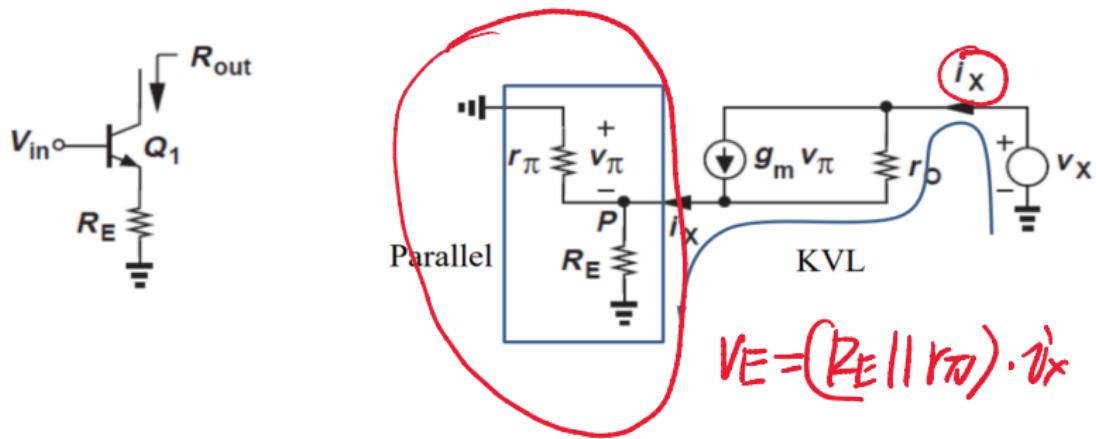
③ R_{out}

$$\hat{i}_t = g_m V_{\pi} + \frac{V_{out}}{R_C}$$

$$R_{out} = \frac{V_{out}}{\hat{i}_t} = R_C$$

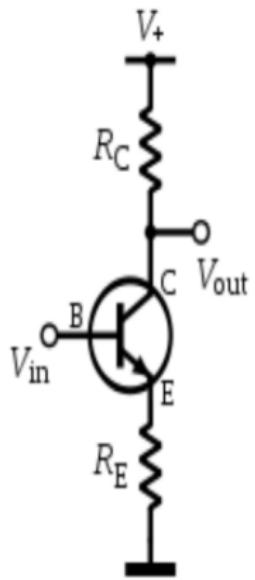
$$KVL: V_{\pi} + V_E = 0 \Rightarrow V_{\pi} = 0$$

CE Stage With Emitter Degeneration (With Early Effect)



$$R_{out} = r_o + (g_m r_o + 1)(R_E \parallel r_\pi) \approx r_o[1 + g_m(R_E \parallel r_\pi)] \quad (29)$$

Summary



	Definition	Expression	
		With emitter degeneration	Without emitter degeneration; i.e., $R_E = 0$
Current gain	$A_i \triangleq \frac{i_{\text{out}}}{i_{\text{in}}}$	β	β
Voltage gain	$A_v \triangleq \frac{v_{\text{out}}}{v_{\text{in}}}$	$-\frac{\beta R_C}{r_\pi + (\beta + 1)R_E}$	$-g_m R_C$
Input impedance	$r_{\text{in}} \triangleq \frac{v_{\text{in}}}{i_{\text{in}}}$	$r_\pi + (\beta + 1)R_E$	r_π
Output impedance	$r_{\text{out}} \triangleq \frac{v_{\text{out}}}{i_{\text{out}}}$	R_C	R_C

Suggestion

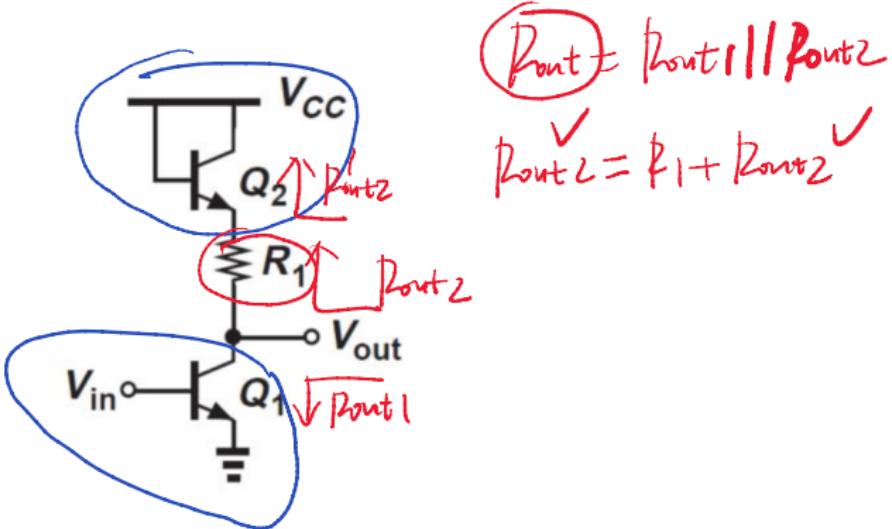
Suggestion:

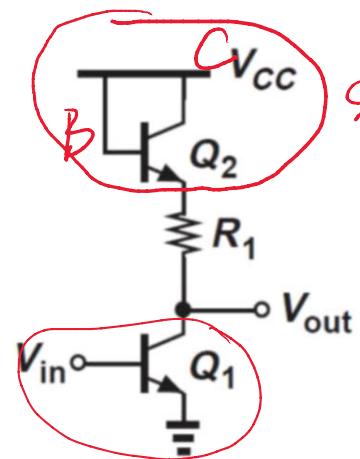
- ▶ Remember the general case
- ▶ First identify B, C, E port
- ▶ Know how to analyze small signal model
- ▶ Understand all the exercise in lecture slides
- ▶ Don't ignore some small values too easily! Be careful!

r_o

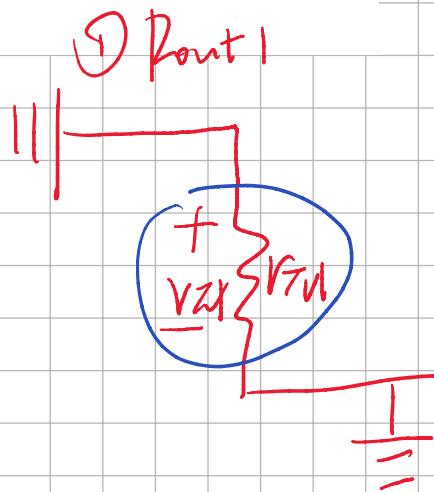
Exercise 5

(23FA Mid/5) Using a small-signal model, determine output impedance of the circuit shown below with and without Early effect. [10 points]





self-biased

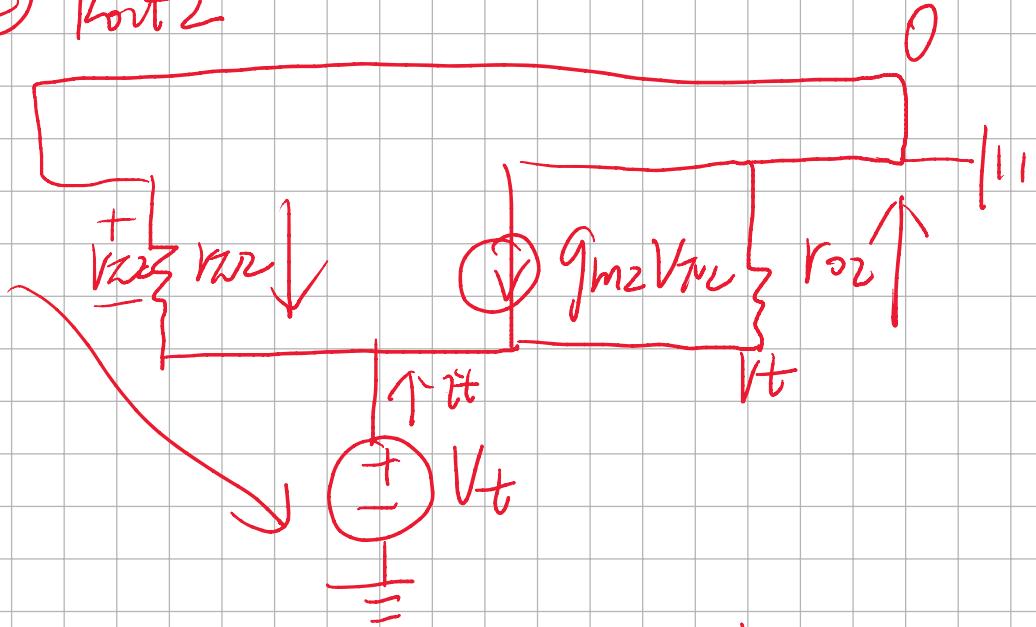


$$V_{TU1} = 0$$

$$\dot{i}_t = \frac{V_t}{R_{o1}}$$

$$\Rightarrow R_{out1} = \frac{V_t}{\dot{i}_t} = R_{o1}$$

② Rout2



$$\dot{i}_t + \frac{V_{Z22}}{R_{Z22}} + g_{m2}\dot{V}_{t2} = -\frac{V_t - 0}{R_{o2}}$$

$$\Rightarrow \dot{i}_t = \frac{V_t}{R_{o2}} - \frac{V_{Z22}}{R_{Z22}} - g_{m2}V_{t2}$$

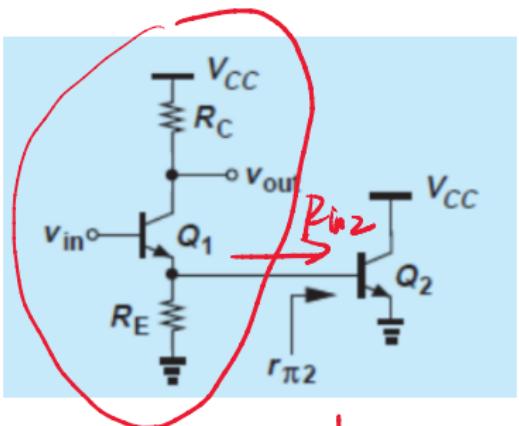
$$KVL: V_{Z22} + V_t = 0 \Rightarrow V_{Z22} = -V_t$$

$$\Rightarrow \dot{i}_t = V_t \left(\frac{1}{R_{o2}} + \frac{1}{R_{Z22}} + g_{m2} \right)$$

$$\Rightarrow R_{out2} = \frac{1}{\frac{1}{R_{o2}} + \frac{1}{R_{Z22}} + g_{m2}} = R_{o2} || R_{Z22} || \frac{1}{g_{m2}}$$

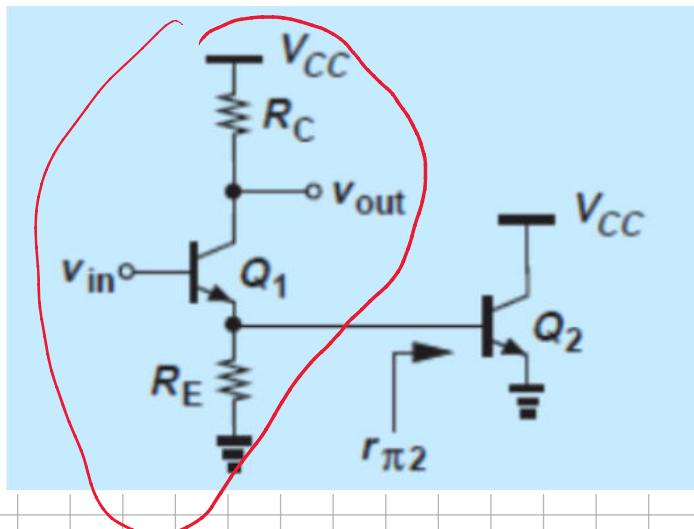
Exercise 6

Determine the voltage gain of the stage shown below. No Early effect



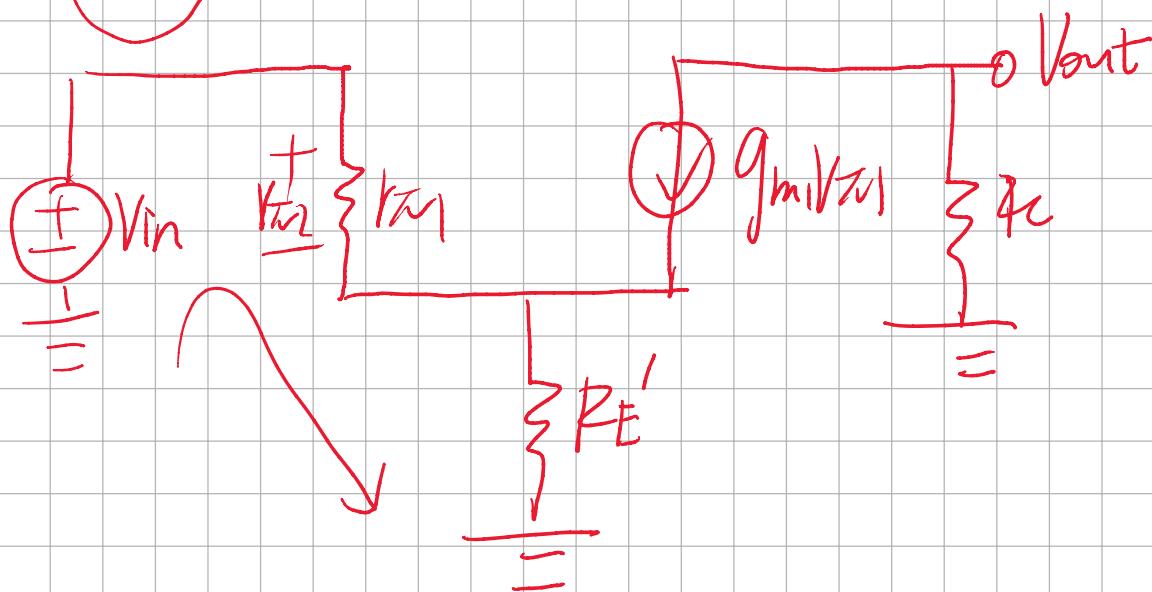
$$\begin{aligned} R'_E &= R_E \parallel R_{in2} \\ &= R_E \parallel r_{\pi2} \end{aligned}$$

$$\begin{aligned} \text{Input circuit: } & V_A \xrightarrow{\rightarrow 2i} V_{in} - V_{in2} \parallel r_{\pi2} \\ & \text{Output circuit: } \left(g_m r_{\pi2} \parallel R_{in2} \right) \parallel R'_E \\ & i_o = \frac{V_{in2}}{R_{in2}} \\ & \Rightarrow R_{in2} = V_{in2} \end{aligned}$$



$$KCL: \frac{V_{out}}{R_C} + g_m V_{in} = 0$$

$$\Rightarrow \frac{V_{out}}{V_{in}} = -\frac{g_m R_C}{1 + (R_E || r_{\pi 2})(r_{\pi 2} + g_m)}$$

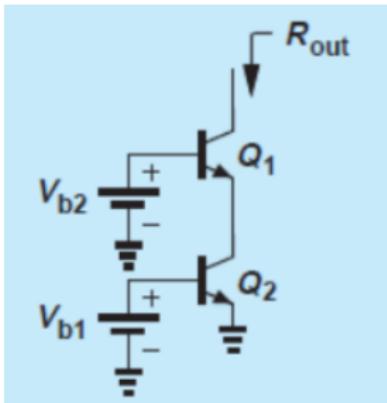


$$KVL: -V_{in} + V_{in} + I_E \cdot R_E' = 0$$

$$KCL: \frac{V_{in}}{R_{\pi 2}} + g_m V_{in} = I_E$$

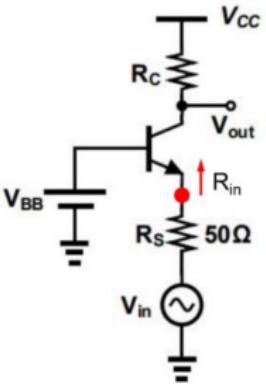
Extra Exercise 1

Determine the output resistance of the circuit below. With Early Effect.



Extra Exercise 2

(23FA Mid/9) The figure below shows a BJT amplifier. Assume $V_{BE} = 0.7$ V, $V_T = 25$ mV, β is very large (to be infinity). No Early effect. [15 points]



- (a) Draw the small signal model and derive the gain for the amplifier.
 [5 points]

Extra Exercise 2

- (b) Find values of V_{BB} and R_C to have a gain of 20 and a matched resistance of 100Ω at the input, i.e. $R_{in} = 100 \Omega$ from the point above R_S . [5 points]
- (c) By cascading another BJT circuit to the circuit in part b as shown below, find the total parametric gain of the amplifier. [5 points]

