

Due Date: Saturday, September 5 at 11:59pm

Submit: eLearning

Late Policy: -10 points per hour late

Instructions: This is an individual assignment. Answers should be your own work.

## Chapter 2

6 pts

1. In the definition of Big-O, why is the "for  $N \geq n_0$ " needed?

6 pts

2. If  $f_1(N) = 2N$  and  $f_2(N) = 3N$ , why are they both  $O(N)$ , since  $3N$  is larger than  $2N$  for  $N \geq 1$ ?

6 pts

3. a) For  $f_1(N) = 2N$  and  $f_2(N) = 3N$ :  
calculate  $f_1(5)$  and  $f_2(5)$ , then  $f_1(10)$  and  $f_2(10)$ . When  $N$  was doubled in each case, what happened to the result? Explain why this happens.  
b) For  $f_1(N) = 2N^2$  and  $f_2(N) = 3N^2$ :  
calculate  $f_1(5)$  and  $f_2(5)$ , then  $f_1(10)$  and  $f_2(10)$ . When  $N$  was doubled in each case, what happened to the result? Explain why this happens.

6 pts

4. Since Big-O notation is a mathematical tool for functions like  $f(N)$  or  $g(N)$ , how is it applicable to algorithm analysis?

6 pts

5. Which grows faster,  $2^n$  or  $n!$ ? Explain why.

10 pts (2 each)

6. Give the Big-O notation for the following expressions:

- $4n^5 + 3n^2 - 2$
- $5^n - n^2 + 19$
- $(3/5)^n$
- $3n * \log(n) + 11$
- $[n(n+1)/2 + n] / 2$

Questions 7-12 are 10 points each.

Assume numItems has the role of  $N$ , which may vary from one run to the next.

7. What is the Big-O running time for this code? Explain your answer.

```
for (int i=0; i<numItems; i++)
    System.out.println(i+1);
```

8. What is the Big-O running time for this code? Explain your answer.

```
for (int i=0; i<numItems; i++)
    for (int j=0; j<numItems; j++)
        System.out.println( (i+1) * (j+1) );
```

9. What is the Big-O running time for this code? Explain your answer.

```
for (int i=0; i<numItems+1; i++)
    for (int j=0; j<2*numItems; j++)
        System.out.println( (i+1) * (j+1) );
```

10. What is the Big-O running time for this code? Explain your answer.

```
if ( num < numItems )
    for (int i=0; i<numItems; i++)
    {
        System.out.println(i);
    }
else
    System.out.println("too many");
```

11. What is the Big-O running time for this code? Explain your answer.

```
int i = numItems;
while (i > 0)
    i = i / 2;    // integer division will eventually reach zero
```

12. What is the Big-O running time for this code? Explain your answer.  
(You do not need to work out a recurrence formula).

```
public static int div(int numItems)
{
    if (numItems == 0)
        return 0;
    else
        return numItems%2 + div(numItems/2);
}
```

Submit these files:

hw2.doc (.doc can be .txt, .jpg, etc.)