

# Subset Sum (medium)

## We'll cover the following

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- Bottom-up Dynamic Programming
  - Code
  - Time and Space complexity
- Challenge

### Problem Statement #

Given a set of positive numbers, determine if a subset exists whose sum is equal to a given number 'S'.

#### Example 1: #

```
Input: {1, 2, 3, 7}, S=6
Output: True
The given set has a subset whose sum is '6': {1, 2, 3}
```

#### Example 2: #

```
Input: {1, 2, 7, 1, 5}, S=10
Output: True
The given set has a subset whose sum is '10': {1, 2, 7}
```

#### Example 3: #

```
Input: {1, 3, 4, 8}, S=6
Output: False
The given set does not have any subset whose sum is equal to '6'.
```

### **Basic Solution #**

This problem follows the **0/1 Knapsack pattern** and is quite similar to Equal Subset Sum Partition

(https://www.educative.io/collection/page/5668639101419520/5671464854355968/633601277296 6400/). A basic brute-force solution could be to try all subsets of the given numbers to see if any





So our brute-force algorithm will look like:

1 for each number 'i'
2 create a new set which INCLUDES number 'i' if it does not exceed 'S', and recursively
3 process the remaining numbers
4 create a new set WITHOUT number 'i', and recursively process the remaining numbers
5 return true if any of the above two sets has a sum equal to 'S', otherwise return false

Since this problem is quite similar to Equal Subset Sum Partition (https://www.educative.io/collection/page/5668639101419520/5671464854355968/633601277296 6400/), let's jump directly to the bottom-up dynamic programming solution.

## Bottom-up Dynamic Programming #

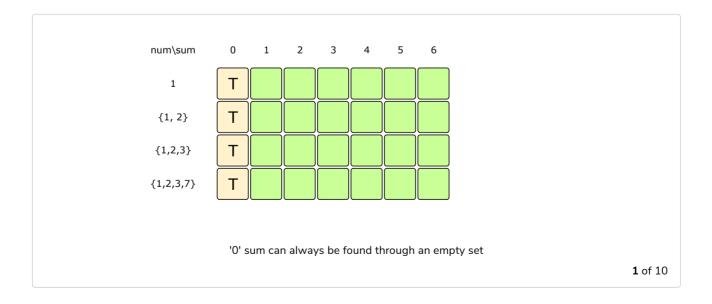
We'll try to find if we can make all possible sums with every subset to populate the array dp[TotalNumbers][S+1].

For every possible sum 's' (where  $0 \le s \le S$ ), we have two options:

- 1. Exclude the number. In this case, we will see if we can get the sum 's' from the subset excluding this number => dp[index-1][s]
- 2. Include the number if its value is not more than 's'. In this case, we will see if we can find a subset to get the remaining sum => dp[index-1][s-num[index]]

If either of the above two scenarios returns true, we can find a subset with a sum equal to 's'.

Let's draw this visually, with the example input {1, 2, 3, 7}, and start with our base case of size zero:







 num\sum
 0
 1
 2
 3
 4
 5
 6

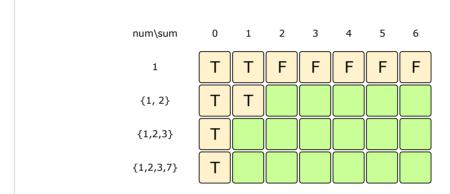
 1
 T
 T
 F
 F
 F
 F

 {1,2}
 T
 T
 T
 T

 {1,2,3}
 T
 T
 T
 T

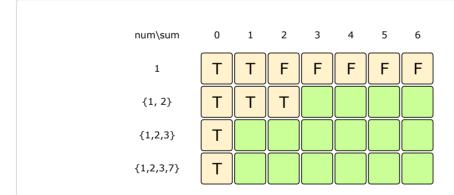
With only one number, we can form a subset only when the required sum is equal to that number

**2** of 10



sum: 1, index:1=> (dp[index-1][sum] , as the 'sum' is less than the number at index '1' (i.e., 1 < 2)

**3** of 10



sum: 2, index:1=> (dp[index-1][sum] || dp[index-1][sum-2])

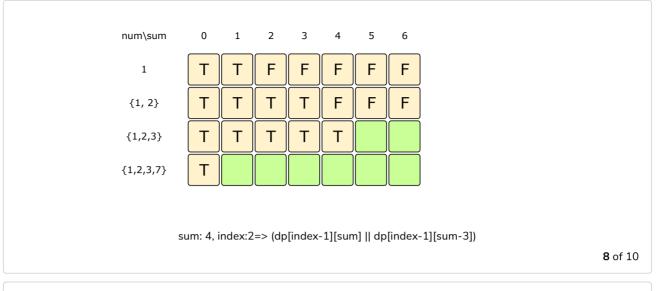
**4** of 10

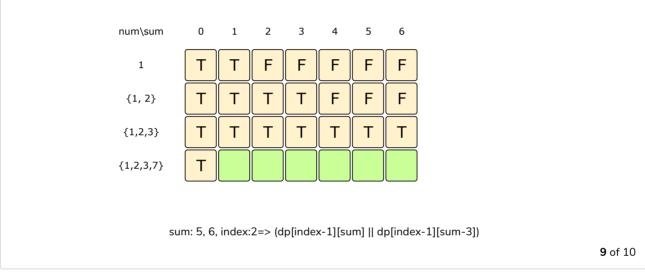


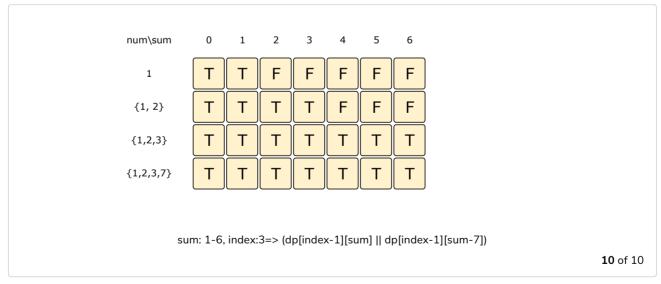












— []

### Code #

Here is the code for our bottom-up dynamic programming approach:



```
def can partition(num, sum):
 2
      n = len(num)
 3
      dp = [[False for x in range(sum+1)] for y in range(n)]
 4
 5
      # populate the sum = 0 columns, as we can always form '0' sum with an empty set
 6
      for i in range(0, n):
 7
        dp[i][0] = True
 8
 9
      # with only one number, we can form a subset only when the required sum is
10
      # equal to its value
11
      for s in range(1, sum+1):
        dp[0][s] = True if num[0] == s else False
12
13
14
      # process all subsets for all sums
15
      for i in range(1, n):
16
        for s in range(1, sum+1):
          # if we can get the sum 's' without the number at index 'i'
17
18
          if dp[i - 1][s]:
19
            dp[i][s] = dp[i - 1][s]
20
          elif s >= num[i]:
            \# else include the number and see if we can find a subset to get the remaining sum
21
            dp[i][s] = dp[i - 1][s - num[i]]
22
23
24
      # the bottom-right corner will have our answer.
25
      return dp[n - 1][sum]
26
27
28
   def main():
                                                                                             ()
\triangleright
```

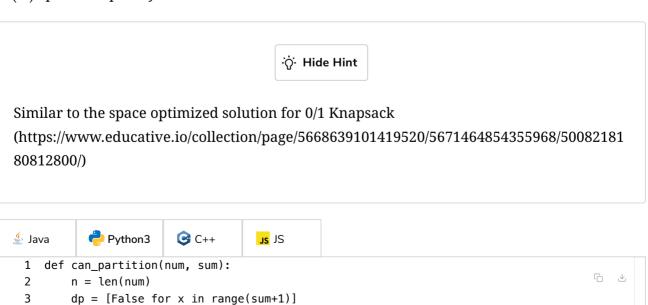
### Time and Space complexity #

The above solution has the time and space complexity of O(N\*S), where 'N' represents total numbers and 'S' is the required sum.

## Challenge #

5

Can we improve our bottom-up DP solution even further? Can you find an algorithm that has O(S) space complexity?



# handle sum=0, as we can always have '0' sum with an empty set

```
б
        apιω] = Irue
 7
        # with only one number, we can have a subset only when the required sum is equa
 8
 9
        for s in range(1, sum+1):
10
            dp[s] = num[0] == s
11
12
        # process all subsets for all sums
        for i in range(1, n):
13
14
            for s in range(sum, -1, -1):
15
                \# if dp[s]==true, this means we can get the sum 's' without num[i], hence we c
16
                # the next number else we can include num[i] and see if we can find a subset t
17
                # remaining sum
18
                if not dp[s] and s >= num[i]:
19
                    dp[s] = dp[s - num[i]]
20
        return dp[sum]
21
22
23
    def main():
24
25
        print("Can partition: " + str(can_partition([1, 2, 3, 7], 6)))
        print("Can partition: " + str(can_partition([1, 2, 7, 1, 5], 10)))
26
        print("Can partition: " + str(can_partition([1, 3, 4, 8], 6)))
27
28
                                                                                              ()
\triangleright
```



Next →

Equal Subset Sum Partition (medium)

Minimum Subset Sum Difference (hard)



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? Ask a Question

(https://discuss.educative.io/tag/subset-sum-medium\_\_pattern--01-knapsack-dynamic-programming\_\_grokking-the-coding-interview-patterns-for-coding-questions)