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## COMPUTING PHD

#### COMPUTATIONAL MATH SCIENCE AND ENGINEERING

Comprehensive Exam Synthesis Paper

# Modeling ice-ocean interaction

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#### 1 Introduction

The Antarctic and Greenland ice sheets, glaciers are the important components of the global climate system. Over the past decades, the anthropogenic forces due to human activities have caused the atmosphere and especially the ocean to warm (Noble et al., 2020); as a result, its leads to mass loss in the global ice sheets, glaciers, and sea ice. According to Straneo and Heimbach (2013) the mass loss from the Greenland ice sheets quadrupled over the past two decades, contributing to the observed global sea-level rise. The authors also found that the ice loss in Greenland is twice that from the Antarctic ice sheets; this ice loss increased due to both increased surface melting and ice discharge to the ocean. The latter is attributed to the acceleration of ice flow and thinning of fast-flowing marine-terminating outlet glaciers (Nick et al., 2013). Although outlet glaciers extend far into the ice sheet's interior, much work has focused on the terminal boundary at the ocean, as this is where changes in mass balance have been most significant. The Widespread changes in surface melt and ice flow indicate a response to external forcings and are consistent with observations of atmospheric and oceanic evolution over and around Greenland (Box et al., 2009; Bersch et al., 2007; Straneo and Heimbach, 2013). Changes in precipitation and increasing air temperatures are the external forcings that have led to increased surface melting of the ice sheet (van den Broeke et al., 2009; Straneo and Heimbach, 2013). However, the processes behind the increased ice discharge remain elusive. The acceleration of the glaciers is a result of the initial retreat of the marine terminations that decreased the flow resistance of the ice (Nick et al., 2009). The central hypothesis supporting initial glacier retreat involves increased submarine melting of the ice-ocean interface (Straneo et al., 2013). Oceanrelated reduction of Greenland glacier calving faces have been observed over the past two decades (e.g., Rignot et al. (2010); Straneo and Cenedese (2015); Schaffer et al. (2017)). Progress has been made through field observations, modeling, and theoretical studies to understand the mechanisms of ice-ocean interaction and examine the plausibility of the hypothesis. However, the question regarding the submarine melting remains, as the field observation are limited.

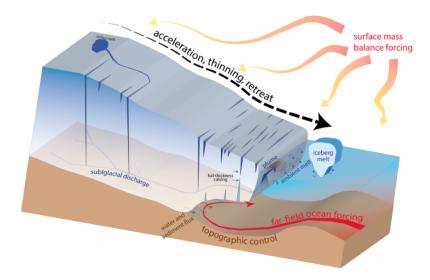


Figure 1: Source Catania et al. (2020). Conceptual diagram of outlet glacier processes that play in the terminal zone where the atmosphere, ice sheet, bedding and ocean interact. The red arrow indicates ocean thermal forcing occurring at depth in the fjords. The black arrow indicates that dynamic changes in outlet glaciers are more pronounced toward the end of the glacier. The blue arrows indicate subglacial water, which rises at the submarine terminus and rises along the end face, carrying sediment and nutrients with it (brown arrows). Subglacial plumes, melting icebergs, and distant ocean circulation all influence the circulation in the fjords (Catania et al., 2020).

The mass balance of ice sheets, glaciers that have marine termini is partially determined by the interaction between ice and ocean (Jenkins, 2011), and the region where that interaction occurs might include the base and front of a floating extension of the grounded ice. Different authors have done many works to understand some of the processes in ice-ocean interaction, ice base melting. Jenkins (2011) studied the convection-driven melting near the grounding lines of ice shelves and tidewater glaciers. The focus of their work was on the plumes generated by the meltwater from the ice shelves. Kerr and McConnochie (2015), and Gayen et al. (2016) worked on the convection at the vertical ice face dissolving where the focus was on the buoyancy-controlled dissolving. Gayen et al. (2016) solved the Navier-Stokes equations for turbulent flow at a vertical ice-ocean interface at a scale similar to that obtained in the laboratory using Direct Numerical Simulations. They found good agreement with Kerr and McConnochie (2015) experiments, consistent with buoyancy controlling the width of the interfacial sublayer. The basal ice melting is a significant component of mass loss from the Antarctic ice sheet (Pritchard et al.; Malyarenko et al., 2020). However, projections of Antarctic contributions under future warming global and regional climate scenarios have significantly higher uncertainty due to poorly understood processes that could lead to rapid ice melting or discharge (Weertman, 1974; DeConto and Pollard, 2016; Gwyther et al., 2020). Therefore, more studies have to be done to understand basal melting better, address the uncertainty in current contributions, and improve future projections of Antarctic contributions.

Jenkins (2011) emphasized that most melting estimates near the ice shelf grounding line have been based on observations of ice flux. Also, on the assumption of a steady-state, calculated melting or freezing and known surface ablation or accumulation balance the convergence or divergence of ice flux. Results suggest melt rates ranging from a few meters to a few tens of meters per year, with peak either at the grounding line or a short distance downstream (Jenkins and Doake, 1991; Rignot and Jacobs, 2002; Jenkins, 2011). Melting of the vertical calving front of a tidewater glacier is more challenging to observe; however, the net supply of meltwater to the ocean from observations of water properties in the fjord in front of LeConte Glacier front was melting at over 10 m per day (Motyka et al., 2003). Ocean circulation models under ice shelves can capture the large-scale characteristics of buoyancy-driven overturning circulation and reproduce the observed distribution of melting and freezing under ice shelves (Jenkins and Holland, 2002; Jenkins, 2011). However, the resolution of all processes operating at the grounding line is generally beyond the capabilities of most ocean circulation models.

## 2 Plume dynamics

Much of the meltwater from the ice sheets, glaciers, ice caps are discharged directly into the ocean at depth, generating buoyant plumes that move up the ice-ocean interface and merge with the surrounding ocean water (Hewitt, 2020). The dynamics of these plumes are essential in regulating the heat transfer that drives submarine melt and controlling the depth to which glacial meltwater is exported to the open ocean. Therefore, they are crucial in the ice sheet response to ocean warming (Joughin et al., 2012; Hewitt, 2020) and the ocean response to ice sheet melt Straneo and Heimbach (2013).

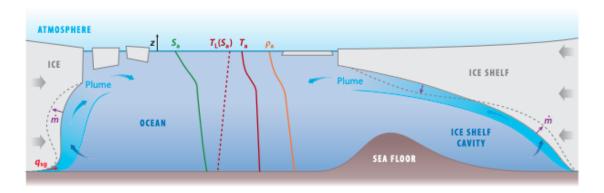


Figure 2: Source Hewitt (2020). Plumes occur at the front of tidewater glaciers and beneath floating ice shelves. Subglacial discharge  $q_{sg}$  (red arrow) and submarine melting m (purple arrows) produce buoyant water that rises up the ice front, entraining warmer ocean water. Typical profiles of ambient salinity  $S_a$ , temperature  $T_a$ , and density  $\rho_a$ , as well as liquidus  $T_L(S_a)$ , are shown. The plume controls the melt rate and hence the shape of the ice—ocean interface. It can reach a level of neutral buoyancy and separate from the ice front, controlling the depth at which glacially modified water is exported to the open ocean. Decompression raises the freezing point so the plume can become supercooled, resulting in freeze-on of marine ice to the ice shelf base and creating cold waters that subsequently sink to produce Antarctic Bottom Water (Hewitt, 2020).

As depicted in figure 3, the plumes form at the near-vertical front of tidewater glaciers and beneath relatively low-slope ice shelves. The former is typical of Greenland, while the latter is typical of the Antarctic ice sheet. According to Hewitt (2020), on tidewater glaciers, melting driven by plumes affects the shape of the front; thus plays an essential role in the calving of icebergs. Under ice shelves, melt and freezing affect the shape of the ice shelf, which significantly affects the location of the grounded line and the flow of ice across it.

Seawater in the vicinity of the ice is within a few degrees of freezing point and is a mixture of water of different origins and properties. A common assumption is that the only source of buoyancy that acts to stratify the water column and drive the overturning circulation in the ice cavity is the generation of meltwater at the ice-seawater interface (Jenkins, 2011). However, in a critical region such as Greenland, where outlet glaciers are grounded several hundred meters below sea level and terminate in a narrow fjord, freshwater will flow across the grounding line from the glacier bed. In Greenland, there are no direct observations of glaciers. However, theory and models indicate that the boundary layer is dominated by buoyant plumes driven by freshwater release from the surface melt at the ice sheet's base and from grounding line melt along along the glacier face (Jenkins, 2011; Straneo and Heimbach, 2013).

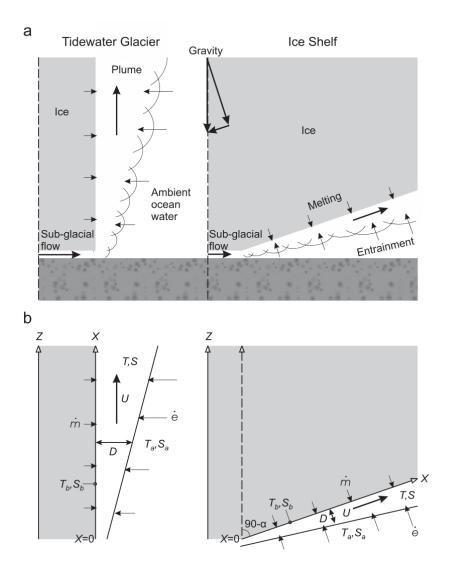


Figure 3: Source Jenkins (2011). (a) Conceptual representation of a buoyant plume from freshwater flow at the grounding line of an ice shelf or tidewater glacier and (b) schematic picture of the numerical representation of (a) with the key variables defined. The plume rises on the ice face, entraining seawater in its way. The entrained seawater provides the heat that drives the melting of the ice face, and the meltwater thus derived adds to the buoyancy of the plume. Near the grounding line, most of the freshwater carried in the plume will be provided by subglacial flow, although freshwater provided by melt will dominate with sufficient downstream evolution (Jenkins, 2011).

Simple one-dimensional models provide valuable insights and scaling arguments. Plume theory was initially developed by Morton et al. (1956) to study convection driven by point sources of buoyancy and then applied by Ellison and Turner (1959) in a slightly modified form to the case where buoyancy-driven flow is constrained to follow a solid boundary. MacAyeal (1985) was the first to apply this concept to large-scale circulation beneath ice shelves. According to Jenkins (2011), the main characteristic of all plumes is that their volume flux increases with height by the entrainment of fluid from the surroundings. The approach present here was used in the work of (Jenkins, 2011). It accounts for all observed melting near the grounding lines. The only difference from previous applications is that the dominant source of buoyancy is defined by the initial conditions rather than the later evolution of the plume. The model describes mass, momentum, heat, and salt conservation and considers plume thickness D, velocity U, salinity S, and temperature T as prognostic variables

$$\frac{d}{dX}(DU) = \dot{e} + \dot{m}$$

$$\frac{d}{dX}(DU^2) = D\left(\frac{\rho_a - \rho}{\rho_0}\right)g\sin\alpha - C_dU^2$$

$$\frac{d}{dX}(DUT) = \dot{e}T_b + \dot{m}T_b - C_d^{1/2}U\gamma_T(T - T_b),$$

$$\frac{d}{dX}(DUS) = \dot{e}S_b + \dot{m}T_b - C_d^{1/2}U\gamma_S(S - T_b),$$

where  $\alpha$  is the angle of the ice shelf base from the horizontal,  $\dot{m}$  is the melt rate, and the subscripts indicate conditions in the ambient water column a and conditions at the ice—ocean interface b.  $\gamma_T$  and  $\gamma_S$  is referred as temperature and salinity exchange velocity respectively,  $C_d$  is a dimensionless drag coefficient. We will discuss about the melt rate, and the ice-ocean interface properties further in the following section.

Wells and Worster (2008) also developed a detailed model for a plume rising along a vertical wall, suggesting two transitions. The first from a laminar state to a turbulent regime with a sublayer width set by the Rayleigh number  $R_a = g'\delta^3/\kappa\nu$  with  $g' = (\rho - \rho_0)g/\rho_0$  where  $\rho$  is the density,  $\rho_0$  is the reference density, g the gravity and  $\delta$  the molecular sublayer thickness. And then to a second turbulent regime with a sublayer width set by the shear stress of the turbulent external flow, determined by a critical Reynolds number,  $R_e = U\delta/\nu$ . Despite increasing applications on ocean forcing of glaciers in the past decades, they have not been able to cover the region near the grounding line. For example, the grounding line region, such as in the large vertical Tidewater glaciers of southwest and southeast Greenland, extends 5-10 km from the terminus due to vigorous calving, and the glaciers of northern Greenland, with ice tongues that extend several tens of kilometers. Thus, with no exception, these studies have failed to sample the ice-ocean boundary layer where the meltwater plume is expected to rise (Straneo et al., 2012). However, it is possible to better understand the dynamics at the ice-ocean boundary by studying the transformation of ocean waters by the glacier in conjunction with thermodynamic models of ice melt in saline waters (Holland and Jenkins, 1999). This approach was recently applied in different studies (e.g. Jenkins (2011); Gayen et al. (2016); Hewitt (2020)).

### 3 Thermodynamic models of ice-ocean interaction

The aim of modeling the ice-ocean interaction is to obtain a melt rate, interface temperature, and salinity at the ice shelf base as realistic as possible. To determine the characteristics exactly, three physical constraints have to be considered. The interface must be at the freezing point, heat and salt must be conserved at the interface during any phase change (Holland and Jenkins, 1999).

#### 3.1 Freezing point dependence

The freezing point of seawater is a weakly nonlinear function of salinity and a linear function of pressure (Millero, 1978). However, a linearized form is used in most of the studies to simplify the solution to the three-equations system. The relationship between the temperature and salinity at the ice-ocean interface,  $T_b$  and  $S_b$  is given by

$$T_b = aS_b + b + cp_b \tag{1}$$

where  $p_b$  is the pressure at the interface and a, b, c are constants. Equations is valid only in the salinity range 4-40 psu and does not apply to pure freshwater (Holland and Jenkins, 1999).

#### 3.2 Conservation of heat and salinity

The conservation of heat at the interface requires that the divergence of the heat flux balances the source of latent heat resulting from ablation at the interface

$$Q_i^T - Q_a^T = Q_{latent}^T, (2)$$

where  $Q_{latent}^T = -\rho_a \dot{m} L_i$  is the latent heat with  $\rho_a \dot{m}$  representing the mass of ice that melted per unit time.  $\dot{m}$  is the melt rate and  $\rho_a$  is the seawater density. The heat flux at the interface in ice is given by

$$Q_i^T = -\rho_i c_i \kappa_i^T \frac{\partial T}{\partial x},$$

and the heat flux at the interface in water is

$$Q_a^T = -\rho_a c_a \kappa_a^T \frac{\partial T}{\partial x},$$

where  $c_i$ ,  $c_a$  are the specific heat capacities of ice and ocean;  $\kappa_i^T$ ,  $\kappa_a^T$  are the thermal diffusivities of ice and ocean, and  $\rho_i$  is the ice density.

The heat conservation at the interface is then

$$\rho_i c_i \kappa_i^T \frac{\partial T}{\partial x} \bigg|_b + \rho_a c_a \kappa_a^T \frac{\partial T}{\partial x} \bigg|_b = \rho_a \dot{m} L_i. \tag{3}$$

Similarly, the conservation of salinity is given by

$$Q_i^S - Q_a^S = Q_{brine}^S, \tag{4}$$

where  $Q_{brine}^S = \rho_a \dot{m}(S_i - S_b)$  is the salt flux necessary to maintain the interface salinity at  $S_b$ .  $Q_i^S$  is the diffusive salt flux into the ice and the salinity in the ice,  $S_i$  are negligible (Oerter et al., 1992; Gayen et al., 2016) and the salt flux in the water is

$$Q_a^S = -\rho_a \kappa_a^S \frac{\partial S}{\partial x},$$

where  $\kappa_a^S$  is the salinity diffusivity of the seawater. The salt conservation at the interface becomes

$$\rho_a \kappa_a^s \frac{\partial S}{\partial x} \bigg|_{t} = \rho_a \dot{m} S_b. \tag{5}$$

The equations (3) and (5) represent the boundary conditions at the ice-ocean interface. In some studies, the authors also neglect the heat flux into ice,  $Q_i^T$  (eg. Gayen et al. (2016)). The boundary conditions are expressed in terms of melt rate  $\dot{m}$ , salinity,  $S_b$  and temperature,  $T_b$  at the boundary, thus we need to compute them in order to solve the boundary equations.

#### 3.3 Three-equation formulation

The three equations formulation is one of the different approaches used to compute the melt rate, the interface temperature, and salinity. It divides the interface region into ice, the interface of ice-ocean, and the far-field ocean. It describes the conservation of heat equation and salt equation with fluxes across each boundary. This approach was developed by Holland and Jenkins (1999) where the boundary layer is assumed to be laminar. Under this assumption the temperature and salinity would vary linearly between the interface and the mixed temperatures, so we have

$$Q_a^T = -\rho_a c_a \gamma_T (T_b - T_a), \tag{6}$$

and

$$Q_a^S = -\rho_a \gamma_S (S_b - S_a), \tag{7}$$

where  $\gamma_T$  and  $\gamma_S$  is referred as temperature and salinity exchange velocity respectively. The exchange velocities can be either assumed constant or as function dependence on friction velocity, we refer to (Holland and Jenkins, 1999) for the their parameterization. The temperature gradient for the ice at the ice-ocean interface is given by

$$\left. \frac{\partial T}{\partial x} \right|_b = \frac{\rho_a \dot{m}}{\rho_i \kappa_i^T} \left( T_i - T_b \right). \tag{8}$$

By using the approximation of the heat and salt gradient at the interface, we obtain the three-equation formulation as

$$T_b = aS_b + b + cp_b (9)$$

$$c_i V \left( T_i - T_b \right) + c_a \gamma_T (T_a - T_b) = \dot{m} L_i \tag{10}$$

$$\gamma_S(S_a - S_b) = \dot{m}S_b. \tag{11}$$

After some algebraic, we solve for  $S_b$  and find that

$$AS_b^2 + BS_b + C = 0, (12)$$

where

$$A = a(c_a\gamma_T - c_i\gamma_S),$$
  

$$B = -c_a\gamma_T(T_a - b - cp_b) + c_i\gamma_S(T_i - b - cp_b + aS_a) - \gamma_S L_i,$$
  

$$C = \gamma_S L_i S_a - c_i\gamma_S S_a(T_i - b - cp_b).$$

Although the three-equation formulation is commonly used in recent studies (eg. Gayen et al. (2016); Gwyther et al. (2020) to model the oceanic flux at ice-ocean interface, various approaches have been adopted by some others authors. The one-equation formulation described by equation (1) has been used by (eg. Jenkins and Doake (1991); Holland (1998)) and its formulation is based on the fact that if the upper ocean layer relaxes to the freezing point instantaneously, there is no distinction between the properties of the interface and mixed layer. The disadvantage of using this approach come from the fact that the melting rate cannot be computed from the boundary condition. Jenkins et al. (2010) and Jenkins (2011) used, the two equation formulation define by

$$T_f = aS + b + cp_b (13)$$

$$c_i \dot{m} (T_i - T_f) + c_a c_d^{1/2} \gamma_{TS} (T_a - T_f) = \dot{m} L_i$$
 (14)

(15)

where  $T_f$  is the freezing temperature of the plume, and  $c_d^{1/2}\gamma_{TS}$  is called Stanton number. Jenkins et al. (2010) shows that the observation of water and melt properties at a Ronne Ice Shelf site can be fitted using either the three-equation or two-equation formulation. One advantage is its use to determine the melting rate.

Now, with the formula of the melt rate, temperature and salinity at the interface, the boundary conditions, equations (3) and (5) can be rewritten as follows by neglecting the heat flux into ice

$$\frac{\partial T}{\partial x}\Big|_{b} = -\lambda_1 T\Big|_{b} + \lambda_1 T_a, \quad \lambda_1 = \frac{\gamma_T}{\rho_a \kappa_T},$$
 (16)

for the temperature and

$$\frac{\partial S}{\partial x}\Big|_{b} = -\lambda_{2}S\Big|_{b} + \lambda_{2}S_{a}, \quad \lambda_{2} = \frac{\gamma_{S}}{\rho_{a}\kappa_{S}}.$$
 (17)

for salinity.

#### 4 Vertical ice face

There have been several studies on quantifying the melt rate in the region dominated by freshwater discharge (Wells and Worster, 2011; Kerr and McConnochie, 2015; Gayen et al., 2016). The melting rate depends not only on the thermal and salt diffusivities but also on the structure of the boundary layer. In the laminar regime, the melting rate is lower due to the thicker thermal boundary layer. At the same time, within the transition region, the interface temperature and melting rate increase rapidly with the rising plume (Gayen et al., 2016). Kerr and McConnochie (2015) in their work considered vertical ice adjacent to the ocean, the melting rate is controlled by the buoyancy-driven, and it is independent of the depth and plume velocity. They found in their analysis that the melting rate is

$$V = constant \times (T_w - T_L)^{1.34}, \tag{18}$$

which is consistent with the theory prediction. The authors also pointed out that when the ambient temperature exceeds  $3-4^{\circ}C$  above the freezing point temperature, a transition into turbulent melting is approached, and the interface temperature is overestimated. Gayen et al. (2016) solved the Navier-Stokes equations for turbulent flow at a vertical ice-water interface and found good agreement with the experiments of Kerr–McConnochie (2015), consistent with buoyancy controlling the width of the interfacial sublayer. Another theoretical scaling for both vertical and horizontal boundaries suggests the existence of the second regime of turbulent natural convection at high Rayleigh numbers ( $R_a > 10^{16}$ ). During that regime, the thickness of the inner laminar boundary layer near the ice face is controlled by shear production rather than convective production of turbulence (Grossmann and Lohse, 2000; Wells and Worster, 2008; Kerr and McConnochie, 2015; Gayen et al., 2016).

#### 5 Numerical Models

Numerical models that include the thermodynamic interaction between the ocean and the ice sheet are the best option for studying current and future Antarctic contributions to sea level (e.g. ROMS: Dinniman et al. (2007); MITgcm: Losch (2008); FESOM: Timmermann et al. (2012); COCO: Kusahara and Hasumi (2013); FVCOM: Zhou and Hattermann (2020)). Fully coupled ice sheet-ocean models will allow a comprehensive study of how ocean-driven basal melting affects Antarctica, but they are still in their infancy for large realistic domains. Therefore, the best current option is ice shelf-ocean models that neglect ice dynamics and assume steady-state ice geometry (Gwyther et al., 2020). These ice shelf-ocean models explore this data-deficient environment by simulating both small-scale processes and the large-scale spatial and temporal evolution of basal melting in Antarctica. In the recent study done by Gwyther et al. (2020) provides a test case for development of ice-ocean model applications; and better understand ice-ocean interactions. The study used three different modeling

frameworks, the Regional Ocean Modeling System (ROMS), the Center for Climate System Research Ocean Component Model (COCO), and the Model for Predictions Across Scales: Ocean (MPAS-O).

According to the results of Gwyther et al. (2020), there are significant differences in the basal melting rate between these models, especially with COCO and MPAS compared to ROMS. Melting is lower in ROMS by a factor of two compared to COCO and MPAS-O. In addition, the ROMS model shows lower thermal entrainment (difference between the ambient ocean water temperature  $T_a$  and the pressure freezing point  $T_f$ ) across the ice shelf than COCO and MPAS-O models. According to the authors, the main reason for these results in ROMS is its higher vertical resolution. Their results also suggest a strong sensitivity of melt rates to the choice of vertical resolution, discretization, and boundary layer parameterization that could reasonably affect the sensitivity of the melt rate to changes in ocean forcing. Many authors recognize the limitations of the current treatment of the ice-ocean boundary layer that results in a resolution dependence in melt rates. Gwyther et al. (2020) suggest that until the complete turbulent process can be solved explicitly, parameterizations of processes in the boundary layer will need to evolve with increased vertical resolution.

Understanding the structure and mechanism that governs the thermodynamics and momentum exchange in the ice-ocean boundary layer is limited by the lack of observations and spatial non-uniformity of the ice-ocean interface. The three-equation formulation that describes the thermodynamics of the ice-ocean interface assumes only vertical flows with no horizontal flows. However, Jenkins 2016 shows that an equilibrium state could be reached only in the boundary layer with a sloping interface and a buoyant plume if spatial gradients were present in properties such as temperature or horizontal velocity. The three-equation formulation has been applied to many ice-ocean models with different vertical configurations. The practical implementation of these parameterizations differs among model settings; thus, the results of ice-ocean simulations with different models may treat this vertical resolution dependence differently (Gwyther et al., 2020). Although the three-equation formulation has been used in many models and studies to quantify melt rate, observations of double diffusive staircases under the George VI ice shelf (Kimura et al., 2015) are an illustration where it has been shown that the three-equation formulation does not accurately resolve melt rate. Davis and Nicholls (2019) showed that the wall law assumption inherent in the three-equation formulation does not hold at low flow rates.

Given the non-uniformity of ice-ocean interactions and non-uniform ice melt, the ice face cannot be planar. Therefore, current numerical models developed based on finite difference and element methods cannot provide an appropriate discretization of the ice face. Thus, a model such as the spectral element method can solve the problem of discretizing the ice interface. The spectral element method has some advantages in ocean modeling, which involves the complex interaction of stratified flows with topography (Ilıcak et al., 2009). The authors suggest that the spectral element method offers good convergence with the refinement of the elemental grid or increasing the order of the interpolation polynomial. The method has no significant numerical dissipation and offers geometric flexibility, especially for problems with complex geometry. Another advantage is the scalability of its code in parallel machines.

## 6 Limitations in ice-ocean interaction modeling

The large-scale numerical models have not been able to cover the region near the grounding line in the region such as in the large vertical tidewater glaciers of Greenland, extends 5-10 km from the terminus. Thus, with no exception, these studies have failed to sample the ice-ocean boundary layer where the meltwater plume is expected to rise (Straneo et al., 2012). Considering the topography of the ice face it will be unrealistic to use most of the current models that are based on the finite different and volume methods to access that topography. Also, for large scale models it may be unrealistic to resolve plumes that are on the order of 10 m. Plume models assume a vertical ice front, but real ice

fronts have a more complicated geometry, partly due to nonuniform submarine melting.

# 7 Future Research Ideas

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