

## Homework #4 Solutions

### 9.6.1

**Immediate Dominators:**

	B1	B2	B3	B4	B5	B6
idom	Entry	B1	B2	B3	B3	B5

**Dominator Tree:**

B1 -> B2 -> B3 -> B4  
                  |  
                  ---> B5 -> B6

**Retreating Edges:** B4->B3, B5->B2

**Graph is reducible:** All retreating edges are back edges.

**Depth:** 2 (corresponding acyclic path: B4->B3->B5->B2)

**Natural loops:** {B3, B4}, {B2, B3, B4, B5}

### 9.6.6

When  $n \leq 2$ , a complete flow graph on  $n$  nodes is reducible.

### 9.6.7

For all  $n$ , a complete, acyclic flow graph on  $n$  nodes is always reducible because there are no retreating edges and back edges.

Even with self-loops ( $i \rightarrow i$ ), the self-loops are all the retreating edges and at the same time back edges, so the graph is still reducible.