

Assignment #8

Due Date: Saturday, November 7 at 11:59pm

Submit: eLearning

Late Policy: -10 points per hour late

Instructions: This is an individual assignment. Answers should be your own work.

Chapter 8

100 points total

10 points

1) Given the array below representing disjoint sets, draw the associated trees.

| | | | | | | | | | | | | | | | | | | |
|-------|---|--|---|--|----|--|----|--|---|--|----|--|----|--|---|--|---|--|
| | 2 | | 2 | | -1 | | -1 | | 3 | | -1 | | -1 | | 6 | | 7 | |
| ----- | | | | | | | | | | | | | | | | | | |
| | 0 | | 1 | | 2 | | 3 | | 4 | | 5 | | 6 | | 7 | | 8 | |

15 points

2) Using a set of values from 0 to 5 as separate roots, perform the following unions by making the root of the second tree be a child of the root of the first tree. What do you notice about the resulting tree and what consequence would it have on a find(5)?

```
union(4, 5)
union(3, 4)
union(2, 3)
union(1, 2)
union(0, 1)
```

15 points

3) Using a set of values from 0 to 8 as separate roots, perform the following unions using union-by-size. Show the result of each union. When sizes are the same, make the second tree be a child of the first tree.

Notice the finds return roots, and a union will union two roots.

```
union(find(0),find(2))
union(find(0),find(3))
union(find(0),find(4))
union(find(0),find(7))
union(find(1),find(5))
union(find(6),find(8))
union(find(5),find(8))
union(find(7),find(8))
```

10 points

4) Illustrate the array for the final forest of the previous problem (note that roots are not simply -1 when using union-by-size).

15 points

5) Same as #3, but using union-by-height. When heights are the same, make the second tree be a child of the first tree.

10 points

6) Illustrate the array for the final forest of the previous problem (note that roots are not simply -1 when using union-by-height).

15 points

7) Given the disjoint set array shown, what would the array look like after a find(10) if path compression is used?

| | | | | | | | | | | |
|----|---|---|---|---|---|---|---|---|---|----|
| -1 | 0 | 0 | 2 | 2 | 1 | 1 | 5 | 5 | 8 | 9 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |

10 points

8) Illustrate the trees for the final forest of the previous problem.

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hw8.doc (.doc can be .txt, .jpg, etc.)