```
In [1]: import numpy as np
    from numpy.linalg import inv
    import _pickle as cp
    import matplotlib.pyplot as plt

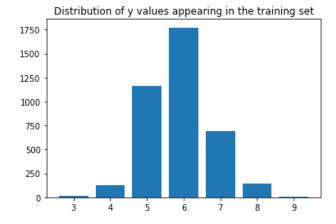
In [2]: X, y = cp.load(open('winequality-white.pickle', 'rb'))

In [3]: N, D = X.shape
    N_train = int(0.8 * N)
    N_test = N - N_train
    X_train = X[:N_train]
    Y_train = y[:N_train]
    X_test = X[N_train:]
    Y_test = y[N_train:]
```

Handin 1

```
In [4]: def categorize(train):
    hist = {}
    for i in train:
        hist[i] = hist.get(i, 0) + 1
    return hist

count = categorize(y_train)
    plt.bar(count.keys(), count.values())
    plt.title('Distribution of y values appearing in the training set')
    plt.show()
```



Handin 2

```
In [5]: average_y_train = np.mean(y_train)

def mseError(predictor, y):
    y = y - predictor
    y = y * y
    return np.sum(y)/len(y)

print("Eorror on the training dataset", mseError(average_y_train, y_train))
print("Eorror on the testing dataset", mseError(average_y_train, y_test))

Eorror on the training dataset 0.7767772386501117
Eorror on the testing dataset 0.8138573000045535
```

Handin 3

```
In [6]: def standarlize(x):
    var = np.var(x)
    mean = np.mean(x)
    return (mean, var)

def transformData(x, mean, var):
    x -= mean
    x /= np.sqrt(var)
    return x

def find_weight(X, y):
    X_trans = X.T
    return np.matmul(np.matmul(inv(np.matmul(X_trans, X)), X_trans), y)
```

```
In [41]: # Placeholder for the standalized data
        X_train_standard = np.zeros(shape = X_train.shape)
        X_test_standard = np.zeros(shape = X_test.shape)
        # For each feature, calculate for mean and std, transform the data for both tes
        t/train
        for i in range(D):
           train data = X train[:, i]
           test_data = X_test[:, i]
           m,v = standarlize(train data)
           X train standard[:, i] = transformData(train data, m, v)
           X test standard[:, i] = transformData(test data, m, v)
           print("training: mean =", np.mean(X train standard[:, i]), "var =", np.var
        (X train standard[:, i]))
           print("Testing: mean =", np.mean(X_test_standard[:, i]), "var =", np.var(X_
        test standard[:, i]))
        training: mean = 2.3122562228027764e-17 var = 1.0
        Testing: mean = 0.0030527846038981995 \text{ var} = 1.0559133327466625
        training: mean = -1.269474004676034e-17 var = 1.0
        Testing: mean = -0.007511859999128221 \text{ var} = 1.1233168622542755
        training: mean = 1.8135342923943342e-17 var = 1.0
        Testing: mean = -0.02820964217791591 var = 0.741905848945599
        training: mean = 9.067671461971671e-18 var = 1.000000000000000002
        Testing: mean = -0.03437040308176073 var = 1.01439428211428
        Testing: mean = -0.011299108564615596 \text{ var} = 1.0831531580187885
        training: mean = -8.614287888873087e-18 var = 1.000000000000000002
        Testing: mean = -0.005327945753180028 \text{ var} = 0.9445614430786275
        training: mean = 1.0881205754366006e-17 var = 1.0
        Testing: mean = -0.017991526288517565 \text{ var} = 1.022899496018027
        Testing: mean = -0.02239597338629517 var = 1.0361602306269688
        Testing: mean = 0.05970897162986136 var = 1.0664289520416237
        Testing: mean = 0.03499859792244784 var = 1.0987830603456172
        Testing: mean = 0.010960253895340912 var = 1.0418353212866018
```

```
In [42]: # Include a column of ones to data matrices
b_training = np.ones((N_train,1))
b_test = np.ones((N_test,1))
b_tot = np.ones((N,1))

new_X_train_standard = np.hstack((b_training, X_train_standard))
new_X_test_standard = np.hstack((b_test, X_test_standard))

weights = find_weight(new_X_train_standard, y_train)

# Expected y
y_train_expected = np.dot(new_X_train_standard, weights)
y_test_expected = np.dot(new_X_test_standard, weights)

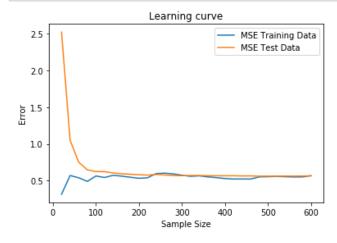
print("Eorror on the training dataset", mseError(y_train_expected, y_train))
print("Eorror on the testing dataset", mseError(y_train_expected, y_train))

Eorror on the training dataset 0.5639996173941925
Eorror on the testing dataset 0.5639996173941925
```

Handin 4 Learning Curve

```
In [52]: def FirstNmseError(predictor, y, N):
    t = y[0:N] - predictor[0:N]
    t = t * t
    return np.sum(t)/len(t)
```

```
In [70]:
        train_error = []
         test_error = []
         for i in range(20, 601, 20):
             weights = find_weight(new_X_train_standard[:i], y_train[:i])
             # Expected y
             y_train_expected = np.dot(new_X_train_standard[:i], weights)
             y_test_expected = np.dot(new_X_test_standard, weights)
             train_error.append(FirstNmseError(y_train_expected, y_train, i))
             test_error.append(mseError(y_test_expected, y_test))
         mat1 = np.array(train error)
         mat2 = np.array(test error)
         plt.figure()
         plt.title('Learning curve')
         plt.xlabel("Sample Size")
         plt.ylabel('Error')
         plt.plot(np.linspace(20,600, num=mat1.shape[0]), mat1, label='MSE Training Data
         plt.plot(np.linspace(20,600, num=mat2.shape[0]), mat2, label='MSE Test Data')
         plt.legend()
         plt.show()
```



```
In [ ]:
```