MTH 4320 Homework 1

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1 Problem 1

Solution.

We have a triple nested loop and for the outermost loop we run n-1 operations then we run n-1 operations in the inner loop for every operation in the outer loop and so on. The running time is $O(n) \cdot O(n) \cdot O(n) = O(n^3)$.

2 Problem 2

Solution.

We have n-2 operations from the outer loop where n is the input number num. Then we call the is_prime function twice for every operation and the function runs at most n-2 operations every time. The running time is $2 \cdot O(n) \cdot O(n) = O(n^2)$.

3 Problem 3

Solution.

- 1. Store the first element of the input list L in a variable M.
- 2. For every element in L:
 - If it is greater than M then update M with that element.

- 3. We found the first largest element M in L.
- 4. Let N be the first element of L and $N \neq M$.
- 5. For every element in L:
 - If it is greater than N but less than M then update N with that element.
- 6. We found the second largest element N in L.
- 7. Let M := N and N be the first element of L where $N \neq M$.
- 8. Repeat steps 2-6 until we found the 10th largest element M.

The running time is $10 \cdot O(n) + O(1) = O(n)$.

4 Problem 4

Solution.

- 1. Let M be the middle element of the list, L be the first element, and R be the last element.
- 2. If M < x then we update L to the M+1 element else we update R to the M element. Repeat until we find the leftmost x.
- 3. Similarly, we repeat steps 1-2 but we change the condition to $M \le x$ to find the rightmost x.
- 4. The index of the rightmost x minus the index of the leftmost x is the number of times x appears in the list.

The running time is $2 \cdot O(\log n) + O(1) = O(\log n)$.