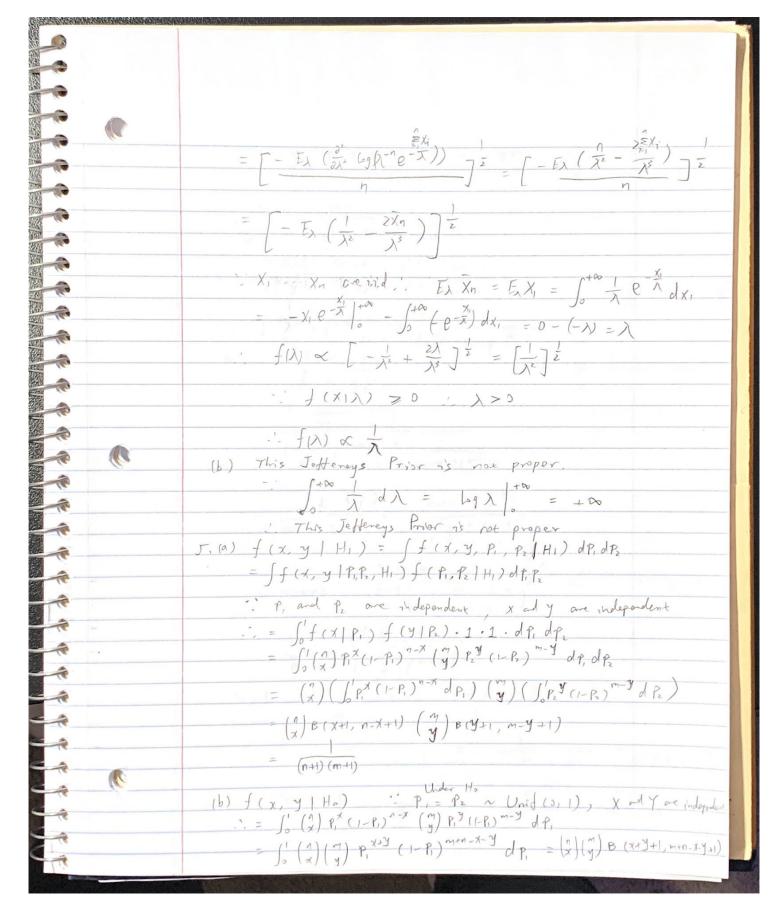
(4)	STAT 2018 Homework 4 Hanze Ya	0
	3033093286	
	$1. (a) f(x x^n) \propto f(x^n x) f(x)$	
	$= \left(\frac{1}{\lambda}\right)^n e^{-\frac{1}{\lambda} \frac{\mathcal{E}}{\mathcal{E}} \chi_i}  \frac{b^{\alpha}}{b^{\alpha}} \lambda^{-\alpha-1} e^{-b/\lambda}$	
	7 (a)	
	$\propto \lambda^{-n} e^{-\frac{1}{\lambda} \sum_{i=1}^{n} x_i} \lambda^{-\alpha-1} e^{-b/\lambda}$	
	7-(n+a)-1 p-1 (EX+b)	
	. f (N/X") also satisfies Inverse Gamma dist	n bu
	$(a',b')$ where $a'=n+a$ $b'=\frac{2}{5}X_1+b$	
	(b) Now the prior mean is a-	V ,
	$\frac{\partial}{\partial \lambda} \log \left( \lambda^{-n} e^{-\frac{\lambda^{-1}}{\lambda}} \right) = \frac{\partial}{\partial \lambda} \left( -n \right) \log \lambda - \frac{\sum_{i=1}^{n} \chi_i}{\lambda} \right) = -n \times \frac{1}{\lambda} + \frac{\sum_{i=1}^{n} \chi_i}{\lambda}$	2
	$\lambda = \frac{1}{n} \sum_{i=1}^{n} X_i = \overline{X}_n$	
	Chack the $\frac{\partial^2}{\partial \lambda^2} \log (\lambda^{-\eta} e^{-\frac{i}{2}\lambda^2}) = \frac{n}{\lambda^2} = \frac{2 + i}{\lambda^2}$	
(2)		
	When $1 = \overline{X}_{1}$ $\frac{\partial^{2}}{\partial x^{2}} (\log (1^{-n} e^{-\frac{1}{2} \frac{x^{2}}{2}}) = n^{2} - 2n^{3}$	-
	$(\underbrace{\xi}_{i} \times_{i})^{2} (\underbrace{\xi}_{i} \times_{i})^{2}$	(8
	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	< 0
	The posterior mean is $b' = \frac{2}{n+a-1} \times \frac{1}{a-1} \times \frac{1}{a-1}$	+
	6.1	
	$\frac{b}{a+1} \rightarrow X_n$ $(n+a-1)$	1
	when n > 20 the posterior mean will be dose to Xn,	
	$(a-1)^2$ $(a-2)$	
	$(m(a-1))^2 = V(a-1)^2(a-2)$	
	$m^{2}(\alpha-1)^{2} = V(\alpha-1)^{2}(\alpha-2)$	
	$\alpha = 2$ $m^2 - \sqrt{(\alpha - 2)}$ $\alpha - 2 = m^2$ $\alpha = mr_2 \sqrt{\alpha}$	
	$b = (a-1) m = (\frac{m+v}{v}) m = \frac{m+mv}{v}$	
	b = W+mV	
	(b) Based on my current knowledge, I have lived in Borkeley for	
	IT month now and I have felt two earthquakes. The time	
	m to be 365. But I completely have no knowledge about	255
	The state of the s	

the prior variance V, So I guess this variance to be V=1000 (C) The R code and the plat of the prior and posterior PDF are on the last page. From the place I can see that the mean & value is a little smaller then my knowledge which is about 310 days. the variance is smaller than my guess too. According to the definition of rejection sampling, the probability of the acceptance of grand is:  $\left( u < \frac{f(x^n) \circ cand}{f(x^n) \cdot \hat{\theta}_n} \right) =$  $f(x^n | \hat{\theta}_n) \Rightarrow M$ WIE of 8 u~ Vif (21))  $M = f(x^n | \theta_n) = \sup f(x^n | \theta_n)$ If  $M < f(x^n | \hat{\theta}_n)$ the probability of the acceptance of a cand min { | f(x) | g cond) } Then When M & f (x" | Dy)
Those probability may not be f(x" to cand) & f ( ) card) P (accopance of g cand Then f (o accep) may not & f (o cond) x f(x) o cond) may not a figured) fix10 cand) may not of ( g cand / xn)

. When M < f (xn 10 cand ), o accept may not satisfy the posterior distribution 4. (a) Obviously  $f(x|\lambda)$  belongs to exponential femily.  $x_1 \quad x_2 \quad x_3 \quad x_4 \quad x_5 \quad x_6 \quad x_$ 



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m! (x+y)! (m+n-x-y)!
               x! (n-x)! y! (m-y)! (m+n+1)!
                  (x+y)! (m+n-x-y)!
                                        (m+n+1)!
                                      (m+n+1) (m+n)
         (C) BF10 = f(x, y 1 H1)
                       7 (x, y | Ho)
                         (m+1) (n+1)
                     (m+n+) (m+n+) (m+n+) (m+n)
1
                                     (m+n+1) (m+n)
                    M+1) (7+1)
                             (m+n+2) (m+n+1) (m+n)! / (m+1) m! (n+1) n!
                                          n-X
                      m+n+2
               Pujols: +146 at bars
         (1)
                            5146+6099+2 (1717+270) (5146+6099-1717-2030
                                                             ~ 0,0222
10
                .. The evidence against Ho and Jersy H, is used
                 So Ht favors Ho
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